Experimental comparison of control strategies for trajectory tracking for mobile robots

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Abstract: The purpose of this paper is to implement, test and compare the performance of different control strategies for tracking trajectory for mobile robots. The control strategies used are based on linear algebra, PID controller and on a sliding mode controller. Each control scheme is developed taking into consideration the model of the robot. The linear algebra approaches take into account the complete kinematic model of the robot; and the PID and the sliding mode controller use a reduced order model, which is obtained considering the mobile robot platform as a black-box. All the controllers are tested and compared, firstly by simulations and then, by using a Pioneer 3DX robot in field experiments.

Keywords: sliding mode control; SMC; mobile robot; trajectory tracking; linear algebra; controller; algorithm; comparison; control.


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1 Introduction

There are an emergent amount of control research on mobile robotics due to the inherent nonlinearity in dynamics and also because they are very useful in industrial applications, in military actions, in challenging access or dangerous areas and for domestic and entertainment activities (Scaglia et al., 2009, 2010; Rosales et al., 2009b, 2010). In practical situations, there are many difficult problems in controlling mobile robots because of the inevitable uncertainties (Toibero et al., 2009; Roth and Batavia, 2012).

The use of trajectory tracking, which is related with the design of control laws that force the robot to reach and follow a time parameterised reference, is justified in structured workspaces as well as in partially structured workspaces, where unexpected obstacles can be found during the navigation. In the first case, the desired trajectory can be set from a global trajectory planner (Rico et al., 2001). In the second case, the algorithms used to avoid obstacles usually re-plan the trajectory in order to avoid a collision, generating a new reference trajectory from this point (Dong-Shu and Hua-Fang, 2011). In general, the objective is to find the control actions that make the mobile robot reach Cartesian position \((x, y)\) with a pre-established orientation \(\theta\) in each sampling period. These combined actions result in tracking the desired trajectory of the mobile robot. The actual challenge is to design controllers that can be easily implemented and
can react appropriately to different kinds of external disturbances, setting of tracking accuracy and robustness (Furat and Eker, 2012; Auat and Scaglia, 2013).

Several control strategies have been proposed for tracking trajectory, some of which are based on either the kinematic or the dynamic models of the mobile robot. The considered model used for this purpose can be both the kinematic model (Hedjar et al., 2005; Kanayama and Kimura, 1990; Kühne et al., 2005; Lee et al., 1999) as well as the dynamic model (Brennan and Alleyine, 2002; Dong and Kuhnert, 2005; Shuli, 2005; Yang and Kim, 1999; Zhang et al., 1998), which use a variety of approximations to obtain the controller, such as the Lyapunov method (Kanayama and Kimura, 1990), fuzzy logic (Lee et al., 1999) or predictive control (Kühne et al., 2005).

Scaglia et al. (2009) presented a control methodology based on the application of linear algebra (LA) for trajectory tracking, where the control actions are obtained by solving a system of linear equations. In order to get this objective, only two control variables are available: the linear velocity ($v$) and the angular velocity ($\omega$) of the robot.

By other side, sliding mode control (SMC) is a robust and simple procedure that allows synthesising controllers for linear and nonlinear processes (Utkin, 1977). The main advantages of using SMC are robustness to parameter uncertainty, insensitivity to load disturbance and fast dynamics response. Generally, the design of this controller depends completely on the process model, and the numbers of tuning parameters are in proportion to the model order (Slotine and Li, 1991). The major drawback of SMC is the so called chattering phenomenon. Various approaches of SMC have been proposed to control mobile robots (Jung et al., 2007; Solea et al., 2009; Yue et al., 2011; El’Youssef et al., 2010; Proaño et al., 2015).

This work shows a different approach of SMC for trajectory tracking for mobile robots. The SMC used in this work was developed by Camacho and Smith (2000) for chemical processes and it is based on easy concepts, and there is no need of complex calculations, with low computational cost to achieve the control signal.

The aim of this paper is to make a comparison of different control strategies for tracking trajectory for mobile robots. The control strategies used are two LA controllers, a PID controller and a SMC controller. Each control scheme is developed taking into account the model of the robot. The LA approaches take into account the complete kinematic model of the robot, and the PID and the SMC controllers use a reduced order model of the robot. All the controllers are tested using a Pioneer 3DX robot.

This paper is structured as follows. Section 2 presents the kinematic model of the mobile robot. Section 3 presents the fundamentals and formulation of the proposed controllers. In Section 4, the controllers’ synthesis is outlined. In Section 5, simulation, experimental results and their discussion are presented. Finally, Section 6 contains the conclusions.

2 Process model

This section describes briefly the process model to be used in the designing of different kind of controllers that will be used and compared in the tracking trajectory of the robot Pioneer 3DX. The model of this robotic platform is depicted in Figure 1. The complete kinematic model is described by equation (1).
The position of the robot for analysis is defined by the point \((x, y)\), which locates in this case in the point \(G\) (gravity centre). \(G\) is a certain distance \(a\) from \(B\), which is the centre of the line that connects the wheels. \(v'_x\) and \(v'_y\) are the speeds of the centre of mass (longitudinal and lateral), \(\omega\) is the angular speed of the robot, \(v\) is the linear speed and \(\varphi\) is the orientation angle.

\[
\begin{bmatrix}
\dot{x} \\
\dot{y} \\
\dot{\varphi}
\end{bmatrix} =
\begin{bmatrix}
\cos(\varphi) & -a \sin(\varphi) \\
\sin(\varphi) & a \cos(\varphi) \\
0 & 1
\end{bmatrix}
\begin{bmatrix}
v \\
\omega
\end{bmatrix}
\tag{1}
\]

The objective of the controllers is to track a reference trajectory that consists of two dimensions to follow, and that are generated according to previously specifications selected by the user, which will be called reference trajectories.

### 3 Controllers basic concepts

In this part, a brief description of the SMC and the two approaches based on LA are presented. The idea is to show basic concepts useful in their application.

#### 3.1 SMC from a reduced order model of the robot.

The use of the complete model of the robot for the SMC synthesis becomes in a complex controller. Besides, and considering that there are other factors that influence the performance of the platform (such as worn or old parts or temperature), it is not always possible to use the exact model.

For this reason, the robot is considered as a black box (Figure 2), where only the input (linear speed \(v\) and angular speed \(\omega\)) and output (odometry data \(x, y\) and \(\varphi\)) are known. Using an identification procedure, the obtained model represents a general one, therefore the resulting controller will be applicable for any other platform with similar behaviour.
This proposal allows obtaining a reduced order model for designing purposes. Hence, the job of the controller consists on receiving the data from the linear and angular speeds and generates the control signals to reach the speed references and thus the position references, satisfying the desired trajectory tracking.

Figure 3 shows the platform responses when a step signal is applied to the linear and angular speeds, the responses look like as first order plus dead time (FOPDT) models.

The general form of an FOPDT model can be written as in (2).

\[
\frac{\chi(s)}{U(s)} = \frac{Ke^{-t_0s}}{\tau s + 1}
\]

where
\( \chi(s) \) is the process output
\( U(s) \) is the controller output
\( \tau \) is the time constant of the system
\( K \) is the steady state gain of the process
\( t_0 \) is the time delay (deadtime).

The original and the approximated responses are depicted in Figure 4.
Following the procedure as was presented (Camacho, 1996), the sliding surface can be structured as a PID controller (3):

\[ s(t) = \frac{de(t)}{dt} + \lambda_1 e(t) + \lambda_0 \int_0^t e(t) \]  

(3)

And the SMC can be easily implemented in discrete time by using (Pérez de la Parte, 2005):

\[ U = \frac{\dot{X}(m)}{K} + \tau_0 \tau \lambda_0 (R(m) - X(m)) + K_D \frac{s(m)}{|\dot{X}(m)| + \delta} \]  

(4)

The tuning parameters (Camacho, 1996), for the continuous part are:

\[ \lambda_1 = \frac{\tau + \tau_0}{\tau_0 \tau} \]  

(5)

\[ \lambda_0 \leq \frac{\lambda_1^2}{4} \]  

(6)

and for the discontinuous part, the parameters are:

\[ K_D = \frac{0.51}{|K|} \left( \frac{\tau}{\tau_0} \right)^{0.76} \]  

(7)

\[ \delta = 0.68 + 0.12 (K \ K_D \ \lambda_1) \]  

(8)

The characteristic process parameters are obtained from the reaction curve method (Smith and Corripio, 2006).
3.2 LA controllers

The idea behind this approach consists in calculating the optimal control action (Strang, 1980), which allows the robot to go from the actual to the desired state (Scaglia et al., 2009; Capito and Proaño, 2015).

To apply the method, two approximations are used; these are Euler and trapezoidal approximations. In each case, the kinematic model of robot is substituted in the algebraic expressions and therefore, the controller action calculated.

### 3.2.1 For the Euler approximation

\[
\begin{bmatrix}
  x_{m+1} \\
  y_{m+1} \\
  \phi_{m+1}
\end{bmatrix} =
\begin{bmatrix}
  x_m \\
  y_m \\
  \phi_m
\end{bmatrix} +
\begin{bmatrix}
  \cos(\phi) & -a \sin(\phi) & 0 \\
  \sin(\phi) & a \cos(\phi) & 1
\end{bmatrix}
\begin{bmatrix}
  V_m \\
  \omega_m
\end{bmatrix}
\]  

\( (9) \)

\[
T_0
\begin{bmatrix}
  \cos(\phi) & -a \sin(\phi) & 0 \\
  \sin(\phi) & a \cos(\phi) & 1
\end{bmatrix}
\begin{bmatrix}
  V_m \\
  \omega_m
\end{bmatrix} =
\begin{bmatrix}
  x_{m+1} - x_m \\
  y_{m+1} - y_m \\
  \phi_{m+1} - \phi_m
\end{bmatrix}
\]  

\( (10) \)

\[
\frac{1}{T_0}
\begin{bmatrix}
  \Delta x_m \\
  \Delta y_m \\
  \Delta \phi_m
\end{bmatrix} =
\begin{bmatrix}
  \cos(\phi) & -a \sin(\phi) & 0 \\
  \sin(\phi) & a \cos(\phi) & 1
\end{bmatrix}
\begin{bmatrix}
  V_m \\
  \omega_m
\end{bmatrix}
\]  

\( (11) \)

Therefore, it can be represented as:

\[ Au = b \]  

\( (12) \)

where

\[
u =
\begin{bmatrix}
  v_m \\
  \omega_m
\end{bmatrix}
\]  

\( (13) \)

The speeds \( v_m \) and \( \omega_m \) need to be determined. When having an inconsistent system, the least square method (Strang, 1980) is used to satisfy the equation (12) and find the expression for \( u \).

\[ A^T Au = A^T b \]  

\( (14) \)

Applying this method, the expressions for the desired \( v_m \) and \( \omega_m \) are found:

\[
v_m = \frac{1}{T_0} \left( \Delta x_m \cos(\phi_m) + \Delta y_m \sin(\phi_m) \right)
\]  

\( (15) \)

\[
\omega_m = \frac{1}{T_0 (a^2 + 1)} \left( -a^2 \Delta x_m \sin(\phi_m) + a \Delta y_m \cos(\phi_m) + \Delta \phi_m \right)
\]  

\( (16) \)
3.2.2 For the trapezoidal approximation

Following the procedure presented in Section 3.2.1, we have:

\[
\begin{bmatrix}
    x_{m+1} \\
    y_{m+1} \\
    \varphi_{m+1}
\end{bmatrix} = \begin{bmatrix}
    x_m \\
    y_m \\
    \varphi_m
\end{bmatrix} + \frac{T_0}{2} \begin{bmatrix}
    v_m \cos(\varphi_m) - a\omega_m \sin(\varphi_m) \\
    v_m \sin(\varphi_m) + a\omega_m \cos(\varphi_m) \\
    \omega_m
\end{bmatrix} \\
+ \begin{bmatrix}
    \cos(\varphi_{m+1}) - a \sin(\varphi_{m+1}) \\
    \sin(\varphi_{m+1}) + a \cos(\varphi_{m+1}) \\
    0 & 1
\end{bmatrix} \begin{bmatrix}
    v_{m+1} \\
    \omega_{m+1}
\end{bmatrix}
\]

(17)

\[
\begin{bmatrix}
    \Delta x_m \\
    \Delta y_m \\
    \Delta \varphi_m
\end{bmatrix} = \frac{2}{T_0} \begin{bmatrix}
    v_m \cos(\varphi_m) - a\omega_m \sin(\varphi_m) \\
    v_m \sin(\varphi_m) + a\omega_m \cos(\varphi_m) \\
    \omega_m
\end{bmatrix} \\
= \begin{bmatrix}
    \cos(\varphi_{m+1}) - a \sin(\varphi_{m+1}) \\
    \sin(\varphi_{m+1}) + a \cos(\varphi_{m+1}) \\
    0 & 1
\end{bmatrix} \begin{bmatrix}
    v_{m+1} \\
    \omega_{m+1}
\end{bmatrix}
\]

(18)

\[
\begin{bmatrix}
    \cos(\varphi_{m+1}) - a \sin(\varphi_{m+1}) \\
    \sin(\varphi_{m+1}) + a \cos(\varphi_{m+1}) \\
    0 & 1
\end{bmatrix} \begin{bmatrix}
    v_{m+1} \\
    \omega_{m+1}
\end{bmatrix} = \frac{2}{T_0} \begin{bmatrix}
    \Delta x_m - v_m \cos(\varphi_m) + a\omega_m \sin(\varphi_m) \\
    \Delta y_m - v_m \sin(\varphi_m) - a\omega_m \cos(\varphi_m) \\
    \frac{2}{T_0} \Delta \varphi_m - \omega_m
\end{bmatrix}
\]

(19)

In a similar way, as it was presented for the Euler approximation

\[
A u = b
\]

(20)

where

\[
u = \begin{bmatrix} v_{m+1} \\ \omega_{m+1} \end{bmatrix}
\]

(21)

To find \(v_m\) and \(\omega_m\) we use again the least square method (Strang, 1980) to solve this inconsistent system (20) and find the expression for \(u\).

\[
A^T A u = A^T b
\]

(22)

Applying this method the expressions for the desired \(v_m\) and \(\omega_m\) are now found for this case:

\[
v_{m+1} = \frac{2}{T_0} v_m + \epsilon
\]

(23)
where
\[ e = \left( \Delta x_m \cos(\varphi_{m+1}) + \Delta y_m \sin(\varphi_{m+1}) \right) \] (24)
and
\[ e = -v_m \cos(\varphi_{m+1} - \varphi_m) + a_0 \omega_m \sin(\varphi_m - \varphi_{m+1}) \]
\[ \alpha_{m+1} = \frac{1}{a^2 + 1} (\gamma + \delta) \] (25)
where
\[ \gamma = \frac{2}{T_0} \Delta \varphi_m - \omega_m \]
\[ + \frac{2a}{T_0} \left( \Delta y_m \cos(\varphi_{m+1}) - \Delta x_m \sin(\varphi_{m+1}) \right) \] (26)
and
\[ \delta = a v_m \sin(\varphi_{m+1} - \varphi_m) - a^2 \omega_m \cos(\varphi_{m+1} - \varphi_m) \] (27)

3.2.3 Minimisation of the error

To minimise the error a vector \( \mathbf{b}(CA) \) should be found, it belongs to the column space of the matrix \( A \) and that is the closest to vector \( \mathbf{b} \) (28):
\[ Au = \mathbf{b} = \mathbf{b}(CA) + \mathbf{b}(NA^T) \] (28)
The column space of \( A \) is the group of vectors in \( \mathbb{R}^m \) that can be expressed as a linear combination of the \( n \) columns of the matrix \( A \), and it can be represented as follows.
\[ k_1 \mathbf{v}_1 + k_2 \mathbf{v}_2 = \mathbf{b}(CA) \] (29)
where \( \mathbf{v}_1 \) and \( \mathbf{v}_2 \) are base vectors of the column space of \( A \) and they are perpendicular. The constants \( k_1 \) and \( k_2 \) correspond therefore to the speeds \( v_m \) and \( \omega_m \) previously found.
To ensure an exact solution, the \( \mathbf{b} \) component on the left side of the null space of \( A^T \) must be zero (Scaglia et al., 2009):
\[ \mathbf{b}(NA^T) = 0 \] (30)
Finally (29) and (30) are replaced in (28) in order to obtain the expression that ensures that the minimum error is made. The obtained expression is a restriction for the selection of the angle \( \varphi_{m+1} \) which allows guiding the robot every sample time to its next goal, as observed in Figure 5.
Using the obtained value for the angle, it is assured that the solution is exact or has minimum error (Rosales et al., 2009a).
Figure 5  Robot’s orientation with angle (see online version for colours)

Minimising the error we obtain the following angle restrictions:

- For the Euler approximation
  \[ \varphi_{\text{E}} = \tan^{-1}\left(\frac{\Delta y_m}{\Delta x_m}\right) \]  
  \[ (31) \]

- For the trapezoidal approximation
  \[ \varphi_{\text{T}} = \tan^{-1}\left(\frac{\Delta y_m}{\Delta x_m} \frac{2v_m}{T_0} - \frac{v_m}{T_0} \sin(\varphi_m)\right) \]  
  \[ \frac{\Delta x_m}{\Delta y_m} \frac{2v_m}{T_0} - \frac{v_m}{T_0} \cos(\varphi_m) \]  
  \[ (32) \]

3.2.4 Considerations to make the error tend to zero stably

Equation (33) is used to guarantee that the error will decrease smoothly as the time elapses. This is necessary to avoid that the system reaches the reference abruptly, which could cause instabilities (Rosales et al., 2009a).

\[ x_{n+1} = x_{\text{ref}_{n+1}} - k_x (x_{\text{ref}_n} - x_n) \]  
\[ (33) \]

\[ 0 < k_x < 1 \]  
\[ (34) \]

where \( k_x \) defines the speed with which the error will reach zero, and it must be between zero and one (34). Replacing the position data in (33) and solving, the set of equations for \( \Delta x \), \( \Delta y \) and \( \Delta \varphi_{\text{E}} \) (35) is obtained.
4 Experimental results

In this section, the four controllers are tested and their performance compared firstly by simulations and then in a realistic way. In the simulation case, a double frequency trajectory is used. This test could not be verified by real experimentation due to insufficient physical space. In the realistic experiments, square and circular trajectories are used.

The IAE index (Kealy and O’Dwyer, 2003; Himmelblau, 1972) is used to measure the performance of the controllers; it is defined as in (36).

\[
\text{IAE} = \frac{\int_0^T |e(t)| \, dt}{T}
\]  

(36)

The controller with the minimum IAE has the best performance.

4.1 Simulation for a double frequency trajectory

Figures 6, 7, 8, 9 and 10 illustrate how perform each controller for a double frequency trajectory. Figure 6 is a XY graph, Figure 7 shows the X and Y responses vs. time, Figure 8 is the trajectory error responses vs. time, in Figure 9 linear and angular speeds vs. time are plotted, finally Figure 10 displays the angular positions vs. time.

**Figure 6**   XY graph (see online version for colours)
Experimental comparison of control strategies for trajectory tracking

Figure 7  X and Y trajectory vs. time (see online version for colours)

Figure 8  Trajectory error vs. time (see online version for colours)

Figure 9  Linear and angular speeds vs. time (see online version for colours)
The first thing to notice is the fast response of the SMC, it is the first controller to reach the desired path. The performance of the LA controllers are practically the same, the Euler approach presents the best results. The PI appears to be the slowest, but its overall performance is very acceptable. In spite that the SMC, uses a reduced order model of the robot, its overall performance is very close to the LA approaches which use a complete model of the robot, and much better than the PI controller.

4.2 Realistic experiments

In this part, two different trajectories are used: a square one with each side = 2.5 m and a circular one with radius = 2 m. Figure 11 shows a picture of the Pioneer 3DX that was used in these experimental tests with the four controllers.
4.2.1 Square trajectory

Figure 12 shows the Pioneer 3DX responses for each controller. Figures 13 to 16 depict the same aspects as in the simulation case.

**Figure 12** XY graph (see online version for colours)

![XY graph](image)

**Figure 13** X and Y trajectory vs. time (see online version for colours)

![X and Y trajectory vs. time](image)

**Figure 14** Trajectory error vs. time (see online version for colours)

![Trajectory error vs. time](image)
According to the results shown in the previous plots and Table 2, it is possible to appreciate that the SMC presents the best reaction when facing abrupt changes, and also the best performance. The PI controller reacts well in this experiment, presenting the second best performance. If the speed increases, the LA controllers take more time to react; this causes bigger overshoots and longer settling times. This happens because of the structure of the controllers by themselves, as the Euler and trapezoid approximation, can anticipate only the next sample time.

### 4.2.2 Circular trajectory

In a similar way as was presented for the square trajectory, Figures 17, 18, 19, 20 and 21 display the same experiments as before.
Experimental comparison of control strategies for trajectory tracking

Figure 17  XY graph (see online version for colours)

Figure 18  X and Y trajectory vs. time (see online version for colours)

Figure 19  Trajectory error vs. time (see online version for colours)
Figure 20  Linear and angular speed vs. time (see online version for colours)

![Linear and angular speed vs. time](image)

Figure 21  Angular position vs. time (see online version for colours)

![Angular position vs. time](image)

Table 3  IAE comparison – circular trajectory

<table>
<thead>
<tr>
<th>O</th>
<th>Euler</th>
<th>Trapezoidal</th>
<th>PI</th>
<th>SMC</th>
</tr>
</thead>
<tbody>
<tr>
<td>250</td>
<td>IAE * 10^3</td>
<td>IAE * 10^3</td>
<td>IAE * 10^3</td>
<td>IAE * 10^3</td>
</tr>
<tr>
<td>X</td>
<td>8,027</td>
<td>7,438</td>
<td>8,566</td>
<td>7,792</td>
</tr>
<tr>
<td>Y</td>
<td>3,163</td>
<td>2,284</td>
<td>4,246</td>
<td>3,433</td>
</tr>
</tbody>
</table>

For the circular trajectory the results presented indicate that the trapezoidal approximation has the lowest settling time, and Table 3 provides that the trapezoidal approximation produces the best performance. The SMC presents a good response when reaching its trajectory, however, as the speed increases the overshoot increases too. It can be seen from Table 3 that the SMC presents a very close performance index compared with LA controllers.
5 Conclusions

The controllers developed using LA approximations have shown good performances in general way, the stabilisation times are similar for both controllers. On the other side, the PID and the SMC, from a reduced order model of the robot, produce in general satisfactory results, especially for the square trajectory, where they presented the best responses.

The experimental results, simulations and field tests, indicated that the presented SMC has a good performance, better than the PI controller, and closer to those controllers based on the complete model of the robot.

Moreover, the proposed SMC approach used in this work can be easily implemented since it uses a PID controller as sliding surface and also presents a set of tuning equations based on the characteristic parameters of the process.

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