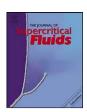
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Equation of state modeling of the phase equilibria of asymmetric CO₂ + n-alkane binary systems using mixing rules cubic with respect to mole fraction

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ABSTRACT

Both the equation of state (EOS) and the quadratic mixing rules proposed by van der Waals towards the end of the XIX century were enormous contributions to the understanding and modeling of fluids phase behavior. They set the basis for a consistent and useful representation of phase equilibria for a great diversity of mixtures. Nevertheless, the models for representing phase equilibria and physico-chemical properties of asymmetric systems may require more flexible mixing rules than the classical quadratic van der Waals (vdW) mixing rules or their equivalent (with regard to the number of available interaction parameters) in modern equations of state.

In particular, the phase equilibria of binary mixtures containing CO_2 and heavy n-alkanes have been studied by an important number of authors and using different types of models, achieving only partially accurate results and realizing the difficulties that these systems showing type III phase behavior (from C14 on) present for predicting or even correlating their phase equilibrium data in wide ranges of temperature and pressure.

Cubic mixing rules (CMRs), implemented as a natural extension of the classical quadratic mixing rules, constitute the simplest alternative among different flexible approaches. In addition, they have the advantage of allowing correlation of multicomponent data by fitting ternary interaction parameters, while leaving invariant the description of the constituent binary systems.

In this work, and after having detected the need for temperature-dependent interaction parameters in a previous study, we implemented an automated parameterization procedure based on characteristic key-points for binary systems showing type III phase behavior. Using the RK-PR EoS coupled to CMRs we present the parameters obtained and results showing for the first time a quite successful complete description of asymmetric CO_2 + n-alkane binary systems, with n-alkane carbon number from 14 to 22. © 2010 Elsevier B.V. All rights reserved.

1. Introduction

Before van der Waals, the liquid state of a substance was believed to be formed of atomic complexes, greater in size than the single molecules existing in the gas phase. Johannes van der Waals expressed "...both portions of the isotherm belong to one curve...there would then only be a difference of greater or smaller density in the two states, and thus only a quantitative difference." [1].

Being such concept, i.e., the continuity between the liquid and vapor states, already a historical contribution, it is remarkable that at the same time van der Waals moved forward and proposed the first model allowing to describe continuously the liquid, vapor and

supercritical states of pure fluids. Today, more than 130 years later, such model continues to be the root of many present equations of state.

In 1890, Van der Waals provided the practical tools for describing simultaneously both vapor–liquid and liquid–liquid phase separation in binary mixtures, by generalizing his equation of state for application to phase separation of binary fluid mixtures. It was a triumph of the Van der Waals mixture equation that it could produce both vapor–liquid and liquid–liquid phase separation of binary mixtures (Levelt Sengers [2] and ref. cited therein).

His quadratic mixing rules (QMRs) allowed for a consistent modeling of mixtures phase behavior. Based on the van der Waals EOS and QMRs, van Konynenburg and Scott, "generated the first, nearly comprehensive classification of fluid phase equilibria" [3]. Their calculations were mainly devoted to binary systems without differences in molecular size. They identified five types of fluid phase behavior (I, II, III, IV and V). Studies for size-asymmetric binary sys-

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tems are also available [4]. In combination with later improvements for the density and temperature dependences of the attractive term (including the nowadays classic SRK and PR EOS) the van der Waals approach allowed for a good quantitative representation of vapor–liquid equilibria in a significant number of mixtures studied for decades, including mainly those of interest for the oil and gas or petrochemical industries (see for example [5–7]).

Nevertheless, mixtures which are very asymmetric, either in size or attractive forces, have demonstrated to present a much higher degree of difficulty for their phase behavior modeling. These mixtures appear more frequently in newer applications, including an important diversity of supercritical fluid technologies, such as extraction, fractionation or anti-solvent precipitation, but also in the petroleum industry. One representative and very important family of asymmetric binary mixtures is the $\rm CO_2 + n$ -alkane series. The importance of this series, sometimes taken as a reference in the analysis of other non-alkane + $\rm CO_2$ binary mixtures, is clear when considering $\rm CO_2$ injection as a method for enhanced oil recovery or recent approaches for $\rm CO_2$ sequestration in exploited oil wells.

Available previous attempts to describe the phase equilibria of CO₂ + n-alkane systems in wide ranges of conditions were not completely successful. One of the most interesting and relatively successful approaches has been the one by Polishuk et al. [8]. Using a four-parameter "close-to-cubic" equation of state combined with classical quadratic mixing rules, they proposed generalized equations for the estimation of all repulsive interaction parameters (l_{12}) and all temperature-dependent attractive interaction parameters (k_{12}) for the whole series of CO₂ + n-alkane binary systems. The constants for their correlation were obtained by considering data only for a few global key-points (KPs). Examples of global key-points are upper critical end points (UCEPs) and local minima or maxima in the pressure-temperature projection of a vapor-liquid critical line. The results of Polishuk et al. [8] showed a good representation of the liquid-vapor part of critical lines while overestimating the size of the liquid-liquid separation region, specially at higher pressures. Predictions for vapor-liquid equilibrium were quite good in general at high temperatures, but overestimation of the CO₂ content in the liquid phase can be observed in the lower temperature region and specially for the heavy liquid under conditions of liquid-liquid-vapor equilibrium (LLVE).

Following a similar approach with the RK-PR EoS [9] and quadratic mixing rules, Cismondi achieved better prediction of critical lines – and also light phase compositions – for $CO_2 + n$ -alkane binary systems, but at the cost of a systematic overestimation of CO_2 solubility in heavy phases [10].

Vitu et al. [11] proposed a group-contribution temperature-dependent functionality for the k_{12} interaction parameter to be used with the PPR78 EoS [12] and regressed the required constants for some series of binary systems, including $CO_2 + n$ -alkanes. They obtained very good predictions for systems with low or moderate molecular weight for the n-alkane, i.e., those mixtures showing type I or II phase behavior, but predicted type III for $CO_2 + n$ -tridecane (which shows type IV experimentally [13]) and failed to quantitatively describe the behavior of systems showing type III phase behavior (C14 and higher).

Some other works, based on different modeling approaches, achieved only partially successful results, i.e., those studies were restricted to specific types of phase equilibria in relatively narrow ranges of temperature (*T*) and pressure (*P*), instead of considering the global phase behavior of systems in ranges of conditions as wide as those of the available experimental data. For example, Fu et al. [14] show good correlation results using the PC-SAFT EoS for mixtures of CO₂ with light hydrocarbons, and also with heavier n-alkanes, but in this case only for the lower pressure range, without commenting on the very large deviations and systematic overestimation of the phase separation region that occurs at higher

pressures (see also the work by Nguyen-Huynh et al., using a Group-Contribution SAFT equation [15] and ref. cited therein). Recent studies have used excess free energy based mixing rules [16,17], but considering only vapor-liquid equilibria (VLE) in a moderate pressure range, i.e., below 80 bar, for the systems being discussed in this work. The same applies to the use of the recent and more theoretically based PCP-SAFT [18].

Our hypothesis is that such apparent impossibility for a reasonable good description of the complete phase behavior of this type of systems is essentially due to the lack of flexibility, in terms of composition, of the implemented mixing rules.

Cubic mixing rules (CMRs) have been recently proposed as a consistent and natural extension of van der Waals quadratic mixing rules [19]. CMR are the following:

$$a = \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N} x_i x_j x_k a_{ijk}$$
 (1)

$$a_{ijk} = (a_i a_j a_k)^{(1/3)} (1 - k_{ijk})$$
(2)

$$b = \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N} x_i x_j x_k b_{ijk}$$
(3)

$$b_{ijk} = \left(\frac{b_i + b_j + b_k}{3}\right) (1 - l_{ijk}) \tag{4}$$

where N is the number of components in a multicomponent mixture, a_i , b_i and x_i are, for component i, the attractive energy parameter, the repulsive co-volume parameter and the mole fraction in the system respectively, k_{ijk} and l_{ijk} are respectively the energy interaction parameter and the covolume interaction parameter. For a binary system of components 1 and 2, the cubic mixing rules provide four independent interaction parameters, i.e., k_{112} , k_{122} , l_{112} and l_{122} . Thus, the number of available interaction parameters in cubic mixing rules doubles the number which quadratic mixing rules provide. The conventional quadratic mixing rules are a particular case of cubic mixing rules [19]. Recently, Polishuk has used CMRs but in a form that cannot be extended to multicomponent mixtures [20].

For ternary or higher systems, Eqs. (2) and (4) require ternary interaction parameters. Such parameters can be either regressed from experimental information on ternary systems or predicted from parameters obtained from experimental data on binary systems [19]. The potential correlation of ternary data by fitting ternary interaction parameters, while leaving invariant the description of the constituent binary systems, makes the CMR very appealing and some promising preliminary results have been presented by Pisoni et al. [21]. The partial molar properties for component 1, when component 1 is infinitely diluted in component 2, depend on k_{122} and on l_{122} but not on k_{112} and l_{112} . Analogously, the partial molar properties for component 2, when component 2 is infinitely diluted in component 1, depend on k_{112} and l_{112} but not on k_{122} and l_{122} [19]. Thus, the dominant interaction parameters for a given concentration limit are clearly identified for CMRs.

Our general goal is to explore and analyze the possibilities that these flexible, yet simple, cubic mixing rules offer for modeling the high pressure phase behavior of different types of asymmetric mixtures, identifying their strengths and limitations. In previous preliminary works [22,23], we used CMRs in combination with the RK-PR EoS [9] and focused on the binary carbon dioxide (1)+n-hexadecane (2), as a representative case of the most common phase behavior observed for asymmetric systems of interest, known as type III in the classification of Scott and van Konynemburg [24]. In the first work we carried out a parameter sensitivity analysis that paid attention to the global phase equi-

librium behavior using the GPEC software [25,26] and arrived to a unique set of (temperature-independent) cubic interaction parameters, which showed a clear improvement over the performance of quadratic mixing rules for CO_2 (1)+n-hexadecane (2) [22]. Nevertheless, the results suggested that a proper description of the phase equilibria for this system would require the introduction of temperature dependent interaction parameters. We did so later, proposing a consistent temperature dependence for the k_{112} and k_{122} parameters. The results demonstrated that, in combination with temperature dependent attractive interaction parameters, the flexibility that cubic mixing rules offer in composition, in comparison to the classical quadratic mixing rules, can be used to quite accurately represent the phase equilibria of very asymmetric mixtures [23].

The present work deals with the procedure and results for the automated numerical optimization of the interaction parameters of CMRs coupled to the RK-PR EOS for reproducing the fluid phase behavior for all the $\rm CO_2+n$ -alkane binary mixtures experimentally showing type III phase behavior, i.e., those with n-alkane carbon numbers from 14 to 22. Our final goal is to improve the description of the phase equilibria of such systems with respect to previous approaches and to verify our previously stated hypothesis.

2. Methodology

Our goal is clearly to optimize the representation of the fluid phase behavior over a wide range of conditions for the $\rm CO_2 + n$ -alkane binary mixtures with n-alkane carbon number from 14 to 22, using cubic mixing rules (CMRs) with temperature dependent attractive interaction parameters.

When translating a general objective like that into specific tasks to be performed, a number of choices have to be made with regard to, e.g., the particular equation of state, the pure compound parameters, the experimental data sets to be considered, the definition of the objective function, etc.

In the following sections, we discuss some details and comment on each of these issues, which define as a whole the methodology we followed in the study presented in this work.

2.1. Equation of state

CMRs can be used, in principle, with any equation of state susceptible of implementation of one-fluid type mixing rules. We believe that, roughly, the ability of an equation-of-state (EoS) type model to represent the phase behavior of real mixtures, with regard to the relationship among T, P and phase compositions, depends more on the mixing rules used than on the form of the relationship among temperature, pressure and molar volume for the pure compounds, provided that the EOS properly reproduces the experimental pure compound liquid-vapor saturation line. Therefore, considering the relative simplicity of van der Waal's type cubic equations of state, and that they continue to be the most used models for representing phase equilibrium, specially for practical applications, we decided to use CMRs in combination with cubic equations of state (CEOS). CEOS, never give more than three real molar volume roots at a given temperature (as long as the mixing rules are not density-dependent). Other more modern EOSs may lead to inconsistent behavior due to the appearance of more than three roots, at set temperature, for a given pure compound. For instance, Privat et al. [27] have recently shown, very clearly for pure n-decane (see their Fig. 12), that the PC-SAFT EOS gives three stable fluid-fluid saturation curves that meet at a triple purecompound liquid-liquid-vapor point. Multiple stable fluid-fluid saturation lines and stable fluid-fluid-fluid triple points have never

Table 1Pure compound parameters^a for the RK-PR EOS (this work).

Compound	a_c (bar × L^2/mol^2)	b (L/mol)	δ_1	k
Carbon dioxide	3.8796	0.027595	1.995049	2.14904
n-Tetradecane	106.1728	0.241220	4.483807	2.95470
n-Pentadecane	118.3736	0.257929	4.659300	3.04467
n-Hexadecane	131.2301	0.275390	4.804542	3.10300
n-Heptadecane	141.9859	0.293282	4.787073	3.26364
n-Octadecane	155.2174	0.310493	4.939278	3.34726
n-Nonadecane	168.3692	0.328251	5.038376	3.43935
n-Eicosane	180.7048	0.345322	5.100415	3.57697
n-Heneicosane	194.4869	0.362952	5.197945	3.64879
n-Docosane	209.6567	0.379792	5.365185	3.68889

^a They reproduce the experimental (DIPPR, [31]) T_c , P_c , acentric factor and liquid molar volume at triple point.

been found experimentally for pure compounds, according to current knowledge.

The results from preliminary studies for the representation of experimental ternary mixtures phase diagrams with CMRs did not show important differences between using the Peng–Robinson or the RK-PR equation of state [21].

In this work, due to its better representation of volumetric properties, we used the three-parameter RK-PR EoS [9]:

$$P = \frac{RT}{v - b} - \frac{a}{\left(v + \delta_1 b\right) \left(v + (1 - \delta_1/1 + \delta_1)b\right)};$$

$$a_i(T) = a_{c,i} \left(\frac{3}{2 + T/T_{c,i}}\right)^{k_i}$$
(5)

(with linear mixing rule for the third parameter δ_1) which in contrary to the limitations of the SRK or PR equations should lead to a good prediction of densities when correlating phase equilibrium in the pressure–temperature–composition (P–T–z) space. Besides, the RK-PR EoS has been found to provide a better correlation capacity for synthetic natural gas mixtures when compared to other EoS like PR and even PC-SAFT (consider results in ref. [28,29]). Recently, the RK-PR model was also successfully used for the dynamic modeling of a liquefied gas tank in wide ranges of temperature and pressure, with internal energy, volume and numbers of moles as independent thermodynamic variables [30].

2.2. Pure compound parameters

Having one extra parameter in comparison to classical cubic EoS's like SRK and PR, the RK-PR model allows to match the critical temperature (T_c) and critical pressure (P_c), and also the acentric factor for a given pure compound, while leaving one degree of freedom for the adjustment of volumetric properties. In the original paper, a universal value of 1.168 for the ratio between calculated and experimental critical compressibility factors (Z_c) was proposed as a default specification when no other information is available [9]. In this work, instead, we decided to match the experimental liquid molar volume at the triple point for each compound. The values were taken from the DIPPR database [31] and the resulting parameters are presented in Table 1.

2.3. The temperature dependence for the k_{112} and k_{122} parameters

In our previous preliminary studies [22,23] we found that a temperature dependence was needed for the attractive interaction parameters, i.e., for k_{112} and k_{122} , in binary systems, and defined the following functionality, which has finite limits both at zero and

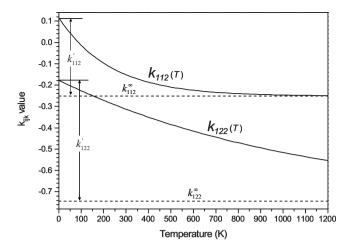


Fig. 1. The behavior of k_{112} and k_{122} for the system $CO_2(1)$ +n-hexadecane (2) as a function of temperature, according to Eq. (6) and parameters in Table 5.

at infinite temperature.

$$k_{ijk} = k_{iik}^{\infty} + k_{iik}' e^{-T/T_{ijk}^*}$$
 (6)

It can be seen that this is a monotonically decreasing or increasing function of temperature, depending on the sign of k'_{ijk} . Parameter k_{ijk} asymptotically tends to k^∞_{ijk} [Eq. (6)]. Fig. 1 shows how k_{112} and k_{122} depend on temperature for the case of CO₂ (1)+n-hexadecane (2) according to parameters obtained in this work. In Section 3 we show the curves for all systems considered, in a restricted temperature range of interest.

2.4. Definition of key-points and other data

When fitting parameters to obtain a good correlation of experimental phase equilibria it is common practice to include a large number of data points in the objective function, usually all points available. In this work we followed a different approach for a number of reasons.

First of all, it is a fact that there is a considerable scatter in the data available for asymmetric systems like CO_2 + heavy n-alkane, specially for the compositions of two phases at equilibrium. There can be different reasons for this and they will be explored and discussed in a subsequent publication.

Second, van der Waals type equations of state provide qualitatively correct patterns for phase diagrams and their evolution, and some regions are much sensitive to interaction parameters than others. Taking that into account, it was found that it is possible to achieve a good parameterization for describing the global phase behavior of a system by considering only a few carefully selected key-points (KPs), instead of the undiscriminated totality of points available. This was shown by Polishuk et al. (see for example [8,32] for the series of CO_2 binary mixtures with alkanols and n-alkanes) and then by Cismondi (types II and III for CO_2 +n-alkane binary systems [10]) and Secuianu et al. (CO_2 +alkanol binary systems showing type I or II [33–35]).

Finally, we are not interested just in correlating some particular isotherms or isobars for a limited number of systems. Our goal is to describe the global phase behavior, in wide ranges of T and P, and paying attention to the evolution of such behavior in nine differ-

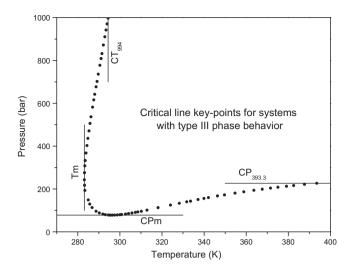


Fig. 2. Illustration of the four key-points defined for the representation of a critical line, for the case CO₂ (1)+n-tetradecane (2). See Table 2 for numerical values.

ent consecutive binary systems of the CO_2 + n-alkane homologous series. Therefore, we would prefer, or even need, a single procedure and a single objective function form, both valid and equivalent for all systems considered.

In this work, having an important degree of model flexibility provided by the CMRs, we decided to consider a sufficient number of key-points for properly placing both the critical line and the liquid branches of the LLV line of each system.

Each critical line is represented by four particular key-points, defined previously by Cismondi [10] for systems with type III phase behavior. They are illustrated in Fig. 2 for the case of CO₂+ntetradecane: CPm is pressure coordinate of the local minimum of the curve; $T_{\rm m}$ the minimum temperature in the liquid-liquid like part of the critical line. CT₉₉₄ represents the critical temperature at the maximum pressure experimentally available for these lines and, accordingly, CP_{393,3} represents the critical pressure at the maximum temperature experimentally available. More details are given in Table 2, which reports the critical line key-point values for all systems considered. Those for systems with n-alkane carbon numbers 14 to 17, 19 and 22 were taken from the critical lines measured in Bochum, Germany, by the Group of Prof. Schneider [36,37]. These data show a consistent and smooth evolution from one system to another along the series. For that reason, we generated the corresponding key-points for C18, C20 and C21 by predicting values from a regression for the whole series (values with superscript a in Table 2).

For representing the LLV behavior of each binary system we defined six key-points which provide information regarding the low temperature and middle temperature ranges, besides the Upper Critical End Point (UCEP) which marks the maximum temperature limit of the three-phase line. More details are given in Table 3, which reports the values for the six key-points considering the nine binaries from C14 to C22. Table 3 also informs the values assigned to $T_{\rm lowLLV}$ and $T_{\rm midLLV}$ which are somewhat arbitrary, depending on the experimental data available for each system.

We found no LLV data for the binaries with C17, C18 and C22. Analogous to what we did for critical line key-points, we generated artificial LLV key-points for these three systems based on the observation of the data for the whole series. Fig. 3 shows both the experimental and generated key-points for all the binaries considered, from C14 to C20. Notice that, although we use some generated key-points in our parameter fitting procedure, we assess the quantitative performance of the final parameter values through comparisons only with experimental data.

¹ The success in all those works was limited, as already pointed out in Section 1. But the main reasons for that were found not in the approach based on key-points, but in the limitations of quadratic mixing rules. That is our conclusion, supported now by the results achieved in the present work.

Table 2Critical line key-points considered in this work for CO₂ + n-alkane binary mixtures. CN: carbon number of the n-alkane. Temperatures are expressed in K and pressures in bar. CT₉₉₄: critical temperature assigned to a pressure value of 994 bar. The pressures informed in the references range from 991 to 997.8 bar. CP_{393.3}: critical pressure assigned to a temperature value of 393.3 K. The temperatures informed in the references range from 393.14 to 393.59 K.

CN	CT ₉₉₄ (K)	$T_{\rm m}$ (K)	CPm (bar)	CP _{393.3} (bar)	References for experimental data (values)
14	294.40	283.1	78	226.6	Scheidgen [37]
15	299.54	290.0	121	237.8	Scheidgen [36] Scheidgen and Schneider [47]
16	305.45	297.6	166	256	Scheidgen [36] Spee and Schneider [48]
17	311.43	304.7	203	272.2	Scheidgen [37]
18	316.4 ^a	311.0 ^a	237.9a	287	Pöhler [42]
19	321.51	317.2	269	304	Scheidgen [37]
20	326.5a	323.2a	299.8 ^a	320	Kordikowski and Schneider [43]
21	331.3a	328.9a	326.2a	338.6 ^a	
22	335.97	334.2	350	357	Scheidgen [37]

^a Values obtained from regressions based on experimental data for other CN.

Table 3Liquid-liquid-vapor equilibrium (LLV) key-points considered in this work for $CO_2 + n$ -alkane binary mixtures. Six LLV key-points are considered: composition of the two liquid phases at a selected low temperature T_{lowLLV} (x_{lowLLV} and y_{lowLLV}). Composition of the two liquid phases at a selected mid-range temperature T_{midLLV} (x_{midLLV} and y_{midLLV}). Temperature and composition of the alkane-richer phase at the upper critical end point (T_{UCEP} and x_{UCEP}). CN: carbon number of the n-alkane. Temperatures are expressed in K. x and y: CO_2 molar fraction.

CN	T_{lowLLV} (K)	x_{lowLLV}	y_{lowLLV}	$T_{ m midLLV}$ (K)	$x_{ m midLLV}$	$y_{ m midLLV}$	$T_{\text{UCEP}}\left(\mathbf{K}\right)$	χ_{UCEP}	References for experimental data
14	270.0	0.707	0.9815	291.2	0.819	0.9631	311.2	0.820a	van der Steen et al. [38] and Hottovy et al. [39]
15	273.4	0.689	0.9847	293.5	0.767	0.9785	309.4	0.769^{a}	van der Steen et al. [38] and Hottovy et al. [39]
16	283.2	0.716	0.9868	298.1	0.751	0.9898	307.9 ^b	0.749^{a}	van der Steen et al. [38]
17	287.0°	0.712 ^c	0.9900 ^c	298.0 ^c	0.736 ^c	0.9925 ^c	306.8 ^b	0.740^{b}	
18	290.0°	0.708^{c}	0.9930 ^c	298.0 ^c	0.725 ^c	0.9947 ^c	306.0 ^b	0.729^{b}	
19	292.9	0.704	0.9958	298.5	0.716	0.9966	305.5	0.722^{a}	Fall et al. [40]
20	300.3	0.716	0.9985	302.5	0.715	0.9985	305.2	0.714^{a}	Fall et al. [40]
21	301.5	0.708	0.9986	303.4	0.710	0.9986	305.0	0.709^{a}	Fall et al. [40]
22	301.0°	0.702^{c}	0.9987^{c}	303.0 ^c	0.706 ^c	0.9987^{c}	304.8 ^b	0.706^{b}	

^a Values for x_{UCEP} estimated from LLV data at temperatures below the UCEP.

LLV data for the binaries with C14, C15 and C16 were taken mainly from van der Steen et al. [38]. Hottovy et al. [39] had also reported data for the binaries with C14 and C15 but these data may present larger uncertainties (probably due to assuming the vapor phase as pure carbon dioxide, see van der Steen et al. [38]).

Note that the binary with n-docosane does not show LLVE experimentally (Table 3), due to the precipitation of solid n-docosane [40]. Artificial LLVE data were also generated for this binary, in order to follow the same procedure applied to lighter n-alkanes for the parameterization of their interactions with ${\rm CO_2}$ for the representation of fluid phase equilibrium.

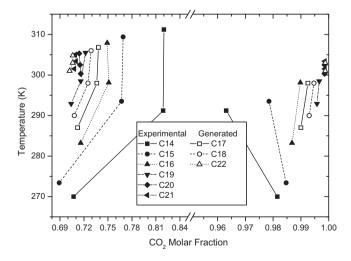


Fig. 3. Experimental and generated LLV key-points (composition of the liquid phases) selected for their use in the objective function (see Table 3) corresponding to CO₂ + n-alkane systems.

Besides the critical line and LLV key-points considered for all systems, we also evaluated the possibility of adding experimental two-phase equilibrium compositions at specified temperature and pressure to the database used to fit the model parameters. After trying also with some points for C19 and C20, in the final results shown in Section 3 only the data specified in Table 4 for $\rm CO_2$ (1)+n-hexadecane (2) were considered. Note that the points taken from Brunner et al. [41] at 573 K allowed us to considerably extend the temperature range covered.

There are also unpublished Pxy and Txy data in the PhD thesis by Pöhler [42], which Prof. Schneider kindly provided us with, together with the already cited thesis by Scheidgen [37]. The data by Pöhler concerns the binary systems of CO₂ with C17, C18 and C22. Nevertheless, and taking for example the data at 393.2 K, they do not follow a trend when put together with the data for C16 in Table 4 and other published data for C19 and C20 from the same group in Bochum [43], and not even among themselves. For this reason, we used only critical lines data from the thesis by Scheidgen (which do show regular trends, as already pointed out, see Table 2) but no compositional data for phase separation was taken from these thesis for use in the objective function.

Table 4 Two-phase experimental equilibrium points considered in the objective function for the parameterization of CO_2 (1)+n-hexadecane (2) binary mixture. x_1 and y_1 are mole fractions of CO_2 in the heavy and light phase respectively.

T(K)	P (bar)	<i>x</i> ₁	<i>y</i> ₁	Reference
393.2	100	0.4968	0.9982	Spee and Schneider [48]
393.2	200	0.7473	0.9909	Spee and Schneider [48]
573.2	101	0.428	0.962	Brunner et al. [41]
573.2	201	0.700	0.938	Brunner et al. [41]

^b Values obtained from regressions based on UCEP experimental data and pseudo-experimental data for other CN.

^c Artificial LLV points estimated based on data for other CN (see Fig. 3).

Table 5Optimum CMR parameters obtained, with the corresponding minimum value found for the objective function (OF). Eq. (6) was used with $T_{112}^* = 230 \,\text{K}$ and $T_{122}^* = 1100 \,\text{K}$ in all cases. CN: carbon number of the alkane in the binary system CO₂ (1)+n-alkane (2).

CN	k'_{112}	k'_{122}	k_{112}^{∞}	k_{122}^{∞}	l_{112}	l_{122}	Terms	OF
14	0.39714	0.55412	-0.24429	-0.70425	0.05028	0.02446	15	0.01041
15	0.38194	0.56133	-0.24851	-0.72217	0.05918	0.03310	15	0.00550
16	0.36666	0.56603	-0.25117	-0.74370	0.07140	0.04106	31	0.00995
17	0.48983	0.57027	-0.32618	-0.81594	0.06434	0.06220	15	0.00009
18	0.43254	0.56899	-0.30442	-0.82480	0.06682	0.03727	15	0.00007
19	0.48211	0.69346	-0.32164	-0.94012	0.07207	0.02923	15	0.00007
20	0.29759	0.10168	-0.31339	-0.54799	0.06345	0.05074	15	0.00015
21	0.19131	0.38747	-0.25494	-0.74192	0.06374	-0.01493	15	0.00014
22	0.11505	0.24985	-0.24667	-0.65598	0.06365	-0.01199	15	0.00021

2.5. Objective function and optimization

Having already defined our key-points, now we need to specify how they will be mathematically introduced in the objective function. For temperature and pressure values such as those of Table 2, in order to neutralize the arbitrary choice of units and trying to avoid weight factors, we decided to use the square of the relative deviation for the corresponding term in the objective function, which is a natural choice and common practice in defining objective functions.

At the beginning we did the same (relative differences) for composition key-points, such as those in the third and fourth column of Table 3, using CO₂ mole fractions, but soon realized that each compositional point should count for two, considering terms for both compound 1 and compound 2 (the alkane in this case) in order to give also a reasonable weight to phases rich in CO₂. Moreover, for composition points we have observed that using squares of relative deviations gave too much weight to those terms accounting for deviations in the n-alkane mole fraction when it is of the order or around 10^{-3} or smaller, in detriment of the representation of the other points, specially the critical line. On the other hand, if we define objective function terms as the square of the absolute difference between the calculated and experimental mole fractions, then we do not penalize properly the objective function for the cases of important relative errors in CO2 rich phases. We finally found that using the square of the absolute difference divided by the experimental value led to a proper balance in the objective function and allowed us to achieve the results presented in this work.

Therefore, the objective function (OF) takes the following form:

$$OF = \sum_{i=1}^{5} \left(\frac{KP_i^{calc} - KP_i^{exp}}{KP_i^{exp}} \right)^2 + \sum_{j=1}^{Nz} \left[\frac{(z_{j,1}^{calc} - z_{j,1}^{exp})^2}{z_{j,1}^{exp}} + \frac{(z_{j,2}^{calc} - z_{j,2}^{exp})^2}{z_{j,2}^{exp}} \right]$$
(7)

where KP_i is a temperature or pressure key-point [there are four critical key points (Table 2) plus a $T_{\rm UCEP}$ key point (Table 3)] and the mole fractions $z_{j,1}$ and $z_{j,2}$ correspond to a compositional key-point in Table 3 or to two-phase equilibrium compositions (Table 4) when they are used. For a given binary $\rm CO_2 + n$ -alkane system, the total number of compositional points Nz will then be five (from Table 3) plus the number of phase compositions to be considered from specific two-phase points.

To fix ideas, note that the objective function for each system using only the key-points given in Tables 2 and 3 will contain 15 terms (since a given compositional key point of Table 3 contributes with two terms to the objective function OF), while two extra terms will be added per each phase composition of two-phase equilibrium points (eight phases, contributing with 16 terms, when considering

Table 4 for C16, leading to a total count of 31 terms in the objective function OF).

2.6. Phase equilibrium calculations

All calculated values required by the objective function were obtained using a reduced and adapted GPEC algorithm [25]. The numerical continuation methods used to generate the different lines involved and the set of equations for each specific type of calculation are described elsewhere [44–46]. Predicted global keypoints (see Section 2.4 and Tables 2 and 3) were detected while following the calculation of the main critical line and the LLV line according to the general scheme illustrated by Fig. 1 in [45]. Biphasic calculations for single *T*, *P* specifications (see Table 4) were performed solving the following reduced set of equations like described in [44]:

$$X = \begin{bmatrix} \ln x_1 \\ \ln y_2 \\ \ln v_x \\ \ln v_y \end{bmatrix}; \quad F = \begin{bmatrix} \ln P_x(x, T, v_x) - \ln P \\ \ln P_y(y, T, v_y) - \ln P \\ \ln \hat{f}_1^x(x, T, v_x) - \ln \hat{f}_1^y(y, T, v_y) \\ \ln \hat{f}_2^x(x, T, v_x) - \ln \hat{f}_2^y(y, T, v_y) \end{bmatrix} = 0$$
(8)

where X is the vector of independent variables and F = 0 is the set of equations to solve. Experimental values were used as initial estimates for the phase mole fractions (x and y) and initial v_x and v_y molar volume values were obtained by solving the pressure equation at the specified T and P. The system of Eq. (8) accounts for the uniformity of temperature, pressure and component fugacities throughout the two phase system under equilibrium conditions.

Phase diagrams shown in Section 3 were also generated with GPEC [26]. Pxy and Txy diagrams are organized in regions, which are calculated after identifying the limiting points of such regions, as a number of intersections between a straight line corresponding to the specified temperature or pressure [44] and the

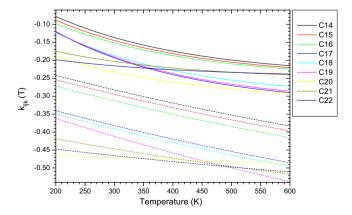


Fig. 4. Behavior of the interaction parameters k_{112} (solid lines) and k_{122} (dashed lines) as a function of temperature, according to Eq. (6) and Table 5, for the nine CO₂ (1) + n-alkane (2) systems studied.

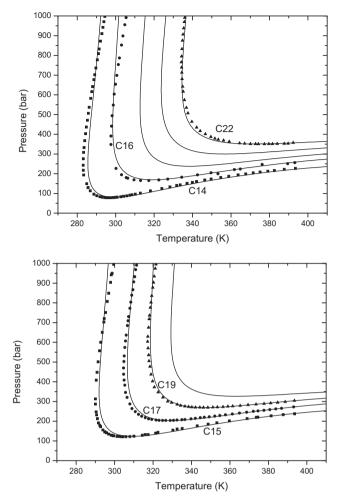


Fig. 5. Critical lines for CO_2 + n-alkane binary systems with type III phase behavior. Even and odd carbon number systems in the upper and bottom part respectively. References for data points are given in Table 2. Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

univariant lines of the global phase equilibrium diagram (i.e., LLV, critical, azeotropic or pure-compound vapor-liquid lines in the pressure-temperature space).

3. Results

We first conducted minimizations for the system CO₂ (1)+n-hexadecane (2) using different initial sets of parameters, and leaving free either six or eight parameters. In the first case, T_{112}^* and T_{122}^* were kept at constant values. We found that $T_{112}^*=230\,\mathrm{K}$ and $T_{122}^*=1100\,\mathrm{K}$ led to the minimum value for the objective function OF, which was – as expected – more influenced by the other six constants for each system: I_{112} , I_{122} , I_{112} , I_{122} , I_{112} , and I_{112}^* . We therefore decided to keep those constant I_{112}^* values for all the systems and proceeded to the minimization with six parameters in each case.

Table 5 shows the final interaction parameter sets for the nine systems studied, with the n-alkane varying from C14 to C22. These are the CMR parameters that, using the RK-PR EoS with pure compound parameters from Table 1, gave in each case the minimum value for the objective function OF defined in Section 2.5. The relatively high value in the objective function OF for C16, when compared to the other systems, is naturally explained by the extra terms involving the data in Table 4, which are not present for the rest. On the contrary, the higher values for C15 and specially C14 might be explained by more extreme shapes of the highly non-

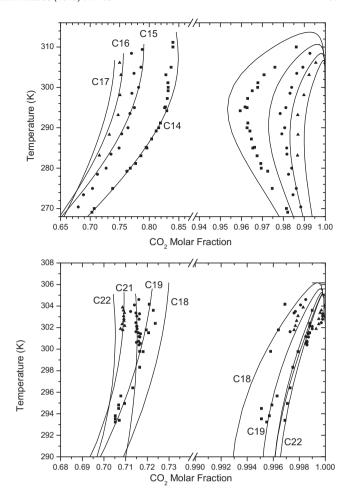
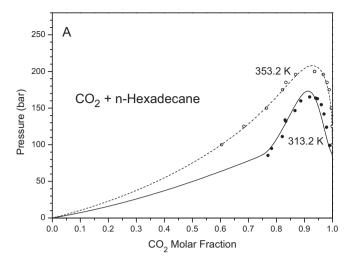


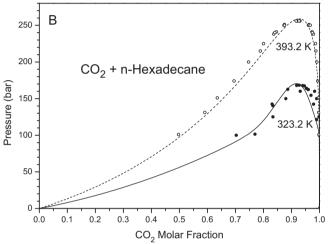
Fig. 6. Branches of the LLV equilibrium lines for $CO_2 + n$ -alkane binary systems with type III phase behavior. Data points taken from van der Steen et al. [38] (C14–C15–C16), Hottovy et al. [39] (C14–C15) and Fall et al. [40] (C19–C20–C21). Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

linear critical lines (and very low CPm), related to the proximity to type IV phase behavior, which is observed for C13 with CO₂.

Note that all k' values are positive, which means that all k functions decrease with temperature, as it can be observed in Fig. 4. Also notice that all k^{∞} are negative, while the repulsive interaction parameters (l_{112} and l_{122}) fall all in the range from -0.015 to 0.072. Moreover, some regular trends can be observed, specially among the first three systems.

Figs. 5 and 6 show the evolution of the global phase behavior along the series through calculated critical lines in the P-T space (Fig. 5) and through computed phase compositions along LLV lines in the temperature-composition space (Fig. 6). Note the high quality of the critical lines description both in the vapor-liquid and in the liquid-liquid regions, equivalent to or better than in previous attempts (see references in Section 1) but achieving simultaneously a good description of the composition of heavy phases under LLV conditions. The same is observed in Fig. 7, where Pxy diagrams of CO₂ + n-hexadecane are presented for different temperatures ranging from 313.2 to 573.2 K. Also in Fig. 8, with Txy diagrams for the same system and pressures between 100 and 250 bar, we see a good performance. The high correlation capability offered by the CMRs flexibility is therefore demonstrated through these modeling results for CO₂ + n-hexadecane, which may then be regarded as semi-predictive, since only a few but sufficient, consistent and carefully selected, experimental data points, covering wide ranges





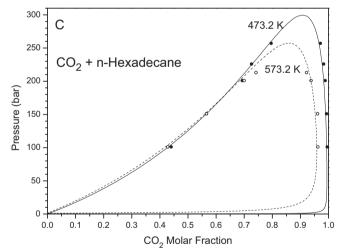


Fig. 7. Prediction of Pxy diagrams for the system CO_2 + n-hexadecane at six different temperatures, and comparison to data from Nieuwoudt et al. [49] (313.2 and 323.2), Pöhler [42] (323.2 K), Kordikowski and Schneider [43] (353.2), Spee and Schneider [48] (393.2) and Brunner et al. [41] (473.2 and 573.2 K). Only points for two pressures at 393.2 K and two pressures at 573.2 K were considered in the parameter fitting process (see Table 4). Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

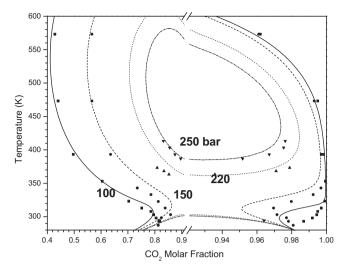


Fig. 8. Prediction of the Txy diagrams for the system $CO_2 + n$ -hexadecane at four different pressures, and comparison to data from Scheidgen [37] (100 and 150 bar), Brunner et al. [41] (100 and 150 bar), Pohler [42] (220 bar) and Spee and Schneider [48] (100, 150 and 250 bar). Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

of temperature and pressure, have been considered for building the objective function.

On the other side, the predictions presented in Figs. 9 and 10 for the binaries with C19 and C20 seem to suffer from some systematic deviations with respect to experimental data, particularly in the heavy phase. This is clearly a consequence of not having included two phase equilibrium points besides critical line and LLV information for these systems. The result is a good matching of the critical pressure while underestimating the composition range in which phase separation occurs at lower pressures. This is a wellknown behavior for analytical equation-of-state-type models not accounting for long range fluctuations in the critical region. Still, the results obtained for CO₂ + n-hexadecane in Fig. 7 show that CMRs make possible to achieve a much better overall agreement, between the model and the experimental data, when both critical point and phase equilibrium information are considered. And, when looking at the behavior in a wider temperature range, like in the Txy diagram shown in Fig. 11, we see that the predictions obtained in this work are already quite acceptable for systems like

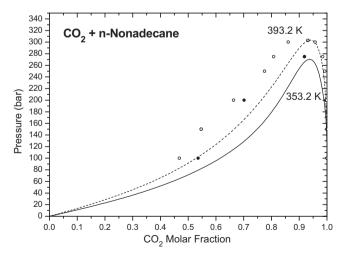


Fig. 9. Prediction of the Pxy diagrams for CO_2 + n-nonadecane at 353.2 K (solid line) and 393.2 K (dashed line), and comparison to data from Kordikowski and Schneider [43]. Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

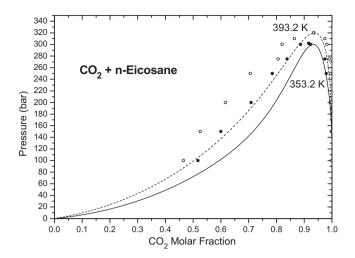


Fig. 10. Prediction of the Pxy diagrams for $CO_2 + n$ -eicosane at 353.2 K (solid line) and 393.2 K (dashed line), and comparison to data from Kordikowski and Schneider [43]. Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

 CO_2 + n-nonadecane, with parameters regressed from only a few selected critical line and LLV points.

The only clear systematic deviation that can be observed for different systems when comparing calculations to experimental data, including $CO_2 + n$ -hexadecane, is in the composition of the light liquid phases along the LLV range for the cases of C14, C15 and C16 (Fig. 6). And still the magnitude of that error, which appears magnified by the scale in the figure, is not very important for the CO_2 mole fractions. Note that these deviations appear to be expressed with more clarity for $CO_2 + n$ -tetradecane, the system which is closest to show a double critical end point (which would mark the transition to Type IV) and could therefore be related to the common limitations of analytical models in near-critical regions, which could possibly be overcome by implementing a crossover approach.

Although a deeper study of barotropic and/or isopycnic behavior is beyond the scope of the present work, we show in Fig. 12 the predicted densities for the three phases along LLV equilibrium for $\rm CO_2+n$ -hexadecane and we also show the corresponding experimental data. The quality of the predictions both for the vapor and for the alkane-richer liquid phases is remarkable considering that no

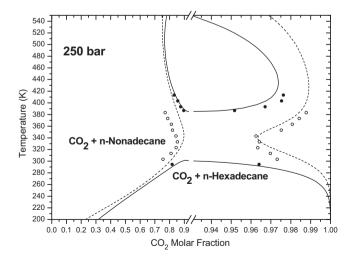


Fig. 11. Prediction of the Txy diagrams for CO_2 +n-hexadecane (solid line) and CO_2 +n-nonadecane (dashed line) at 250 bar, and comparison to data from Spee and Schneider [48] and Kordikowski and Schneider [43]. Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

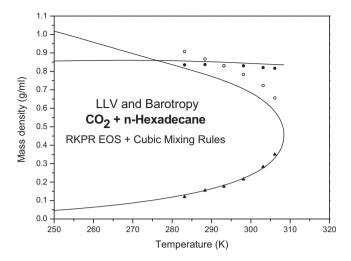


Fig. 12. Prediction of density and barotropy along the LLV equilibrium region for CO₂ + n-hexadecane, and comparison to data (markers) from van der Steen et al. [38]. Lines were calculated with the RK-PR EOS coupled with CMRs and parameters from Tables 1 and 5.

mixture density data has been considered as input for the present study. Nevertheless, there is a 10% underestimation of the CO_2 -richer liquid density. This could be related, at first sight, to the error in composition for the same phase, which can be observed in Fig. 6 and was referred in the previous paragraph. Actually, it is more the consequence of the underestimation of pure CO_2 saturated liquid densities in the temperature range considered. We expect an improvement in the description of CO_2 -rich liquid phases (and, consequently, also in barotropy temperatures) if the CO_2 parameters in Table 1 are modified in order to match the saturated liquid density, not at the triple point (216.6 K) but at a higher temperature.

In summary, we can see that the results obtained through the automated procedure for parameter fitting proposed in this work, based on a judicious definition of the objective function, led to significant improvements in the representation of phase behavior of $\text{CO}_2 + \text{n-alkane}$ binary systems, both when comparing to our previous preliminary studies and to other authors approaches.

The reader might tend to believe that this good representation of phase behavior for complex binary systems could be ascribed, at first sight, only to the added mathematical flexibility obtained from the greater number of available interaction parameters for CMRs, when compared to QMRs. Nevertheless, note that, although a strictly rigorous theoretical basis for the CMRs might not be found, it is generally accepted that molecular interactions between two given types of molecules can be different, in terms of both geometrical arrangements and energetically, depending on the concentration of the mixture, especially when comparing the opposite limits of infinite dilution. And, as already pointed out in Section 1, that is exactly what the CMRs interaction parameters account for, i.e., they affect independently the properties of compound A infinitely diluted in B, and those corresponding to B infinitely diluted in A. It is also important to stress that, in this work, we have used CMRs for both, the mixture attractive parameter, and the mixture co-volume (repulsive) parameter. Thus, we have accounted for the differences existing for the opposite limits of infinite dilution not only with regard to the attractive forces but also with respect to the repulsive forces, which, as quite generally accepted, significantly affect the thermodynamic properties of dense fluids.

4. Conclusions

In this work we have demonstrated that, in combination with temperature dependent attractive interaction parameters, the flexibility that cubic mixing rules offer with respect to composition, in comparison to the classical quadratic mixing rules, can be used to accurately represent the phase equilibria of highly asymmetric binary mixtures showing type III phase behavior, like $CO_2 + n$ -alkanes, and in the full ranges of temperature and pressure available.

In our study the objective function for the optimization of parameters used four critical line key-points and six LLV key-points for each system. In addition, it also included a few carefully selected two-phase points only for CO₂ + n-hexadecane, the system with more complete experimental information available. From the results we draw the following conclusions for CO₂ + n-alkanes binary mixtures showing type III phase behavior (C14 to C22):

- (1) The cubic mixing rules (CMRs), used for both, the attractive and the repulsive mixture parameters, together with temperaturedependent interaction parameters, coupled to the RK-PR EoS, made it possible to achieve the best simultaneous representation of critical lines and LLV equilibria that, to our knowledge, has ever been reported, irrespective to the modeling approach used, in the open literature.
- (2) Equivalent accuracy is not guaranteed for predictions of liquid-vapor equilibrium, specially at higher temperatures, if no representative points are considered for the optimization.
- (3) A correct and accurate overall description of the phase behavior is possible through a proper balance in the objective function, that combines critical line and LLV information with representative two-phase data points, as it was done for CO₂ + n-hexadecane in this work.

From these conclusions and from the experience we gained in the present study, a predictive correlation will be developed in a new work, which we expect will provide complete results for the whole series as good as those presented for CO_2 + n-hexadecane in this work.

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