



RESEARCH NOTE

REVISED Optimal threshold estimation for binary classifiers using game theory [version 3; referees: 3 approved]

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Abstract

Many bioinformatics algorithms can be understood as binary classifiers. They are usually compared using the area under the receiver operating characteristic (ROC) curve. On the other hand, choosing the best threshold for practical use is a complex task, due to uncertain and context-dependent skews in the abundance of positives in nature and in the yields/costs for correct/incorrect classification. We argue that considering a classifier as a player in a zero-sum game allows us to use the minimax principle from game theory to determine the optimal operating point. The proposed classifier threshold corresponds to the intersection between the ROC curve and the descending diagonal in ROC space and yields a minimax accuracy of 1-FPR. Our proposal can be readily implemented in practice, and reveals that the empirical condition for threshold estimation of “specificity equals sensitivity” maximizes robustness against uncertainties in the abundance of positives in nature and classification costs.

Keywords

Binary classifier, ROC curve, accuracy, optimal threshold, optimal cutoff, class imbalance, game theory, minimax principle.



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REVISED version 2 published 15 Dec 2016		↑	? report
version 1 published 25 Nov 2016	✓ report	✓ report	

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Comments (1)

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Competing interests: No competing interests were disclosed.

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REVISED Amendments from Version 2

We have prepared a revised version of the article that aims at answering the concerns raised by the reviewers Brun and ten Have.

1. Unspecified bioinformatics context that is never specified.
Context is provided in part by references 5 and 7, for example. A deeper review and/or discussion in terms of pattern recognition is out of the scope of this short note.
2. The problem studied in this article is the one where the classifier model is already defined.
We have modified the first discussion paragraph accordingly.
3. ROC curves used for comparison, not training of classifiers.
We have modified the abstract and the second introduction paragraph accordingly.
4. The assumption on $a=d=1, c=b=0$ could start earlier.
We would rather keep the current, more general, formulation and use the assumption only for our particular analysis.
5. Mathematical proof of the minimax threshold $FPR+TPR=1$
We have modified the last results paragraph accordingly.
6. Equation 1 uses q_n , which is only defined later.
We have modified the third introduction paragraph accordingly.
- 7 and 8. Generality of the result.
As shown in reference 4, section 2.2, the values of a, b, c and d represent the relative importance of positives and negatives in a given context, regardless of the source of the skew. Therefore, it is sufficient to study the effect of q_P in the case $a=d=1, c=b=0$.
9. Discrete versus continuous ROC curve.
We have modified the last results paragraph accordingly.
10. Utility in a zero-sum game vs. other performance measures.
We have modified the first discussion paragraph accordingly.

See referee reports

Introduction

Many bioinformatics algorithms can be understood as binary classifiers, as they are used to investigate whether a query entity belongs to a certain class¹. Supervised learning trains the classifier by looking for the rule that gives the correct answers to a training set of question-answer pairs. On the other hand, score-based binary classifiers are trained in a non-supervised manner. Such classifiers use a scoring function that assigns a number to the query. During training, the scoring function is modified to give different scores to the positives and negatives in the training set. After training, the classifier is used by assigning a query to the class under consideration if its score surpasses a threshold. A minority of users is able to choose a threshold using their understanding of the algorithm, while the majority uses the default threshold.

Binary classifiers are often compared under a unified framework, the receiver operating characteristic (ROC) curve². Briefly, classifier output is first compared to a training set at all possible classification thresholds, yielding the confusion matrix with the number of true positives (TP), false positives (FP), true negatives (TN) and false negatives (FN) (Table 1). The ROC curve plots the true positive rate ($TPR = TP/(TP + FN)$), also called sensitivity, against the false positive rate ($FPR = FP/(FP + TN)$), which equals 1-specificity)

(Figure 1, continuous line). Classifier model selection often aims at maximizing the area under the ROC curve, which amounts to maximizing the probability that a randomly chosen positive is ranked before a randomly chosen negative³. This summary statistic measures performance without committing to a threshold.

Practical application of a classifier requires using a threshold-dependent performance measure to choose the operating point^{1,3}. This is in practice a complex task because the application domain may be skewed in two ways⁴. First, for many relevant bioinformatics problems the prevalence of positives in nature $q_p = (TP + FN)/(TP + TN + FP + FN) = 1 - q_n$ does not necessarily match the training set q_p and is hard to estimate^{2,5}. Second, the yields (or costs) for correct and incorrect classification of positives and negatives in the machine learning paradigm ($Y_{TP}, Y_{TN}, Y_{FP}, Y_{FN}$) may be different from each other and highly context-dependent^{1,3}. Points in the ROC plane with equal performance are connected by iso-yield lines with a slope, the skew ratio, which is the product of the class skew and the yield skew⁴:

$$SKEW\ RATIO = \frac{q_N \cdot (Y_{FP} + Y_{TN})}{q_P \cdot (Y_{TP} + Y_{FN})} \tag{1}$$

The skew ratio expresses the relative importance of negatives and positives, regardless of the source of the skew⁴. Multiple

Table 1. Confusion matrix for training of a binary classifier. TP: Number of true positives. FP: Number of false positives. FN: Number of false negatives. TN: Number of true negatives.

		Training set	
		p	n
Classifier output	p'	TP	FP
	n'	FN	TN

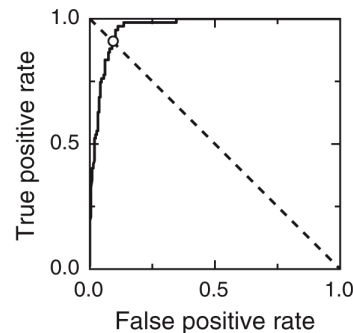


Figure 1. Optimal threshold estimation in ROC space for a binary classifier using game theory. The descending diagonal $TPR = 1 - FPR$ (dashed line) minimizes classifier performance with respect to q_p . The intersection between the receiver operating characteristic (ROC) curve (continuous line) and this diagonal maximizes this minimal, worst-case utility and determines the optimal operating point according to the minimax principle (empty circle).

threshold-dependent performance measures have been proposed and discussed in terms of skew sensitivity^{3,4}, but often not justified from first principles.

Theory

Game theory allows us to consider a binary classifier as a zero-sum game between nature and the classifier⁶. In this game, nature is a player that uses a mixed strategy, with probabilities q_p and $q_n=1-q_p$ for positives and negatives, respectively. The algorithm is the second player, and each threshold value corresponds to a mixed strategy with probabilities p_p and p_n for positives and negatives. Two of the four outcomes of the game, TP and TN , favor the classifier, while the remaining two, FP and FN , favor nature. The game payoff matrix (Table 2) displays the four possible outcomes and the corresponding classifier utilities a , b , c and d . The *Utility* of the classifier within the game is:

$$UTILITY = \frac{aTP + dTN + bFP + cFN}{TP + TN + FP + FN} \quad (2)$$

The payoff matrix for this zero-sum game corresponds directly to the confusion matrix for the classifier, and the game utilities a , b , c , d correspond to the machine learning yields Y_{TP} , Y_{FP} , Y_{FN} , Y_{TN} respectively (Table 1). In our definition of the skew ratio, the uncertainty in the values of a , b , c and d is equivalent to the uncertainty in the values of q_p and q_n ⁴. Thus, we can study the case $a=d=1$ and $b=c=0$ without loss of generality⁴. Classifier *Utility* within the game then reduces to the *Accuracy* or fraction of correct predictions²⁻⁴. In sum, maximizing the *Utility* of a binary classifier in a zero-sum game against nature is equivalent to maximizing its *Accuracy*, a common threshold-dependent performance measure.

We can now use the *minimax* principle from game theory⁶ to choose the operating point for the classifier. This principle maximizes utility for a player within a game using a pessimistic approach. For each possible action a player can take, we calculate a worst-case utility by assuming that the other player will take the action that gives them the highest utility (and the player of interest the lowest). The player of interest should take the action that maximizes this minimal, worst-case utility. Thus, the *minimax* utility of a player is the largest value that the player can be sure to get regardless of the actions of the other player. In our case, nature is not a conscious player that chooses the action that gives them the highest utility. We instead understand our application of the minimax principle as the consideration of a worst-case scenario for the skew ratio.

In our classifier *versus* nature game, *Utility/Accuracy* of the classifier is skew-sensitive, depending on q_p for a given threshold^{3,4}:

$$UTILITY = 1 - FPR + q_p \cdot (FPR + TPR - 1) \quad (3)$$

For a convex *ROC* curve in which *TPR* increases as *FPR* increases, the derivative of the *Utility* with respect to q_p is zero along the $TPR = 1 - FPR$ line in *ROC* space (Figure 1, dashed line). The derivative is negative below this line and positive above it, indicating that points along this line are minima of the *Utility* function with respect to the strategy q_p of the nature player. According to the *minimax* principle, the classifier player should operate at the point along the $TPR = 1 - FPR$ line that maximizes *Utility*. In *ROC* space, this condition corresponds to the intersection between a continuous *ROC* curve and the descending diagonal (Figure 1, empty circle) and yields a *minimax* value of $1 - FPR$ for the *Utility*. It is worth noting that this analysis regarding class skew is also valid for yield/cost skew⁴.

Discussion

We showed that binary classifiers may be analyzed in terms of game theory. From the *minimax* principle, we propose a criterion to choose an operating point for the classifier that maximizes robustness against uncertainties in the skew ratio, i.e., in the prevalence of positives in nature and in yield skew, i.e., the yields/costs for true positives, true negatives, false positives and false negatives. This can be of practical value, since these uncertainties are widespread in bioinformatics and clinical applications. However, it should be noted that this strategy assumes that a score optimized for a restricted training set is of general validity. Future studies may apply the minimax principle to optimization of the classifier model and to classifier comparison using other performance measures.

In machine learning theory, $TPR = 1 - FPR$ is the line of skew-indifference for *Accuracy* as a performance metric⁴. This is in agreement with the skew-indifference condition imposed by the *minimax* principle from game theory. However, to our knowledge, skew-indifference has not been exploited for optimal threshold estimation. Furthermore, the operating point of a classifier is often chosen by balancing sensitivity and specificity, without reference to the rationale behind⁷. Our game theory analysis shows that this empirical practice can be understood as a maximization of classifier robustness.

Table 2. Payoff matrix for a zero-sum game between nature and a binary classifier.

a : Player I utility for a true positive. b : Player I utility for a false positive. c : Player I utility for a false negative. d : Player I utility for a true negative.

		Player II: Nature	
		p	n
Player I: Classifier	p'	a	b
	n'	c	d

Competing interests

No competing interests were disclosed.

Grant information

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Version 3

Referee Report 16 February 2017

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The authors addressed properly the concerns raised in our previous review.

Competing Interests: No competing interests were disclosed.

We have read this submission. We believe that we have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Referee Report 08 February 2017

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Competing Interests: No competing interests were disclosed.

I have read this submission. I believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Version 2

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The author presents an interesting solution to the problem of selecting the best threshold for a binary classifier which defines a bioinformatics algorithm, when the proportion of positive and negative samples in nature is unknown. His approach consists on using the minimax approach, considering that the goal is to maximize the gain/accuracy (in the specific the case where the yields are 1 for TP and TN, and 0 for FP and FN) in a worst case scenario. For that, the author describes the utility as a function of both the threshold and the nature proportion of negatives q_n .

Based on the analysis of page 3, given any action of the player (a point in the ROC curve, defined by a threshold), its worst performance (lower utility) will be obtained for some q_n value. The idea is to maximize this minimal, across all possible actions (pairs of FPR,TPR across the ROC curve). This is obtained when the point in the ROC complies with $TPR+FPR=1$.

The article is original in the sense that it proposes a valid requirement for the design, to be robust against the unknown state of nature (proportion of positives and negatives), deriving a threshold selection that attains that condition ($FPR+TPR=1$). Despite the originality of the approach, the article needs minor revisions. In particular it seems the manuscript deals with aspects of pattern recognition from the perspective of Bioinformatics. Although understandable, this is a pattern recognition problem and the work would improve significantly when the role of ROC curves on classifier design, and the mathematics leading to the main result are explained with more detail and improved formalization.

Below follows a more detailed list of issues that need to be addressed:

1. The author presents this article in a bioinformatics context that is never specified. For example, in the introduction the authors says "Many bioinformatics algorithms can be understood as binary classifiers, ...", and then refers to "score based binary classifiers". At no part of the article the author provides a list, or some examples, of such algorithms in bioinformatics. Since this is presented as a bioinformatics article, it would be good to include some of such algorithms, which surely were the inspiration for this work. Alternatively, this might be presented in the more mathematical setting of pattern recognition, although this might require more profound changes.
2. Also, it is clear that the problem studied in this article is the one where the classifier model is already defined, producing one ROC curve, and the only adjusting parameter the user has is the threshold. Although this is a rather typical solution in computational biology, it should be mentioned that if the user were able to adjust the classifier, better results might be obtained. There are many references in literature of robust classifier design, some are indicated below.
3. The author should review the statement that ROC curves are often being used for the training of classifiers. The training of classifiers is usually done by minimization or maximization of quality metrics, via the adjustment of the classifier parameters, once the model is defined. Few works are related to training classifiers based on ROC (Some examples are Blockeel, 2002¹ and Srinivasan, 2001²). On the other hand, classifier evaluation (after training) and model selection are often done via ROC curves.

For example, in the second paragraph of the introduction, the author comments that "Binary

classifiers are often trained and compared under ... the ROC curve", presenting a reference on the ROC curve, but not to classifier training. Here the term "training" may be confusing, since it is used, usually, for the process of selecting the parameters of the classifiers, from the data, once the model is already selected³. Usually the ROC is used for model selection, where different classifier models are trained (without considering the ROC), and then compared based on their ROC, as described in the reference 2 of the paper.

Based on the previous comment, the author should also review the sentence, in the same paragraph, where he states "Classifier training often aims at maximizing the area under the ROC". Actually, the training aims, usually, to minimize error, or cost, or other measures of accuracy. Reference 4 of the article, in the first paragraph of the introduction, also makes clear the difference between model building (training), and model evaluation, where the ROC is used.

4. In general, the assumption on $a=d=1$, $c=b=0$ could start earlier, simplifying the concepts and equations 1 and 2.
5. The mathematical proof that the minimax threshold is obtained by $FPR+TPR=1$ requires some elaboration. In one hand, given a classifier trained from data, with a variable threshold t , both FPR and TPR are functions of the threshold, so they would be $FPR(t)$ and $TPR(t)$. From this, the utility is dependent of two variables, q_n and t , so it would be $Utility(q_n, t)$. Now, the problem of finding a minimax value of t would be a bit more complex than the solution described in the article. Still more, one should impose the restriction on the curve $(TPR(t), FPR(t))$ to be increasing, so that if $t_2 \geq t_1$, then $TPR(t_2) \geq TPR(t_1)$ and $FPR(t_2) \geq FPR(t_1)$. If such condition is held (which is expected on a properly designed ROC curve), then the proof that $FPR(t)+FNR(t)=1$ is the minimax solution is almost straightforward.

Without that condition defined above (which is not defined in the paper), one could have a pair $(0.8, 0.2)$ which complies with $FPR+TPR=1$ and $(0.81, 0.18)$ that does not comply with that rule, and where the minimum utility (as function of q_n) for the first pair is 0.8, and for the second pair is 0.81, which disagree with the mathematical result presented in the paper. The key here is the increasing nature of the ROC curve. An increasing ROC curve (where TPR increases when FPR increases) could not contain these two points, since an increase in TPR (0.8 to 0.81) should be accompanied by an increase on the FPR (but it goes from 0.2 to 0.18).

6. Equation 1 uses q_n , which is only defined later, after the equation.
7. The author presents the work in the general context of zero-sum game, with general yield values, but for the main theoretical result, the problem is reduced to the specific situation of $a=d=1$ and $b=c=0$. Therefore, the result is not general, only specific to that situation, so it is a little superfluous to maintain all these generic yield values across the paper. For example, Equation 1, when using the costs $a=d=1$, $c=b=0$, studied in the theory section, reduces to skew ratio = q_n/q_p , which is more informative for the rest of the paper.
8. In the discussion the author talks about maximizing robustness, but actually the goal is to design "a robust classifier"⁴. The discussion section also states that the robustness is obtained against a) skew ratio and b) yield skew. This last part (b) is not proved in the paper, since the theoretical results show a minimax results (robustness) against skew ratio, for the specific case of $a=d=1$ and $b=c=0$.

It seems true that no other methods for choosing the operating point present a good rationale beyond mathematical considerations. To strengthen the impact I suggest the author should at least name some of such approaches, like the three ones described by Song, 2014.

9. In a situation of continuous ROC curve, this point should always exist, since it is an increasing curve from (0,0) to (1,1). In the discrete ROC case, which is the usual one when the classifier and the ROC are based on a finite amount of data, this intersection may not occur, and the thresholds may have to be selected using an appropriate interpolation technique. This needs to be clarified.
10. Finally there is a question about the approach. Despite the theoretical attractiveness of the proposed approach, it is not clear how the maximization of expected utility is a desirable quality for a classifier being used in bioinformatics. There is a lot of study and discussion about whether is it better to optimize accuracy, precision, recall, etc, and how each application may require a different goal, but there is not so much discussion about why a classifier should maximize utility in a zero-sum game. The author could address this issue, with a brief statement on the advantages of this measure (the utility) in the context of bioinformatics.

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Competing Interests: No competing interests were disclosed.

We have read this submission. We believe that we have an appropriate level of expertise to confirm that it is of an acceptable scientific standard, however we have significant reservations, as outlined above.

Version 1

Referee Report 07 December 2016

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Luis Diambra 

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The author presents a criterion to choose the operating point for a binary classifier. This criterion is analyzed in term of the game theory. By using the mininax principle author proposes to use as classifier threshold the intersection between the ROC curve and the descending diagonal in ROC space. This operating point for the classifier could maximizes the robustness against some bias in the training set. I

found some novelty in the fact to consider such bias for an optimal threshold estimation. The paper is well written and organized but I think also that it could be improved by incorporating some general considerations that helping readers to a better understanding of the problem and the present proposition [1,2].

In the binary classification problem one is trying to deduce the answers to new questions, rather than just recall the answers to old ones. In order to do that we need to train the classifier from question-answer pairs (the training set). This is called supervised learning, because it requires a teacher, knowing the rule, which gives the correct answer to the example questions. In the case here, the author consider score-based binary classifiers, which does not need such learning stage. Could the author put the problem in the context supervised vs. no-supervised?

In the supervised learning context the classifier threshold is a parameter that is found during the learning stage. Training the classifier maximizing the area under ROC curve is an strategy for the classifier learn the training set. Consequently, the proposed strategy could be considered as a "learning rule". However, the performance over new examples is not guaranteed. Other point which can improve the manuscript would be to consider the ability of generalization of the proposed strategy. Could the author add a discussion in this sense?

I believe that this manuscript is of an acceptable scientific standard, and that it will be of interest to a wide audience; however, the manuscript could be revised, as outlined above.

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I have read this submission. I believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Referee Report 06 December 2016

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Pieter Meysman 

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The article by Ignacio Enrique Sanchez concerns a common problem in machine learning, namely the selection of the optimal classification threshold, and provides a mathematical solution based on the principles of game theory. The main concern of the article deals with the unknown distribution of positive and negative samples in the 'real world' or 'nature', thus beyond the provided training data set. The provided derivation is very elegant, and luckily for those researchers in the field the solutions turns out to be to select a threshold where sensitivity and specificity are equal in the training data set.

The biggest concern from the perspective of game theory is that 'nature' is not a conscious agent, and

thus will not mischievously choose a positive/negative fraction where the classifier will perform the worst. However as stated in the article, this is to simulate the worst case scenario. However this also means that the threshold calculation may only be optimal in this worst case scenario, but suboptimal in all other cases. It is therefore still not the final word in threshold optimisation, and still leaves machine learning researchers the flexibility to choose other thresholds.

However I do have a minor comment on the derivation, that I expect can be addressed with small clarifications to the text:

1. The *Accuracy* equals the *Utility* as defined by the payoff matrix in the specific case $a=d=1$ and $b=c=0$, which is stated without a loss in generality. However in my understanding, this step makes the assumption that the cost for a false negative and the cost for a false positive is equal, which may not be the case for all classifiers. Thus it is unclear if this specific case can be transposed to all classifiers in general.

Competing Interests: No competing interests were disclosed.

I have read this submission. I believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Discuss this Article

Version 1

Reader Comment 12 Dec 2016

Matúš Kalaš, Computational Biology Unit, Department of Informatics, University of Bergen, Norway

Just a note, perhaps an interesting complement is the article [Saito & Rehmsmeier 2015](#) and website [Classifier evaluation with imbalanced datasets](#).

Competing Interests: No competing interests were disclosed.

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