Comparison of Different Techniques for Tropospheric Wet Delay Retrieval Over South America and Surrounding Oceans

A. Calori, G. Colosimo, M. Crespi, and M.V. Mackern

Abstract

Water vapour (WV) plays a fundamental role in several weather processes that deeply influence human activities. Satellite based radiometers, Ground based Global Navigation Satellite Systems (GNSS) and Numerical Weather Models (NWM) permit to obtain either measurements or estimates or forecasts of WV. This work presents a 2 years systematic comparison to address the agreement on the tropospheric wet delay retrieved by the three mentioned independent techniques over permanent stations belonging to SIRGAS (Sistema de Referencia para las Américas) GNSS network. SIRGAS tropospheric total delay estimations are compared with the official International GNSS Service (IGS) ones, with the measurements from the Jason-1 satellite radiometer (JMR) in terms of Zenith Wet Delays (ZWD) and, finally, with the ZWD computed from ERA Interim, the last reanalysis dataset from the European Center for Medium-Range Weather Forecasts (ECMWF). All the differences between the techniques, which were considered in order to yield a reliable comparison, are discussed. The statistical results of mean (μ), standard deviation (σ) and correlation (ρ), show that the highest agreement is reached between SIRGAS and IGS products ($\mu = -0.5$ mm, $\sigma = 5.6$ mm, $\rho = 0.98$), whereas slightly worse values are obtained in the comparisons with the JMR measurements ($\mu = -7.4$ mm, $\sigma = 15.4$ mm, $\rho = 0.91$), and the ERA Interim data ($\mu = -1.5 \text{ mm}, \sigma = 16.6 \text{ mm}, \rho = 0.91$).

Keywords

GNSS • Jason-1 radiometer • Numerical Weather Model • SIRGAS • ZWD retrieval

1 Introduction

Water Vapour (WV) plays a fundamental role in several weather processes that deeply influence human activities and it has been recognised as the most important among the greenhouse gases (Mitchell 1989). Several studies have

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G. Colosimo • M. Crespi DICEA-Area di Geodesia e Geomatica, University of Rome "La Sapienza", Roma, Italy e-mail: gabriele.colosimo@uniroma1.it confirmed how deeply water vapour is bound to climate 6 changes, for instance by showing the high correlation 7 between the yearly temperature variation and the WV content 8 in the atmosphere (Wentz and Schabel 2000). It has been 9 clearly understood that the knowledge of high accurate WV 10 content and its distribution in the atmosphere improves short 11 term weather forecasts significantly. At the same time, WV 12 reveals very rapid changes both in the temporal and in the 13 spatial domains such that, at present, there are no theoretical 14 models that can reliably predict its behaviour. 15

Retrieving WV content in the atmosphere can be 16 performed in different ways using independent techniques: 17 starting from the more traditional and established ones, such 18 as radiosondes and ground-based microwave radiometers, up 19 to the more recent ones, such as satellite based techniques 20

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like satellite radiometers (Christensen et al. 1994), Global 21 Navigation Satellite Systems (GNSS) (Bevis et al. 1992), 22 Radio Occultation (Kursinski et al. 1997) and Numerical 23 Weather Models (NWM). Since each of these techniques 24 presents advantages and limitations, researchers' efforts have 25 been recently focused on comparing the different approaches 26 with the aim of combining them to retrieve WV content 27 with the highest possible accuracy. The issues addressed in 28 this work are related to the research activities promoted by 29 the International GNSS Service (IGS) Troposphere Working 30 Group. 31

Satellite based radiometers can provide integrated water 32 vapor (IWV) measurements at different epochs. However, 33 their application is limited over sea and ocean surfaces, 34 the revisit time on the same location is rather low and 35 reliable measurements are obtained only at certain weather 36 conditions (e.g., no rain). Ground based GNSS stations can 37 be used to estimate the signal delay caused by tropospheric 38 refraction (Hogg et al. 1981). This delay, which is referred 39 to as Zenith Total Delay (ZTD), can be unfolded into two 40 components: the Zenith Hydrostatic Delay (ZHD) and the 41 Zenith Wet Delay (ZWD), which are due to the contribution 42 of the hydrostatic gases and to the water vapour, respectively. 43 The GNSS technique has been proven capable of estimating 44 the ZTD and then using these estimates to infer the IWV 45 with accuracies of few millimetres (e.g., Rocken et al. 1997). 46 Moreover, thanks to its dense station networks and to the very 47 high temporal resolution of the estimates (up to few minutes) 48 the interest in GNSS as IWV data source is continuously 49 increasing. NWM, such as the European Center for Medium-50 Range Weather Forecasts (ECMWF), exploit data from many 51 different sources and can be used to compute and forecast 52 IWV all over the world with a medium-high temporal reso-53 lution (i.e., a few hours). 54

This work presents the results of a 2 years (i.e., June 55 2008-2010) comparison of the three described techniques 56 for the determination of the tropospheric wet delay ZTD 57 and the IWV over the South and Central American region. 58 Initially, in order to assess the performances of SIRGAS 59 estimations, the results were compared with the official 60 ZTD distributed by the IGS. Then, the consistency of the 61 products was evaluated with respect to: (1) ZWD measured 62 by Jason-1 satellite mission; (2) ZWD computed from data 63 of the ECMWF ERA-Interim reanalysis model. Following 64 this introductory section, Sect. 2 describes the main features 65 of the used techniques. The results from the comparison are 66 discussed in Sect. 3. Finally, conclusions and future research 67 prospects are outlined in Sect. 4. 68

Data Processing: Retrieving the ZTD from the Different Techniques

2.1 Ground Based GNSS Stations

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2.1.1 ZTD from the SIRGAS Network

SIRGAS-CON is the regional densification of the 73 International Terrestrial Reference Frame (ITRF) over 74 Latin America and Caribbean, it spans a huge extension 75 $-65^{\circ} < \phi < 20^{\circ}, -109^{\circ} < \lambda < -2^{\circ}$, with altitudes 76 up to 3.770 m and, at present, it encompasses about 250 77 continuously operating GNSS reference stations, 48 of them 78 belonging to the global IGS network (Brunini et al. 2012). 79

Within this research work, the site-specific ZTD_{SIR} were ⁸⁰ estimated for approximately 100 GNSS SIRGAS stations ⁸¹ (SIRGAS-CON-D-SUR) (Mackern et al. 2009) with a global ⁸² formal precision of few millimeters, as described in detail in ⁸³ Calori et al. (2013). Figure 1 shows the overall distribution ⁸⁴ of the used GNSS stations over the South American region. ⁸⁵

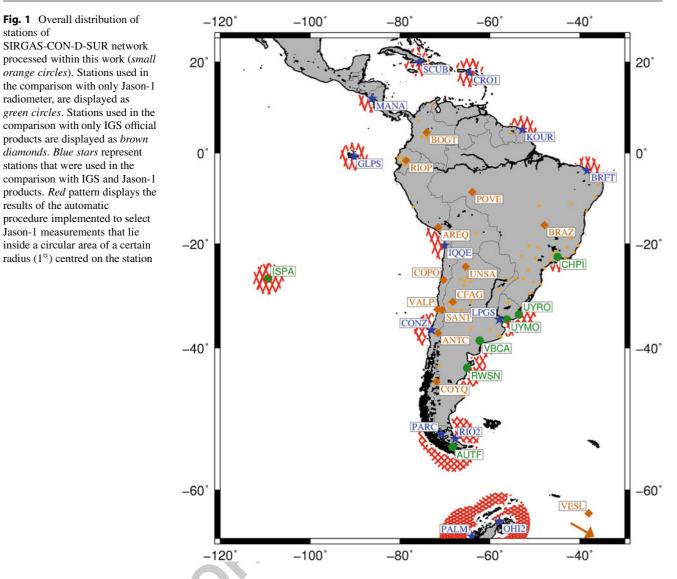
The main processing features which are relevant for the 86 next sections are as follows: 87

- Software: Bernese GPS Software 5.0 (Dach et al. 2009)— 88
 Differential positioning
 Elevation angle cutoff: 3°
- Mapping function: Niell (1996) for hydrostatic and wet 91 component 92
- A priori values: (Berg 1948; Saastamoinen 1973)
- Temporal resolution of ZTD estimates: 15 min (tropospheric gradients not estimated)
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2.1.2 IGS Tropospheric Products

Ever since 2003, a precise point positioning (PPP) approach 97 is used within IGS to estimate ZTD values using raw GPS 98 range measurements and the IGS Final Orbits and Clocks. 99 This process produces one file per site per day containing 100 a time series of ZTD with temporal resolution of 5 min 101 and a formal precision of few millimetres (Buyn and Bar-Sever 2009). The main processing features relevant for the 103 comparison are detailed: 104

- Software: GIPSY—Precise Point Positioning
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- Elevation angle cutoff: 7°
- Mapping function: Niell (1996) and GMF (Böhm et al. 107 2006) 108
- A priori values: Hydrostatic delay based on altitude (2.3 m 109 at sea level), and 0.1 m for the wet delay
 110
- Temporal resolution of ZTD estimates: 5 min (tropo- 111 spheric gradients estimated)
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The comparison between the ZTD_{SIR} and ZTD_{IGS} was carried out over 27 sites common to both networks (Fig. 1, blue stars and brown diamonds).

2.2 Jason-1 and Satellite Radiometry

Jason-1 has been an altimetry satellite mission jointly operated by the French aerospace agency—Centre National d'Etudes Spatiales (CNES) and the United States National Aeronautics and Space Administration (NASA).

To retrieve the ocean topography with an accuracy of a few centimeters, Jason-1 was equipped with a Microwave Radiometer (JMR) used to measure the delay caused by the water vapor along the altimeter beam. JMR measures the brightness temperatures in the nadir direction over a circular footprint approximately between 20 and 30 km (Picot et al. 2003). Using a combination algorithm (described in p. 155 Kheim et al. 1995), the brightness temperatures can be coupled to retrieve the delay caused by the water vapor in the 129 atmosphere (i.e. the ZWD) with a Root Mean Square Error 130 (RMSE) of 1.2 cm that is, however, limited to open ocean 131 areas (Ruf et al. 1994). 132

For the present work, we have chosen to utilize the Geophysical Data Records (GDR) version c. Besides the altimeter measurements, GDR contain as ancillary information the hydrostatic meteorological correction (ZHD) provided by the ECMWF, which are then used to obtain the ZTD according to the standard equation

$$ZTD = ZHD + ZWD \tag{1}$$

For this research, Jason-1 GDR version c binary data 139 corresponding to the period from June 2008 to June 2010 140 were downloaded from the web. Then, a tuned software was 141 implemented to filter out only those measurements which 142 are close to the GNSS sites. Since JMR provides reliable 143 measurements only over open ocean areas, 20 stations were 144 **Table 1** Statistical results(compared product, number ofstations, size of the dataset,average bias and standarddeviation of the differences,correlation coefficient betweenthe products) of the comparisonsperformed

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	Stations	Samples	μ	σ	
Product	(#)	(#)	(mm)	(mm)	ρ
IGS-SIR	27	1,309,868	-0.5	6.9	0.98
ERA-SIR	30	65,534	-1.5	16.6	0.91
JMR-SIR	14	1,052	-7.4	15.4	0.93
ERA-IGS	27	67,638	-2.4	14.8	0.92
JMR-IGS	11	983	-5.6	14.9	0.93
JMR-ERA	14	958	-8.5	15.5	0.94

Different techniques have been compared in terms of ZWD whereas GNSS intra-comparison refers to ZTD

selected which fulfil the geographical criteria being located 145 within a limited distance from coastline and the height of 146 the station. Figure 1 shows the distribution of the selected 147 stations (green dots and blue stars) subset and the Jason-1 148 ground tracks (red lines) for orbit cycle 275. As described 149 in detail in Calori et al. (2013), the differences between 150 the radiometer measurements and the GNSS estimates were 151 addressed to yield a reliable comparison between the tech-152 niques. 153

2.3 ERA Interim

ERA-Interim is the latest global atmospheric reanalysis 155 product computed by the ECMWF. This contains gridded 156 data that describe the weather as well as ocean-wave and 157 land-surface conditions together with upper-air parameters 158 covering the troposphere and stratosphere (Dee et al. 2011). 159 With the purpose of retrieving the ZWD at the GNSS sites 160 from meteorological information, the binary data in grib 161 format of 3 meteorologic parameters (i.e. the mean sea level 162 pressure (P_{atm}) , the total column water vapour (TCWV) 163 and the 2 m temperature (2T)) were downloaded from the 164 ECMWF web site for the time frame of the present analysis. 165 These grids have a spatial resolution of $0.75^{\circ} \times 0.75^{\circ}$ and 166 a temporal resolution of 6h (i.e. at 0, 6, 12 and 18 UTC). 167 Here, it is also worth noting that both the TCWV and 2T are 168 referred to the orography height (h_o) , so that some height 169 corrections were needed to retrieve the tropospheric delays 170 (ZHD and ZWD) at the GNSS station height. As first step, 171 the atmospheric pressure was computed at the GNSS station 172 height (*h*) according to the standard pressure model of Berg 173 (1948)174

$$P_h = P_{atm} (1 - d \cdot h)^{5.225}$$
(2)

where d = 0.0000226. Then, the ZHD at the GNSS station height (i.e., $ZHD_{ERA,h}$) was retrieved following Davis et al. (1985)

$$ZHD_{ERA,h} = a \frac{P_h}{\left(1 - b \cdot \cos(2\phi) - c \cdot h\right)}$$
(3)

where a = 0.0022768, b = 0.00266, $c = 0.28 \cdot 10^{-6}$, ϕ is 178 the station latitude. The mean temperature of the troposphere 179 (T_m) was modelled using the 2T according to Mendes et al. 180 (2000, Eq. 17), model *UNB*98*Tm*1. This step was neces-181 sary in order to retrieve the ZWD at the orography height 182 *ZWD*_{*ERA,ho*} using the relation between the TCWV and the 183 ZWD introduced by Askne and Nordius (1987, Eq. 25). To 184 refer the ZWD retrieved by the ECMWF to the GNSS station 185 height, the empirical relation proposed by Kouba (2008) was 186 applied 187

$$ZWD_{ERA,h} = ZWD_{ERA,h_o} \cdot e^{-(h-h_o)/2000}$$
(4)

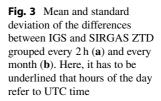
Finally, according to Eq. (1), we computed ZWD_{SIR} using 188 ZHD_{ERA} . The comparison with ZWD_{SIR} was performed for all 189 sites at which a comparison with either IGS or JMR values 190 was already available (displayed as blue stars and brown 191 diamonds in Fig. 1). At this stage of the research, no temporal 192 interpolation was introduced so that GNSS and ECMWF 193 were analysed only at identical times (i.e., 4 times per day). 194

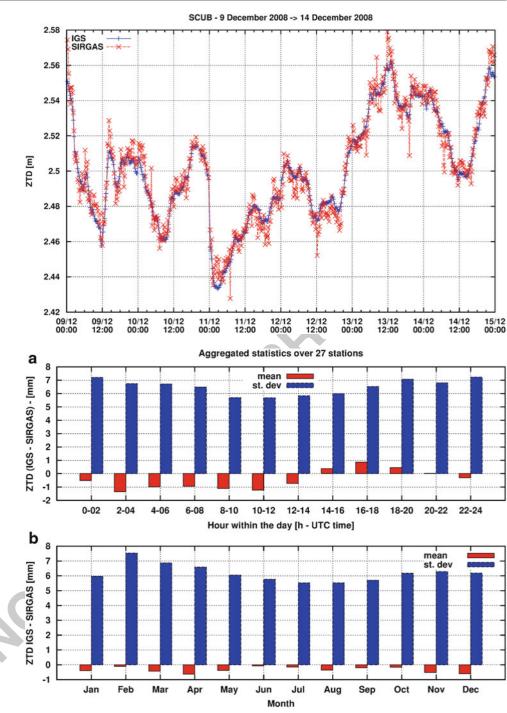
3 Results and Discussion

The accuracy of the tropospheric estimations retrieved from 196 SIRGAS network was assessed in terms of consistency with 197 three different products: (1) the official ZTD generated by 198 IGS; (2) the ZWD computed using meteorological infor- 199 mation provided by ERA-Interim, ECWMF; (3) the ZWD 200 measured by the JMR aboard the Jason-1 satellite altimetry 201 mission. The comparison was carried out from June 2008 202 to 2010 and, because of the inter-techniques differences, it 203 involved separate clusters of SIRGAS stations: 27 sites for 204 comparison 1, 30 sites for comparison 2 and 14 sites located 205 along the coastline for comparison 3. In each comparison, 206 the agreement between the techniques was evaluated using 207 the bias (μ), the standard deviation (σ) of the differences and 208 the correlation coefficient (ρ) of the time series as statistical 209 indexes. 210

Table 1, which reports the statistical inter-techniques 211 indicators averaged over the whole set of stations, reveals 212

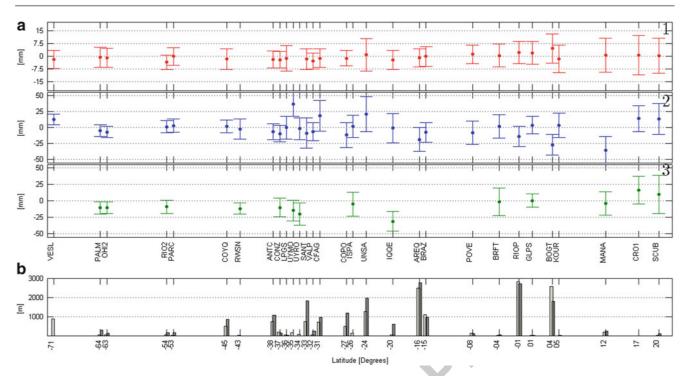
Fig. 2 5 days (9–14 December 2008) time series of IGS (*blue*) and SIRGAS (*red*) ZTD estimations





that SIRGAS GNSS tropospheric delays agree with those 213 obtained from the different techniques (i.e., with a bias 214 in the difference varying from a minimum of 0.5 mm for 215 the IGS values up to a maximum of 7.4 mm for the JMR 216 measurements). As expected from using the same technique, 217 the best agreement is found between SIRGAS and IGS 218 ZTD. Nonetheless, the different strategies used to process the 219 GPS observations (Sect. 2.1) influence the ZTD estimations: 220 in particular, a refined analysis showed that ZTD_{SIR} are 221

characterized by a higher estimation noise, as it is shown 222 in Fig. 2. Further, to investigate possible dependencies either 223 on the epoch of the day or on the month of the year, 224 the differences for the whole period have been grouped 225 every 2 h and every month, respectively. Figure 3, which 226 displays the results of the hourly and monthly compar-227 ison, does not highlight any degradation of the ZTD_{SIR} 228 neither with the epoch of the day nor within the whole 229 year. 230



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Fig. 4 (a) Bias and standard deviation over the 2 years of analysis on each SIRGAS site used in the 3 comparisons: (1) $ZTD_{IGS} - ZTD_{SIR}$ in red; (2) $ZWD_{ERA} - ZWD_{SIR}$ in blue; (3) $ZWD_{JMR} - ZWD_{SIR}$ in green.

(**b**) The height in meters of each SIRGAS site: ellipsoidal height in *light grey*, orography height from ERA-Interim in *dark grey*

Table 1 shows that SIRGAS estimates agree to a high 231 extent both with JMR measurements and with ERA-Interim. 232 weather data and the achieved results are fully consistent. 233 with Fernandes et al. (2013), Edwards et al. (2004), Bock 234 et al. (2010). For each station, the results of the three 235 comparisons are summarized in Fig. 4a; here, to investigate 236 any latitudinal dependency of the results, the stations are 237 sorted from north to south. Importantly, Fig. 4b displays 238 the difference between the ellipsoidal height of the GNSS 239 stations and the orography height of the ERA-Interim grid 240 (i.e., h and h_o). 241

Although no clear latitudinal dependency in terms of bias 242 is visible, Fig. 4a shows a slow decrease of standard deviation 243 in the southern regions. The same situation is described by 244 Teke et al. (2011) in their multi-technique comparison of 245 ZTD and is most probably related to the lower content of WV 246 in the colder regions as compared to the hotter regions, where 247 the evaporation is dominating. Such effect is clearly visible 248 in the inter-technique comparison 2 and 3. From the results 249 of comparison 2 it is important to notice that large biases are 250 obtained both for large and for little height differences (e.g., 251 BOGT, UNSA and UYMO, MANA, respectively); therefore 252 it appears difficult to infer a clear dependency between the 253 results and the height differences. 254

Conclusions and Perspectives

In the period from June 2008 to June 2010, the ZTD of 256 approximately 100 permanent stations belonging to SIRGAS 257 network were estimated and then compared with the official 258 ZTD distributed by the IGS. Then, the accuracy of the 259 products was assessed in terms of consistency with respect 260 to 2 independent techniques: (1) ZWD measured by Jason-1 261 satellite mission; (2) ZWD retrieved from observations data 262 of the ECMWF ERA-Interim reanalysis model. The best 263 agreement is reached between SIRGAS and IGS products 264 ($\mu = -0.5$ mm, $\sigma = 6.5$ mm), whereas slightly worse 265 statistical values are obtained in the comparisons with the 266 JMR measurements ($\mu = -7.4$ mm, $\sigma = 15.4$ mm), and the 267 ERA Interim data ($\mu = -1.5$ mm, $\sigma = 16.6$ mm). 268

A more detailed comparison undertaken with the IGS 269 products confirmed that SIRGAS estimations quality is con-270 stant, independent from the local time or season of the year; 271 at the same time, to mitigate the higher estimation noise in 272 the final ZTD a further refinement of the processing parameters is required (e.g., using tighter constraints for parameters 274 estimation). Overall, the achieved results are in accordance 275 with previous researches. On one hand this testifies that the inter-technique differences were correctly accounted for, on the other, it further confirms SIRGAS capabilities to contribute to short and long term meteorological studies.

²⁷⁸ contribute to short and long term meteorological studies.

Future investigations are oriented to evaluate the impact of including other GNSS (GLONASS, Compass, Galileo) constellation in ZTD estimation to derive reliable near realtime short weather forecast over the whole South and Central

American region.

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- AQ2. "City" has been inserted in the affiliation field. Please check if it is correct.
- AQ3. Ref. "Kheim et al. (1995)" is cited in the text but not provided in the reference list. Please provide it in the reference list or delete the citation from the text.
- AQ4. Please provide complete details for Refs. Mendes et al. (2000); Saastamoinen (1973).

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