

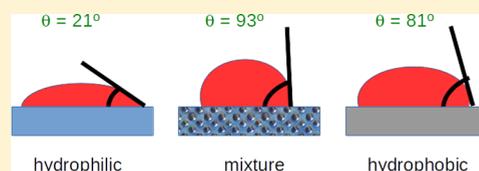
## 1 Hydrogen-Bond Heterogeneity Boosts Hydrophobicity of Solid 2 Interfaces

3 Matías Factorovich,<sup>†</sup> Valeria Molinero,<sup>‡</sup> and Damián A. Scherlis<sup>\*,†</sup>

4 <sup>†</sup>Departamento de Química Inorgánica, Analítica y Química Física/INQUIMAE, Facultad de Ciencias Exactas y Naturales,  
5 Universidad de Buenos Aires, Buenos Aires C1428EHA. Argentina

6 <sup>‡</sup>Department of Chemistry, University of Utah, 315 South 1400 East, Salt Lake City, Utah 84112-0850, United States

7 **ABSTRACT:** Experimental and theoretical studies suggest that the hydro-  
8 phobicity of chemically heterogeneous surfaces may present important  
9 nonlinearities as a function of composition. In this article, this issue is  
10 systematically explored using molecular simulations. The hydrophobicity is  
11 characterized by computing the contact angle of water on flat interfaces and the  
12 desorption pressure of water from cylindrical nanopores. The studied interfaces  
13 are binary mixtures of hydrophilic and hydrophobic molecules, with and  
14 without the ability to form hydrogen bonds with water, intercalated at different scales. Water is described with the milliwatts  
15 (mW) coarse-grained potential, where hydrogen-bonds are modeled in the absence of explicit hydrogen atoms, via a three-body  
16 term that favors tetrahedral coordination. We found that the combination of particles exhibiting the same kind of coordination  
17 with water gives rise to a linear dependence of contact angle with respect to composition, in agreement with the Cassie model.  
18 However, when only the hydrophilic component can form hydrogen bonds, unprecedented deviations from linearity are  
19 observed, increasing the contact angle and the vapor pressure above their values in the purely hydrophobic interface. In  
20 particular, the maximum enhancement is seen when a 35% of hydrogen bonding molecules is randomly scattered on a  
21 hydrophobic background. This effect is very sensitive to the heterogeneity length-scale, being significantly attenuated when the  
22 hydrophilic domains reach a size of 2 nm. The observed behavior may be qualitatively rationalized via a simple modification of  
23 the Cassie model, by assuming a different microrugosity for hydrogen bonding and non-hydrogen bonding interfaces.



### 24 ■ INTRODUCTION

25 The behavior of fluids in contact with solid surfaces has been a  
26 subject of research for over two centuries, inspiring some of the  
27 most renowned scientists of the 19th century, from Young's  
28 phenomenological description of the angle formed by a droplet  
29 on a homogeneous and flat surface,<sup>1</sup> to the later interpretation  
30 of Gibbs who gave a thermodynamic insight into Young's  
31 ideas.<sup>2</sup> Taking Gibbs' work as a starting point, Wenzel and  
32 Cassie in the 20th century studied the wetting phenomena of  
33 rough and chemically heterogeneous surfaces, respectively,  
34 leading to the well-known Wenzel and Cassie–Baxter  
35 equations.<sup>3,4</sup> The former provides the contact angle as a  
36 function of rugosity, whereas the latter establishes its  
37 dependence on the composition of the interface.

38 A lot has been done since those early works. Marmur<sup>5</sup> has  
39 described the wetting of a rough surface in two different  
40 regimes: one corresponding to the Wenzel equation for slightly  
41 rough surfaces, and another for highly irregular morphologies  
42 where air can be trapped at the interface, envisioned as a  
43 combination of a rough surface with chemical heterogeneity.  
44 He also studied the case of droplets on heterogeneous surfaces  
45 with periodic patterns, to find that the final contact angle  
46 depends on the length of these patterns with respect to the  
47 droplet size.<sup>6</sup> Hysteresis, characterized as the difference  
48 between the advancing and receding contact angles, has been  
49 experimentally observed in almost all cases.<sup>7</sup> A few theoretical  
50 approaches have been devised for a number of ideal situations,

51 where the existence of hysteresis was ascribed to roughness and  
52 chemical heterogeneity generating local minima in the free  
53 energy landscape as a function of the contact angle.<sup>8–12</sup> This  
54 theoretical framework is a key aspect in the rational design of  
55 materials for applications related to wetting and spreading.<sup>13–15</sup>  
56 In particular, an understanding of the effect of droplet size on  
57 wetting is essential for applications into the nanoscale. Gibbs  
58 was the first to formulate a dependence of the contact angle on  
59 size,<sup>2</sup> by introducing the concept of line tension, which is the  
60 excess energy associated with the boundary of three bulk  
61 phases.<sup>16–18</sup> As a droplet becomes smaller, the magnitude of  
62 the free energy originating in the line tension approaches the  
63 surface tension contribution and influences the final value of  
64 the contact angle. This may be of relevance in the nucleation of  
65 droplets on surfaces,<sup>19–21</sup> capillary condensation in pores, or  
66 the dynamics of contact line spreading.<sup>22,23</sup>

67 Despite the large body of experimental and theoretical  
68 research on wettability at the nanoscale, various fundamental  
69 questions remain unanswered. The magnitude and even the  
70 sign of the line tension are a matter of debate, with reported  
71 results spanning 7 orders of magnitude.<sup>16–18,24–26</sup> Realistic  
72 systems combining both chemical heterogeneity and roughness  
73 are beyond the scope of the available analytic models, posing a  
74 challenge to theory and experiments. A nanoscopic under-

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standing of superhydrophobicity and hydrophobic enhancement effects is only starting to emerge.<sup>27–33</sup> In this context, simulations have played a significant role to elucidate at the nanoscale level the dependence of hydrophobicity on the surface topography, on the molecular interactions and on the droplet size,<sup>28,30,34,35</sup> and the factors controlling dewetting, nucleation and condensation of water in confinement,<sup>36,37</sup> or film growth on hydrophobic surfaces.<sup>38,39</sup> The modeling of heterogeneous surfaces combining polar and nonpolar sites suggests that hydrophobicity is not a linear function of composition, but that important deviations may occur which are dependent on the heterogeneity length-scale,<sup>28,30,36,40</sup> in line with experimental estimates of interfacial energies.<sup>31</sup>

The purpose of this work is to characterize the hydrophobicity of chemically heterogeneous surfaces as a function of composition and length-scale. Large-scale molecular dynamics simulations are performed to investigate the wettability of a heterogeneous surface resulting from the mixture of hydrophobic and hydrophilic particles, randomly blended at the molecular level, or arranged in patches of different sizes. The hydrophobicity of the interface is assessed in terms of contact angle and desorption pressure. Through the present analysis, we elucidate in what cases the hydrophobicity of an interface turns out to be a linear combination of its chemical components, and what are the factors leading to—sometimes dramatic—deviations from linearity. Finally, we show how the observed behavior can be qualitatively accounted for with a simple modification to the Cassie model.

## METHODOLOGICAL APPROACH

Water molecules are described using the milliwatts (mW) coarse-grained model, in which each H<sub>2</sub>O molecule is treated as a single particle interacting through anisotropic short-ranged potentials that encourage tetrahedrally coordinated structures.<sup>41</sup> The  $\epsilon$  parameter determines the strength of the two-body interactions, while the  $\lambda$  term enforces the formation of tetrahedrally coordinated structures. In spite of not including electrostatic terms or explicit hydrogen atoms, the mW model is able to accurately reproduce the phase behavior and the thermodynamic properties of water in bulk and in confinement.<sup>37,39,41–49</sup>

Water is studied on square plates and in cylindrical pores with different hydrophilicities. The particles composing the plates and the pores can have four different kinds of interactions with water: hydrophilic with and without hydrogen bonding, and hydrophobic with and without hydrogen bonding. Thus, we define the four kinds of particles listed in Table 1, named I, II, III and IV, for which the degree of hydrophilicity and the formation of H-bonds are controlled via the  $\epsilon$  and  $\lambda$  parameters of the mW model. We note that we classify surfaces II and IV as hydrophobic even if their contact angles fall below 90°, because they resemble the wetting of graphite (86°), which is considered to be hydrophobic. Within the present coarse-grained

**Table 1. Characterization of the Four Kinds of Particles That May Form the Solid Surface<sup>a</sup>**

particle	interaction with water	H-bonding	$\epsilon$ (kcal/mol)	$\lambda$	$\theta$ (deg)
I	hydrophilic	no	0.55	0	23
II	hydrophobic	no	0.35	0	82
III	hydrophilic	yes	5.25	23.15	21
IV	hydrophobic	yes	3.50	23.15	81

<sup>a</sup>The parameters  $\epsilon$  and  $\lambda$  determine the interactions with water (see text). The contact angles ( $\theta$ ) refer to those measured on an amorphous interface made of such particles.

representation, hydrogen-bonds between water and the solid surface are the result of the three-body term in the Stillinger-Weber potential, and become manifest in the local tetrahedral order.<sup>37,39,41,43,45</sup> The  $\epsilon$  parameter involved in the solid–water interaction was tuned to provide the desired contact angle. Since the three-body term is repulsive, to achieve a given value of  $\theta$ , a stronger two-body interaction is necessary in the presence of hydrogen bonds ( $\lambda = 23.15$ ) that in their absence ( $\lambda = 0$ ), which explains the different magnitudes of  $\epsilon$  appearing in Table 1.

Contact angles were measured on square plates of sides ranging from 18 to 55 nm, depending on the size of the droplet. System dimensions are given in Table 2. The thickness of the plates is of 14.5

**Table 2. Number of Water Molecules in the Droplet, Size of the Square Plates Employed in the Computation of Contact Angles, and Average Droplet Radii on Different Surfaces: <sup>a</sup>type II; <sup>b</sup>type III; <sup>c</sup>atomic scale mixture of types II and III**

molecules number	plate size (Å × Å)	droplet radius (Å)
1192	183 × 183	24 <sup>a</sup> /26 <sup>b</sup> /22 <sup>c</sup>
4162	274 × 274	37 <sup>a</sup> /37 <sup>b</sup>
8932	274 × 274	49 <sup>a</sup> /56 <sup>b</sup> /43 <sup>c</sup>
23872	365 × 365	82 <sup>a</sup> /61 <sup>c</sup>
46012	365 × 365	90 <sup>b</sup> /75 <sup>c</sup>
111892	547 × 547	118 <sup>b</sup> /101 <sup>c</sup>

Å, larger than the cut-offs of the water–solid interactions, which are 4.30 and 6.40 Å on the hydrophilic and the hydrophobic surfaces, respectively. Therefore, it is large enough to provide converged results with respect to the normal dimension of the slab. The structures of the plates correspond to amorphous interfaces derived from molecular dynamics simulations of water at 298 K, and composed of the particles defined in Table 1 arranged in three different patterns: randomly, and in hydrophilic spots of 1 and 2 nm diameter. Randomly mixed configurations are generated by replacing, in a random fashion, hydrophilic by hydrophobic particles in a region extending down to 3 Å inside the exposed face. This is done for fractions ranging from 25% to 90%. Plates with circular hydrophilic patches of 10 or 20 Å are made only for a composition of 50%.

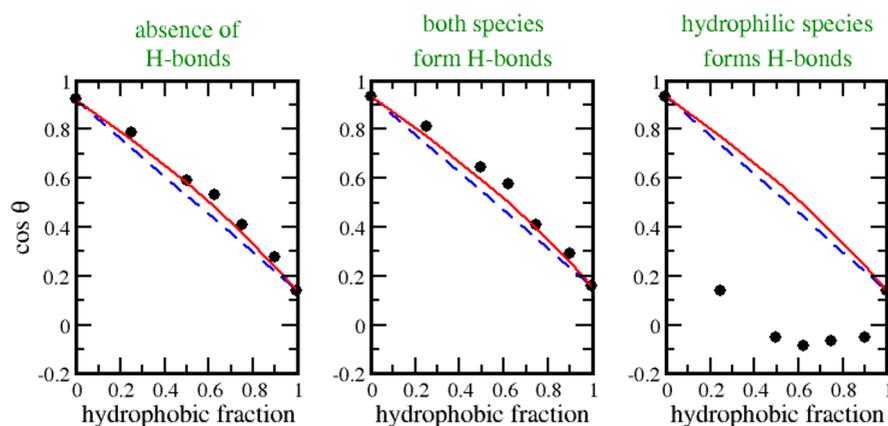
The contact angles were measured from the average 3D density profiles of water nanodroplets, following the protocol already established in the literature.<sup>35,37</sup> Density profiles were sampled on time windows of at least 10 ns after 1 ns of thermalization. Desorption pressures from nanopores were computed using grand canonical molecular dynamics simulations, following the procedure reported elsewhere.<sup>37</sup> The diameter of the pores was 28 Å and the length 77 Å, with amorphous walls made of the particles in Table 1 and organized in the same patterns as described for the plates. All simulations were carried out with the LAMMPS code<sup>50</sup> in periodic boundary conditions. Molecular dynamics were simulated in the canonical ensemble, using the Nosé–Hoover thermostat at 298 K and a time step of 5 fs.

## RESULTS AND DISCUSSION

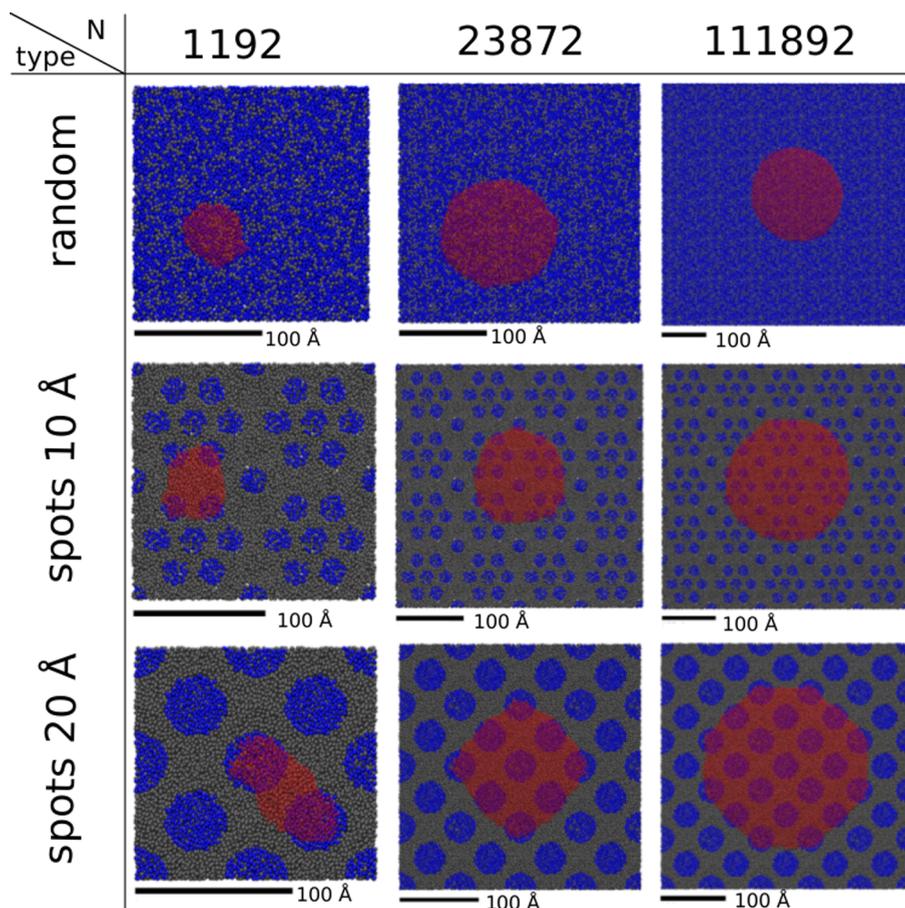
Figure 1 shows the effect of a random intercalation at the atomic level of hydrophilic and hydrophobic particles, on the contact angle of a water droplet of 1192 molecules. The left panel shows that, for a mixture of hydrophilic and hydrophobic particles interacting with water without any orientational preference (particle kinds I and II,  $\lambda = 0$ ), the cosine of the contact angle turns out to be almost linear with respect to composition  $x_A$  or  $x_B$ . This is the result predicted by the Cassie–Baxter equation,

$$\cos \theta = x_A \cos \theta_A + x_B \cos \theta_B \quad (1)$$

indicated in Figure 1 with a dashed line. Martic and collaborators have already employed molecular simulations to



**Figure 1.** Contact angle as a function of hydrophobic fraction for solid surfaces composed of hydrophilic and hydrophobic molecules randomly mixed at the atomic scale. The circles show the results from simulations, whereas dashed and continuous curves correspond to the Cassie–Baxter and to the Israelachvili–Gee<sup>54</sup> models, respectively. The labels on top of each panel indicate the composition of the interface in terms of the particle types defined in Table 1. Left: hydrophilic and hydrophobic without H-bonds (I + II). Center: hydrophilic and hydrophobic with H-bonds (III + VI). Right: hydrophilic with H-bonds plus hydrophobic without H-bonds (II + III).



**Figure 2.** Structures of water droplets (red particles) on plates containing a 50% mixture of hydrophilic (blue) and hydrophobic (gray) molecules in various patterns. From left to right, the number of water molecules  $N$  increases. From top to bottom, the heterogeneity length-scale changes from the molecular level to 2 nm spots.

175 corroborate the validity of the Cassie’s law for a Lennard-Jones  
176 fluid adsorbed on a pore with a randomly heterogeneous  
177 surface.<sup>51</sup>

178 If both the hydrophilic and hydrophobic particles can form  
179 hydrogen bonds, the situation is similar. The central panel of  
180 Figure 1 shows that for a random mixture of particles III and  
181 IV, there is also an approximately linear dependence of contact

angle with respect to concentration. While it seems unlikely to  
observe in nature a hydrophobic interaction involving hydrogen  
bonds, we have examined this case as a proof of concept.

However, if only one of the species can form hydrogen  
bonds, we find that the behavior changes dramatically. The  
right panel of Figure 1 depicts the contact angle as a function of  
composition for a random mixture of hydrophilic and

189 hydrophobic particles, where only the hydrophilic sites can  
 190 form hydrogen-bonds. This combination of particles II and III  
 191 produces a strong negative deviation from the Cassie–Baxter  
 192 equation. The synergism is so pronounced, that for a range of  
 193 compositions, from  $x_{II} \approx 0.4$  to  $x_{II} \approx 0.9$ , the hydrophobicity of  
 194 the mixture becomes larger than that of the purely hydrophobic  
 195 plate. The largest effect is seen for  $x_{II} \approx 0.65$ , when the contact  
 196 angle exceeds the one corresponding to  $x_{II} = 1$  by  $13^\circ$ . This  
 197 result is in line with previous observations that a single OH  
 198 group in a nonpolar background has a stronger effect than the  
 199 reciprocal combination.<sup>30,40</sup> The magnitude of this nonlinearity,  
 200 however, has no precedents in the literature reporting the  
 201 wettability of chemically heterogeneous interfaces.

202 The behaviors described above do not seem to be a  
 203 consequence of the limited size of the droplets. We have  
 204 performed simulations for increasingly larger droplets, from  
 205 1192 to 111892 particles, to assess the impact of the system size  
 206 on the trend in contact angles. Figure 2 depicts some of the  
 207 model systems explored, corresponding to water droplets of  
 208 different sizes on the patterned plates. As the number of  
 209 molecules in the droplet is increased, thermalization and  
 210 sampling must be extended over tens of nanoseconds to get a  
 211 converged result. On the other hand, hysteresis effects become  
 212 more important and the final contact angle may depend on the  
 213 starting configuration. These technical issues render these  
 214 simulations both costly and arduous. However, once these issues  
 215 are overcome, we find that the dependence of the contact  
 216 angle on the radius of the droplet is very minor. The contact  
 217 angle as a function of the inverse drop radius is plotted for the  
 218 different surfaces in Figure 3. The values corresponding to the

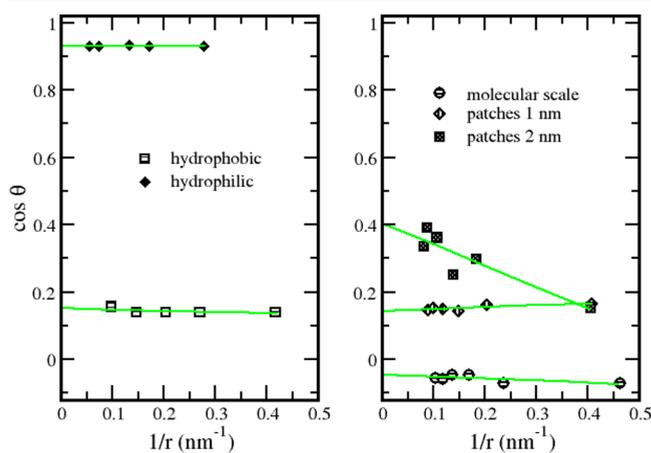


Figure 3. Contact angles as a function of droplet size. Left: pure surfaces of types II and III. Right: 50% mixtures. The straight lines show the linear regressions. The contact angle shows only a minor dependence with respect to radius in the range studied, with the exception of the interface with 2 nm spots, where the dimensions of the heterogeneous pattern is comparable to that of the droplet.

219 large droplets limit ( $\theta_\infty$ ), extrapolated from the intercept of the  
 220 linear regressions, are given in Table 3 for particle types II and  
 221 III, and for their atomic scale mixture. The nonadditive  
 222 behavior is still present if we consider the large droplet limit:  
 223 the linear combination of  $\theta_\infty$  of the pure interfaces, equal to  
 224  $57^\circ$ , is very far from the value of  $\theta_\infty$  in the 50% mixture, equal  
 225 to  $93^\circ$ . These results indicate that the synergism observed in  
 226 the hydrophilic–hydrophobic mixture does not disappear with  
 227 the increase of the droplet size.

Table 3. Extrapolated Contact Angle for Infinite Radius ( $\theta_\infty$ ) as a Function of the Hydrophobic Fraction, for Particle Types II and III<sup>a</sup>

$X_{\text{pho}}$	0	0.5	1
$\theta$ (deg)	21.5	92.7	81.3

<sup>a</sup>Fraction of 0.5 corresponds to the atomic scale mixture.

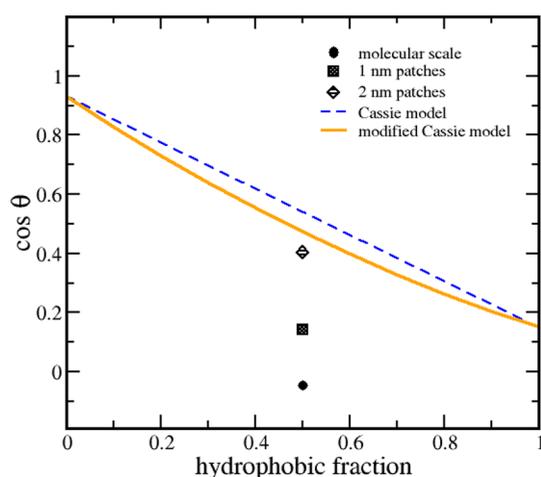
The line tension  $\tau$  can be estimated from the dependence of the  
 contact angle with respect to droplet radius, according to the  
 modified Young equation.<sup>52</sup> This yields for the hydrophobic,  
 the hydrophilic, and the atomic-scale mixed surfaces,  
 respectively, have values of  $-2.4 \pm 6.2$ ,  $0.4 \pm 3.5$ , and  $2.4 \pm$   
 $5.2$  pN. As we have mentioned above, there is not a general  
 agreement regarding the magnitude or even the sign of  $\tau$ , with  
 experimental values for water ranging from 10 to  $10^6$  pN.<sup>53</sup>  
 Large discrepancies have been reported for the same substrates  
 measured with similar approaches that have been ascribed to  
 sample preparation, poor experimental techniques, out of  
 equilibrium measurements, or oversimplifications in the  
 analysis.<sup>16</sup> Comparable discrepancies are also present through-  
 out the theoretical results. One of the most recent experimental  
 studies has settled for the line tension of water in hydrophobic  
 cavities a value of  $-30$  pN,<sup>18</sup> in conflict with the majority of  
 previous reports for solid–liquid–vapor systems, which have  
 yielded a positive sign. Our estimations fall, in magnitude, in  
 the lower range of the existing data. In any case, to the best of  
 our knowledge, the present estimates are the most involved in  
 terms of sampling and system size, if compared with other  
 calculations based on the same approach.

The Cassie–Baxter equation must hold when the size of the  
 hydrophilic and the hydrophobic domains reaches the macro-  
 scopic limit. In this context, we have investigated the role of the  
 length of the heterogeneity on the deviation from the linear  
 regime. To this end, we analyzed the water contact angle on  
 plates exhibiting equal fractions of H-bonding hydrophilic and  
 hydrophobic molecules (particles II and III in the same  
 proportions), but arranged in regular hydrophilic patches of 10  
 and 20 Å diameter. For these systems, the macroscopic contact  
 angles were estimated from linear regressions with respect to  
 the inverse radii, as already done for the random mixtures. The  
 right panel of Figure 3 shows that there is not a significant  
 dependence of the contact angle with respect to droplet size on  
 the interface with spots of 1 nm diameter, but this is not the  
 case when this diameter reaches 2 nm and becomes comparable  
 to the dimensions of the droplet. This is evident from the  
 bottom panel of Figure 2, which shows that the droplet of 1192  
 molecules is strongly distorted by the underlying patterning.  
 The results summarized in Table 4 or Figure 4 indicate that as

Table 4. Extrapolated Contact Angles for Infinite Radius ( $\theta_\infty$ ) as a Function of the Length of Heterogeneity for 50% Hydrophobic–Hydrophilic Mixtures of Particles II and III

length (Å)	molecular	10 Å	20 Å	Cassie's law
$\theta$ (deg)	92.7	81.8	66.2	57.3

the length of the chemical heterogeneity becomes larger, the  
 nonlinear behavior tends to vanish. In particular, for 2 nm  
 patches the value of  $\theta_\infty$  falls close to Cassie's law prediction.  
 This is making manifest that the Cassie–Baxter or the  
 Israelachvili–Gee<sup>54</sup> models do not consider the cooperative  
 effects arising from the molecular heterogeneity of the systems.

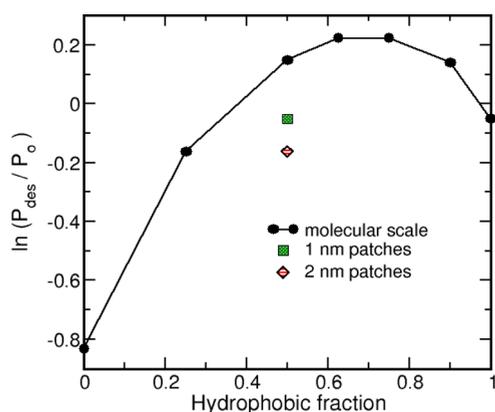


**Figure 4.** Contact angle as a function of hydrophobic fraction for solid surfaces composed of hydrophilic and hydrophobic molecules of types II and III, intercalated at different length-scales. The orange curve represents the modified Cassie model (eq 4) with a rugosity ratio of 0.6.

275 Such cooperative effects rapidly decrease when the hetero-  
276 geneity length-scale goes above the molecular dimensions, and  
277 are clearly attenuated in the case of 20 Å diameter patches.

278 As an independent measure of hydrophobicity, we computed  
279 the desorption pressures of water from a cylindrical pore with  
280 open ends. These pressures were calculated using the grand  
281 canonical screening scheme proposed in our recent work.<sup>44,55</sup>

282 Vapor desorption from open-ended pores is an equilibrium  
283 process which is well described by the Kelvin equation in  
284 nanopores down to 3 nm size.<sup>37,56</sup> The present simulations  
285 were performed in 3 nm wide nanopores of 7.7 nm length,  
286 displaying the same patterning of hydrophilic and hydrophobic  
287 particles already investigated in the plates. The results, depicted  
288 in Figure 5, reflect the same trends reported for the contact  
289 angles: the random mixture of hydrogen-bonding and non  
290 hydrogen-bonding particles induces a strong deviation from the  
291 linear behavior, which appears gradually attenuated when the  
292 sizes of the hydrophilic spots are 10 and 20 Å. We emphasize  
293 that contact angles and vapor pressures have been calculated  
294 from two different kinds of computational experiments on



**Figure 5.** Desorption pressure from a nanopore as a function of the composition of the solid interface. The pore is 3 nm wide and its surface contains hydrophilic and hydrophobic molecules of types II and III intercalated at different length-scales: molecular, and hydrophilic spots of 1 and 2 nm.

different model systems. The fact that these two independent  
295 properties attest a similar hydrophobic enhancement for the  
296 same range of compositions is remarkable and reinforces the  
297 present findings.  
298

Our simulations show that a random intercalation at the  
299 nanoscale of hydrophilic and hydrophobic molecules is not  
300 enough to lead to any significant nonlinear effects: the  
301 necessary ingredient to observe the enhancement of the  
302 hydrophobicity appears to be the heterogeneity in the  
303 formation of hydrogen bonds with water. The question is,  
304 then, why does this hydrogen bond heterogeneity boost the  
305 hydrophobicity of the interface? Different studies have pointed  
306 that a small number of hydrophilic sites on a hydrophobic  
307 background may dramatically change the wetting properties of  
308 the interface.<sup>36,57,58</sup> Garde and other authors have explained  
309 this effect in terms of the water density fluctuations at the  
310 interface.<sup>29,30,32</sup> From a thermodynamic viewpoint, an answer  
311 can be found at the level of the Cassie model, if we think of  
312 hydrogen-bond heterogeneity as a rugosity effect. In this way, it  
313 is possible to characterize the hydrogen-bonding surface with a  
314 different microscopic rugosity than the non-hydrogen-bonding  
315 interface. Then, making use of the Wenzel formula, we can  
316 rewrite the thermodynamic differential relations leading to eq 1  
317 under the assumption that the hydrophilic and the hydrophobic  
318 particles exhibit, respectively, microscopic rugosities  $r_1$  and  $r_2$ .  
319 The infinitesimal change in free energy  $F$  as a function of  
320 contact angle  $\theta$  for a droplet of radius  $a$  on a mixed interface  
321 can be written:  
322

$$dF = \gamma_{LV} dS_{LV} + (x_1\gamma_{SL1} + x_2\gamma_{SL2}) dS_{SL} + \gamma_{SV} dS_{SV} \quad (2) \quad 323$$

$$dS_{LV} = 2\pi a \cos \theta da$$

$$dS_{SL} = -dS_{SV} = f(x_1; x_2)2\pi a da \quad (3) \quad 324$$

where  $\gamma$  represents interfacial free energies,  $S$  is the area,  $x_1$  and  
325  $x_2$  are the molar fractions of species 1 and 2 composing the  
326 solid surface,  $f(x_1; x_2)$  is its rugosity, and the subindices LV,  
327 SL, and SV indicate the liquid–vapor, solid–liquid, and solid–  
328 vapor interfaces, respectively. If we assume that the global  
329 rugosity is a linear combination of the individual rugosities,  
330  $f(x_1; x_2) = x_1r_1 + x_2r_2$ , then the equilibrium condition  $dF/da = 0$   
331 leads to the following result:  
332

$$\cos \theta = \alpha x_1^2 + \beta x_1 + \delta \quad (4) \quad 333$$

$$\alpha = \cos \theta_1 + \cos \theta_2 - \frac{r_1}{r_2} \cos \theta_2 - \frac{r_2}{r_1} \cos \theta_1$$

$$\beta = \frac{r_1}{r_2} \cos \theta_2 + \frac{r_2}{r_1} \cos \theta_1 - 2 \cos \theta_2$$

$$\delta = \cos \theta_2$$

where  $\theta_1$  and  $\theta_2$  are the contact angles on the pure interfaces.  
334 The interesting point about this simple model is that it predicts  
335 a quadratic behavior for the global contact angle, with negative  
336 deviations occurring for  $r_1/r_2 < 1$ . In particular, Figure 4 shows  
337 the prediction of eq 4 if the ratio between the hydrophobic and  
338 hydrophilic rugosities is 0.6. For this ratio and  $x_1 = 0.5$ , the  
339 contact angle yielded by the modified Cassie formula falls close  
340 to the one obtained in our simulations on 20 Å patches (Table  
341 4). Hence, this rudimentary model seems to be enough to give  
342 a qualitative description of the contact angle when the  
343 heterogeneity length-scale is higher than 2 nm. Below this  
344

345 limit, when the heterogeneity reaches the molecular scale,  
346 strong deviations are observed which can not be captured by  
347 this approach.

#### 348 ■ FINAL REMARKS

349 To conclude, we highlight the most significant findings of this  
350 work: (i) on chemically heterogeneous surfaces where the  
351 hydrophobic and hydrophilic species present the same kind of  
352 coordination with water, contact angles and vapor pressures  
353 show a linear behavior with respect to surface composition; (ii)  
354 if only the hydrophilic species interacts via hydrogen bonding,  
355 pronounced deviations from linearity can be observed, to the  
356 extent that the hydrophobicity of the mixture exceeds that of  
357 the purely hydrophobic interface; (iii) the strong nonlinear  
358 behavior stems from the admixing at the molecular scale, and  
359 tends to vanish when the size of the hydrophilic domains goes  
360 above 2 nm; (iv) this coordination heterogeneity can be  
361 incorporated to the Cassie model by assigning different  
362 microscopic rugosities to hydrogen and non-hydrogen bonding  
363 surfaces, which explains the nonlinear dependence of the  
364 contact angle with respect to composition.

#### 365 ■ AUTHOR INFORMATION

##### 366 Corresponding Author

367 \*damian@qi.fcen.uba.ar

##### 368 Notes

369 The authors declare no competing financial interest.

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