

A two-component model for the high-energy variability of blazars

Application to PKS 2155-304

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ABSTRACT

Aims. We study the production of very-high-energy emission in blazars as a superposition of a steady component from a baryonic jet and a time-dependent contribution from an inner e^-e^+ beam launched by the black hole.

Methods. Both primary relativistic electrons and protons are injected in the jet, and the particle distributions along it are found by solving a one-dimensional transport equation that accounts for convection and cooling. The short-timescale variability of the emission is explained by local pair injections in turbulent regions of the inner beam.

Results. For illustration, we apply the model to the case of PKS 2155-304, reproducing a quiescent state of emission with inverse Compton and synchrotron radiation from primary electrons, as well as proton-proton interactions in the jet. The latter also yield an accompanying neutrino flux that could be observed with a new generation km-scale detector in the northern hemisphere such as KM3NeT.

Key words. radiation mechanisms: non-thermal – BL Lacertae objects: individual: PKS 2155-304 – neutrinos

1. Introduction

Blazars are the active galactic nuclei (AGNs) in which the jet points mainly in the direction of the line of sight. They exhibit the most extreme high-energy phenomena of all AGNs. Their spectral energy distributions (SEDs) are characterized by non-thermal continuum spectra with a broad low-frequency component from X-rays to γ -rays. Blazars show rapid variability across the entire electromagnetic spectrum. Variability at high energies on timescales of a few minutes has been observed for some of them, such as PKS 2155-304 (e.g. Aharonian et al. 2006).

In this work we present a two-component jet model with both relativistic leptons and hadrons to explain the high-energy emission from these objects. The basic scenario consists of a steady baryonic jet launched by the accretion disk, and an e^+e^- beam launched by the black hole ergosphere. The quiescent component of the signal is assumed to be produced by the jet, while the variable component is due to shocked regions in the inner e^+e^- beam. Inhomogeneities and turbulence can be generated by Kelvin-Helmholtz instabilities. In Sect. 2 we describe the basics of the model. Its application to PKS 2155-304 is presented in Sects. 3 and 4 for the quiescent and variable emission, respectively. In Sect. 5 we focus on the neutrino output expected for the same blazar, analyzing the detectability with a next generation neutrino telescope such as KM3NeT. We finish in Sect. 6 with a discussion.

2. Description of the model

We assume that matter is captured by the central black hole through a dissipationless accretion disk (Kelner & Bogolobov 2010) and that a fraction of this accreted material is expelled

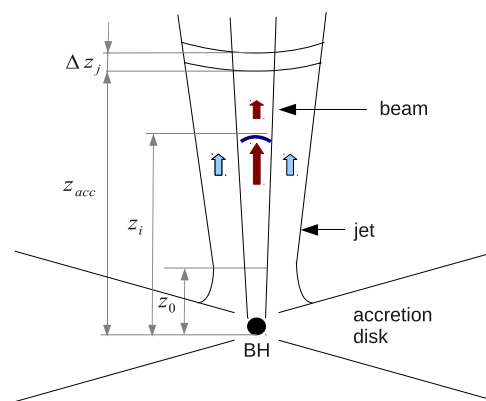


Fig. 1. Basic elements of the model. See the text for details.

by the accretion disk in two oppositely directed jets. An inner beam of relativistic electrons and positrons is launched by the spinning black hole. This two-component setup is similar to the ones implemented in several previous models (e.g. Sol et al. 1989; Romero 1995; Ghisellini et al. 2005; Boutelier et al. 2008). A sketch of the basic elements of the scenario is depicted in Fig. 1.

The introduction of a model with two components is motivated by observations as a means to reconciling available data with the unified AGN paradigm (e.g. Urry & Padovani 1995), as noted by Chiaberge et al. (2000). One-component jet models require high bulk Lorentz factors (10–20) when applied to blazars and lower values when applied to FR radiogalaxies. Including of a second component serves to solve this discrepancy, for example, through the combination of a fast spine and a slower (but still

relativistic) layer, so that the emission at small viewing angles is dominated by the fast component, whereas the slow component dominates for larger angles.

Some additional observational facts also favor the two-component interpretation. For instance, the presence of a fast spine surrounded by a slower outflow can be inferred from the observed limb-brightened radio morphology of the radiogalaxies jets (Giroletti et al. 2004). On the other hand, whereas VLBI observations of powerful TeV BL Lacs suggest that the pc-scale jets move slowly (Piner & Edwards 2004; Giroletti et al. 2004), rapid variability of the TeV emission implies that, in the region where this emission is produced, the jet should be extremely relativistic (e.g., Dondi & Ghisellini 1995; Ghisellini et al. 2002; Konopelko et al. 2003).

On the theoretical side, the presence of both a spinning black hole and an accretion disk would unavoidably yield the launching of outflows through the BZ process (Blandford & Znajek 1977) and the BP process (Blandford & Payne 1982). The coexistence of both mechanisms has been investigated by Meier (2003), among others. Whereas the BZ process yields the launching of a Poynting flux that gives rise to a leptonic beam, the BP process can generate a baryon-rich jet launched centrifugally from the inner accretion disk (e.g. Komissarov et al. 2007; Sadowski & Sikora 2010).

The stability and structure of this type of jets have been discussed, for instance, in Hardee (2007), Narayan et al. (2009), and Perucho (2012). For general discussion of fluid instabilities see, e.g., Shore (2008).

For the jet, we adopt the model developed by Reynoso et al. (2011). Equipartition between jet kinetic energy and magnetic energy takes place at $z_0 = 50R_g$ from the black hole, the jet half-opening angle is ξ_j , the jet Lorentz factor is Γ_j at z_0 , and the viewing angle is i_j . The bulk kinetic power of the jet at z_0 is a fraction q_j of the Eddington power,

$$L_j^{(\text{kin})}\Big|_{z_0} = q_j L_{\text{Edd}} = (\Gamma_j - 1) \dot{m}_j c^2, \quad (1)$$

and the cold particle density in the jet is

$$n_j = \frac{\dot{m}_j}{m_p \pi z^2 \chi_j^2 v_j}, \quad (2)$$

with $\chi_j = \tan \xi_j$. The magnetic field varies along the jet according to

$$B(z) = B_0 \left(\frac{z_0}{z} \right)^m \quad \text{with } m \in (1, 2),$$

and the Γ_j increases slowly as magnetic energy density decreases along the jet.

The e^+e^- -beam, with a half-opening angle $\xi_b < \xi_j$, is confined by the jet by requiring that the pressure is less than in the jet: $P_b = \eta_b P_j$, where $\eta_b < 1$. The initial Lorentz factor of the beam is $\Gamma_b^{(0)}$ at distance $z_b^{(0)} < z_0$ from the black hole, where equipartition with the beam magnetic energy holds. This condition is used to fix $B_b^{(0)}$. For $z > z_b^{(0)}$ in the beam, we assume

$$B_b = B_b^{(0)} \left(\frac{z_b^{(0)}}{z} \right)^{m_b} \quad \text{with } m_b \in (1, 2), \quad (3)$$

so that the Lorentz factor of the beam also increases gradually along it. This behavior of the magnetic field also enables Kelvin-Helmholtz instabilities to develop, as we discuss below in Sect. 4, where we deal with the production of variable emission in the beam. As mentioned, this contribution is added to the one from the quiescent jet, which is discussed in next.

3. The quiescence emission from the jet

The quiescent state of the emission can be reproduced using a leptohadronic model for the jet. Acceleration of relativistic electrons and protons takes place at $z_{\text{acc}} > z_0$, where the power injected in these primary particles is L_e and $L_p = aL_e$, with $a > 0$. The total power in the injected, $L_{\text{rel}} = L_e(1 + a)$, is a fraction of the bulk kinetic power of the jet, $L_{\text{rel}} = q_{\text{rel}} L_j^{(\text{kin})}$ (see Reynoso et al. 2011). The distribution of particles in the steady jet, $N(E, z)$ in units $\text{GeV}^{-1} \text{cm}^{-3}$, is governed by an inhomogeneous transport equation with cooling and convection:

$$\frac{\partial (\Gamma_j v_j N(E, z))}{\partial z} + \frac{\partial (b(E, z) N(E, z))}{\partial E} + \frac{N(E, z)}{T_{\text{dec}}(E)} = Q(E, z), \quad (4)$$

where z is the distance to the black hole in the AGN frame, and $b(E, z) = -\frac{dE}{dt}$.

This equation is solved in the jet co-moving frame, and the injection or source term is taken as

$$Q(E, z) = K_i \left(\frac{z_{\text{acc}}}{z} \right)^2 E^{-s} \exp \left[- \left(\frac{E}{E_i^{(\text{max})}} \right) \right], \quad (5)$$

where the cut-off energy $E_i^{(\text{max})}$ is determined by equating the acceleration rate to the cooling one. The particle injection is normalized in the AGN frame, that where the central black hole is at rest, as

$$L_i = \int_{\Delta E} dE' \int_{4\pi} d\Omega' \int_{\Delta V} dV E' \frac{dQ'_i(E', z)}{d\Omega'}, \quad (6)$$

where

$$\frac{dQ'_i(E', z)}{d\Omega'} = \left[\frac{E'^2 - m_i^2 c^4}{E^2 - m_i^2 c^4} \right]^{1/2} \frac{Q_i(E, z)}{4\pi}, \quad (7)$$

and

$$E = \Gamma_j \left(E' - \beta_j \cos \theta \sqrt{E'^2 - m_i^2 c^4} \right). \quad (8)$$

The acceleration rate is given by

$$\dot{\tau}_{\text{acc}}^{-1}(E, z) = \eta \frac{ceB(z)}{E}, \quad (9)$$

with an efficiency η , and the loss rate corresponds to synchrotron emission, inverse Compton interactions, pp and py interactions, and adiabatic cooling (see Reynoso et al. 2011). In Fig. 2, we show the acceleration and cooling rates for electrons and protons at the position z_{acc} in the jet. The list of assumed and derived parameters for the jet is shown in Table 1. The values for the black hole mass and redshift are taken as $M_{\text{bh}} = 10^9 M_{\odot}$, and $z_{\text{rs}} = 0.116$, respectively, following Aharonian et al. (2007), and the column density of HI is taken as $N_{\text{H}} = 1.3 \times 10^{20} \text{cm}^{-2}$ after Lockman & Savage (1995). The rest of the parameters in Table 1 corresponds to the above described jet model, which is discussed in detail in Reynoso et al. (2011). These parameters are fixed to obtain a SED that fits the quiescence emission represented by the same set of observational data used in Aharonian et al. (2009).

The SED is dominated by synchrotron and inverse Compton (IC) emission of the electrons, and pp originated very-high-energy (VHE) gamma-rays, as shown in Fig. 3. In our calculations, the VHE energy emission has been corrected by the effect of extragalactic background light (EBL) absorption following Domínguez et al. (2011).

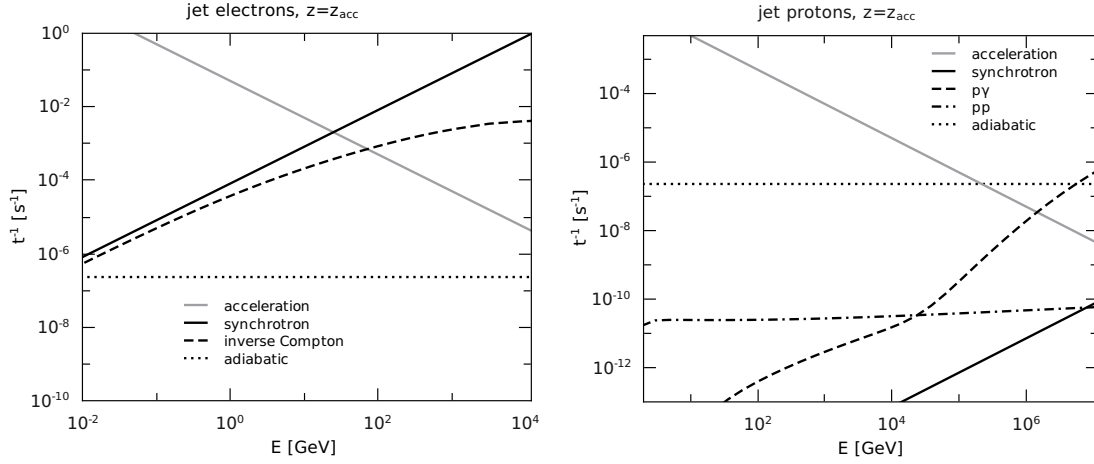


Fig. 2. Acceleration and cooling rates for primary electrons and protons in the jet at z_{acc} .

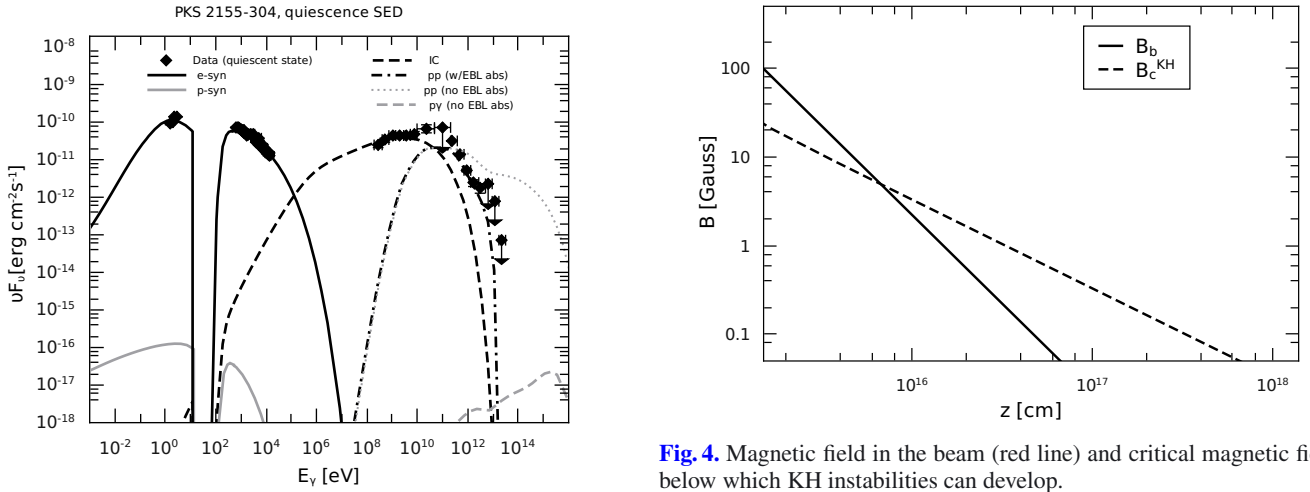


Fig. 3. SED corresponding to the quiescent state of PKS 2155-304. The contributions shown are electron synchrotron (black solid line), IC (dashed line), pp (dashed-dotted line), proton synchrotron (gray solid line), and py (gray dashed line).

Table 1. Model parameters for the quiescence emission from the jet of PKS 2155-304.

Parameter	Description	Value
M_{bh}	black hole mass	$10^9 M_{\odot}$
q_j	ratio $2L_j^{(\text{kin})}/L_{\text{Edd}}$	0.1
$\Gamma_j(z_0)$	bulk Lorentz factor of the jet at z_0	10
i_j	viewing angle	1°
ξ_j	jet's half-opening angle	1.5°
q_{rel}	jet's content of relativistic particles	0.1
a	hadron-to-lepton power ratio	50
z_0	jet's launching point	$50 R_g^a$
q_m	magnetic to kinetic energy ratio at z_{acc}	0.02
z_{acc}	injection point	$575 R_g$
Δz_j	size of injection zone	$z_{\text{acc}} \tan \xi_j$
m	index for magnetic field	1.8
s	spectral index injection	2.1
η	acceleration efficiency	10^{-6}
$E_p^{(\text{min})}$	minimum proton energy	2 GeV
$E_e^{(\text{min})}$	minimum electron energy	0.9 GeV
N_{H}	column density of HI	$1.3 \times 10^{20} \text{ cm}^{-2}$
z_{rs}	redshift	0.116

Notes. ^(a) $R_g = 1.48 \times 10^{14} \text{ cm}$.

Fig. 4. Magnetic field in the beam (red line) and critical magnetic field below which KH instabilities can develop.

4. Variable emission from the beam

The variable emission is assumed here to have its origin in shocked regions in the internal e^+e^- beam that can arise, e.g., due to Kelving-Helmholtz (KH) instabilities. These instabilities will be able to develop in the beam if the magnetic field is below a critical value (e.g. Romero 1995):

$$B_b < B_c^{\text{KH}} = \frac{\sqrt{4\pi n_b m_e c^2 (\Gamma_b^2 - 1)}}{\Gamma_b}. \quad (10)$$

In Fig. 4 we show the beam magnetic field and the critical value B_c^{KH} , considering that $\Gamma_b^{(0)} = 5$ at $z_b^{(0)} = 5R_g$. It can be seen from this plot that for $z \gtrsim 10^{16} \text{ cm}$ KH instabilities start to develop and create inhomogeneities if the pinching modes dominate (see Romero 1995). The rarefactions produced in the beam by the instabilities act as obstacles for the fast plasma, and strong shocks are expected to appear at $z \sim 10^{16} \text{ cm}$. These shocks re-accelerate the pairs (Araudo et al. 2010) producing a local injection of relativistic particles.

A shock front originating in the beam at a position z_i with a Lorentz factor Γ_s will form a post-shocked region of a certain size

$$\Delta z = \frac{z_i \chi_b}{b}, \quad (11)$$

with $\chi_b = \tan \xi_b$, and particles are injected during a time

$$\Delta t_{\text{inj, obs}} \approx \frac{\Delta z}{c}, \quad (12)$$

as seen in the observer frame.

The distribution of the injected pairs is computed in the post-shock frame, where the population is assumed to be isotropic. The corresponding source term is a power law with an exponential cutoff at the maximum Lorentz factor γ_{max} :

$$q_e(\gamma, t) = H(t - t_{\text{on}}) H(t_{\text{off}} - t) q_0 \gamma^{-s_b} \exp\left(-\frac{\gamma}{\gamma_{\text{max}}}\right), \quad (13)$$

is where H is the Heavyside step function, t_{on} the time when the injection is switched on, and the time when it is switched off is

$$t_{\text{off}} = t_{\text{on}} + \frac{\Delta t_{\text{inj, obs}}}{\Gamma_{\text{ps}}(1 + z_{\text{rs}})}, \quad (14)$$

both corresponding to the post-shock frame. We note that, for example, the onset time is transformed to the observer frame as

$$t_{\text{on, obs}} = \Gamma_{\text{ps}}(1 - z_{\text{rs}}) t_{\text{on}}. \quad (15)$$

The constant q_0 is found through normalization taking into account the particle density in the post-shock frame:

$$n_{\text{ps}} = \int_{t_{\text{on}}}^{t_{\text{off}}} dt \int_{\gamma_{\text{min}}}^{\infty} d\gamma q_e(\gamma, t). \quad (16)$$

This can be related to the beam density n_b by the compression factor ζ as

$$n_{\text{ps}} = \zeta n_b, \text{ with } \zeta = \left(\frac{\hat{\gamma} \Gamma'_{\text{ps}} + 1}{\hat{\gamma} - 1}\right), \quad (17)$$

where $\hat{\gamma} = 4/3$ is the polytropic index,

$$\Gamma'_{\text{ps}} = \Gamma_{\text{ps}} \Gamma_b (1 - \beta_{\text{ps}} \beta_b)$$

is the Lorentz factor of the shock in the undisturbed beam frame, and the Lorentz factor of the post-shock (ps) region is $\gamma_{\text{ps}} \approx \gamma_s / \sqrt{2}$. The density of the beam, in turn, is fixed as a fraction λ of the jet density of Eq. (2):

$$n_b = \lambda n_j. \quad (18)$$

The maximum Lorentz factor of the locally accelerated pairs γ_{max} is obtained from the balance between the acceleration rate and the cooling rate, where the latter is due to synchrotron and synchrotron self-Compton (SSC) interactions.

We solve the following kinetic equation to obtain the distribution of pairs as a function of time $n_e(\gamma, t)$:

$$\frac{\partial n_e}{\partial t} - \frac{\partial}{\partial \gamma} (n_e |\dot{\gamma}|_{\text{loss}}) = q_e(\gamma, t), \quad (19)$$

where the loss term is given by

$$|\dot{\gamma}|_{\text{loss}} = |\dot{\gamma}|_{\text{syn}} + |\dot{\gamma}|_{\text{SST}}. \quad (20)$$

An iterative process is implemented to work out $n_e(\gamma, t)$ from this equation. As a zero-order approximation, we adopt the solution corresponding to no SSC interactions, just synchrotron losses. Then, the solution is successively improved by computing the SSC cooling term using the previous solutions found for $n_e(\gamma, t)$. This cooling rate is computed in the Thompson

regime to save computing time, since this simplification was tested not to affect the final result. The self-synchrotron Thomson (SST) cooling rate is then (e.g. Schlickeiser & Lerche 2007):

$$|\dot{\gamma}|_{\text{SST}} = A_0 \gamma^2 \int_1^{\infty} d\gamma' \gamma'^2 n_e(\gamma', t), \quad (21)$$

where

$$A_0 = \frac{4}{3} c \sigma_T \frac{B_{\text{ps}}^2}{8\pi}.$$

The synchrotron cooling rate is

$$|\dot{\gamma}|_{\text{syn}} = \frac{\sigma_T B_{\text{ps}}^2}{6\pi m_e c} \gamma^2. \quad (22)$$

The acceleration rate is worked out using Eq. (9) along with the magnetic field corresponding to the post-shock frame,

$$B_{\text{ps}}(z_i) = B_b(z_i) \sqrt{\zeta^2 + 1}. \quad (23)$$

For any injection point z_i in the beam, we solve the kinetic equation, and work out the resulting synchrotron and SSC emission. In the local AGN frame, the emissivity is given by

$$\frac{dQ'_{\gamma}(E', t')}{d\Omega'} = D \frac{dQ_{\gamma}(E, t)}{d\Omega}, \quad (24)$$

where the Doppler factor is $D = \Gamma_{\text{ps}}^{-1}(1 - \beta_{\text{ps}} \cos i_j)^{-1}$, E is the photon energy in the ps frame, and $E' = D E$ is the photon energy in the local AGN frame. In the case of synchrotron radiation, the emissivity in the ps-frame is

$$\frac{dQ_{\gamma, \text{syn}}(E, t)}{d\Omega} = \frac{1}{4\pi E} \left(\frac{1 - e^{-\tau_{\text{SSA}}(E, t)}}{\tau_{\text{SSA}}(E, t)} \right) \int_{m_e c^2}^{\infty} d\gamma' P_{\text{syn}} n_e(\gamma', t), \quad (25)$$

where τ_{SSA} is the optical depth corresponding to synchrotron-self absorption, and the synchrotron power per unit energy emitted by the electrons is given by (Blumenthal & Gould 1970):

$$P_{\text{syn}}(E, \gamma, z) = \frac{\sqrt{2} e^3 B_{\text{ps}} E}{m_e c^2 h E_{\text{cr}}} \int_{E/E_{\text{cr}}}^{\infty} d\zeta K_{5/3}(\zeta), \quad (26)$$

where $K_{5/3}$ is the modified Bessel function of order 5/3 and

$$E_{\text{cr}} = \frac{\sqrt{6} h e B_{\text{ps}}}{4\pi m_e c} \gamma^2.$$

The soft photon density in the ps frame is

$$n_{\text{ph}}(E, t) \approx Q_{\text{syn}}(E, t) \frac{z_i \tan \xi_b}{c}, \quad (27)$$

and the IC emissivity in the this frame is

$$Q_{\gamma, \text{IC}}(E, t) = \frac{r_e^2 c}{2} \int_{E_{\text{(min)}}}^E dE_{\text{ph}} \frac{n_{\text{ph}}(E_{\text{ph}}, t)}{E_{\text{ph}}} \times \int_{\gamma_{\text{min}}}^{\gamma_{\text{max}}} d\gamma' \frac{n_e(\gamma', t)}{\gamma^2} F(q). \quad (28)$$

Here r_e is the classical electron radius, and we integrate in the target photon energy E_{ph} and in the electron Lorentz factors γ' between

$$\gamma_{\text{min}} = \frac{E}{2m_e c^2} + \sqrt{\frac{E}{4E_{\text{ph}}} + \frac{E^2}{4m_e^2 c^4}} \text{ and } \gamma_{\text{max}} = \frac{E}{m_e c^2 \left(1 - \frac{E}{E_{\text{ph}}}\right)}.$$

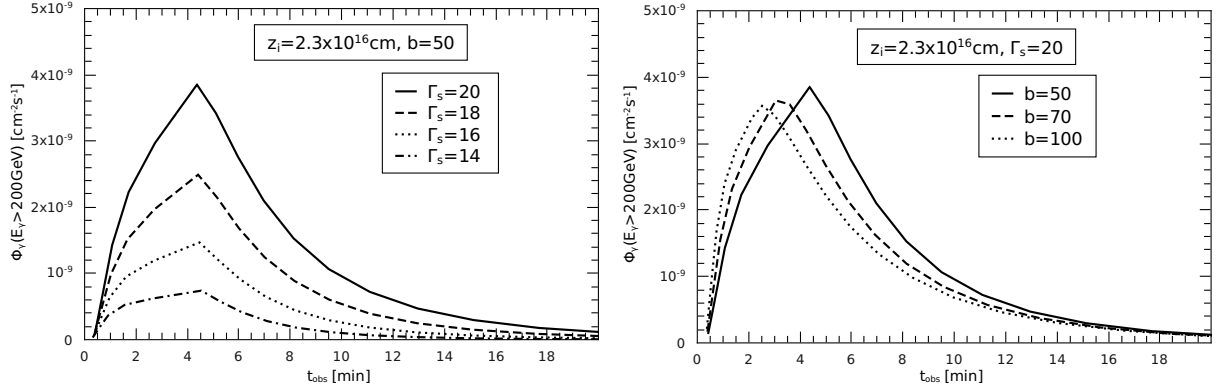


Fig. 5. Light curves of gamma-rays above 200 GeV produced by e^+e^- injection in the beam at $z_i = 2.3 \times 10^{16}$ cm with $\Gamma_s = \{14, 16, 18, 20\}$ in the left panel, and with $\Gamma_s = 20$ and $b = \{50, 70, 100\}$ in the right panel.

The function $F(q)$ is given by

$$F(q) = 2q \ln q + (1 + 2q)(1 - q) + \frac{1}{2}(1 - q) \frac{(q\Gamma_e')^2}{1 + \Gamma_e'}, \quad (29)$$

with $\Gamma_e = 4E_{\text{ph}}\gamma'/(m_e c^2)$ and

$$q = \frac{E}{\Gamma_e E_{\text{ph}}(1 - E/E_{\text{ph}})}.$$

The differential photon flux is first obtained in the AGN local frame as

$$\frac{d\Phi'_\gamma(E', t')}{dE'} = (\pi z_i^2 \tan^2 \xi_b \Delta z) \frac{dQ'_\gamma(E', t')}{d\Omega'} \frac{d\Omega'}{dA'} \exp[-\tau_{\gamma\gamma}], \quad (30)$$

where $\tau_{\gamma\gamma} = \tau_{\gamma\gamma}^{(b)} + \tau_{\gamma\gamma}^{(j)}$ is the $\gamma\gamma$ optical depth due to the jet and the beam photons. The latter is estimated as

$$\tau_{\gamma\gamma}^{(b)}(E', t') = (z_i \tan \xi_b) \int_{-1}^1 dx (1 - x) \times \int_{\frac{2m_e^2 c^4}{E(1-x')}}^{\infty} dE_{\text{ph}} n_{\text{ph}}(E_{\text{ph}}, t') \sigma_{\gamma\gamma}(E, E_{\text{ph}}), \quad (31)$$

and $\tau_{\gamma\gamma}^{(j)}$ is obtained from a similar expression.

If d_C is the comoving distance, then

$$\frac{d\Omega'}{dA'} = \frac{1}{d_C^2},$$

and taking into account that the observed energy and time are transformed as

$$E_\gamma = \frac{E'}{1 + z_{\text{rs}}} \text{ and } t_{\text{obs}} = t'(1 + z_{\text{rs}}),$$

the differential photon flux arriving on Earth from a source at redshift z_{rs} is

$$\frac{d\Phi_\gamma(E_\gamma, t_{\text{obs}})}{dE_\gamma} = \frac{(1 + z_{\text{rs}})^2}{d_L^2} \frac{d\Phi'_\gamma(E_\gamma(1 + z_{\text{rs}}), \frac{t_{\text{obs}}}{1 + z_{\text{rs}}})}{dE'} \times \exp[-\tau_{\text{EBL}}(E_\gamma, z_{\text{rs}})], \quad (32)$$

where d_L is the luminosity distance and τ_{EBL} is the optical depth due to $\gamma\gamma$ absorption on the extragalactic background light. In these terms, the usual amount νF_ν in units $\text{erg cm}^{-2} \text{s}^{-1}$ is expressed as $E_\gamma \frac{d\Phi_\gamma}{dE_\gamma}$. A light curve can be obtained simply by integrating Eq. (32) on the desired energy range for different times.

Table 2. Beam parameters.

Parameter	Description	Value
$z_{(b)}^{(0)}$	launching point [R_g]	5
$\Gamma_b^{(0)}$	Lorentz factor at $z_{(b)}^{(0)}$	5
λ	beam to jet density ratio	0.1
ξ_b	half-opening angle [$^\circ$]	0.5

In Fig. 5 we show the light curves that can be obtained if the injection point in the beam is $z_i = 2.3 \times 10^{16}$ cm for different shock Lorentz factors Γ_s and sizes of the injection zone $\Delta z = R_b/b$. The values adopted for beam parameters are shown in Table 2. More complex light curves can be obtained, for instance, by successive shock injections at the same position with Γ_s , b , and t_{on} chosen randomly in the ranges:

$$\Gamma_s \in \{17, 18, 19\} \quad (33)$$

$$b \in \{50, 60, 70, 80, 90\} \quad (34)$$

$$t_{\text{on}} \in [1 \dots 15] \text{ min.} \quad (35)$$

Some example light curves obtained in this way are plotted in Fig. 6 with the parameters shown in Table 3.

In particular, in view of the flaring activity detected in 2006 (Aharonian et al. 2007), we see that a similar lightcurve can be obtained for the flux of gamma-rays above 200 GeV by adding up six different injections at a fixed position in the beam, $z_i = 4 \times 10^{16}$ cm, each being switched on at appropriate times t_{on} , as seen in Fig. 7. The values of the different parameters are shown in Table 4. The multiple shock scenario resembles the one proposed to explain the rapid variability in gamma-ray bursts (GRBs), e.g., Kobayashi et al. (1997). The whole SED evolution shown in Fig. 8 shows that multiwavelength observations, including studies of rapid variability in radio, X-ray, and γ -ray bands, can be used to test the proposed model.

In Fig. 8, we show for illustration two instantaneous contributions to the SED due to the shocked beam at $t_1 \simeq 40$ min and $t_2 \simeq 50$ min. The acceleration and cooling rates corresponding to t_1 are shown in Fig. 9, where it can be seen that the Lorentz factors of the electrons are $\sim 10^6$ in the post-shock frame. The inverse Compton interactions with target photons created in the jet was verified to be unimportant for the adopted value of z_i .

5. Neutrino emission

The acceleration of protons in the jet and their interactions with synchrotron photons and cold jet protons lead to the production

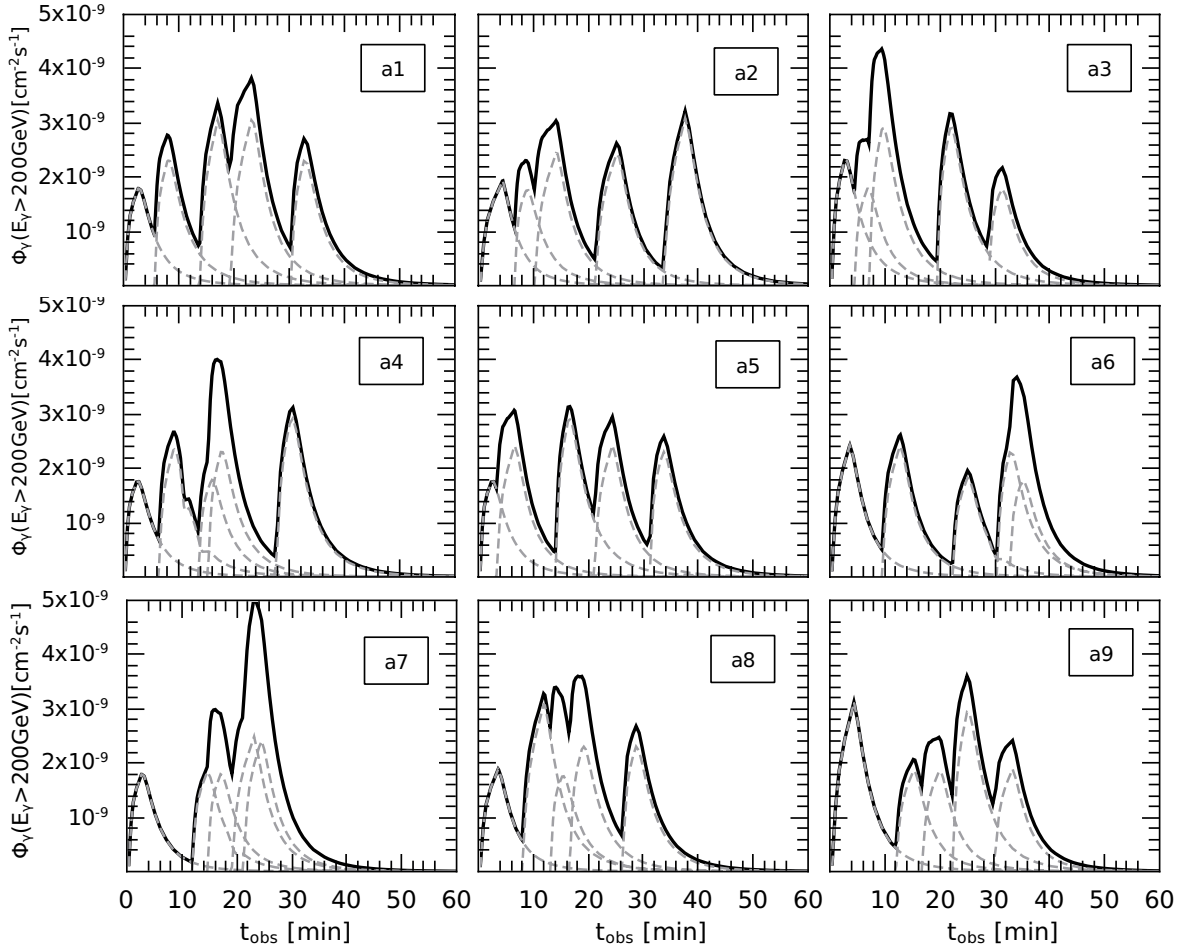


Fig. 6. Light curves of gamma-rays above 200 GeV produced by e^+e^- injection in the beam at $z_i = 2.3 \times 10^{16}$ cm with the randomly chosen values for Γ_s , b , and t_{on} of Table 3.

Table 3. Randomly chosen values for the parameters corresponding to Fig. 6.

Label	Γ_s	b	$t_{\text{on}}[\text{min}]$
a1	17, 18, 19, 19, 18	80, 80, 60, 50, 80	5.3, 8.1, 5.5, 11
a2	17, 17, 18, 18, 19	50, 90, 50, 50, 50	6.3, 3.6, 11, 12.4
a3	18, 17, 19, 19, 17	90, 80, 80, 80, 80	4.2, 2.6, 12.3, 9.4
a4	17, 18, 17, 18, 19	90, 70, 80, 90, 70	6, 7.2, 1.7, 12.3
a5	17, 18, 19, 18, 18	90, 60, 80, 60, 90	3, 10.7, 7, 10.1
a6	18, 18, 17, 18, 17	60, 60, 70, 90, 80	9.1, 12.9, 8.1, 2.2
a7	17, 17, 17, 18, 18	80, 70, 80, 50, 60	11.6, 2.8, 4.4, 2.1
a8	17, 19, 17, 18, 18	80, 70, 80, 50, 60	7.6, 5.2, 3.5, 9.6
a9	19, 17, 17, 19, 17	50, 60, 60, 70, 60	11.7, 4.7, 5.5, 7.6

of VHE gamma-rays after π^0 decays, as seen in the SED of Fig. 3. These pp and pp interactions also give rise to charged pions that decay to muons and neutrinos. The stationary distributions of pions and muons in the jet, $N_\pi(E, z)$ and $N_\mu(E, z)$, are found using the transport equation Eq. (4). The corresponding neutrino emissivity from direct pion decay can be computed in the jet comoving frame following Lipari et al. (2007):

$$Q_{\pi \rightarrow \nu_\mu}(E, z) = \int_E^\infty dE_\pi T_{\pi, d}^{-1}(E_\pi) N_\pi(E_\pi, z) \times \frac{\Theta(1 - r_\pi - x)}{E_\pi(1 - r_\pi)}, \quad (36)$$

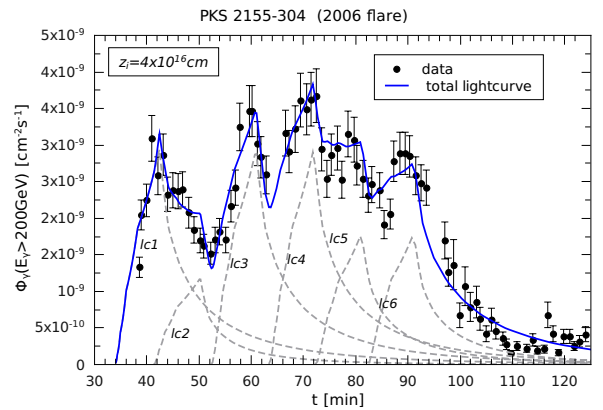


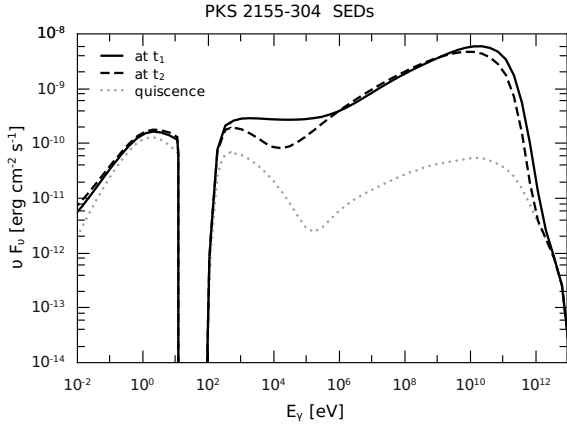
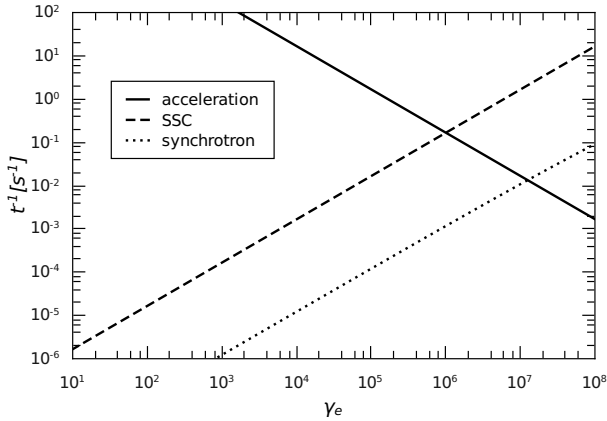
Fig. 7. Lightcurve of gamma-rays above 200 GeV (blue line), generated as the superposition of six injections in the beam ($lc1$, $lc2$, $lc3$, $lc4$, $lc5$, $lc6$, in gray-dashed lines), as compared to data of the 2006 flare of PKS 2155-304.

with $x = E/E_\pi$ and $T_{\pi, d} = 2.6 \times 10^{-8}$ s. The contribution from muon decays ($\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$, $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$) can be calculated as

$$Q_{\mu \rightarrow \nu_\mu}(E, z) = \sum_{i=1}^4 \int_E^\infty \frac{dE_\mu}{E_\mu} T_{\mu, d}^{-1}(E_\mu) N_{\mu_i}(E_\mu, z) \times \left[\frac{5}{3} - 3x^2 + \frac{4}{3}x^3 \right]. \quad (37)$$

Table 4. Model parameters for the variable emission from the beam of PKS 2155-304.

Parameter	description	lc1 value	lc2 value	lc3 value	lc4 value	lc5 value	lc6 value
Γ_s	shock Lorentz factor	13	10.5	13	13	11.5	11.5
η_b	acceleration efficiency	10^{-2}	10^{-2}	10^{-2}	10^{-2}	10^{-2}	10^{-2}
s_b	power law injection index	2.1	2.1	2.1	2.1	2.1	2.1
z_i	position of injection at the beam [cm]	4×10^{16}	4×10^{16}	4×10^{16}	4×10^{16}	4×10^{16}	4×10^{16}
Δz	size of injection zone	$z_i \chi_b / 50$	$z_i \chi_b / 50$	$z_i \chi_b / 50$	$z_i \chi_b / 50$	$z_i \chi_b / 50$	$z_i \chi_b / 50$
$t_{\text{on, obs}}$	observed onset time [min]	0	7.5	11	11	9	10
γ_{min}	minimum Lorentz factor of injection	10	10	10	10	10	10
B_{ps}	post-shock magnetic field at z_i [Gauss]	0.95	0.97	0.95	0.95	0.96	0.96


Fig. 8. Instantaneous SEDs originating in the beam at $t_1 \simeq 40$ min, and $t_2 \simeq 50$ min corresponding to the plot of Fig. 7. The quiescent SED is also shown (gray dashed lines).

Fig. 9. Acceleration and cooling rates in the post-shock frame corresponding to $t_1 \simeq 40$ min in the lightcurve of Fig. 7.

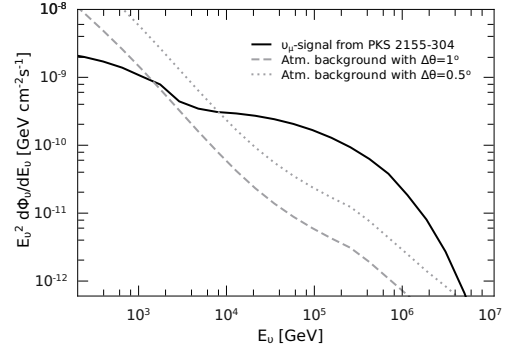
In this expression, $x = E/E_\mu$, $\mu_{1,2} = \mu_L^{-,+}$, $T_{\mu,d} = 2.2 \times 10^{-6}$ s, and $\mu_{3,4} = \mu_R^{-,+}$.

In the local AGN frame, the differential neutrino emissivity, in units ($\text{GeV}^{-1} \text{cm}^{-3} \text{sr}^{-1} \text{s}^{-1}$) is given by

$$\frac{dQ'_\nu(E', z)}{d\Omega'} = D \frac{Q_{\pi \rightarrow \nu_\mu}(E, z) + Q_{\mu \rightarrow \nu_\mu}(E, z)}{4\pi}, \quad (38)$$

where z is the distance from the black hole to the position in the jet in the AGN frame and $D = \Gamma_j^{-1} (1 - \beta_j \cos i_j)^{-1}$. The differential neutrino flux is then

$$\frac{d\Phi'_\nu}{dE'} = \frac{1}{d_C^2} \int_{z' > z_{\text{acc}}} dV' \frac{dQ'_\nu(E', z')}{d\Omega'}, \quad (39)$$


Fig. 10. Predicted muon neutrino differential flux weighted by the squared neutrino energy as compared to the flux of atmospheric neutrinos for $\Delta\theta_{\text{bin}} = \{0.5^\circ, 1^\circ\}$.

and in the observer frame, since the redshifted neutrino energy is $E_\nu = E'/(1 + z_{\text{rs}})$,

$$\frac{d\Phi_\nu(E_\nu)}{dE_\nu} = \frac{d\Phi'_\nu(E_\nu(1 + z_{\text{rs}}))}{dE'}. \quad (40)$$

On Earth, neutrino telescopes are used to observe this flux in the presence of the atmospheric neutrino background, $\frac{d\Phi_\nu(E_\nu)}{dE_\nu d\Omega}$, which introduces more events depending on the size of the angular search bin of the detector,

$$\Delta\Omega_{\text{bin}} = 2\pi \left(1 - \cos \frac{\Delta\theta_{\text{bin}}}{2}\right).$$

This depends on the resolution of the detector $\Delta\theta_{\text{bin}}$, which is expected to be below 1° for KM3NeT. In the case of PKS 2155-304, we compare in Fig. 10 the predicted neutrino flux with the atmospheric background for $\Delta\theta_{\text{bin}} = \{0.5^\circ, 1^\circ\}$.

The signal to be searched for in neutrino telescopes such as ANTARES or KM3NeT, can be calculated as

$$N_s(E_\nu > E_\nu^{(\text{min})}) = T_{\text{obs}} \int_{E_\nu^{(\text{min})}} dE_\nu \frac{d\Phi_\nu(E_\nu)}{dE_\nu} A_\nu^{\text{eff}}(E_\nu), \quad (41)$$

where $A_\nu^{\text{eff}}(E_\nu)$ is the neutrino effective area of the detector and T_{obs} is the observation time. These signal events are to be detected among the background events caused by the flux of atmospheric neutrinos, which are given by

$$N_b(E_\nu > E_\nu^{(\text{min})}) = T_{\text{obs}} \Delta\Omega_{\text{bin}} \int_{E_\nu^{(\text{min})}} dE_\nu \frac{d\Phi_\nu^{(\text{atm})}(E_\nu)}{dE_\nu d\Omega} A_\nu^{\text{eff}}(E_\nu). \quad (42)$$

Considering the neutrino effective area expected for this detector, we compute the predicted number of signal events of $(\nu_\mu + \bar{\nu}_\mu)$

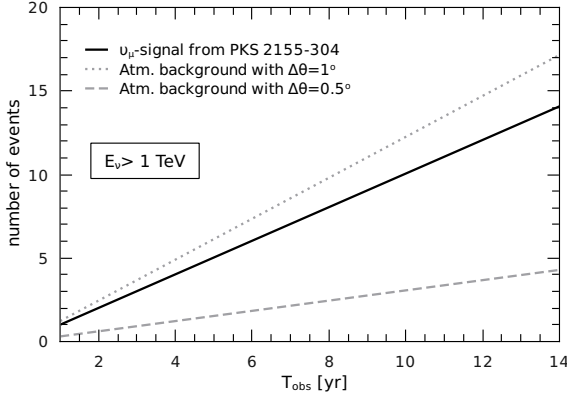


Fig. 11. Muon neutrino events from PKS 2155-304 and atmospheric background for $\Delta\theta_{\text{bin}} = \{0.5^\circ, 1^\circ\}$ as a function of the observation time.

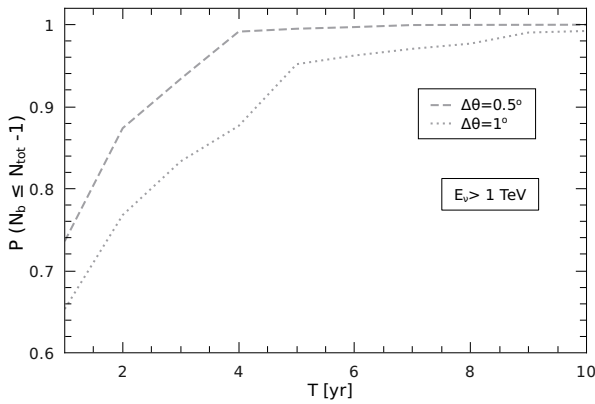


Fig. 12. Cumulative probability that at least one event corresponds to the neutrino signal from PKS 2155-304 as a function of the observation time.

from PKS 2155-304 as a function of the observation time, and compare it with the background events corresponding to $\Delta\theta_{\text{bin}} = 1^\circ$ and 0.5° . The result is shown in Fig. 11 and corresponds to neutrinos above $E_\nu^{(\text{min})} = 1$ TeV, yielding many events in a few years.

We can proceed to compute the cumulative probability that at least one of the total events corresponds to the signal, and not to the background, as a function of the observation time. This can be done by assuming that the occurrence of the signal event and background events N_s and N_b follow Poisson distributions. As a result, the probability that out of a total of events $N_{\text{tot}} = N_s + N_b$ we have at most $N_b < N_{\text{tot}}$ can be expressed as

$$P(N_b < N_{\text{tot}}) = \sum_{k=0}^{N_{\text{tot}}-1} \frac{N_b^k \exp(-N_b)}{k!}. \quad (43)$$

We show this cumulative probability in Fig. 12 for both $\Delta\theta_{\text{bin}} = \{0.5^\circ, 1^\circ\}$, where it can be seen that if PKS 2155-304 actually emits neutrinos at the level suggested here, a neutrino telescope like the planned KM3NeT would be able to ascribe to at least one event to this blazar with a probability very close to one after an observation period of four years. We point out here that a resolution of 0.5° is actually conservative (e.g. Kappes et al. 2007; Bersani 2012).

6. Discussion

We have implemented a two-component model to study the emission of the blazar PKS 2155-304. The quiescent state of electromagnetic emission was associated with the contribution produced in a heavy barionic jet, in which both electrons and protons can be accelerated. Specifically, this low state of emission is dominated by synchrotron and inverse Compton interactions of the primary electrons, and also by pp interactions in the jet. The time-dependent contribution is produced by multiple shocks in an internal electron-positron beam, surrounded by the jet. We showed that if shocks are injected in this beam, as would be expected as a consequence of Kelvin-Helmholtz instabilities, then a variable emission can be generated via SSC interactions, giving rise to gamma-ray light curves similar to those observed by HESS.

Other important output predicted by the present model is in the form of VHE neutrinos produced by pp interactions. If this accompanying flux remains constantly produced over a period of four years, the detection of at least one event from PKS 2155-304 should be guaranteed in a detector like KM3NeT with a probability very close to one. This would be a very important piece of evidence for hadronic acceleration in the source. Conversely, if the neutrinos are not detected at this level, this would be evidence of a leptonic-dominated source.

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