Some stylized facts of the Bitcoin market

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Research highlights:

- We study statistical features and long-range dependence of Bitcoin returns.
- Hurst exponent is computed for sliding windows.
- Liquidity does not affect the level of long-range dependence
- Similar behavior of Hurst exponent at different time scales
Some stylized facts of the Bitcoin market

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Abstract

In recent years a new type of tradable assets appeared, generically known as cryptocurrencies. Among them, the most widespread is Bitcoin. Given its novelty, this paper investigates some statistical properties of the Bitcoin market. This study compares Bitcoin and standard currencies dynamics and focuses on the analysis of returns at different time scales. We test the presence of long memory in return time series from 2011 to 2017, using transaction data from one Bitcoin platform. We compute the Hurst exponent by means of the Detrended Fluctuation Analysis method, using a sliding window in order to measure long range dependence. We detect that Hurst exponents changes significantly during the first years of existence of Bitcoin, tending to stabilize in recent times. Additionally, multiscale analysis shows a similar behavior of the Hurst exponent, implying a self-similar process.

Keywords: Bitcoin, Hurst, DFA, Bitcoin, long memory

1. Introduction

According to the traditional definition, a currency has three main properties: (i) it serves as a medium of exchange, (ii) it is used as a unit of
account and (iii) it allows to store value. Along economic history, monies were related to political power. In the beginning, coins were minted in precious metals. Therefore, the value of a coin was intrinsically determined by the value of the metal itself. Later, money was printed in paper bank notes, but its value was linked somewhat to a quantity in gold, guarded in the vault of a central bank. Nation states have been using their political power to regulate the use of currencies and impose one currency (usually the one issued by the same nation state) as legal tender for obligations within their territory. In the twentieth century, a major change took place: abandoning gold standard. The detachment of the currencies (specially the US dollar) from the gold standard meant a recognition that the value of a currency (specially in a world of fractional banking) was not related to its content or representation in gold, but to a broader concept as the confidence in the economy in which such currency is based. In this moment, the value of a currency reflects the best judgment about the monetary policy and the “health” of its economy.

In recent years, a new type of currencies, a synthetic one, emerged. We name this new type as “synthetic” because it is not the decision of a nation state, nor represents any underlying asset or tangible wealth source. It appears as a new tradable asset resulting from a private agreement and facilitated by the anonymity of internet. Among this synthetic currencies, Bitcoin (BTC) emerges as the most important one, with a market capitalization of 15 billions, as of December 2016. There are other cryptocurrencies, based on blockchain technology, such as Litecoin (LTC), Ethereum (ETH), Ripple (XRP). The website https://coinmarketcap.com/currencies/ counts up to 641 of such monies. However, as we can observe in Figure 1, Bitcoin represents 89% of the capitalization of the market of all cryptocurrencies. One open question today is if Bitcoin is in fact a, or may be considered as a, currency. Until now, we cannot observe that Bitcoin fulfills the main properties of a standard currency. It is barely accepted as a medium of exchange (e.g. to buy some products online), it is not used as unit of account (there are no financial statements valued in Bitcoins), and we can hardly believe that, given the great swings in price, anyone can consider Bitcoin as a suitable option to store value. Given these characteristics, Bitcoin could fit as an ideal asset for speculative purposes. There is no underlying asset to relate its value to and there is an open platform to operate round the clock.

The aim of this paper is to study some statistical characteristics of Bitcoin et al. vis-à-vis some major currencies, during the period 2011-2017. We will focus our attention on the evolution of the long memory of the time series. This article contributes to the literature in three important aspects.
First, we expand the empirical studies by analyzing the long memory of a new asset. Second, we compare the behavior of Bitcoin with some major currencies. Third, we highlight the evolution in the underlying dynamics of this new market. The rest of the paper is organized as follows: Section 2 describes the recent emerging literature on Bitcoin, Section 3 describes the methodology used in the paper, Section 4 presents the data and results of our empirical analysis and, finally Section 5 draws the main conclusions.

2. Brief literature review

2.1. Bitcoin

Speculation has a long history and it seems inherent to capitalism. One common feature of speculative assets in history has been the difficulty in valuation. Tulipmania, the South Sea bubble, and more others, reflect on one side human greedy behavior, and on the other side, the difficulty to set an objective value to an asset. All speculative behaviors were reflected in a super-exponential growth of the time series [2].

Cryptocurrencies can be seen as the libertarian response to central bank failure to manage financial crises, as the one occurred in 2008. Also cryptocurrencies can bypass national restrictions to international transfers, probably at a cheaper cost. Bitcoin was created by a person or group of persons under the pseudonym Satoshi Nakamoto. The description of Bitcoin Core, i.e. the open source client of the Bitcoin cryptocurrency, is described in [3].

The discussion of Bitcoin has several perspectives. The computer science perspective deals with the strengths and weaknesses of blockchain technology. In fact, according to [4], the introduction of a “distributed ledger” is the key innovation. Traditional means of payments (e.g. a credit card), rely on a central clearing house that validate operations, acting as “middleman”
between buyer and seller. On contrary, the payment validation system of Bitcoin is decentralized. There is a growing army of miners, who put their computer power at disposal of the network, validating transactions by gathering together blocks, adding them to the ledger and forming a 'block chain'. This work is remunerated by giving the miners Bitcoins, what makes (until now) the validating costs cheaper than in a centralized system. The validation is made by solving some kind of algorithm. With the time solving the algorithm becomes harder, since the whole ledger must be validated. Consequently it takes more time to solve it. Contrary to traditional currencies, the total number of Bitcoins to be issued is beforehand fixed: 21 million. In fact, the issuance rate of Bitcoins is expected to diminish over time. According to [5], validating the public ledger was initially rewarded with 50 Bitcoins, but the protocol foresee halving this quantity every four years. At the current pace, the maximum number of Bitcoins will be reached in 2140. Taking into account the decentralized character, Bitcoin transactions seem secure. All transactions are recorded in several computer servers around the world. In order to commit fraud, a person should change and validate (simultaneously) several ledgers, which is almost impossible. Additional, ledgers are public, with encrypted identities of parties, making transactions “pseudonymous, not anonymous” [6].

The legal perspective of Bitcoin is fuzzy. Bitcoin is not issued, nor endorsed by a nation state. It is not an illegal substance. As such, its transaction is not regulated.

The economic perspective is still under study. The use of Bitcoin in daily life is marginal. At the time of writing this paper, there were only 8367 retailers worldwide who accepted Bitcoins as a means of payment, mostly concentrated in North America, western Europe, and some major cities in South America and South East Asia [7]. There is not too much information regarding Bitcoin exchanges. This gray situation raises some concerns about a possible Ponzi scheme. There are no savings accounts in Bitcoins and consequently no interest rates. All these elements together contribute to its difficulty to assess a fair value. Cheung et al. [8] detect several price bubbles over the period 2010-2014. Three of them lasted from 66 to 106 days to burst. Ciaian and coworkers [9] find no macro-financial indications driving Bitcoin price, and they do not discard that investor speculation affects significantly the price evolution.

2.2. The Efficient Market Hypothesis

As recalled in the previous section, the nature of the Bitcoin is not yet clear. In particular, given the nonexistence of saving accounts in Bitcoin,
and consequently the absence of a Bitcoin interest rate, precludes the idea of studying the price behavior in relation with cash flows generated by Bitcoins. As a consequence, we aim to analyze the underlying dynamics of the price signal, using the Efficient Market Hypothesis as a theoretical framework. The Efficient Market Hypothesis (EMH) is the cornerstone of financial economics. One of the seminal works on the stochastic dynamics of speculative prices is due to Bachelier [10], who in his doctoral thesis developed the first mathematical model concerning the behavior of stock prices. The systematic study of informational efficiency begun in the 1960s, when financial economics was born as a new area within economics. The classical definition due to Eugene Fama [11] says that a market is informationally efficient if it “fully reflect all available information”. Therefore, the key element in assessing efficiency is to determine the appropriate set of information that impels prices. Following [12], informational efficiency can be divided into three categories: (i) weak efficiency, if prices reflect the information contained in the past series of prices, (ii) semi-strong efficiency, if prices reflect all public information and (iii) strong efficiency, if prices reflect all public and private information. As a corollary of the EMH, one cannot accept the presence of long memory in financial time series, since its existence would allow a riskless profitable trading strategy. If markets are informationally efficient, arbitrage prevent the possibility of such strategies.

An important part of the literature focused its attention on studying the long-range dependence. If we consider the financial market as a dynamical structure, short term memory can exist (to some extent) without contradicting the EMH. In fact, the presence of some mispriced assets is the necessary stimulus for individuals to trade and reached an (almost) arbitrage free situation. However, the presence of long range memory is at odds with the EMH, because it would allow an stable trading rule to beat the market.

Given the novelty of Bitcoin, this is one of the first papers (probably with the single exception of [13]) to study the Hurst exponent of this market. Previous works on long range dependence focused their attention in stocks, bonds or commodities markets. In particular, [14] and [15] use the Hurst exponent to detect the presence of long memory in the US and the UK stock markets, respectively. In [16] positive short term autocorrelation and negative long term autocorrelation is found, after examining the returns of a diversified portfolio of the NYSE. This result reinforces the idea of an underlying mean-reverting process. Long memory is also found in the Spanish stock market [17] and the Turkish stock market [18]. In the same line, Barkoulas et al. [19] finds evidence of long memory in the weekly returns of the Athens Stock Exchange during the period 1981-1990, and
suggest that the strength of the memory could be influenced by the market size. Also long memory behavior in the Greek market was found by Panas [20]. Cajueiro and Tabak [21] find that developed markets are more informationally efficient than emerging markets and that the level of efficiency is influenced by market size and trading costs. Cajueiro and Tabak [22] relate long-range dependence with specific financial variables of the firms under examinations. Zunino and coworkers [23] find that the long-range memory in seven Latin-American markets is time varying. In this line, Bariviera [24] finds evidence of a time varying long-range dependence in daily returns of Thai Stock Market during the period 1975-2010 and concludes that it is weakly influenced by the liquidity level and market size. Vodenska et al. [25] show that volatility clustering in the S & P 500 index produces memory in returns. [26] finds long memory in the sign of transactions but not in the signs of returns. Ureche-Rangau and de Rorthays,[27] investigate the presence of long memory in volatility and trading volume of the Chinese stock market. Cajueiro and Tabak [28] present empirical evidence of time-varying long-range dependence for US interest rates. It concludes that long memory has reduced over time. Moreover, Cajueiro and Tabak[29] find that this long-range dependence, is affected by the monetary policy. Similarly, Cajueiro and Tabak [30] find long range dependence in Brazilian interest rates and their volatility, providing important implications for monetary studies. Time-varying long range dependence in Libor interest rates is found in [31, 32]. The authors conclude that such behavior is consistent with the Libor rate rigging scandal.

Cheung and Lai [33] use the fractional differencing test for long memory by [34] and find evidence of long memory in 5 out of the 18 markets under study. Using a different methodology, [35] applies spectral regression to time series of 30 firms, 7 sector indices and 2 broad stock indices at daily and monthly frequency, and finds evidence of long memory only in 5 of the individual firms. Wright [36] compares the memory content of the time series in developed and emerging stock markets, finding that the latter exhibits short term serial correlation in addition to long-range memory. Henry [37] concludes that there is strong evidence of long-range memory in the Korean market and some weak evidence on the German, Japanese and Taiwanese markets, after analyzing monthly returns of nine stock markets. Also, Tolvi [38] uses a sample of 16 stock markets of OECD countries and finds evidence of long memory only in 3 of them and Kasman et al. [39] finds that among the four main central European countries (Czech Republic, Hungary, Poland and Slovak Republic), only the last one exhibits long memory. Cheong [40] computes the Hurst exponent by means of three heuristic methods and find
evidence of long memory in the returns of five Malaysian equity market indices. This study finds that the Asian economic crisis affected the extent of long-range memory of the Malaysian stock market.

With respect to the fixed income market, Carbone [41] finds local variability of the correlation exponent in the German stock and sovereign bond markets. Bariviera et al. [42] finds empirical evidence of long memory in corporate and sovereign bond markets and detects that the current financial crisis affects more the informational efficiency of the corporate than sovereign market. Zunino et al. [43], using the complexity-entropy causality plane for a sample of thirty countries, finds that informational efficiency is related to the degree of economic development. Recently, Bariviera et al. [44] finds that the long range memory of corporate bonds at European level are affected unevenly during the financial crisis. In particular, sectors closely related to financial activities were the first to exhibit a reduction in the informational efficiency.

There are some works that find no evidence of long memory in the financial time series. Among others we can cite Lo [45], in the returns of US stocks, and Grau-Carles [46] in the stock indices of US, UK, Japan and Spain.

As we can appreciate, the empirical studies on sovereign and corporate bond markets and stock markets are abundant. Giving the increasing amounts involved in Bitcoin trading, we believe that this topic deserves a detailed study.

3. Long range dependence

The presence of long range dependence in financial time series generates a vivid debate. Whereas the presence of short term memory can stimulate investors to exploit small extra returns, making them disappear, long range correlations poses a challenge to the established financial model. As recognized by [9], Bitcoin price is not driven by macro-financial indicators. Consequently a detailed analysis of the underlying dynamics becomes important to understand its emerging behavior.

There are several methods (both parametric and non parametric) to calculate the Hurst exponent. For a survey on the different methods for estimating long range dependences see [47] and [48]. Serinaldi [49] makes a critical review on the different estimation methods of the Hurst exponent, concluding that an inappropriate application of the estimation method could lead to incorrect conclusions about the persistence or anti-persistence of financial series. Although R/S method is probably one of the most extended...
methods to approximate long run memory in time series, it is not robust to departures from stationarity. Consequently, if the process under scrutiny exhibits short memory, the R/S statistic could indicate erroneously the presence of long memory. In this sense, [50] develops the method called Detrended Fluctuation Analysis (DFA) that is more appropriate when dealing with nonstationary data. As recognized by [51], this method avoids spurious detection of long-range dependence due to nonstationary data. Due to this reason we select the DFA method in order to assess the existence of long memory in this paper.

The algorithm, described in detail in [52], begins by computing the mean of the stochastic time series $y(t)$, for $t = 1, \ldots, M$. Then, an integrated time series $x(i)$, $i = 1, \ldots, M$ is obtained by subtracting mean and adding up to the $i$-th element, $x(i) = \sum_{t=1}^{i} [y(t) - \bar{y}]$. Then $x(i)$ is divided into $M/m$ non overlapping subsamples and a polynomial fit $x_{pol}(i, m)$ is computed in order to determine the local trend of each subsample. Next the fluctuation function

$$F(m) = \sqrt{\frac{1}{M} \sum_{i=1}^{M} [x(i) - x_{pol}(i, m)]^2} \quad (1)$$

is computed. This procedure is repeated for several values of $m$. The fluctuation function $F(m)$ behaves as a power-law of $m$, $F(m) \propto m^H$, where $H$ is the Hurst exponent. Consequently, the exponent is computed by regressing $\ln(F(m))$ onto $\ln(m)$. According to the literature the maximum block size to use in partitioning the data is $(\text{length}(\text{window})/2)$, where $\text{window}$ is the time series window vector. Consequently, in this paper we use six points to estimate the Hurst exponent. The points for regression estimation are: $m = \{4, 8, 16, 32, 64, 128\}$.

There are other methodologies to verify the presence of long-range memory. Rosso et al. [53] introduces the complexity-causality plane in order to discriminate between Gaussian from non-Gaussian processes. Zunino et al. [54] shows that this innovative approach could be used to rank stock markets according to their stage of development. In Zunino et al. [55], the application of the complexity-entropy causality plane was extended to the study of the efficiency of commodity prices. This method reveals that it is not only useful to produce a ranking of efficiency of different commodities, but it also allows to identify periods of increasing and decreasing randomness in the price dynamics. Zunino et al. [43] uses this representation space to establish an efficiency ranking of different markets and distinguish different bond market dynamics and concludes that the classification derived from the complexity-entropy causality plane is consistent with the qualifications
assigned to sovereign instruments by major rating companies.

4. Data and results

The period under study goes from 2011 until 2017 for daily data and from 2013 until 2016 for intraday data. We downloaded the daily prices of Bitcoin and exchange rates of Euro and Sterling Pound, in US dollars. These daily data were downloaded from Datastream. Additionally, we downloaded Bitcoin intraday transaction data from Bitcoin charts website [56]. The original dataset comprises a total of 9540332 transactions. Given that transactions take place irregularly in time, we sampled data each \{5, 6, ..., 12\} hours. The minimum sample space corresponds to the maximum time without transactions in our dataset.

We compute the instantaneous return, measured as \( r_t = \log(P_t) - \log(P_{t-1}) \). With this values we calculate the Hurst exponent using DFA method. In order to assess the change in time in long range memory, following [57, 58], we use sliding windows. We estimate the Hurst exponent using two year sliding windows (500 datapoints). In particular, we use overlapping windows, moving forward by 1 datapoint, in order to allow for smooth transitions.

4.1. Daily returns

Our first analysis focuses on the descriptive statistics of daily returns of Bitcoin (BTC) vis-à-vis two major currencies such as Euro (EUR) and the British Pound (GBP). Results are presented in Table 1. Whereas EUR and GBP exhibit similar mean, median and standard deviation values, BTC presents a significant positive mean and median. Moreover, BTC standard deviation is 10 times greater than of the other currencies. All three currencies are clearly non-normal according to the Jarque-Bera test [59].

We continue our analysis computing the long-range memory of all three assets using the DFA method. Figure 2, shows important difference with respect to the stochastic behavior of all three assess. On the one hand, EUR and GBP wanders roughly within the interval \( H = (0.45, 0.55) \), which reflects an approximate random walk behavior. Except for the last period in GBP, we can say that both currencies behaves accordingly the Efficient Market Hypothesis. Taking into account that both are very liquid markets, we can expect such behavior. On the other hand, BTC returns exhibits long range correlations for most of the period under study. The convergence in memory behavior begins in 2014, where all three currencies meets around \( H = 0.5 \).
Table 1: Descriptive statistics of daily returns of BTC, EUR and GBP, from 2011 until 2017

<table>
<thead>
<tr>
<th></th>
<th>GBP</th>
<th>EUR</th>
<th>BTC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observations</td>
<td>1404</td>
<td>1404</td>
<td>1404</td>
</tr>
<tr>
<td>Mean</td>
<td>0.0205</td>
<td>0.0219</td>
<td>0.3172</td>
</tr>
<tr>
<td>Median</td>
<td>0.0000</td>
<td>0.0033</td>
<td>0.2151</td>
</tr>
<tr>
<td>Std Deviation</td>
<td>0.5701</td>
<td>0.5731</td>
<td>6.2416</td>
</tr>
<tr>
<td>Skewness</td>
<td>2.2166</td>
<td>-0.0418</td>
<td>-1.1775</td>
</tr>
<tr>
<td>Kurtosis</td>
<td>36.1865</td>
<td>4.8014</td>
<td>25.5677</td>
</tr>
<tr>
<td>Jarque Bera</td>
<td>65578.4593</td>
<td>190.2491</td>
<td>30118.6642</td>
</tr>
</tbody>
</table>

Figure 2: Hurst exponent of BTC, EUR and GBP daily values, using a sliding window of 500 datapoints and stepping forward 1 datapoint.
We test if the Hurst exponent is, specially in recent times, related to the liquidity level of the market. In order to do so, we run the Spearman’s non parametric test, to assess the association between the Hurst exponent and BTC turnover by volume. If we consider the whole period, there is no significant association between both variables. However, if we study this association over time, we observe a time-varying relationship. This situation (see Figure 3) could reflect a detachment of the underlying dynamics from one important market liquidity indicator.

4.2. Intraday returns

Taking into account that one of the advantages of Bitcoin is its open source philosophy, there is much available data, in order to analyze. Consequently we obtained transaction data from the 31th March 2013 to 2nd August 2016, and we sampled it in order to generate returns by hours, with the aim of dissecting the behavior at different time scales.

In Figure 4, we appreciate the sometimes meteoric runs-up and down of price. In less than a year, between 2013 and 2014, the price rocketed from less than 100 USD to more than 1000 USD, followed by a several falls and rebounds, without reaching an stability zone.

Another aspect we detect is that price volatility (sample variance) shows a diminishing trend. This situation is reflected in Figure 5.

Table 2 shows the descriptive statistics of Bitcoin returns, for each of the sampling intervals. We observe that, whereas the mean return increases pari passu with the interval length, the median return remains around 0.03.
Figure 4: Bitcoin price in USD, sampled every 5 hours.

Figure 5: Bitcoin returns, sampled every 5 hours.
Another feature about returns is that they exhibit huge volatility, either measured by the standard deviation or the return range (max-min). In particular, large range values are reflected in the presence of great swings in returns, which can be observed in Figure 5. Finally, we detect that data is negatively skewed and present an acute excess of kurtosis, which lead to a rejection of the null hypothesis of normality according to the Jarque-Bera statistic. Skewness and kurtosis seem to reduce with greater time spans, which could reflect a slow trend toward a more Gaussian behavior.

### Table 2: Descriptive statistics of returns, sampled at different time spans

<table>
<thead>
<tr>
<th></th>
<th>5h</th>
<th>6h</th>
<th>7h</th>
<th>8h</th>
<th>9h</th>
<th>10h</th>
<th>11h</th>
<th>12h</th>
</tr>
</thead>
<tbody>
<tr>
<td>Length</td>
<td>5746</td>
<td>4879</td>
<td>4182</td>
<td>3659</td>
<td>3252</td>
<td>2927</td>
<td>2661</td>
<td>2439</td>
</tr>
<tr>
<td>Mean</td>
<td>0.0325</td>
<td>0.0382</td>
<td>0.0445</td>
<td>0.0508</td>
<td>0.0572</td>
<td>0.0632</td>
<td>0.0695</td>
<td>0.0751</td>
</tr>
<tr>
<td>Median</td>
<td>0.0359</td>
<td>0.0252</td>
<td>0.0323</td>
<td>0.0246</td>
<td>0.0395</td>
<td>0.0302</td>
<td>0.0235</td>
<td>0.0630</td>
</tr>
<tr>
<td>Max</td>
<td>36.2219</td>
<td>40.3414</td>
<td>46.7465</td>
<td>48.5574</td>
<td>47.7417</td>
<td>47.5930</td>
<td>29.8259</td>
<td>51.3806</td>
</tr>
<tr>
<td>Std. Dev.</td>
<td>2.5994</td>
<td>2.6907</td>
<td>3.0265</td>
<td>3.2340</td>
<td>3.1859</td>
<td>3.6885</td>
<td>3.4752</td>
<td>3.9545</td>
</tr>
<tr>
<td>Skewness</td>
<td>-3.6037</td>
<td>-2.0001</td>
<td>-2.9456</td>
<td>-1.1589</td>
<td>-1.3924</td>
<td>-1.8665</td>
<td>-1.2430</td>
<td>-2.1920</td>
</tr>
<tr>
<td>Kurtosis</td>
<td>107.5232</td>
<td>70.1941</td>
<td>85.9471</td>
<td>45.6609</td>
<td>53.0422</td>
<td>61.2545</td>
<td>27.2200</td>
<td>52.9933</td>
</tr>
<tr>
<td>Jarque-Bera</td>
<td>2775514</td>
<td>1003188</td>
<td>1292625</td>
<td>329076</td>
<td>384041</td>
<td>460864</td>
<td>83211</td>
<td>287323</td>
</tr>
</tbody>
</table>

The analysis of the long range dependence is rather similar for the different time scales. The Hurst exponent profiles for the different subsamples are close regarding temporal behavior and range. In all cases, we notice a marked persistent (procyclical) behavior until 2014. After such year, the time series of Hurst exponents seem to stabilize around a value of 0.5 ± 0.05, inducing to think in a more informational efficient market. However we cannot find the reason for such change in the dynamics, giving the unconnectedness of price behavior with market fundamentals.

### 5. Conclusions

In this paper we study the long range memory and other statistical properties of Bitcoin daily and intraday prices. The period under study goes from 2011 until 2017. We compute the Hurst exponent by means of the Detrended Fluctuation Analysis method, using a sliding window in order to assess the time-varying long range dependence. We detect that:

1. In spite of the fact that Bitcoin presents large volatility, it is reducing over time.
2. We find that the long range memory is not related to market liquidity.
Figure 6: Hurst exponent using DFA method, for 5 to 12 hour BTC returns, using a sliding window of 500 datapoints and one datapoint step forward. Period: 2013-2016
3. The behavior across different time scales (5 to 12 hours) is essentially similar, in terms of long range memory.

4. Until 2014 the time series had a persistent behavior ($H > 0.5$), whereas after such date, the Hurst exponent tended to move around 0.5.

In light of our results, more research should be done in order to uncover the reason for the change in Bitcoin dynamics across time.

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