Eur. Phys. J. D (2016) 70: 243 DOI: 10.1140/epjd/e2016-70320-5

THE EUROPEAN
PHYSICAL JOURNAL D

Regular Article

High-order harmonic generation driven by chirped laser pulses induced by linear and non linear phenomena

Enrique Neyra¹, Fabian Videla^{1,2}, Jose Antonio Pérez-Hernández³, Marcelo F. Ciappina^{4,5}, Luis Roso³, and Gustavo A. Torchia^{1,a}

- Centro de Investigaciones Ópticas (CIOp) CONICET La Plata-CICBA, Camino Centenario y 506, M.B. Gonnet, CP 1897, Provincia de Buenos Aires, Argentina
- ² Departamento de Ciencias B'sicas Facultad de Ingenieraa de la Universidad Nacional de La Plata, Plata, 1900, Buenos Aires, Argentina
- ³ Centro de Láseres Pulsados (CLPU), Parque Científico, 37185 Villamayor, Salamanca, Spain
- ⁴ Max Planck Institute of Quantum Optics, Hans-Kopfermann Str. 1, 85748 Garching, Germany
- ⁵ Institute of Physics of the ASCR, ELI-Beamlines, Na Slovance 2, 182 21 Prague, Czech Republic

Received 12 May 2016 / Received in final form 24 August 2016 Published online 17 November 2016 – © EDP Sciences, Società Italiana di Fisica, Springer-Verlag 2016

Abstract. We present a theoretical study of high-order harmonic generation (HHG) driven by ultrashort optical pulses with different kind of chirps. The goal of the present work is to perform a detailed study to clarify the relevant parameters in the chirped pulses to achieve a noticeable cut-off extensions in HHG. These chirped pulses are generated using both linear and nonlinear dispersive media. The description of the physical mechanisms origin responsible for this extension is, however, not usually reported with enough detail in the literature. The study of the behaviour of the harmonic cut-off with this kind of pulses is carried out in the classical context, by the integration of the Newton-Lorentz equation complemented with the quantum approach, based on the integration of the time dependent Schrödinger equation in full dimensions (TDSE-3D).

1 Introduction

The interaction of ultra-short intense laser with atoms or molecules triggers several nonlinear phenomena, among them the high-order-harmonic-generation (HHG) process [1,2] is one of the most prominent. HHG is a wellknown phenomenon commonly used to generate coherent radiation in the range of extreme ultraviolet (XUV) to Soft-X-Ray spectral range. A simple and intuitive way to describe the underlying physical mechanism behind HHG in atoms and molecules, has been well established in the so-called three-step model [3–6] that can be briefly summarized as follows. In the first step an electronic wave packet is sent to the continuum by tunnel ionization through the potential barrier of the atom, which is a consequence of the non-perturbative interaction between the atom and the laser electric field. Then, the emitted electronic wave packet propagates in the continuum to be finally driven back when the laser electric field changes its sign, and, finally, this electronic wave packet has certain probability to recombine with the ion core, taking place the transformation of the excess of kinetic energy in high-harmonic photons (this last step is also known as recombination).

There exist two fundamental ways for the control of the high-harmonic radiation emitted by atoms and molecules. We can control either the temporal evolution of the driving electric field-envelope and carrier frequency [7,8], or to manipulate the spatial properties of the driven laser field in a broad sense, e.g. by including medium engineering and geometric effects [9,10]. In addition by using spatial inhomogeneous fields it is possible, to drive not only the HHG phenomenon [11–13], but also the ATI electrons [14,15]. Regarding the carrier frequency, it is well known that one of the most important tools in the study of the spectral characteristics of HHG is the control of the chirp in the driven laser pulse. This is so because the HHG strongly depends on this parameter [16,17]. It was already established that the control and shape optimization of the driven pulse are the main points to take into account. Another important aspect to be considered, is the resolution and efficiency of the harmonic yield [16–20]. In some of these works the method used to control the chirping was to achieve a suitable separation distance between the diffracting gratings of the compressor. This kind of chirped pulses is similar to the one obtained in a dispersive media and its magnitude is proportional to the group velocity dispersion (GVD) [21]. Theoretical studies of HHG employing chirped pulses, within the framework of the single atom model, show it is possible to extend

a e-mail: gustavot@ciop.unlp.edu.ar

considerably the HHG cutoff. An additional interesting feature appears: the harmonic spectra present a clear continuum shape being the latter an essential property for the production of isolated attosecond pulses [22–25]. There is one point to emphasize, however: the theoretically proposed chirped pulses differ from the experimental ones because the chirps are nonlinear in nature and it is not possible to achieve this kind of pulses with only linear dispersive media. It is worth mentioning that the spectral properties of all the proposed pulses change according to the chirp parameters. This means that new frequency components will appear, both in the Fourier transform of the pulse and in the HHG spectrum.

In this paper we discuss under which general conditions a typical femtosecond chirped pulse, should extend the cut off the harmonic spectrum. Our model is based on single atom simulations using the time-dependent Schrödinger equation in full dimensions (TDSE-3D). Regarding the latter point, up to now there is not a well-established explanation about what type of chirp and envelope are really able to produce an extension of the HHG spectra [22–25]. Note that by type of chirp we understand the functional dependence of the carrier frequency with respect to the time. After defining this dependence, it will be possible to examine the frequency content in the pulse analysing its influence in the HHG process. Our predictions are in agreement with the general relationship $\omega_{cut-off} \propto I\lambda^2$ between the intensity, I, and wavelength of the driven pulse, λ , and the cut off frequency, $\omega_{cut-off}$, of the harmonic spectrum. In order to effectively calculate the HHG spectra driven by chirped pulses, obtained by linear or nonlinear processes in the medium, we use them as a input in the TDSE-3D. Following the quantum simulation, the results are compared with the classical model showing an excellent agreement. The classical model appears to be instrumental in order to understand the underlying physics behind the HHG cutoff extension. Then different strategies are investigated to modify the type of chirp of the driven pulse, mainly considering the group velocity dispersion (GVD) effects and the utilization of a functional dependence of non linear character.

2 Theoretical methods

According to the three step model [3,4,6] the maximum photon energy, $E_{cut-off}$, in the harmonic spectrum is given by the classical cut-off law,

$$E_{cut-off} = I_p + 3.17U_p \tag{1}$$

(atomic units are used throughout this paper unless otherwise stated) where I_p is the ionization potential of the corresponding target atom or ion (in this work we will focus on the helium atom, $I_p = 0.9$ a.u., i.e. 24.7 eV), ω_0 is the central laser frequency and U_p is the ponderomotive energy given by:

$$U_p = \frac{E_0^2}{4\omega_0^2} \tag{2}$$

with E_0 being the peak amplitude of the laser electric field. For chirped pulses the laser pulse frequency is time-dependent, consequently, the ratio between field and frequency can be thought as a time dependent function $U^*(t)$. This assumption will be justified by the results obtained. In summary we can introduce the following function,

$$U^*(t) = \frac{E(t)^2}{4\omega(t)^2}. (3)$$

Therefore, according to equation (3), we can expect that $U^*(t)$ takes values lower, equal or higher than U_p for certain time intervals Δt . In order to verify this prediction, we can define the following function:

$$\Delta(t) = \frac{E(t)^2}{4U_p} - \omega(t)^2. \tag{4}$$

According to equation (4), if $\Delta(t)$ is negative then $U^*(t) < U_p$. On the other hand, if $\Delta(t)$ is positive then $U_p > U^*(t)$. Consequently, it could be expected, that if $\Delta(t)$ is negative, the chirp induced in the pulse will be unable to extend the cut-off. On the contrary, if $\Delta(t)$ is positive, in principle, a cut-off extension could be observed as we will see below.

In order to complement the above described classical analysis we calculate the harmonic spectra by numerical integration of the TDSE-3D in the length gauge within the dipole approximation. As it is well known the harmonic yield of an atom is proportional to the Fourier transform of the dipole acceleration of its active electron and it can be calculated from the time propagated electronic wave function. We have used our code which is based on an expansion in spherical harmonics, Y_l^m , considering only the m=0 terms due to the cylindrical symmetry of the problem. The numerical technique to solve the TDSE-3D is based on a Crank-Nicolson method implemented on a splitting of the time-evolution operator that preserves the norm of the wave function. Here we base our studies in the helium atom due to the fact that a majority of experiments in HHG are carried out in noble gases. Hence we have considered in our TDSE-3D code the atomic potential reported in reference [26] to accurately describe the level structure of the helium atom under the single active electron (SAE) approximation. In addition, and in order to explore the detailed spectral and temporal behaviour of HHG, we perform a time-frequency analysis of the HHG spectra by means of a wavelet transform [27–29].

3 Results and discussion

3.1 Linear dispersive chirp

The first study of HHG within this context was performed with a chirped pulse induced by a dispersive medium. As it is well known, when an optical pulse passes through a dispersive medium it suffers a temporal broadening [30]. According to the energy conservation, the area under the pulse must remain constant. Consequently, the peak pulse

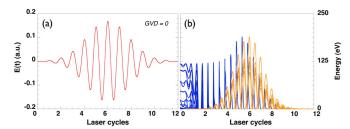


Fig. 1. Panel (a) Driving laser pulse without chirp, i.e. GVD = 0, at $1 \times 10^{15} \text{ W/cm}^2$ of laser peak intensity (i.e. $E_0 = 0.1688 \text{ a.u.}$) and $\lambda = 800 \text{ nm}$. Panel (b) represents the corresponding classical energies, resulting from the integration of the Newton-Lorentz equation, at the recombination time as a function of the ionization time (in blue) and recombination time (in orange) (for more details see e.g. [13]). The maximum photon energy, following (1), is 189 eV (note we have put the origin in energy as the I_p value).

amplitude has to decrease in order to conserve the laser pulse energy. In a dispersive medium the spectral content of the travelling pulse is not modified during the pulse propagation through the medium. The pulse is, however, temporally stretched. This effect can be explained in a first approximation by expanding the temporal phase in power series and considering the dispersive effect through the GVD term [31]. This term is defined as, $\text{GVD} = \frac{d^2k}{d\omega^2}$. Introducing the parameter $a = \frac{1}{2}\frac{d^2k}{d\omega^2}$, the evolution of the temporal broadening of a Gaussian pulse propagating a distance L through the medium can be expressed as:

$$\tau(L) = \tau_0 \sqrt{1 + \left(\frac{8aL\ln(2)}{\tau_0^2}\right)^2},$$
(5)

where τ_0 is the initial FWHM. Consequently, the degree of the chirped pulse can be expressed as a function of the product aL, whose unit is fs² [32].

For a linear dispersive medium it is feasible to use an ordinary glass type where the GVD parameter is calculated for $\lambda = 800$ nm [33]. Note that at this wavelength one laser period corresponds to ≈ 2.6 fs. The temporary broadening is then calculated for different beams propagating through the dispersive medium for several pathways lengths. We will start our analysis by determining the classical electron energy limits. Figure 1a shows a driving laser pulse without chirp, i.e. GVD = 0, at a laser peak intensity of $1\times10^{15}~\rm W/cm^2$ (i.e. $E_0=0.1688~\rm a.u.$) and $\lambda = 800$ nm. Additionally the corresponding classical analysis is shown in Figure 1b, extracted by the integration of the Newton-Lorentz equation. In this analysis was neglected the effect of the magnetic field (for more details about the classical simulations see e.g. [13]). In Figure 2 three chirped laser pulses for different values of aL are plotted, the pulses are besides to the classical electron energy simulations. Figure 2a is for $aL = 26.6 \text{ fs}^2$, Figure $\frac{2}{5}$ b for $aL = 53.3 \text{ fs}^2$ and Figure $\frac{2}{5}$ c for $aL = 88.8 \text{ fs}^2$, respectively. Furthemore, Figures 2d–2f represent the corresponding $\Delta(t)$ functions defined by equation (4). Note that in all cases the $\Delta(t)$ never takes positive values, consequently these linear chirped pulses are not able to increase the harmonic cut-off (see Fig. 1). This fact is confirmed by the classical analysis as it is shown in Figures 2g-2i.

3.2 Non linear chirp

Our second analysis was performed by assuming that the driving laser pulse is given by the following analytical form.

$$E(t) = E_0 \exp\left[-2\ln(2)\left(\frac{t}{\tau_0}\right)^2\right] \cos(\omega_0 t + bt^2) \qquad (6)$$

where E_0 is the laser electric field peak amplitude, τ_0 is the FWHM, and ω_0 is the central frequency. The parameter b in equation (6) determines the degree of chirping. In this case we assume that the pulse envelope does not change, consequently, the maximum field amplitude and the temporal width remain invariant in any of the cases. In the following analysis we will study three particular cases of chirped pulses varying the b parameter.

In Figure 3 we plot three driving laser pulses, described by equation (6), for different values of b. Figure 3a is for $b = 0.0005\omega_0$, Figure 3b for $b = 0.001\omega_0$ and Figure 3c for $b = 0.0015\omega_0$, respectively. The corresponding $\Delta(t)$ function is plotted in Figures 3d–3f, respectively. Note that in this case $\Delta(t)$ takes positive values for certain temporal regions along the pulse. Figure 4 shows one of the key points of this work. In this figure we show that if the b parameter increases, the pulse spectrum broaden. This spectral broadening allow us to obtain new frequencies, lower and higher than ω_0 . As a consequence it will be possible to manipulate the harmonic cut-off in agreement with the cut-off law reported in equation (1).

In the next cases we will use the TDSE-3D in order to compute the harmonic spectrum in a helium atom. In addition we will compare these quantum mechanical predictions with classical simulations. In Figures 5a–5c is plotted the HHG spectra computed with the TDSE-3D. The driven laser pulses are the same as those in Figure 3. The time-frequency analysis is shown in Figures 5d–5f, respectively. From these figures it is possible to account the instant when the harmonics are emitted along the laser pulse. In addition, the classical recombination energies (in solid black lines) have been superimposed. By simple inspection of this figure it is easy to conclude that the quantum simulations fully confirm the cut-off extensions predicted by the classical analysis.

All the cases present an increment of the harmonic cut-off in the single atom response, as shown in Figure 5. Both classical and quantum analysis show an excellent degree of accuracy and are in a complete agreement with the predictions reported by the behavior of $\Delta(t)$ (Fig. 3). The classical analysis confirms that the maximum of recombination energy coincides with the interval in which $\Delta(t)$ is positive. Note that, however, in the case of $b = 0.0015\omega_0$ plotted in Figure 5c, in spite of the fact that an important cut-off enhancement is achieved, the maximum recombination energy reported by the classical

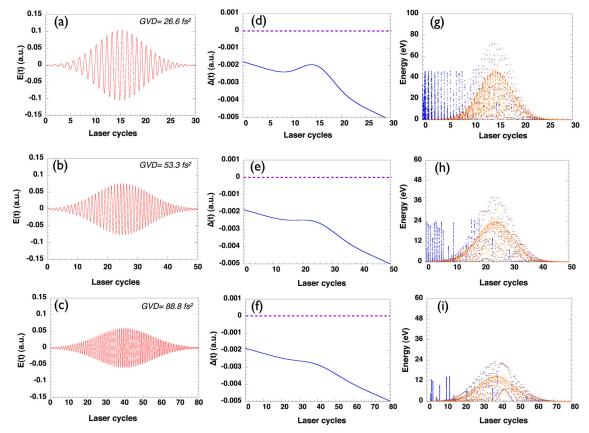


Fig. 2. Panels (a)–(c) represent the driven chirped laser pulses for the same laser parameters (intensity and wavelength) as in Figure 1 but in this case for three different values of the quantity aL. The corresponding values of the $\Delta(t)$ function are plotted in (d)–(f), respectively. Following the same criterion as in panels (g)–(i) represent their respective classical analysis.

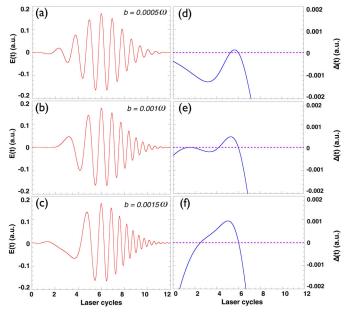


Fig. 3. Driving chirped laser pulses described by equation (6) at the intensity of 1×10^{15} W/cm² for different values of the parameter b. Panel (a) $b = 0.0005\omega_0$, panel (b) $b = 0.001\omega_0$ and panel (c) $b = 0.0015\omega_0$ respectively. Panels (d)–(f) represent the corresponding $\Delta(t)$ function for each case.

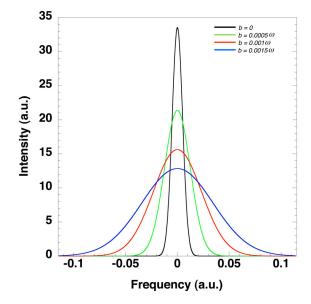


Fig. 4. Fourier Transform of the corresponding driving laser pulses plotted in Figure 3 ($b=0.0005\omega_0$ in green, $b=0.001\omega_0$ in red and $b=0.0015\omega_0$ in blue). The Fourier Transform of the driving pulse without chirp (b=0) is plotted in black. All plots have the same central frequency ω_0 , indicated as zero in the frequency axis.

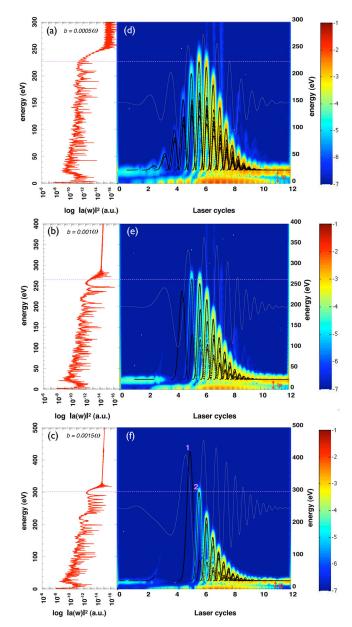


Fig. 5. Panels (a)–(c) represent the corresponding HHG spectra in the helium atom for the three different chirped laser pulses plotted in Figure 3. In (d)–(f) are plotted the respective time-frequency analysis, and superimposed (in solid black lines) the classical recombination energies. The laser field is plotted in solid gray. Note that the ionization potential (I_p) of the target atom, in this case $I_p = 24.7$ eV, has been now included.

analysis, labelled by the *point* 1 does not generate harmonics as shown in Figure 5c. This is so because the peak amplitude which correspond to the first maximum of the field is so weak, around 0.06 a.u., i.e. 1.2×10^{14} W/cm², to produce tunnel ionization in helium. To overcome this limitation we increase the peak laser intensity up to 1.4×10^{15} W/cm² for the case of $b = 0.0015\omega_0$.

We plot these results in Figure 6. On this way, the peak field of the first maximum, responsible of the maximum electron energy at recombination, becomes intense enough

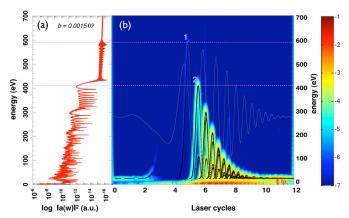


Fig. 6. Idem Figure 5c but in this case the peak laser intensity is $1.4 \times 10^{15} \text{ W/cm}^2$ ($E_0 = 0.2 \text{ a.u.}$) corresponding to the threshold of saturation of helium atom.

to produce tunnel ionization and consequently, harmonic radiation. This fact is depicted in Figure 6 where an important cut-off extension appears in agreement with the classical predictions. Note that the new different plateaus generated can be understood considering that the harmonic efficiency depend on $\lambda^{-5.5}$ [35,36]. In other words, the generation of each new plateau can be interpreted as a result of ionization events with different wavelengths and for this reason the efficiency of the plateau in the region between 400–600 eV is so poor.

4 Conclusions and outlook

We have studied the behavior of the harmonic cut-off in the HHG process driven by two different kind of chirped laser pulses. In the first case we employ a chirped pulse whose spectral content has remained unaltered when it passes through a dispersive media [34]. In the second case, we have considered a chirped pulse whose frequency varies linearly in time and its envelope remains constant. In such a pulse, and by analysing the harmonic spectrum, it was demonstrated that, as the control chirp parameter b increases, the laser spectrum broaden.

The effect of chirped pulses on the harmonic cut-off energy obtained with a dispersive linear media has been evaluated by a classical analysis. As can be observed in Figure 2 when the chirping of the laser pulse increases, for different values of the GVD, its temporal width grows and the maximum cutoff photon energy diminishes. Considering that the pulse is temporally stretched, the maximum electric field peak amplitude decreases. Consequently the associated drop in the laser intensity causes a reduction of the cutoff energy. On the other hand, the $\Delta(t)$ function previously defined in equation (4) provides a practical tool to predict, a priori, the behavior of the harmonic cut-off in the case of chirped pulses.

The next study of the cut-off has been performed using the chirped pulses described by equation (6) and plotted in Figure 3. As can be observed, these pulses have a chirp whose frequency depends linearly on time but its temporal duration remain constant in spite of variations of b, the parameter that controls the chirp. Analysing the behavior of $\Delta(t)$ it is possible to correlate the increasing in the harmonic cut-off with regions in which $\Delta(t) > 0$. This conclusion is in perfect agreement with the classics analysis based on the Newton-Lorentz equation.

In summary, according to the results reported here, chirping laser pulses will be able to produce cut-off enhancements only in the case that the chirp is obtained via a non linear process where new frequencies are generated and a broadening of the laser spectrum is achieved [34]. In particular, lower frequencies, i.e. longer wavelengths, than the central frequency are the ones which produce the most important cutoff extensions. This behavior can be understood based on the simple law $E_{cut-off} \propto I\lambda^2$. These new frequencies are generated by weak laser peak amplitudes, at the turn-on region of the driving pulse. Consequently, as an additional condition needed in order to produce noticeable effects in the HHG spectra, the input pulse has to be intense enough to produce tunnel ionization, and consequently harmonic radiation, at the turn-on temporal region.

This work was partially supported by Agencia de Promoción Científica y Tecnológica (Argentina) under project PICT-2010-2575. J.A.P.-H. and L.R. acknowledge support from Laserlab Europe (Grant No. EU FP7 284464) and the Spanish Ministerio de Economía y Competitividad (FURIAM Project No. 78 FIS2013-47741-R and PALMA project FIS2016-81056-R) and Junta de Castilla y León project CLP087U16. M.F.C. acknowledges support the project ELI-Extreme Light Infrastructure-phase 2 (CZ.02.1.01/0.0/0.0/15 008/0000162) from European Regional Development Fund.

References

- 1. A. L'Huillier, P. Balcou, Phys. Rev. Lett. ${\bf 70},\,774$ (1993)
- 2. J.J. Macklin, C.L. Gordon, Phys. Rev. Lett. **70**, 766 (1993)
- 3. P.B. Corkum, Phys. Rev. Lett. 71, 1993 (1994)
- J.L. Krause, K.J. Schafer, K.C. Kulander, Phys. Rev. Lett. 68, 3535 (1992)
- K.J. Schafer, B. Yang, L.F. DiMauro, K.C. Kulander, Phys. Rev. Lett. 70, 1599 (1993)
- M. Lewenstein, P. Balcou, M.Y. Ivanov, A. L'Huillier, P.B. Corkum, Phys. Rev. A 49, 2117 (1994)
- S. Haessler, T. Balčiunas, G. Fan, G. Andriukaitis, A. Pugžlys, A. Baltuška, T. Witting, R. Squibb, A. Zaïr, J.W.G. Tisch, J.P. Marangos, J.S. Chipperfield, Phys. Rev. X 4, 021028 (2014)
- F. Calegari, M. Lucchini, K.S. Kim, F. Ferrari, C. Vozzi,
 S. Stagira, G. Sansone, M. Nisoli, Phys. Rev. A 84, 041802(R) (2011)
- C. Winterfeldt, C. Spielmann, G. Gerber, Rev. Mod. Phys. 80, 117 (2008)

- T. Pfeifer, R. Kemmer, R. Spitzenpfeil, D. Walter, C. Winterfeldt, G. Gerber, C. Spielmann, Opt. Lett. 30, 1497 (2005)
- M.F. Ciappina, S.S. Aćimović, T. Shaaran, J. Biegert, R. Quidant, M. Lewenstein, Opt. Exp. 20, 26261 (2012)
- J.A. Pérez-Hernández, M.F. Ciappina, M. Lewenstein, L. Roso, A. Zaïr, Phys. Rev. Lett. 110, 053001 (2013)
- M.F. Ciappina, J.A. Pérez-Hernández, M. Lewenstein, Comput. Phys. Commun. 185, 398 (2014)
- M.F. Ciappina, J.A. Pérez-Hernández, T. Shaaran, L. Roso, M. Lewenstein, Phys. Rev. A 87, 063833 (2013)
- M.F. Ciappina, T. Shaaran, R. Guichard, J.A. Pérez-Hernández, L. Roso, M. Arnold, T. Siegel, A. Zaïr, M. Lewenstein, Laser Phys. Lett. 10, 105302 (2013)
- H.T. Kim, I.J. Kim, V. Tosa, C.M. Kim, J.J. Park, Y.S. Lee, A. Bartnik, H. Fiedorowicz, C.H. Nam, Appl. IEEE J. Sel. Top. Quantum Electron. 10, 1329 (2004)
- H.T. Kim, I.J. Kim, D.G. Lee, K.H. Hong, Y.S. Lee, V. Tosa, C.H. Nam, Phys. Rev. A 69, 031805 (2004)
- D.G. Lee, J.H. Kim, K.H. Hong, C.H. Nam, Phys. Rev. Lett. 87, 243902 (2001)
- H.T. Kim, I.J. Kim, K.H. Hong, D.G. Lee, J.H. Kim, C.H. Nam, J. Phys. B 37, 1141 (2004)
- H.T. Kim, D.G. Lee, K.H. Hong, J.H. Kim, I.W. Choi, C.H. Nam, Phys. Rev. A 67, 051801 (2003)
- J.C. Diels, W. Rudolph, Laser Pulse Phenomena: Fundamentals, Techniques, and Applications on a Femtosecond Time Scale, 2nd edn. (Elsevier, New York, 2006), p. 82
- 22. J.J. Carrera, S.I. Chu, Phys. Rev. A 75, 033807 (2007)
- J. Wu, G.T. Zhang, C.L. Xia, X.S. Liu, Phys. Rev. A 82, 013411 (2010)
- 24. H. Du, B. Hu, Phys. Rev. A 84, 023817 (2011)
- Y. Niu, Y. Xiang, Y. Qi, S. Gong, Phys. Rev. A 80, 063818 (2009)
- 26. X.M. Tong, C.D. Lin, J. Phys. B 38, 2593 (2005)
- C.K. Chui, An Introduction to Wavelets (Academic Press, New York, 1992)
- A. Antoine, B. Piraux, A. Maquet, Phys. Rev. A 51, 1750(R) (1995)
- 29. X.M. Tong, S.I. Chu, Phys. Rev. A 61, 021802(R) (2000)
- 30. J.C. Diels, W. Rudolph, Laser Pulse Phenomena: Fundamentals, Techniques, and Applications on a Femtosecond Time Scale, 2nd edn. (Elsevier, New York, 2006), p. 19
- J.C. Diels, W. Rudolph, Laser Pulse Phenomena: Fundamentals, Techniques, and Applications on a Femtosecond Time Scale, 2nd edn. (Elsevier, New York, 2006), p. 16
- 32. M. Rosete-Aguilar, Rev. Mex. Fis. 54, 141 (2008)
- J.C. Diels, W. Rudolph, Laser Pulse Phenomena: Fundamentals, Techniques, and Applications on a Femtosecond Time Scale, 2nd edn. (Elsevier, New York, 2006), p. 44
- J.C. Diels, W. Rudolph, Laser Pulse Phenomena: Fundamentals, Techniques, and Applications on a Femtosecond Time Scale, 2nd edn. (Elsevier, New York, 2006), p. 29
- J. Tate, T. Auguste, H.G. Muller, P. Salières, P. Agostini,
 L.F. DiMauro, Phys. Rev. Lett. 98, 013901 (2007)
- J.A. Pérez-Hernández, L. Roso, L. Plaja, Opt. Exp. 17, 9891 (2009)