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# Topological description of the bond-breaking and bond-forming processes of the alkene protonation reaction in zeolite chemistry: an AIM study

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Abstract Density functional theory and atoms in molecules theory were used to study bond breakage and bond formation in the trans-2-butene protonation reaction in an acidic zeolitic cluster. The progress of this reaction along the intrinsic reaction coordinate, in terms of several topological properties of relevant bond critical points and atomic properties of the key atoms involved in these concerted mechanisms, were analyzed in depth. At B3LYP/6-31++G(d,p)//B3LYP/6-31G(d,p) level, the results explained the electron density redistributions associated with the progressive bond breakage and bond formation of the reaction under study, as well as the profiles of the electronic flow between the different atomic basins involved in these electron reorganization processes. In addition, we found a useful set of topological indicators that are useful to show what is happening in each bond/atom involved in the reaction site as the reaction progresses.

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# Introduction

Zeolites are microporous aluminosilicate minerals that are used widely in the chemical industry. Due to their high selectivity, their reactivity and the presence of Brønsted acid sites, acidic zeolites act as solid acid/base catalysts in a variety of reactions [1-4]. Principally, the alkene protonation reactions by acid zeolites feature prominently in many zeolite-catalyzed hydrocarbon transformations of great industrial importance [1, 5] such as dimerization and oligomerization of olefins, and double bond isomerizations.

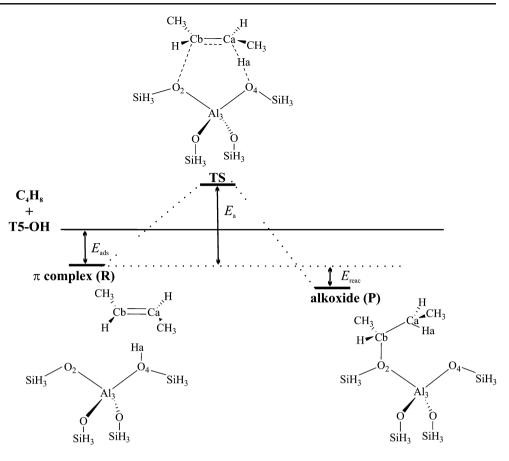
Prior to the protonation reaction, the interaction of the alkene molecule with the zeolite Brønsted acid site results in the formation of an adsorbed alkene or  $\pi$  complex (Eq. 1). The adsorbed alkene then acts as a reactant in the protonation reaction (Eq. 2), as shown in Scheme 1.

$$T5-OH + C_4H_8 \rightarrow [T5-OH \cdots C_4H_8]_{ads}$$
(1)

$$\begin{split} \left[ T5-OH\cdots C_4H_8 \right]_{ads} &\rightarrow \left[ T5-O^-C_4H_9^+ \right]^{\neq} \\ &\rightarrow T5-O-C_4H_9 \end{split} \tag{2}$$

Since the pioneering work of Kazansky [15], the mechanism of the initial protonation of light alkenes over the Brønsted acid sites of zeolites has been studied extensively using diverse experimental methods [6-8] and theoretical calculations [9-14]. Within the broad scope of these theoretical investigations, particular interest has

Scheme 1 Structures of adsorbed alkene on a Brønsted acid site (R), transition state (TS) for olefin protonation reaction, and alkoxide product (P)



focused on extracting information about the stationary points of the potential energy surface. Carbocations and alkoxides are accepted as reaction intermediates in acidcatalyzed hydrocarbon reactions; however, the mode of formation as well as the true nature of these intermediaries is still a matter of controversy [16]. The protonation of an olefin by an acid hydroxyl group results in the formation of a more stable alkoxide product (P), in which the process is concerted and occurs through a transition state (TS), wherein the organic fragment resembles that of a classical carbenium ion. In the course of the reaction, the hydrogen atom of the Brønsted acid site, Ha, protonates a carbon atom of the olefin double bond, Ca. Simultaneously, the positive charge that appears on C<sub>b</sub> interacts with one of the neighboring basic oxygen atoms of the zeolite, O<sub>2</sub>, giving rise to the formation of a C<sub>b</sub>-O<sub>2</sub> bond, and, consequently, the formation of the alkoxide product.

In order to provide a better understanding of the details of the electron redistribution upon chemical transformations, we investigated in a previous work [17] the electron density properties of the stationary points of the ethene protonation reaction by an acidic zeolite, in the framework of the quantum theory of atoms in molecules (QTAIM) [18, 19]. This approach allows clear insight into the nature and properties of the chemical bonds between the interacting species. Although this methodology has been applied successfully to a variety of chemical systems [20], only a very few theoretical studies have reported any topological analysis of the electron density,  $\rho(\mathbf{r})$ , in zeolite chemistry [17, 21–27]. As we found previously [17], the most important topological feature in this process is the electron charge density redistribution. The alkoxide product is formed as a consequence of the electrophilic strength developed by the positively charged C<sub>b</sub> atom; this atom withdraws electrons from the atomic basin of the (basic) O<sub>2</sub> atom, which acts as a Lewis basic site. As the reactions proceed, an electronic redistribution in both the alkene fragment and the zeolite cluster is produced.

In an attempt to extend our knowledge of the course of these chemical reactions, we considered it interesting to study electron density redistribution, not only on the stationary points, but also associated with the topological changes along the intrinsic reaction coordinate (IRC). Analysis of the electron density along the IRC path has been used by several co-workers and has proved useful in analyzing reactions similar to those described here. The keto–enol tautomerism of an acetaldehyde, the pinacol rearrangement of a protonated 1,2-ethanediol, and the unimolecular decomposition of the methanediol, were studied as examples of hydrogen transfer [28]. Additionally, two possible reaction pathways were studied in the Lewis acid mediated reaction of acetonitrile and benzonitrile oxide [29]. Furthermore, the atoms in molecules (AIM) theory was applied to non-stationary states along the IRC in a topological analysis of  $S_N2$  reactions of methyl halides [30]. Also, the properties of bond critical points (BCP) along the IRC were used to establish a quantitative structure–property relationship in calculated reaction pathways [31]. Thus, QTAIM analysis can be used in the discussion of the electron redistribution experienced in such reactions.

In a similar sense, in this work we carried out an analysis of the trans-2-butene reaction protonation by an acidic zeolitic cluster within the framework of the AIM theory by evaluating changes in bond and atomic properties along the IRC. Although several theoretical studies have been performed on these reactions, to our knowledge none have included an electron density topological analysis or computation of atomic properties to describe the evolution of changes along the IRC. Therefore, we analyzed bond breakage and bond formation during this process in order to give topological indicators that show what is happening in each bond/atom involved in the reaction site. To this end, we used topological characterization at BCP in several bonds along the reaction path, as well as a description of the evolution of some of the atomic properties during this concerted process in order to understand the electronic transference between the alkenes and the catalyst as well as the stabilization/destabilization undergone by atoms involved in the reaction site. Furthermore, we demonstrate that analysis of electron density distribution profiles along the IRC is a powerful tool that allows us to visualize the flow of electrons between the different atomic basins involved in the reaction.

#### Methods and calculation details

We selected trans-2-butene as a candidate for the description of the chemical reaction of the alkenes protonation reaction catalyzed by acidic zeolites along the IRC. This alkene molecule is useful when considering the secondary nature of olefinic carbons. The zeolite catalyst was modeled by a widely used cluster,  $H_3Si-OH-Al(-O-SiH_3)_3$ , denoted T5–OH, because this model provides a good description of the bifunctional nature of zeolite active sites and includes, as far as possible, both short- and medium-range electrostatic effects [11, 17].

The geometries of all species were optimized without any constraints. Hybrid density functional theory (DFT) calculations at the Becke3 Lee–Yang–Parr (B3LYP) level [32, 33] with the 6-31G\*\* basis set were carried out using the Gaussian 03 suite of programs [34]. All stationary points were characterized by calculating the Hessian matrix and analyzing vibrational normal modes. Starting at the TS, we calculated the reaction pathways in forward and reverse directions in order to investigate the minima connected by the TS. The reaction path was followed employing the IRC algorithm [35, 36], as implemented in Gaussian 03. A step size of 0.01 amu<sup>1/2</sup>Bohr was used.

A topological analysis of the electron charge density distribution,  $\rho(\mathbf{r})$ , in the framework of AIM theory [18–20] was carried out for the present study. Total electron densities were obtained at B3LYP level with the 6-31++G\*\* basis set. The bond and atomic properties were calculated using the Aim2000 package [37]. Certain structures on the reaction pathway were selected for the electron density analysis. The reaction process was investigated using the AIM partition scheme of electron charge density. In this work, we calculated variations in typical electron density properties calculated at the BCP in order to characterize bond breakage and bond formation. Moreover, we calculated the variations in the integrated atomic properties over the atomic basin along the corresponding IRC path.

# Overview of AIM theory

Here, we present only the essential theoretical information needed for discussion of the results, because the use of topological concepts is well documented in the standard literature [18–20]. The electron charge density,  $\rho(\mathbf{r})$ , is a physical quantity that has a definite value at each point in space. According to AIM theory, an atom in a molecule is defined as the union of an attractor and its associated basin, called an atomic basin. It is bounded by a zero-flux surface in the gradient vector field of the charge density,  $\nabla \rho(\mathbf{r})$ , which defines an atomic boundary. When two atoms share some portion of their surfaces, a line of maximum electronic charge density is formed between the nuclei, and, at the point where the shared surface intersects this atomic interaction line or bond path, there is a saddle point in  $\rho(\mathbf{r})$  called a bond critical point (BCP). In this manner, the AIM theory identifies a unique line of communication between two chemically interacting nuclei, and provides a unique point where it is possible to probe or characterize this interaction.

In AIM theory, an interaction is characterized by: (1) the charge density at the critical point,  $\rho_b$ , as a measure of how much charge is accumulated between the bonded nuclei and reflects the strength of a bond; (2) the Laplacian  $\nabla^2 \rho_b$  as a measure of local charge concentration ( $\nabla^2 \rho_b <0$ ) or local charge depletion ( $\nabla^2 \rho_b >0$ ); (3) the ellipticity,  $\varepsilon$ , as a measure of the  $\pi$  character of a bond but also of its structural stability. Finally, from a topological point of view, the covalent character of an interaction is analyzed quantitatively by taking into account the  $|V_b|/G_b$  relationship, where  $V_b$  and  $G_b$  are the potential and the kinetic energy densities evaluated at the BCP.

# **Results and discussion**

The electron density properties of the stationary points of the ethene protonation reaction catalyzed by acidic zeolite have been investigated recently [17]. Analysis of the global process shows that the bonds that change their properties more significantly are  $H_a-O_4$ ,  $C_a\cdots H_a$ ,  $C_a-C_b$  and  $C_b\cdots O_2$ . Consequently, in the present work, the electron density properties of the aforementioned bonds, for the trans-2butene protonation reaction on the surface extrema (reactant and product), and their variation along the IRC, will be described separately in the following paragraphs.

Bond distances and local topological properties [electron densities ( $\rho_b$ ), the Laplacian ( $\nabla^2 \rho_b$ ), the relationship between the local potential energy density and the local kinetic energy density ( $|V_b|/G_b$ ), and the ellipticity ( $\varepsilon$ )] of the surface extrema are listed in Table 1. The results in Table 1 are in accordance with previously published data on the ethene protonation reaction and therefore will not be discussed in detail.

Table 1 shows that the topological properties at the BCP on the  $C_a-C_b$  and  $O_4-H_a$  bonds in the  $\pi$  complex, **R**, are clearly indicative of shared interactions. Also, the  $C_a\cdots H_a$ interaction shows characteristics of a closed shell interaction. In the alkoxide, **P**, the absence of a BCP between the  $O_4$  and  $H_a$  atoms indicates that the  $O_4-H_a$  bond was broken, whereas a new bond was formed between the  $O_2$  and  $C_b$  atoms (the  $C_b\cdots O_2$  interaction is absent in R). The topological properties at the BCP of the  $C_b\cdots O_2$  bond (formed in **P**) show that this bond can be defined as a weak shared interaction.

The electronic changes along the reaction coordinate reflect the thermochemistry of the trans-2-butene protonation reaction. Our calculation predicts an activation energy of 26.02 kcal mol<sup>-1</sup> (see Scheme 1). The formation of **P** was observed to be exothermic, and the calculated reaction energy (**P** energy relative to the physisorbed  $\pi$  complex energy) was -6.61kcal mol<sup>-1</sup>. These results are in accordance with results obtained by other authors [12]. More-

**Table 1** Bond distances (Å) and local topological properties (au) of the electron charge density distribution calculated at the position of the bond critical points (BCP) of selected bond paths for reactant (R) and

over, the global energy variation and the geometrical distance of the selected bonds along the IRC for trans-2butene protonation reaction by acidic zeolite are shown in Figs. S1 and S2 in the Electronic Supplementary Material.

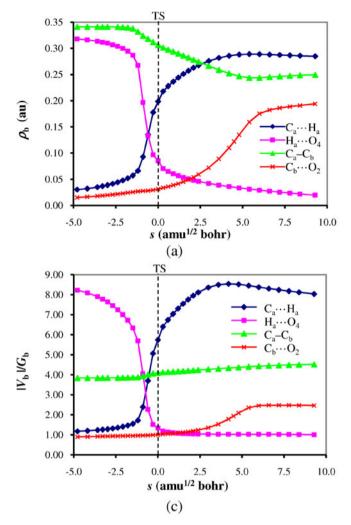
Evolution of the local properties of  $\rho_{(r)}$ during the protonation reaction

Local topological properties of electron density calculated at the BCP along the IRC provide interesting information on bond breakage and bond formation for the reaction under study and allowed us to characterize the interactions between the atoms involved in the reaction site. Figure 1 shows the variation in local topological properties at the BCPs along the IRC corresponding to the interactions involved at the reaction site for the trans-2-butene protonation reaction catalyzed by acidic zeolite. The extreme values for the  $\pi$  complex and the alkoxide product were introduced in Table 1.

As can be seen in Fig. 1a–c, the changes seen in  $\rho_b$ ,  $\nabla^2 \rho_b$ and  $|V_b|/G_b$  at the selected BCP along the IRC are very pronounced. The electron charge density at C<sub>a</sub>...H<sub>a</sub> and  $C_{h}$ ... $O_{2}$  BCPs increases as a result of the formation of these bonds, with a subsequent increase in their strengths. Both the  $C_a \cdots H_a$  and  $C_b \cdots O_2$  bonds are stabilized by the increased accumulation of charge density between them. This viewpoint will be discussed in detail below. In addition, Fig. 1a-c shows that the greatest rate of change in local topological properties at BCPs, corresponding to the  $H_a \cdots O_4$  and  $C_a \cdots H_a$  bonds, is located in the region between -1.5 and +1.2 amu<sup>1/2</sup>Bohr of the reaction coordinate. In this region, the H<sub>a</sub>…O<sub>4</sub> distances lie between 1.03 and 1.66 Å, and the Ca<sup>...</sup>Ha distances lie in the 1.68-1.14 Å range. In addition, it is interesting to highlight that the proton is linked by bond paths to the O<sub>4</sub> atom and simultaneously to the C<sub>a</sub> atom. This implies that the H<sub>a</sub> proton is shared between the two atoms, and that it becomes dicoordinated, i.e., Ca...Ha...O4.

product (P).  $\rho_b$  Electron densities,  $\nabla^2 \rho_b$  the Laplacian,  $|V_b|/G_b$  the relationship between the local potential energy density and the local kinetic energy density,  $\varepsilon$  ellipticity

Bond X-Y	Species	d <sub>X-Y</sub>	$ ho_{ m b}$	$\nabla^2 \rho_{\rm b}$	ε	$ V_{\rm b} /G_{\rm b}$
H <sub>a</sub> –O <sub>4</sub>	R	0.988	0.3286	-1.8822	0.0126	8.6917
	Р	4.884	-	-	-	_
$C_a \cdots H_a$	R	2.161	0.0233	0.0465	0.8420	0.9761
	Р	1.097	0.2772	-0.9417	0.0095	7.1135
C <sub>a</sub> –C <sub>b</sub>	R	1.344	0.3409	-0.9727	0.3686	3.8300
	Р	1.527	0.2531	-0.6016	0.0314	4.6294
$C_b \cdots O_2$	R	3.946	-	-	-	_
	Р	1.493	0.2058	-0.2839	0.0294	2.4001



TS 0.40 0.20 0.00 -0.20 -0.40  $\nabla^2 \rho_{\rm b}$  (au) -0.60 -0.80 -1.00 -1.20 Ha.O4 -1.40  $C_a - C_b$ -1.60 C .... O. -1.80 -5.0 -2.5 0.0 2.5 5.0 7.5 10.0 s (amu<sup>1/2</sup> bohr) (b) TS 0.90 0.80 ···· H\_ 0.70 H .... O4 0.60 0.50 ŝ 0.40 0.30 0.20 0.10 0.00 10.0 -2 5 0.0 25 5.0 7.5 -5.0 s (amu<sup>1/2</sup> bohr) (d)

Fig. 1 Variations in local topological properties at selected bond critical points (BCP) along the intrinsic reaction coordinate (IRC) for the trans-2-butene protonation reaction catalyzed by acidic zeolite. **a** Electron density, **b** Laplacian, **c** relationship between local potential

 $H_a \cdots O_4 BCP$ 

Figure 1a shows a strong decrease in electron density at  $H_a \cdots O_4$  BCP, which indicates that the  $H_a \cdots O_4$  bond weakens to its final breakage (the lower the  $\rho_b$  value at the BCP, the lower the strength of the bond). In Fig. 1b, it can be observed that the  $\nabla^2 \rho_b$  value increases sharply and changes sign near the TS, corresponding to a bond distance of 1.43 Å. This is indicative of the change in nature of this bond. The  $H_a \cdots O_4$  bond loses the characteristics of a shared interaction ( $\nabla^2 \rho_b < 0$ ) to become a closed shell interaction ( $\nabla^2 \rho_b > 0$ ) with some contribution of covalent character in the TS, whereas in the product this interaction is not present, namely, a  $H_a$ -O<sub>4</sub> BCP is not found in the alkoxide product, reflecting the rupture of the bond between the  $H_a$  and  $O_4$  atoms. The  $|V_b|/G_b$  relationship along the IRC shows a strong decrease approaching the

energy density and local kinetic energy density, **d** ellipticity. The transition state (TS) is located at the value s = 0.0 of the reaction coordinate

TS, becoming less as it reaches a  $|V_b|/G_b$  value near to 1 au. This is indicative of a reduction of the covalent character in the first place, with subsequent weakening of the interaction, finally leading to bond breaking process as a consequence. The ellipticity, on the other hand, shows no significant change.

# $C_a \cdots H_a BCP$

Meanwhile, the opposite behavior is observed for the  $C_a \cdots H_a$  bond that is being formed at the same time. The electron density at the  $C_a \cdots H_a$  BCP increases strongly along the IRC to reach an approximately constant value characteristic of a covalent bond (0.27 au). Regarding the Laplacian, Fig. 1b shows a sign change in the  $\nabla^2 \rho_b$  values at the reaction coordinate, *s*, equal to  $-0.9 \text{ amu}^{1/2}$ Bohr, equivalent to a  $C_a \cdots H_a$  distance of 1.51 Å, and, as a

consequence, a Ca-Ha bond is formed. Moreover, the variation in the  $\nabla^2 \rho_{\rm b}$  value confirms these trends with an increasing negative value, reflecting a local concentration of electronic charge in the internuclear Ca...Ha region. As can be observed in Fig. 1c, the  $|V_b|/G_b$  relationship at  $C_a \cdots H_a$  BCP is > 1 and increases when going from the  $\pi$ complex to the TS. In the first part of the IRC, the  $|V_{\rm b}|/G_{\rm b}$ relationship is approximately constant and has a value of less than 2. Consequently, the Ca-Ha interaction shows topological characteristics of closed shell interactions. Then, in the vicinity of the TS, an abrupt increase in  $|V_b|/G_b$ values is observed. At the TS, the Ca-Ha interaction shows topological characteristics of a shared interaction  $(|V_{\rm b}|/G_{\rm b} > 2)$ , and increases the covalent character along the IRC up to a maximum value of about 8.54 au (at s = +4.2amu<sup>1/2</sup>Bohr). The  $|V_{\rm b}|/G_{\rm b}$  relationship then decreases slightly and finally shows a value of 7.11 au in the alkoxide product. These variations in the  $|V_{\rm b}|/G_{\rm b}$  relationship along the reaction coordinate allow us to explain the progressive formation of the Ca<sup>...</sup>Ha bond and the subsequent rearrangement or redistribution of electron density in order to stabilize the C<sub>a</sub>-H<sub>a</sub> bond formed.

# $C_a - C_b BCP$

Analysis of the variation in the local topological properties at the BCP on a  $C_a-C_b$  bond shows that  $\rho_b$  values remain practically constant up to s = -1.8 amu<sup>1/2</sup>Bohr, and then gradually decrease (up to s = +5.4 amu<sup>1/2</sup>Bohr) together with a gradual increase in  $\nabla^2 \rho_b$ . Both properties change gradually during this part of the reaction (Fig. 1a,b). Finally, a very slight increase in  $\rho_b$  values is observed from s = +5.4 amu<sup>1/2</sup>Bohr onwards. The  $|V_b|/G_b$  relationship increases slightly and shows no significant change (Fig. 1c). The most significant topological change observed is a strong decrease in ellipticity values as the reaction progresses, reaching very low values at the end of the reaction (Fig. 1d). This decrease reflects the hybridization change process along the IRC of both carbon atoms involved in the C<sub>a</sub>-C<sub>b</sub> bond. Thus, this bond undergoes a transition from a double to a single bond due to the rupture of the olefin  $\pi$  bond and the lengthening of the C<sub>a</sub>-C<sub>b</sub> bond. However, the Ca-Cb bond retains its covalent character throughout the course of the reaction. As noted by other authors [38], the ellipticity is sensitive to changes in the anisotropy of the electron density in the bond-forming region. This parameter provides an insightful description of the events occurring along the reaction coordinate, and serves as a sensitive index to monitor the  $\pi$  character of double bonds. In a C–C bond, when  $\varepsilon$  is large, the bond has a significant  $\pi$  character, and when  $\varepsilon$  is close to zero, the electron density exhibits the cylindrical character typical of either a single or a triple bond.

### $C_b \cdots O_2 BCP$

The  $C_b \cdots O_2$  interaction is absent in the reactant. When the  $C_b$  atom of the alkene molecule interacts with one of the neighboring basic oxygen atoms of the zeolite ( $O_2$ ), a new BCP appears. This BCP corresponds to the  $C_b \cdots O_2$  bond that is being formed and, consequently, the alkoxide appears. As the reaction proceeds, the  $\rho_b$  at the BCP of the  $C_b \cdots O_2$  interaction becomes larger, which indicates that the  $C_b \cdots O_2$  interaction is becoming stronger. In the first part of the reaction path, a continuous and slight increase in  $\rho_b$  values is observed; then, as soon as the  $\rho_b$  value exceeds 0.04 au, this increase becomes gradually more pronounced, until it slowly reaches a constant value close to 0.2 au (see Fig. 1a).

Considering that the Laplacian magnifies small changes in the electron density of the bond, it should be interesting to investigate the variation in Laplacian at the  $C_{b}$ ... $O_{2}$  BCP along the IRC (Fig. 1b). In the first part of the reaction path, small fluctuations in  $\nabla^2 \rho_b$  values can be observed; however, it should be considered that  $\nabla^2 \rho_b$  remains practically constant during this part of the reaction (maximum variations do not reach 0.05 au). The  $\nabla^2 \rho_b > 0$  indicates a weak electrostatic interaction between the basic oxygen atom and the electron-deficient carbon (a closed shell interaction). In the second part of the reaction path, a continuous decrease in  $\nabla^2 \rho_b$  values is observed, and, at approximately s = +4.8 amu<sup>1/2</sup>Bohr (equivalent to a  $C_b \cdots O_2$  bond distance of 1.678 Å), the  $\nabla^2 \rho_b$  value changes its sign. This result is indicative of the change in the character of the interaction, from closed shell to shared interaction, due to the formation of the Cb-O2 bond. Finally,  $\nabla^2 \rho_b$  values decrease slowly and reach a value close to the equilibrium value of about -0.2 au (from  $s = +6.0 \text{ amu}^{1/2} \text{bohr}$ ).

In addition, an in depth analysis of the  $|V_{\rm b}|/G_{\rm b}$ relationship at Cb...O2 BCP along the IRC was performed. Figure 1c shows that the  $|V_b|/G_b$  values at the  $C_b \cdots O_2$  BCP are positive and increase from reactant to product. However,  $|V_b|/G_b$  is < 1 before the TS is reached; this implies that a pure closed shell interaction takes place in this part of the reaction path. Thereafter, up to s = +4.8amu<sup>1/2</sup>Bohr of the reaction path, the  $|V_b|/G_b$  relationship is within the range of 1-2 au; thus, in this part of the reaction path this bond involves an intermediate character between shared interaction and closed shell interaction (the slight gain of potential vs kinetic energy density at the BCP and  $\nabla^2 \rho > 0$  is indicative of a small degree of covalence in this new bond [39]). Subsequently, the  $|V_{\rm b}|/G_{\rm b}$  relationship increases in value, reaching a maximum of ~2.4 au in the alkoxide product;  $|V_b|/G_b$  values > 2 indicate "weak covalent bond" features for the carbon-oxygen bond as was previously established by our group [17].

Regarding the ellipticity changes, at the beginning of the reaction, it is noticeable that the ellipticity at C–O BCP is of a moderate value (0.85) and then decreases quickly, reaching a value of 0.05, then remains approximately constant until the end of the process (Fig. 1d). These results indicate that, in accordance with what was expressed before, the  $\sigma$ -character of the forming C–O bond is established at a late stage of the reaction (after s = +4.8 amu<sup>1/2</sup>Bohr of the reaction path, when C<sub>b</sub> is located at 1.678 Å from the O<sub>2</sub>).

In the AIM theory, all information about a particular AIM atom is contained in its finite volume, and its properties can be obtained by integrating each corresponding density property over the atomic basin [18, 19]. The ability to determine individual atomic contributions to changes in charge and energy at a given fragment should be of particular use to obtain a better understanding of the subjacent modification produced along the reaction coordinate. Thus, the next section deals with the atomic properties of atoms involved in the reaction site, with the aim of giving a detailed description of the chemical reaction in terms of the electron density rearrangement process along the IRC.

# Evolution of atomic properties during the protonation reaction

A previous study by our group showed that the atoms whose properties are significantly affected by the protonation reaction are the proton that is transferred, both carbon atoms involved in the double bond, and the oxygen atoms at the Brønsted and Lewis site [17]. Consequently, the atomic properties of these atoms at the surface extrema, and their variation along the IRC, will be described separately in the following paragraphs. Table 2 lists the topological atomic properties [atomic net charge,  $q_{(\Omega)}$ , and atomic energy,  $E_{(\Omega)}$ ] of selected atoms involved in the reaction site of the reactant (R) and the alkoxide product (P). The accuracy of the integration was assessed by the magnitude of a function L $(\Omega)$ , which, in all cases, is less than  $10^{-5}$  au for H atom and  $10^{-4}$  au for other atoms.

The proton from the acidic hydroxyl group,  $H_a$ , increases its electronic population from R to P and, consequently, results stabilized. The oxygen atoms in the acidic and the basic site,  $O_4$  and  $O_2$ , respectively, increase/decrease their atomic charge and both become destabilized from reactant to product. On the other hand, both carbon atoms increase their atomic charge and are destabilized from reactant to product. Analysis of the atomic properties of the reactant and product (as well as the TS) provides valuable information about the reaction; however, the electron density redistribution that accompanies bond breaking and bond formation is dominated by the electron exchange between the different basins in the reaction site. As a

**Table 2** Topological atomic properties (in au) of selected atoms in  $\pi$  complex (R) and alkoxide product (P)<sup>a</sup>.  $q_{(\Omega)}$  Net atomic charge,  $E_{(\Omega)}$  total atomic energy

Atom	Species	$q_{(arOmega)}$	$E_{(\varOmega)}$
H <sub>a</sub>	R	+0.627	-0.3169
	Р	-0.025	-0.6383
$O_4$	R	-1.514	-75.6276
	Р	-1.674	-75.5950
O <sub>2</sub>	R	-1.676	-75.5969
	Р	-1.416	-75.5869
Ca	R	-0.043	-37.9008
	Р	+0.088	-37.8363
C <sub>b</sub>	R	-0.044	-37.9021
	Р	+0.413	-37.6324

<sup>a</sup> For *E*, 1 au =  $2.625 \text{ x}10^3 \text{ kJ mol}^{-1}$ 

consequence, and due to the concerted nature of this reaction, it is interesting to investigate this electron exchange in the above-mentioned atoms along the IRC. A profound study of the variation in the AIM atomic charge along the IRC was performed in order to highlight the effect of the charge transfer process between the alkene molecule and the zeolite. The evolution of AIM charges for  $H_a$ ,  $C_a$  and  $C_b$  carbons atoms, and  $O_4$  and  $O_2$  oxygen atoms is shown in Fig. 2a–c, respectively. These atoms display the greatest charge transfer during the reaction.

Analysis of Fig. 2a-c shows that, of the five atoms involved in the reaction site, the most affected is the acidic hydrogen, H<sub>a</sub>. The variations in the AIM atomic properties of the H<sub>a</sub> proton that is been transferred are more significant from s = -1.2 amu<sup>1/2</sup> Bohr onwards. The results show that there is a large decrease in the positive charge of H<sub>a</sub> (from 0.62 to 0.04 au). It is important to highlight that the charge on the proton that is been transferred is considered low (0.3)au in the TS). Interestingly, this is due to the H<sub>a</sub> being bound to two atoms (Ca and O4) or the fact that it becomes dicoordinated (i.e.; Ca...Ha...O4). Both atoms mentioned provide electron density to the H<sub>a</sub> basin, as was stated in our previous work [17]. On the other hand, the carbon atomic charges vary within a range of 0.36 au in C<sub>b</sub> (from +0.02 to +0.38 au) and of 0.21 au in C<sub>a</sub> (from -0.12to +0.09 au). The range of variation for the basic  $O_2$ oxygen atom is only 0.29 au. Finally, the O<sub>4</sub> atom experiences a slight charge variation of about 0.15 au of the global process.

The atomic charge of  $C_a$  increases at the end of the reaction, with the increase in net charge being approximately 0.21 au, as expressed previously. However,  $C_a$  experiences marked changes throughout the process, achieving a minimum value near the TS (at *s* around  $-0.9 \text{ amu}^{1/2}$  Bohr). The variations in atomic charge experienced along the

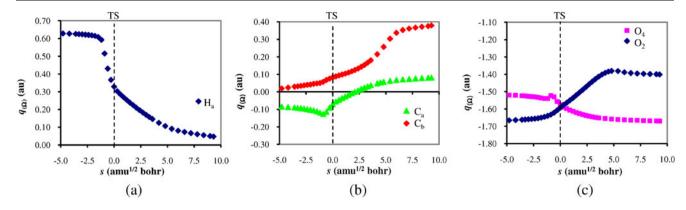


Fig. 2 Atomic net charge profile along the intrinsic reaction paths of the atoms involved in the reaction site. **a**  $H_a$ ; **b**  $C_a$  and  $C_b$ ; **c**  $O_2$  and  $O_4$ . The TS is located at the value s = 0.0 of the reaction coordinate

reaction coordinate indicate that two different stages can be considered for electron charge redistribution of the Ca atom. In the first part of the path, the C<sub>a</sub> atom first extracts electrons from the neighboring C<sub>b</sub> atom and decreases its atomic charge (via the increase in its electron population). Then, the atomic charge on C<sub>a</sub> increases due to the fact that its electron charge density is transferred to the atomic basin of the electrophilic proton that has been transferred from the acid site. At the TS, the atomic charge on Ca is negative, and it changes to positive at s = 2.1 amu<sup>1/2</sup>Bohr (equivalent to a Ca<sup>...</sup>Ha distance of 1.12 Å). On the other hand, an increase of  $q(C_{\rm b})$  along the reaction coordinate is observed, reaching an approximately constant value at s = 6.0 amu<sup>1/2</sup>Bohr (this corresponds to the stabilization of the C<sub>b</sub>-O<sub>2</sub> bond, as seen already in Fig. 1c). In addition, Fig. 2b shows that both carbon atoms have opposite charges at the TS.

The atomic charges of the oxygen atoms of the acidic and basic site of the zeolite cluster,  $O_4$  and  $O_2$ , respectively, display opposite behavior along the IRC path (see Fig. 2c); however, they present similar charges values in the TS. This behavior highlights the bifunctional character of the catalytic site of the protonated zeolite. The loss of electron population in the  $O_2$  atom is higher that the gain of electron population in the  $O_4$  atom. A continuous increase in atomic charge is observed at the  $O_2$  atom along the reaction path (this increase is due to electron donation from  $O_2$  to  $C_b$  atom), until it reaches a maximum value at s = 4.8 amu<sup>1/2</sup>Bohr. It then decreases slowly up to the point of stabilization of the  $O_2$  atom. This maximum corresponds to a character change of the forming  $C_b$ – $O_2$  bond (from closed shell to shared interaction, Fig. 1b). The  $O_4$  charge increases due to the fact that the H<sub>a</sub> atom transfers its electron density to the former, as it takes electrons from the  $C_a$  atom (the migration of H<sub>a</sub> from  $O_4$  to  $C_a$  is accompanied by a progressive transfer of electron charge from  $C_a$  to H<sub>a</sub> and from H<sub>a</sub> to  $O_4$ ).

The atomic energies along the reaction coordinate for  $H_a$ ,  $C_a$  and  $C_b$  atoms, and  $O_4$  and  $O_2$  atoms are shown in Fig. 3a–c, respectively. It can be observed in Fig. 3a from the  $E(H_a)$  values, that this atom is stabilized along the IRC. The trend of the curve is similar to that observed for atomic charge. The stabilization of  $H_a$  increases after TS formation. Figure 3b shows that the energy of both carbon atoms decreases before reaching the TS, followed by an increase that results in the destabilization of both atoms. These energies finally reach an approximately constant value that corresponds to the stabilization of the  $C_b$ – $O_2$  shared

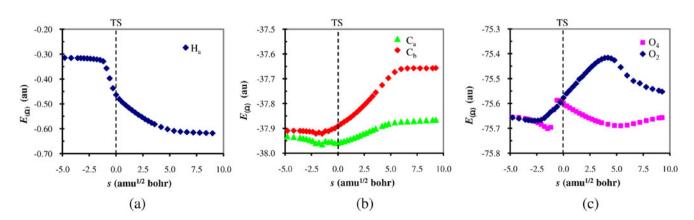


Fig. 3 Atomic energy profile along the intrinsic reaction paths of the atoms involved in the reaction site.  $\mathbf{a} H_a$ ;  $\mathbf{b} C_a$  and  $C_b$ ;  $\mathbf{c} O_2$  and  $O_4$ . The TS is located at the value s = 0.0 of the reaction coordinate

interaction (see Fig. 1b,c). The destabilization of the  $C_b$  atom becomes greater than the  $C_a$  atom as proton transfer proceeds.

Regarding the oxygen atom energies, the evolution observed for the two oxygen atoms is very different, as can be seen in Fig. 3c. Both curves present a maximum and a minimum at different places in the reaction path. The energy of the O<sub>2</sub> atom decreases up to s = -2.7 amu<sup>1/2</sup>Bohr, reaches a maximum at about s = 4.2 amu<sup>1/2</sup>Bohr, and then decreases again. This is indicative of a first stabilization, as a consequence of the weak interaction between the oxygen atom of the basic site and the electron deficient carbon atom. The O<sub>2</sub> atom is then destabilized due to electron donation from the  $O_2$  to the  $C_b$  atom. The maximum of  $E(O_2)$ corresponds to the change in the character of the C<sub>b</sub>-O<sub>2</sub> interaction from closed shell to shared interaction, which means that the O<sub>2</sub> atom is stabilized as soon as the C<sub>b</sub>-O<sub>2</sub> bond acquires the characteristics of a shared interaction (Fig. 1b).

On the other hand, the atomic energy profile of the O<sub>4</sub> atom shows an unexpected shape. The energy of the O<sub>4</sub> atom decreases up to s = -1.5 amu<sup>1/2</sup>Bohr. An abrupt increase is then observed until a maximum energy value is reached (at s = -0.6 amu<sup>1/2</sup>bohr); followed by a decrease and a slow final increase of the  $E(O_4)$ . The first stabilization zone corresponds to the initial slight decrease of  $\rho_b$  at  $O_4 \cdots H_a$ BCP, which means that the O<sub>4</sub> is initially slightly stabilized as the O-H bond lengthens. The zone of abrupt destabilization (between -1.5 to -0.6 amu<sup>1/2</sup>Bohr) corresponds to the rapid decrease of  $\rho_b$  at  $O_4 \cdots H_a$  BCP. The maximum value corresponds to the s coordinate where the Laplacian at the O<sub>4</sub>...H<sub>a</sub> BCP changes its sign, showing the loss of a shared interaction characteristic (or O<sub>4</sub>-H<sub>a</sub> bond breaking). After the O<sub>4</sub>-H<sub>a</sub> bond breaks, the O<sub>4</sub> atom is stabilized and destabilized by the redistribution of electron density.

In summary, we have found that the migration of the  $H_a$ atom from  $O_4$  to  $C_a$  is accompanied by a progressive transfer of electron charge from  $C_b$  to  $C_a$ , from  $C_a$  to  $H_a$  and from  $H_a$  to  $O_4$  atoms. Meanwhile, as  $C_b$  transfers electrons to  $C_a$ , an electronic deficiency in  $C_b$  is generated. This electronic deficiency is compensated by getting the electrons from the oxygen atom of the basic site,  $O_2$ . Therefore, the charge evolution along the reaction coordinate shows the whole electronic displacement process coming from the atom basins in the site of the reaction in order to achieve stabilization of the product. Bond breakage and bond formation are dominated by the electronic exchange between the different basins in the reaction site.

This electronic displacement along the protonation reaction produces the necessary energetic changes in order to achieve the stabilization of the alkoxide product. Finally, our preliminary results suggest that the electron density redistribution that accompanies the proton transfer (that is,  $O_4$ -H<sub>a</sub> bond breaking and  $C_a$ -H<sub>a</sub> bond formation), together with the change from double to single bond at the alkene fragment, determine the activation energy value. These electronic movements, together with the subsequent stabilization of carbocation charge by the zeolitic fragment from the TS toward the alkoxide, determine the global energy of the protonation reaction. However, more data will be required comparing a series of alkenes of greater size. This is currently are under investigation in our laboratory and the results will be published in the near future.

# Conclusions

Bond breakage and bond formation during the trans-2butene protonation reaction catalyzed by acidic zeolites were investigated within the framework of QTAIM, by evaluation of the changes in bonds and atomic properties of the electron density distribution along the IRC. The results revealed that local properties such as  $\rho_{\rm b}$ ,  $\nabla^2 \rho_{\rm b}$ ,  $\varepsilon$  and the  $|V_{\rm b}|/G_{\rm b}$  relationship, as well as the atomic properties  $q_{(\Omega)}$ and  $E_{(\Omega)}$ , are good indicators to prove what is happening in each bond/atom involved in the reaction site as the reaction progresses.

We found out that the electron density properties at relevant BCPs along the reaction coordinate reveal the progressive formation/breakage of different bonds, and the subsequent redistribution of electron density in order to stabilize the product formed. The variations in the local properties of  $\rho_b$ ,  $\nabla^2 \rho_b$  and  $|V_b|/G_b$  on H<sub>a</sub>-O<sub>4</sub> and C<sub>a</sub>-H<sub>a</sub> bonds, which are being broken/formed at the same time, show opposite behaviors as the transfer of the proton goes forward, allowing the identification of specific regions during proton transfer. Ca-Ha bond formation and Ha-O4 bond breakage take place before reaching the TS, in the early part of the reaction, and the process then involves an electronic redistribution. The final Ha-O4 bond breakage can be inferred by the complete disappearance of the BCP at the end of the reaction. Moreover, three regions involved in the formation of the Cb-O2 bond were characterized. The first region implies that a pure closed shell interaction takes place between the  $O_2$  and  $C_b$  atoms. Consequently, an intermediate character between a shared interaction and a closed shell interaction is observed between them, and finally the carbon-oxygen bond takes on the features of a weak covalent bond. We show that the  $\sigma$ -character of the forming C-O bond is established in the late part of the reaction, in contrast to the Ca-Ha bond that is formed previously.

In addition, although the process is concerted, analysis of the profile of the atomic charges and the atomic energies along the IRC has allowed the electron flow between the different basins involved in the reaction site to be described, and, at the same time, identified the different regions of this chemical reaction in terms of the charge redistribution process. We discovered that the migration of the  $H_a$  atom from  $O_4$  to  $C_a$  is accompanied by a progressive transfer of electron charge from  $C_b$  to  $C_a$ , from  $C_a$  to  $H_a$  and from  $H_a$ to  $O_4$ . Meanwhile, as  $C_b$  transfers electrons to  $C_a$ , an electronic deficiency in  $C_b$  is accordingly being generated. This electronic deficiency is compensated by getting the electrons from the oxygen atom of the basic site  $O_2$ . Therefore, the charge evolution along the reaction coordinate reveals the whole electronic displacement process coming from the atom basins at the site of the reaction in order to achieve stabilization of the product. Bond breakage and bond formation are dominated by electron exchange between the different basins in the reaction site.

In summary, we characterized not only the net electronic flow, but the mode of formation of the carbocation and its subsequent stabilization to form the alkoxide product. This electronic flow explains how the electronic deficiency on the  $C_b$  carbon that will give rise to the carbocation is generated; how its electronic demand is satisfied; and, finally, how it is stabilized as the reaction progresses in order to allow formation of the  $C_b-O_2$  bond that is characteristic of an alkoxide product.

Finally, the present work highlights the potential afforded by electron charge density topological analysis along the IRC (and their atomic properties) for the study of electron redistribution in a selected chemical reaction.

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