

# Molecular Dynamics Study of Ionic Liquids Complexation within $\beta$ -Cyclodextrins

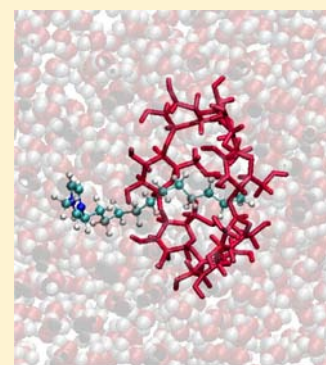
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**ABSTRACT:** We have studied 1:1 inclusion complexes of two imidazole-based ionic liquids within  $\beta$ -cyclodextrin: 1-dodecyl-3-methylimidazolium and 1-butyl-3-methylimidazolium. By means of an adaptive biasing force scheme, we obtained the free energy profile along two different pathways, differing in the orientations of the head-to-tail vector with respect to the primary–secondary rim axis. Regarding 1-dodecyl-3-methylimidazolium, we found one minimum energy structure for each pathway, in which the hydrophobic tail remains embedded within the cyclodextrin, while the headgroup lies  $\sim 11$ – $12$  Å from one of the rims; the structure where the polar head lies near the primary rim is the more stable. The analysis of the free energy of encapsulation of 1-butyl-3-methylimidazolium shows two minima for each insertion pathway, each of them associated with configurations where the imidazolium head lies close to one of the polar rims. As such, the most stable structure corresponds to one where the hydrophobic tail lies embedded within the cyclodextrin, while its head is localized near the secondary rim. The results are interpreted in terms of a simple model which captures the essential features that control the encapsulation process. A comparison with available experimental data is presented.



## 1. INTRODUCTION

Cyclodextrins (CD) are cyclic oligosaccharides composed of six ( $\alpha$ -CD), seven ( $\beta$ -CD), or eight ( $\gamma$ -CD) glucose units,<sup>1</sup> linked together by 1,4 glycosidic bonds. Their overall molecular shape is that of a truncated cone, with an hydrophobic cavity and a polar surface, characterized by hydroxylated, hydrophilic rims (a narrower, primary rim and a wider, secondary rim). This particular geometry gives CDs a highly versatile ability to form inclusion complexes with different kinds of organic solutes, a fact that makes them useful in food industry,<sup>2</sup> as drug carriers,<sup>3–6</sup> as building blocks for polymers,<sup>7,8</sup> and as adsorbents for separation techniques,<sup>9</sup> to cite a few relevant applications.

On the other hand, in the past decade, room temperature ionic liquids (RTILs) have attracted considerable attention as possible replacements for organic solvents, because they are nonvolatile, nonflammable, thermally and chemically stable, highly polar, and environmentally friendly.<sup>10</sup> These molten organic salts have been used together with CDs in a wide range of applications, such as in enantioseparation by electrophoresis,<sup>11–14</sup> in gas and high-performance liquid chromatographies,<sup>15,16</sup> and also in supramolecular chemistry, for the synthesis of new materials with many interesting properties, including polyrotaxanes and polypseudorotaxanes.<sup>17–22</sup> In all these fields, the knowledge of the characteristics of CD–RTIL interactions is of major interest.

Several experimental works have been devoted to systems combining RTILs and CDs. From the structural point of view,

Gao et al. studied the encapsulation of 1-butyl-3-methylimidazolium ( $C_4\text{mim}^+$ ) and 1-dodecyl-3-methylimidazolium ( $C_{12}\text{mim}^+$ ) in  $\beta$ -CD relying on <sup>1</sup>H NMR, among other techniques.<sup>23,24</sup> In their work, the authors proposed different structures for 1:1 inclusion complexes. For the larger RTIL, two possible configurations are described, each of them involving the inclusion of a portion of the hydrophobic tail inside the nonpolar cavity of  $\beta$ -CD, while the polar head remains immersed in the bulk solvent.<sup>24</sup> The difference between these structures resides in the fact that the imidazolium head can rest closer either to the primary or to the secondary rim. Contrasting, for the shorter RTIL, the authors proposed only one structure, where the RTIL is completely embedded within the  $\beta$ -CD cavity, with its head pointing toward the primary rim.<sup>23</sup> From a binding equilibrium perspective, many works have been devoted to the analysis and comparison of different complexation constants.<sup>25–29</sup> Yet many aspects related to the sources of the stabilization and the microscopic characteristics of the RTIL–CD association still remain to be unveiled. In what follows, we will present a microscopic description of the association between  $\beta$ -CD and two imidazolium-based RTILs with different hydrophobic tail lengths, relying on molecular dynamics (MD) simulations and free-energy calculations. The MD approach has been successfully implemented to analyze

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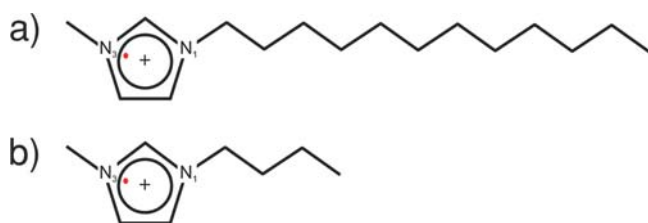
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74 solvation of a large variety of host–CD complexes in vacuo and  
75 in solution. Reference 30 provides a comprehensive review  
76 article about this issue.

77 The organization of this paper is as follows: in section 2 we  
78 describe the system and the molecular dynamics simulations  
79 performed, section 3 includes the results of our simulation  
80 experiments, and section 4 contains the discussion of these  
81 results. Finally, in section 5 we summarize the most relevant  
82 results of this paper.

## 2. SYSTEMS STUDIED AND SIMULATION DETAILS

83 We performed molecular dynamics experiments on aqueous  
84 solutions containing a single  $\beta$ -CD and an infinitely diluted  
85 imidazole-based cation. Two systems, differing in the hydro-  
86 phobicity of the charged solute, were analyzed: the first one  
87 corresponded to 1-dodecyl-3-methylimidazolium, whereas the  
88 second one corresponded to 1-butyl-3-methylimidazolium (see  
89 Figure 1). These molecules are typical cationic species of RTIL,

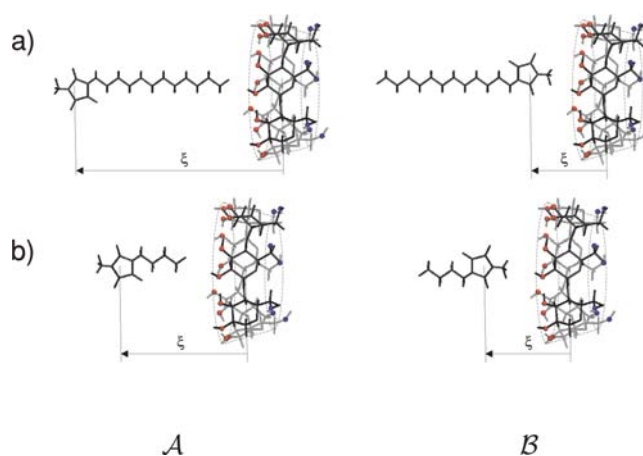


**Figure 1.** Chemical structures of the RTILs investigated: (a) 1-dodecyl-3-methylimidazolium; (b) 1-butyl-3-methylimidazolium. The red dots indicate the positions of the centers of mass of the imidazolium heads.

90 and structurally speaking, both can be portrayed in terms of an  
91 ionic imidazolium headgroup attached to hydrophobic tails of  
92 different lengths.

93 In the two cases, the systems comprised  $N_w = 1654$  water  
94 molecules, confined within a rectangular box with linear  
95 dimensions close to  $30 \text{ \AA} \times 30 \text{ \AA} \times 60 \text{ \AA}$ . The dynamical  
96 trajectories corresponded to isobaric–isothermal (NPT)  
97 simulation runs implemented via a Langevin dynamics, that  
98 maintained the pressure and temperature at the vicinity of 1 bar  
99 and  $T = 298 \text{ K}$ , respectively. The trajectories were generated  
100 using the NAMD package,<sup>31</sup> with interactions taken from the  
101 CHARMM22 force field.<sup>32</sup> Parameters for intra- and  
102 intermolecular interactions involving sites in the ionic liquid  
103 cation were taken from ref 33, whereas water interactions were  
104 modeled using the classical TIP3P model.<sup>34</sup> These Hamil-  
105 tonians have been employed in previous studies dealing with  
106 similar types of systems.<sup>35–38</sup> Long ranged Coulomb forces  
107 were treated using standard Ewald sums, assuming the presence  
108 of a continuous neutralizing background.

109 Coordinates of the  $\beta$ -CD were obtained from neutron  
110 diffraction information.<sup>39</sup> In all simulation experiments, the  
111 initial orientation of the CD was chosen so as to make the  
112 primary rim–secondary rim vector parallel to the longest axis of  
113 the simulation box (hereafter referred to as the  $z$ -axis). Two  
114 insertion paths,  $\mathcal{A}$  and  $\mathcal{B}$  (see Figure 2), differing in the  
115 orientations of the head-to-tail vector with respect to the  $z$ -axis,  
116 were considered. In all cases, the initial intramolecular  
117 configurations of the alkyl chains in the RTIL corresponded  
118 to fully trans conformers. Finally, the systems were filled up  
119 with water molecules and equilibrated for about 200 ps, in a run  
120 in which only the solvent molecules were allowed to move, at



**Figure 2.** Insertion pathways of RTIL's cation within  $\beta$ -CD: (a) 1-dodecyl-3-methylimidazolium; (b) 1-butyl-3-methylimidazolium. For the sake of clarity oxygen atoms corresponding to the primary and secondary hydroxyl groups of the CD are rendered in blue and red, respectively.

121 temperatures close to  $T = 700 \text{ K}$ . From then on, the systems  
122 were gradually cooled down to temperatures close to ambient  
123 conditions, by multiple rescalings of the atomic velocities  
124 during a time interval of 100 ps. During this period, we released  
125 the initial constraints on the cation and on the CD sites, with  
126 the exception of six spherically symmetric, soft harmonic  
127 interactions with restoring force constants  $k_{\text{rst}} \sim 15 \text{ kcal mol}^{-1}$   
128  $\text{\AA}^{-2}$ ,<sup>40</sup> acting on each glycosidic oxygen site that avoided global  
129 modifications of the initial orientation. In all cases, we verified  
130 that this external potential introduced only minor modifications  
131 to the overall dynamics along the insertion channels.

## 3. RESULTS

132 In order to describe the different stages of the insertion process  
133 of the RTIL cation within the CD cavity, we found it  
134 convenient to adopt a simple geometrical order parameter  $\xi$ ,  
135 defined as

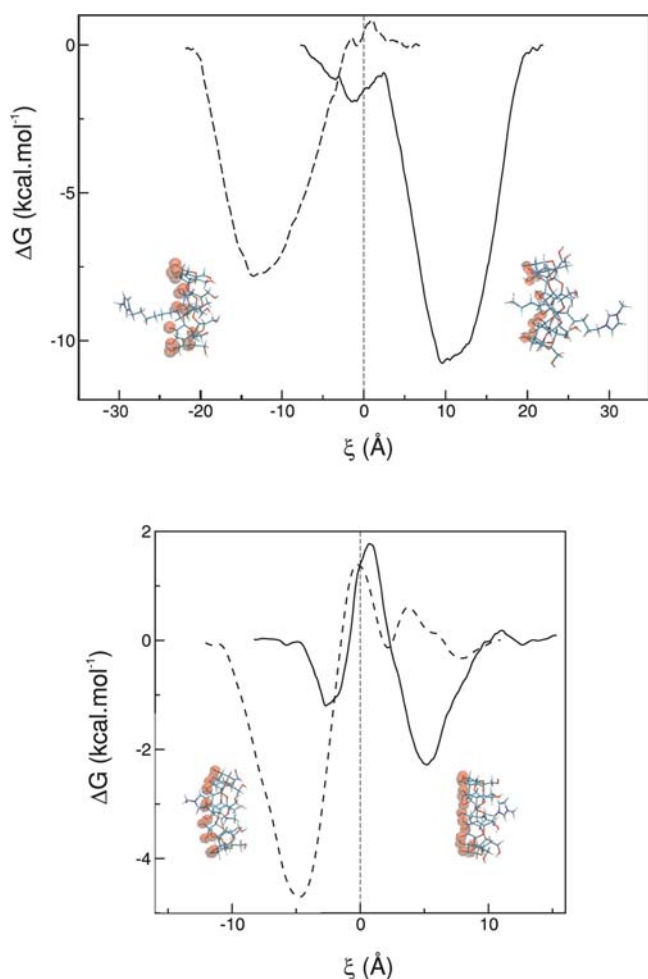
$$\xi = Z_{\text{IL}} - Z_{\text{CD}} \quad (1)$$

137 In eq 1,  $Z_{\text{CD}}$  and  $Z_{\text{IL}}$  correspond to the  $z$ -coordinates of the  
138 centers of mass of the  $\beta$ -CD and the RTIL imidazolium group,  
139 which is located nearby the position of the  $N_3$  atom, slightly  
140 shifted inward the ring (see also Figure 2). Associated with this  
141 order parameter there is a corresponding Gibbs free energy  
142 defined in terms of

$$-\beta G(\xi^0) \propto \ln \langle \delta(\xi - \xi^0) \rangle \quad (2)$$

144 where the angular brackets denote an equilibrium ensemble  
145 average,  $\delta$  corresponds to the delta-function centered at a given  
146 value of the reaction coordinate,  $\xi^0$ , and  $\beta = (k_B T)^{-1}$   
147 corresponds to the inverse of the temperature times the  
148 Boltzmann constant.

149 In Figure 3 we present results for  $\Delta G(\xi) = G(\xi) - G(\xi =$   
150  $\infty)$ . In all cases, the curves were obtained implementing an  
151 adaptive biasing forces (ABF) protocol.<sup>41–43</sup> The latter  
152 methodology has been successfully employed in analysis of  
153 encapsulation processes involving a large variety of guest  
154 molecules in CDs, ranging from simple ionic species<sup>35</sup> up to  
155 much more complex guests such as steroids,<sup>44</sup> rotaxanes,<sup>45</sup>  
156 cholesterol,<sup>46</sup> and Amphotericin B.<sup>47</sup> The basic idea behind this  
157 scheme relies on the generation of trajectories along a chosen



**Figure 3.** Gibbs free energy profiles for the inclusion of RTIL cation within an  $\beta$ -CD. Top panel, 1-dodecyl-3-methylimidazolium; bottom panel, 1-butyl-3-methylimidazolium. The dashed and solid lines correspond to the  $\mathcal{A}$  and  $\mathcal{B}$  insertion pathways, respectively. Typical snapshots of the inclusion complexes at the minimum energy configurations for both insertion pathways are displayed.

158 reaction coordinate, experiencing practically no free energy  
 159 barriers. This is achieved by estimating biasing forces along a  
 160 series of bins, spanning the complete  $\xi$  interval. These forces  
 161 flatten the free energy surface, so that the reaction coordinate  
 162 becomes uniformly sampled. Our procedure to implement the  
 163 algorithm involved the following: (i) we first divided the  
 164 relevant portion of the insertion path interval  $-20 \text{ \AA} \lesssim \xi \lesssim 20$   
 165  $\text{\AA}$  into 20 overlapping windows; (ii) confining potentials along  
 166 the  $x$  and  $y$  directions (harmonic constant  $k_{x-y} \sim 0.5 \text{ kcal mol}^{-1}$   
 167  $\text{\AA}^{-2}$ ) acting on the  $N_3$  site of the imidazolium ring and on the  
 168 terminal C atom of the methyl group in the longest aliphatic tail  
 169 were also applied. In doing so, we preserved the initial overall  
 170 intramolecular geometry of the cation, at large values of  $\xi$ , and,  
 171 incidentally, restricted the sampling over the  $\rho^2 = x^2 + y^2 \lesssim 25$   
 172  $\text{\AA}^2$  cylindrical region. Within each window, instantaneous values  
 173 of the forces were collected in bins  $0.1 \text{ \AA}$  wide. The sampling  
 174 within each window required typically  $\sim 2 \times 10^6$  simulation  
 175 steps to attain proper convergence.

176 The free energy profiles are shown in the top ( $C_{12}\text{mim}^+$ ) and  
 177 bottom ( $C_4\text{mim}^+$ ) panels of Figure 3. Concerning the profiles  
 178 for  $C_{12}\text{mim}^+$ , two important observations are to be noted: (i)  
 179 the magnitudes and (ii) the symmetry of the positions of the full  
 180 corresponding global minima with respect to the full

encapsulation of the headgroup,  $\xi = 0$ . Our simulations show 181  
 that the most stable configuration of the RTIL-CD complex 182  
 corresponds to the insertion pathway  $\mathcal{B}$ , with  $\Delta G(\xi \sim 11 \text{ \AA}) \sim$  183  
 $-12 \text{ kcal mol}^{-1}$ . These values correspond to an arrangement in 184  
 which the cation lies with a substantial portion of its 185  
 hydrophobic tail embedded within the CD cavity, while the 186  
 imidazolium group lies in a position somewhat external with 187  
 respect to the CD primary rim. Similar geometrical character- 188  
 istics are found in the solvation structure that prevails in the 189  
 vicinity of the shallower global minimum along the path  $\mathcal{A}$ , 190  
 $\Delta G(\xi \sim -12 \text{ \AA}) \sim -7.5 \text{ kcal mol}^{-1}$ , except that, along this 191  
 channel, the headgroup lies at the vicinity of the other, 192  
 secondary, rim. These two complex structures, in which the 193  
 hydrophobic tail is embedded within the CD cavity and the 194  
 imidazolium ring lies surrounded by the external solvent, are in 195  
 close agreement with those proposed by Gao et al.<sup>24</sup> 196

At a first glance, the characteristics of the free energy profiles 197  
 for cations with shorter alkyl tails shown in the bottom panel of 198  
 Figure 3 look inverted while the magnitudes of the global 199  
 minima are somewhat less pronounced. As a new feature, in 200  
 both profiles, there is evidence of a local maximum near  $\xi \sim 0$ , 201  
 flanked by two lateral minima. These minima correspond to 202  
 configurations in which the headgroup of the RTIL lies close to 203  
 one of the rims. For each insertion pathway, the most stable 204  
 minimum is the one for which not only does the headgroup 205  
 coincide with one of the polar rims, but also the hydrophobic 206  
 tail lies embedded within the CD cavity. The secondary minima 207  
 correspond to spatial arrangements where the headgroup of the 208  
 RTIL interacts with the other rim of the CD, while its tail is 209  
 surrounded by water molecules, disrupting the hydrogen bond 210  
 network. In particular, for path  $\mathcal{B}$ , the difference between 211  
 minima ( $\Delta(\Delta G_{\text{min}}^{\mathcal{B}}) \sim 1 \text{ kcal mol}^{-1}$ ) is small enough to 212  
 conclude that both structures are comparable in terms of their 213  
 relative stability. Finally, note that the stabilization energy of the 214  
 RTIL-CD complex at the global minimum for path  $\mathcal{A}$  (dashed 215  
 line) is nearly 2 times larger than the corresponding one for 216  
 path  $\mathcal{B}$  (solid line), i.e.,  $\Delta G_{\text{min}}^{\mathcal{A} \rightarrow \mathcal{B}} \sim 2 \text{ kcal mol}^{-1}$ . 217

To conclude, we present an estimate of the free energy of 218  
 encapsulation  $\Delta G_{\text{enc}}^{\circ}$ , which can be readily obtained by 219  
 integrating the corresponding free energy profiles, namely 220

$$-\beta \Delta G_{\text{enc}}^{\circ} = \ln \frac{\pi N_A \int_{-\infty}^{\infty} r_{\text{av}}^2(\xi) \exp[-\beta \Delta G(\xi)] d\xi}{dm^3} \quad (3) \quad 221$$

where  $r_{\text{av}}^2$  is the  $\xi$ -dependent average ratio of the cross section 222  
 of  $\beta$ -CD, and  $N_A$  is Avogadro's number. Results for  $\Delta G_{\text{enc}}^{\circ}$  are 223  
 listed in Table 1, along with available experimental information. 224  
 Note that our simulation results feature two values of  $\Delta G_{\text{enc}}^{\circ}$ , 225  
 one for each insertion pathway, while the experiments provide 226  
 only one value, which contains contributions for the two 227  
 possible orientations and, eventually, includes contributions 228  
 derived from the anion complexation. 229

**Table 1. Experimental and Calculated Encapsulation Free Energies Expressed in  $\text{kcal mol}^{-1}$**

	exptl $\Delta G_{\text{enc}}^{\circ}$ <sup>a</sup>		calcd $\Delta G_{\text{enc}}^{\circ}$	
			$\mathcal{A}$	$\mathcal{B}$
$C_4\text{mim}^+ - \beta\text{-CD}$	$-1.3^b$	$-2.0^c$	-2.8	-0.6
$C_{12}\text{mim}^+ - \beta\text{-CD}$	$-5.5^c$		-5.0	-8.7

<sup>a</sup>From ref 25. <sup>b</sup>Anion:  $\text{Cl}^-$ . <sup>c</sup>Anion:  $\text{BF}_4^-$ .



230 Although our simulation results adequately reproduce the  
 231 experimental trends, the calculated encapsulation energies are  
 232 about  $\sim 2\text{--}3$  kcal mol $^{-1}$  lower than the corresponding  
 233 experimental ones. This difference can be mainly ascribed to  
 234 the loss of configurational entropy in the calculation, due to the  
 235 restraints imposed on the motion of the RTIL to ensure an  
 236 appropriate sampling.<sup>44</sup> Note that our procedure does not  
 237 include relevant rotational and translational degrees of freedom  
 238 of the guest. This leads to an underestimation of  $\Delta G_{\text{enc}}^{\circ}$  values  
 239 of  $\sim RT \sim 0.5$  kcal mol $^{-1}$ , since two rotational degrees of  
 240 freedom are being ignored. Contributions from translational  
 241 degrees of freedom are difficult to estimate. A conservative  
 242 guess would be close to  $\sim 1.5$  kcal mol $^{-1}$ .<sup>48</sup>

243 Other possible sources of the differences between exper-  
 244 imental and theoretical values can be traced back to limitations  
 245 in the parametrization of the force field and, furthermore, to the  
 246 absence of anions in the simulation experiments (experimental  
 247 results seem to be very sensitive to the type of anion of the  
 248 ionic liquid: see for example the differences between  $\Delta G_{\text{enc}}^{\circ}$  for  
 249  $\text{C}_4\text{mim}^+\text{Cl}^-$  and  $\text{C}_4\text{mim}^+\text{BF}_4^-$  in Table 1).

250 Comparison of  $\Delta G_{\text{enc}}^{\circ}$  values between different RTILs shows  
 251 an increment of the order of  $\sim 2\text{--}10$  times for this stabilization  
 252 energy as the hydrophobic tail length increases. In section 4 we  
 253 will present a detailed analysis of the characteristics of each  
 254 RTIL- $\beta$ -CD inclusion process, so as to assess the origin of the  
 255 observed differences.

## 4. DISCUSSION

256 **4.1.  $\text{C}_4\text{mim}^+$ .** In order to gain additional insight into the  
 257 encapsulation process of  $\text{C}_4\text{mim}^+$  in a  $\beta$ -CD, we elaborated a  
 258 simple model capable of capturing the essential features of the  
 259 free energy profiles presented above.

260 The model combines the following ingredients:

261 1. The RTIL was modeled as two rigid spheres in contact,  
 262 with radius  $r_o = 2.7$  Å. The first one mimics the hydrophobic  
 263 tail, whereas the second one—at the center of which a single  
 264 positive charge ( $e$ ) was located—represents the hydrophilic  
 265 headgroup of the RTIL (see Figure 4a)). The volume of the  
 266 model RTIL is  $2V_{\text{ctrl}} = 2(4/3)\pi r_o^3 \sim 165$  Å $^3$ , in close agreement  
 267 with the calculated molecular volume of the probe.<sup>49</sup>

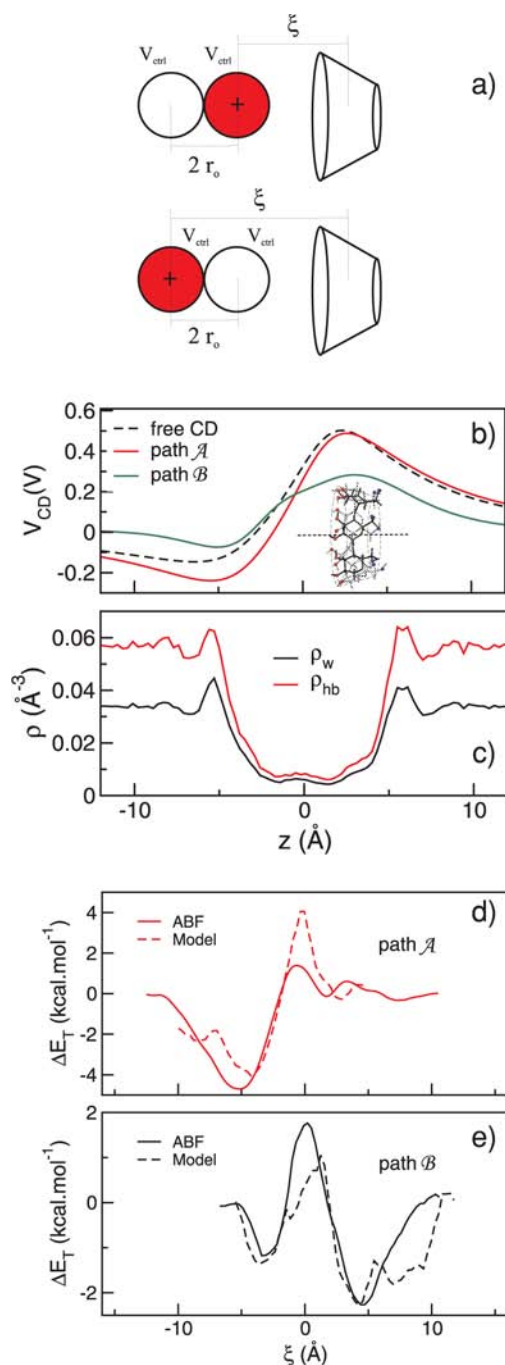
268 2. The interaction between the  $\beta$ -CD and the RTIL is  
 269 represented exclusively by the Coulombic coupling between the  
 270 host and the positive charge. To this end the Coulombic field  
 271 generated by the  $\beta$ -CD along its cylindrical axis was calculated  
 272 according to

$$V_{\text{CD}}(z) = \left\langle \sum_i^{N_{\text{CD}}} \frac{q_i}{x_i^2 + y_i^2 + (z - z_i^2)} \right\rangle \quad (4)$$

274 where  $N_{\text{CD}}$  is the total number of atomic sites of the host;  $q_i$ ,  $x_i$ ,  
 275  $y_i$ , and  $z_i$  correspond to the partial charge and the Cartesian  
 276 coordinates of the  $i$ th site of the CD, respectively. The  
 277 Coulombic potential was averaged over an ensemble of  $\beta$ -CD  
 278 configurations, harvested along the ABF trajectories for the  
 279 different pathways analyzed (see Figure 4b).

280 3. The aqueous solvent was represented by a continuous  
 281 medium within which the RTIL- $\beta$ -CD pair was immersed. The  
 282 dielectric constant of water ( $\epsilon_w$ ) was considered to be a linear  
 283 function of the water local density, according with available  
 284 experimental data.<sup>50</sup> The latter was calculated according to

$$\rho_w(z) = \frac{1}{\pi R^2} \sum_i \langle \delta(z_i^w - Z_{\text{CD}} - z) \rangle_{\text{cyl}} \quad (5)$$



**Figure 4.** (a) Scheme of the model to study the encapsulation complexes of  $\text{C}_4\text{mim}^+$  in a  $\beta$ -CD. The picture above represents  $\mathcal{B}$  pathway, while the one below corresponds to  $\mathcal{A}$  pathway. (b)  $V_{\text{CD}}$  for three different configurations: free CD (black, dashed line), pathway  $\mathcal{A}$  CD (red, solid line), and pathway  $\mathcal{B}$  CD (green, solid line). (c) Water and hydrogen bond densities as a function of the distance. (d, e) Energy profiles obtained by ABF techniques (solid lines) and by the application of our model (dashed lines) for  $\mathcal{A}$  and  $\mathcal{B}$  pathways, respectively.

In eq 5,  $\langle \dots \rangle_{\text{cyl}}$  denotes an equilibrium ensemble average, taken over a cylindrical region of the simulation box axially aligned to the cylindrical axis of the CD, with radius  $R = 8$  Å;  $z_i^w$  represents the  $z$ -coordinate of the oxygen site of the  $i$ th water molecule (see Figure 4c).

4. There is also one more energy contribution left to be considered in the encapsulation process: the work involved in

293 the creation of a cavity, mainly associated with the rearrange-  
 294 ment of the hydrogen bond network required to accommodate  
 295 the two spheres within the water. Note that solvent stabilizes as  
 296 the RTIL moves from rich-to-low density regions. In our  
 297 model, at a given  $\xi$ , the solvent–solvent interactions depend on  
 298 the number of hydrogen bonds within the control volume. The  
 299 hydrogen bond density ( $\rho_{\text{hb}}$ ) is determined in a way similar to  
 300 that described for the calculation of  $\rho_w$ , taking into account the  
 301 hydrogen bond definition presented in ref 51 (see Figure 4c).  
 302 5. In order to compute the energy profiles, the probe was  
 303 displaced along the cylindrical axis of the  $\beta$ -CD, and the  
 304 potential energy,  $E_T(\xi)$ , was calculated as a sum of two  
 305 contributions: (i) the Coulombic coupling between the charge  
 306 and the CD, screened by the dielectric medium, namely

$$E_{\text{coul}}(z) = \frac{eV_{\text{CD}}(z)}{\epsilon_w(z)} \propto \frac{eV_{\text{CD}}(z)}{\rho_w(z)} \quad (6)$$

307 and (ii) the cavity contribution

$$E_{\text{cavity}}(z) \propto \rho_{\text{hb}}(z)V_{\text{ctrl}} \quad (7)$$

309 6. The resulting total energy is determined for pathway  $\mathcal{A}$  by

$$E_T(\xi) = E_{\text{coul}}(\xi) + E_{\text{cavity}}(\xi) + E_{\text{cavity}}(\xi + 2r_o) \quad (8)$$

311 or, for pathway  $\mathcal{B}$  by

$$E_T(\xi) = E_{\text{coul}}(\xi) + E_{\text{cavity}}(\xi) + E_{\text{cavity}}(\xi - 2r_o) \quad (9)$$

314 A graphical representation of the model is depicted in panel a  
 315 of Figure 4.

316 A comparison of the results obtained from this model with  
 317 the ABF potential energy curves for both encapsulation  
 318 pathways is shown in panels d and e of Figure 4. Even though  
 319 there are some minor differences in the positions and depths of  
 320 the minima, our simplified model does reproduce the relevant  
 321 features of the potential curves. The analysis of the different  
 322 energetic contributions suggests that the secondary rim of the  
 323 CD (negative electric potential region) interacts much more  
 324 strongly with the positive charged cationic head than the  
 325 primary rim does. This observation agrees with a previous study  
 326 made in our group, in which anions were found to form  
 327 encapsulation complexes near the primary rim of the CD  
 328 (positive electric potential region).<sup>35</sup> As a consequence, the  
 329 global minimum for the  $C_4\text{mim}^+-\beta$ -CD complex corresponds  
 330 to configurations in which the hydrophobic tail lies within the  
 331 hydrophobic CD cavity, whereas the RTIL headgroup remains  
 332 in close contact with the secondary rim. Furthermore, one  
 333 could speculate that the presence of a secondary minimum ( $\xi \sim$   
 334 3 Å) in pathway  $\mathcal{B}$  would indicate that the coupling between  
 335 the imidazolium head and the secondary CD rim is strong  
 336 enough to compensate the unfavorable interaction between the  
 337 hydrophobic tail and the water molecules.

338 At this point, it is worth commenting on the experimental  
 339 results presented by Gao et al.<sup>23</sup> Based on the analysis of  
 340 chemical shifts in the <sup>1</sup>H NMR spectra of the RTIL– $\beta$ -CD  
 341 complex, the authors have proposed a minimum energy  
 342 inclusion moiety in which the RTIL headgroup lies in close  
 343 contact with the CD primary ring. On the other hand, our  
 344 calculations predict a most stable complex structure in which  
 345 the guest molecule rests in an opposite orientation. The  
 346 interpretation of the experimental signals made by Gao et al. is  
 347 based on the assumption that the imidazolium ring enters the  
 348 cavity of the  $\beta$ -CD from the secondary, wider, rim. Our  
 349 calculations show no significant differences between the

energy barriers associated with the different insertion pathways  
 (see bottom panel in Figure 3). Consequently, it does not seem  
 to be a preferential entrance channel for the RTIL. Beyond this  
 fact, we tend to believe that the structure predicted by our  
 calculations for the minimum is consistent with the  
 experimental results: (i) first, H<sub>3</sub> and H<sub>5</sub> CD protons (located  
 at the inner surface of cavity) should exhibit upfield shifts due  
 to their interactions with both the headgroup and the aliphatic  
 RTIL tail; (ii) contrasting, H<sub>4</sub> and H<sub>5</sub> imidazole ring proton  
 signals should be downfield shifted due to their close  
 interaction with the oxygen atoms at the secondary rim, and  
 probably collapse into a single signal (analysis of radial  
 distributions functions of the type O<sub>2</sub>, O<sub>3</sub>–H<sub>4</sub>, H<sub>5</sub>, not  
 shown here, reveal equivalent environments for both atoms).

4.2.  $C_{12}\text{mim}^+$ . In section 3 we showed that there is a  
 preferential stabilization of  $C_{12}\text{mim}^+$  along pathway  $\mathcal{B}$ , with its  
 hydrophobic tail embedded within the  $\beta$ -CD and its headgroup  
 located  $\sim 11$  Å from the primary rim. Since the distances  
 between the imidazolium head and the CD rims are longer than  
 the ones found for the shorter RTIL, there is no evidence that  
 the Coulombic coupling discussed in section 4.1 contributes to  
 the stabilization of the complexes. As such, the encapsulation  
 seems to be mainly driven by hydrophobic interactions. In the  
 following paragraphs, we will show that the differences in the  
 solvation of the OH groups located in the secondary rim of the  
 CD will be the new relevant feature that might explain the  
 stabilization of the  $C_{12}\text{mim}^+-\beta$ -CD moiety. To this end, a  
 statistic of relevant observables was harvested along uncon-  
 strained trajectories, initially equilibrated at the vicinities of the  
 different global minima of the  $C_{12}\text{mim}^+-\text{CD}$  complexes. Note  
 that the depths of the relevant free energy wells (see Figure 3)  
 are sufficiently large so as to make it possible to collect  
 physically sound averages from unconstrained runs. In fact, we  
 verified that the logarithms of the histograms for the reaction  
 coordinate collected along these trajectories lasting typically  
 $\sim 4$ – $6$  ns (not shown) do reproduce the free energy well  
 profiles obtained from ABF trajectories.

In order to characterize the intramolecular hydrogen bonds  
 in the CD, we calculated radial density profiles of the form

$$\rho_{\text{O}_\alpha\text{HO}_\beta}(r) = \frac{1}{4\pi r^2 N_i} \sum_i \sum_j \langle \delta(|\mathbf{r}_i^{\text{O}_\alpha} - \mathbf{r}_j^{\text{HO}_\beta}| - r) \rangle \quad (10)$$

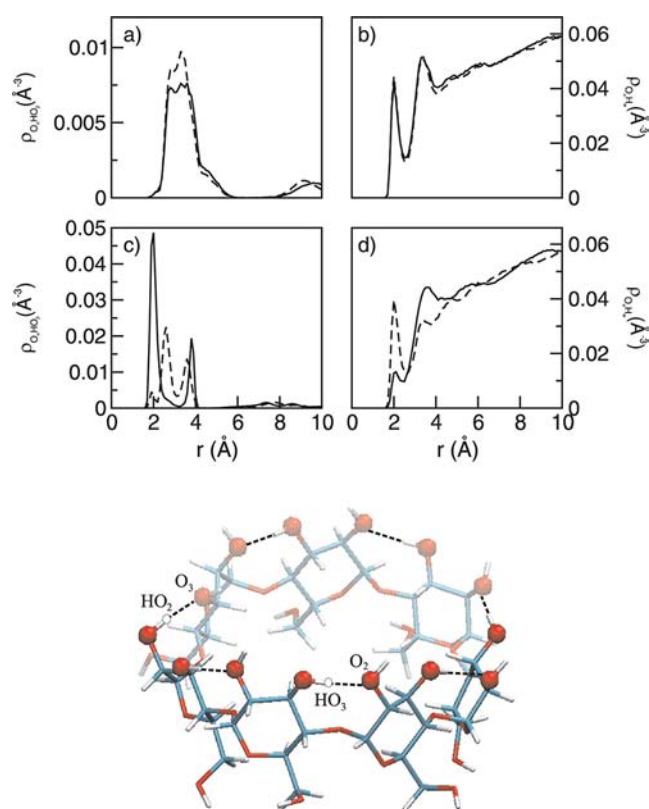
In eq 10,  $N_i = 7$ ,  $\mathbf{r}_i^{\text{O}_\alpha}$  represents the coordinate of the  $i$ th  $\alpha$ -  
 oxygen site, and  $\mathbf{r}_j^{\text{HO}_\beta}$  corresponds to the  $j$ th hydrogen bonded  
 to a  $\beta$ -oxygen, both lying at the secondary rim of CD (see lower  
 panel in Figure 5).

On the other hand, solvation at the secondary rim was  
 described in terms of the following radial density function:

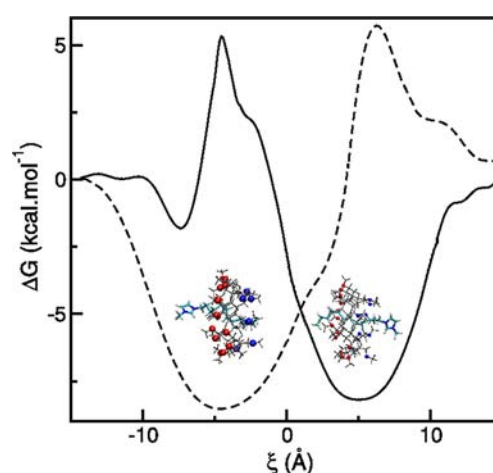
$$\rho_{\text{O}_\alpha\text{H}_w}(r) = \frac{1}{4\pi r^2 N_i} \sum_i \sum_j \langle \delta(|\mathbf{r}_i^{\text{O}_\alpha} - \mathbf{r}_j^{\text{H}_w}| - r) \rangle \quad (11)$$

where  $\mathbf{r}_j^{\text{H}_w}$  corresponds to the  $j$ th water hydrogen site.

In Figure 5 we present plots for these spatial correlations. At  
 a first glance, it is clear that the solvation structures for  
 pathways  $\mathcal{A}$  and  $\mathcal{B}$  look markedly different. Most importantly,  
 in the  $\mathcal{B}$  profile, there is a peak located at  $r \sim 1.95$  Å (more  
 pronounced for  $\rho_{\text{O}_2\text{HO}_3}$ ) that is absent in pathway  $\mathcal{A}$ . This peak  
 is also featured in the hydrated  $\beta$ -CD system in the absence of  
 RTIL (not shown), revealing the presence of intramolecular  
 hydrogen bonding between adjacent glycosidic units. As such,  
 along the  $\mathcal{A}$  pathway, the presence of  $C_{12}\text{mim}^+$  somehow alters



**Figure 5.** Upper panel: Radial density functions for  $C_{12}mim^+$  encapsulation in a  $\beta$ -CD. (a, c)  $\rho_{O_2,H_w}$  for  $\alpha = 2$ ,  $\beta = 3$  (solid lines), or  $\alpha = 3$ ,  $\beta = 2$  (dashed lines); (b, d)  $\rho_{O_3,H_w}$  for  $\alpha = 2$  (solid lines) or  $\alpha = 3$  (dashed lines). The upper (lower) graphs correspond to insertion pathways  $\mathcal{A}$  ( $\mathcal{B}$ ). Lower panel: Labeling scheme for the different atom types involved in intramolecular hydrogen bonds at the secondary rim of CD.



**Figure 6.** Gibbs free energy profiles for the inclusion of  $C_{12}mim^+$  within a permethylated  $\beta$ -CD. The dashed and solid lines correspond to the  $\mathcal{A}$  and  $\mathcal{B}$  insertion pathways, respectively. Typical snapshots of the inclusion complexes at the minimum energy configurations for both insertion pathways are displayed.

407 the solvation structure of the cyclodextrin, despite the fact that  
 408 the polar head lies sufficiently distant from the secondary rim.  
 409 In pathway  $\mathcal{A}$  these missing hydrogen bonds are compensated  
 410 by an increment in the hydration of the secondary rim (see  
 411 profiles for  $\rho_{O_2,H_w}$  and  $\rho_{O_3,H_w}$ , depicted in Figure 5b). For the  
 412 sake of comparison, similar correlation functions for pathway  $\mathcal{B}$   
 413 are shown in Figure 5d. In the former case, both OH groups are  
 414 fully solvated by water molecules, while in the latter, the  
 415 solvation of these moieties is notably reduced (note the  
 416 reduced magnitude of the peak of  $\rho_{O_2,H_w}$  at  $r \sim 1.95$  Å).  
 417 Incidentally, we mention that when this analysis is performed  
 418 for the  $C_4mim^+-\beta$ -CD complex (not shown), the shape of the  
 419 correlation function looks similar to the profile for the  $\beta$ -CD-  
 420 water system, revealing that the presence of the shorter RTIL  
 421 does not modify substantially the intramolecular hydrogen  
 422 bond structure of the CD.  
 423 To carry on with our analysis, we investigated whether the  
 424 perturbation in the solvation of the secondary rim of the CD  
 425 was responsible for the difference between the minimum  
 426 energy structures associated with both encapsulation pathways.  
 427 To this end, we analyzed the free energy profile associated with  
 428 the order parameter  $\xi$  for the encapsulation of  $C_{12}mim^+$  in a  
 429 permethylated  $\beta$ -CD (PMCD). Results are depicted in Figure  
 430 6. For both insertion pathways these profiles look almost  
 431 perfectly symmetric, exhibiting similar stabilities. Furthermore,  
 432 the magnitude of the global minimum is in good agreement

with that of pathway  $\mathcal{A}$  for the nonmethylated  $\beta$ -CD, where  
 433 the intramolecular hydrogen bonds in the secondary rim were  
 434 perturbed due to the presence of the encapsulated RTIL. In  
 435 passing, note that the positions of the global minima and  
 436 maxima are shifted compared with the system studied in Figure  
 437 3, most likely due to changes in the polarities of the rims. 438

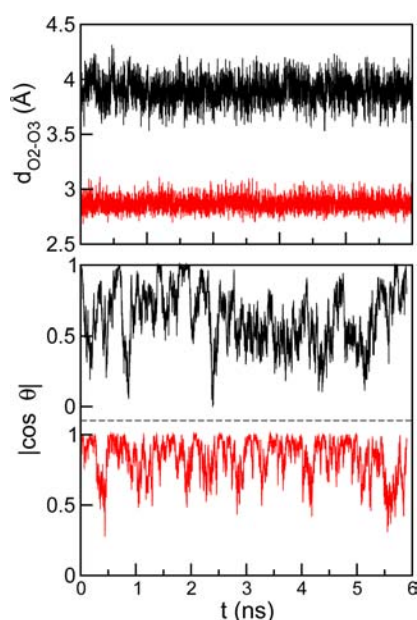
To conclude our analysis, we provide a microscopic  
 439 interpretation for the disruption of the intramolecular  $\beta$ -CD  
 440 hydrogen bonds along the pathway  $\mathcal{A}$ . For this purpose it will  
 441 be useful to focus on the time evolution of two parameters: (i)  
 442 First,  $d_{O_2-O_3}$ , the average distance between oxygens belonging  
 443 to adjacent glycosidic units in the CD. This parameter reflects  
 444 the degree of deformation undergone by the CD, which, in  
 445 turn, should favor or prevent the formation of intramolecular  
 446 hydrogen bonds. In the upper panel in Figure 7 we show the  
 447 time evolution of  $d_{O_2-O_3}$  for the different insertion pathways. 448  
 449 For pathway  $\mathcal{A}$ ,  $d_{O_2-O_3}$  fluctuates around  $\sim 3.9$  Å (see black  
 450 line), while for pathway  $\mathcal{B}$  the average distance is  $\sim 1$  Å smaller  
 451 (see red line). (ii) The second parameter of interest is  $l \cos \theta$ ,  
 452 defined as

$$l \cos \theta = \frac{|Z_{IL} - Z_{CD}|}{|r_{IL} - r_{CD}|} \quad (12) \quad 453$$

where  $r_{CD}$  and  $r_{IL}$  stand for the positions of the centers of mass  
 454 of the  $\beta$ -CD and the RTIL imidazolium group, respectively. 455  
 456 This magnitude provides an estimate of the degree of bending  
 457 of the polar head with respect to its backbone.

The lower panel of Figure 7 depicts the time evolution of  
 458  $l \cos \theta$ . It is clear that, for the  $\mathcal{A}$  pathway, the fluctuation of this  
 459 angle is larger (black lines) than that corresponding to the  
 460 other orientation (red lines). Indeed, it can be seen that the  
 461 glycosidic units of the  $\beta$ -CD that are closer to the bent RTIL  
 462 head rotate almost  $\sim 45^\circ$  over the glycosidic bonds (not  
 463 shown). From these observations it is possible to conclude that  
 464 the larger fluctuations of the RTIL backbone along pathway  $\mathcal{A}$   
 465 promote a stronger deformation of the secondary rim of CD  
 466 and, consequently, prevent the formation of intramolecular  
 467 hydrogen bonds. 468





**Figure 7.** Time evolution of two relevant observables to explain the loss of intramolecular hydrogen bonds in  $C_{12}mim^+$  encapsulation by pathway  $\mathcal{A}$  (black lines) versus pathway  $\mathcal{B}$  (red lines). Upper panel:  $d_{O_2-O_3}$ . Lower panel:  $|\cos \theta|$ .

## 5. CONCLUDING REMARKS

The MD results presented in this paper provide new insights into the microscopic characteristics of the individual encapsulation of two ionic liquids (differing in the lengths of their hydrophobic tails) within a  $\beta$ -CD. By means of an ABF scheme, we were able to obtain free energy profiles associated with the encapsulation processes for each RTIL, along two possible insertion pathways. We found that, for each pathway, there is only one minimum energy configuration for the  $C_{12}mim^+$ - $\beta$ -CD complex. This structure is characterized by the hydrophobic RTIL tail embedded within the CD and the imidazolium head lying at an average distance of  $\sim 11$ – $12$  Å from one of the rims. The arrangement in which the polar head lies closer to the primary rim (pathway  $\mathcal{B}$ ) was found to be  $\sim 50\%$  more stable. The difference in the stability of the two complexes may be ascribed to the formation of intramolecular hydrogen bonds between adjacent glycosidic units in the secondary rim, which is only possible for pathway  $\mathcal{B}$ . Instead, when the insertion proceeds according to channel  $\mathcal{A}$ , the secondary rim suffers a deformation due to larger fluctuations of the alignment of the imidazolium head with respect to the  $z$ -axis, preventing the formation of these intramolecular hydrogen bonds.

On the other hand, the free energy associated with the encapsulation process of the  $C_4mim^+$  shows two minima for each insertion pathway. For both channels, the most stable configurations correspond to an arrangement where the hydrophobic tail lies embedded within the  $\beta$ -CD, while the polar head lies close to one of the rims. The global minimum corresponds to the structure where the imidazolium lies close to the secondary rim. We examined a simplified model that incorporates the basic elements controlling the encapsulation channels. In doing so, we found that the latter difference can be simply ascribed to changes in the RTIL head-CD rim Coulombic couplings. Moreover, along each pathway, the shallower minima correspond to the scenarios where

imidazolium interacts more strongly with one of the rims of the  $\beta$ -CD, while the hydrophobic tail remains surrounded by water molecules.

The obtained results suggest that hydrophobic interactions are the main responsible forces for the complexation process of RTILs in  $\beta$ -CD. Guest–host Coulombic interactions and hydrogen bond interactions could also play significant roles in the encapsulation process, and they are most influential on the characteristics and energetics of the system for imidazolium cations with shorter alkyl chains.

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### Notes

The authors declare no competing financial interest.

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## REFERENCES

- (1) Larger cyclodextrins have also been reported; see, for instance: Larsen, K. L. Large Cyclodextrins. *J. Inclusion Phenom.* **2002**, *43*, 1–13.
- (2) Astray, G.; Gonzalez-Barreiro, C.; Mejuto, J. C.; Rial-Otero, R.; Simal-Gándara, J. A Review on the Use of Cyclodextrins in Foods. *Food Hydrocolloids* **2009**, *23*, 1631–1640.
- (3) Pinho, E.; Grootveld, M.; Soares, G.; Henriques, M. Cyclodextrins as Encapsulation Agents for Plant Bioactive Compounds. *Carbohydr. Polym.* **2014**, *101*, 121–135.
- (4) Mellet, C. O.; Fernández, J. M. G.; Benito, J. M. Cyclodextrin-based Gene Delivery Systems. *Chem. Soc. Rev.* **2011**, *40*, 1586–1608.
- (5) Loftsson, T.; Duchêne, D. Cyclodextrins and their Pharmaceutical Applications. *Int. J. Pharm.* **2007**, *329*, 1–11.
- (6) Fraceto, L. F.; Grillo, R.; Sobarzo-Sánchez, E. Cyclodextrin Inclusion Complexes Loaded in Particles as Drug Carrier Systems. *Curr. Top. Med. Chem.* **2014**, *14*, 518–525.
- (7) Van de Manacker, F.; Vermonden, T.; Van Nostrum, C. F.; Hennink, W. E. Cyclodextrin-based Polymeric Materials: Synthesis, Properties, and Pharmaceutical/Biomedical Applications. *Biomacromolecules* **2009**, *10*, 3157–3175.
- (8) Li, J.; Loh, X. J. Cyclodextrin-based Supramolecular Architectures: Syntheses, Structures, and Applications for Drug and Gene Delivery. *Adv. Drug Delivery Rev.* **2008**, *60*, 1000–1017.
- (9) Crini, G.; Morcellet, M. Synthesis and Applications of Adsorbents Containing Cyclodextrins. *J. Sep. Sci.* **2002**, *25*, 789–813.
- (10) Welton, T. Room-Temperature Ionic Liquids. Solvents for Synthesis and Catalysis. *Chem. Rev.* **1999**, *99*, 2071–2084.
- (11) Cui, Y.; Zhao, M.; Jiang, Z.; Xu, S.; Guo, X. Combined Use of Ionic Liquid and Hydroxypropyl- $\beta$ -Cyclodextrin for the Enantioseparation of Ten Drugs by Capillary Electrophoresis. *Chirality* **2013**, *25*, 409–414.
- (12) François, Y.; Varenne, A.; Juillerat, E.; Villemin, D.; Gareil, P. Evaluation of Chiral Ionic Liquids as Additives to Cyclodextrins for Enantiomeric Separations by Capillary Electrophoresis. *J. Chromatogr. A* **2007**, *1155*, 134–141.
- (13) Wang, B.; He, J.; Bianchi, V.; Shamsi, S. A. Combined Use of Chiral Ionic Liquid and Cyclodextrin for MEKC: Part I. Simultaneous Enantioseparation of Anionic Profens. *Electrophoresis* **2009**, *30*, 2812–2819.
- (14) Wang, B.; He, J.; Bianchi, V.; Shamsi, S. A. Combined Use of Chiral Ionic Liquid and CD for MEKC: Part II. Determination of Binding Constants. *Electrophoresis* **2009**, *30*, 2820–2828.
- (15) Zhou, Z.; Li, X.; Chen, X.; Hao, X. Synthesis of Ionic Liquids Functionalized  $\beta$ -Cyclodextrin-bonded Chiral Stationary Phases and

- 567 their Applications in High-Performance Liquid Chromatography. *Anal.*  
568 *Chim. Acta* **2010**, *678*, 208–214.
- 569 (16) Huang, K.; Zhang, X. T.; Armstrong, D. W. Ionic Cyclodextrins  
570 in Ionic Liquid Matrices as Chiral Stationary Phases for Gas  
571 Chromatography. *J. Chromatogr. A* **2010**, *1217*, 5261–5273.
- 572 (17) Amajjahe, S.; Chow, S.; Munteanu, M.; Ritter, H.  
573 Pseudopolyanions Based on Poly(NIPAAM-co- $\beta$ -CyclodextrinMetha-  
574 crylate) and Ionic Liquids. *Angew. Chem., Int. Ed.* **2008**, *47*, 3435–  
575 3437.
- 576 (18) Amajjahe, S.; Ritter, H. Supramolecular Controlled Pseudo-  
577 LCST Effects of Cyclodextrin-Complexed Poly(Ionic Liquids).  
578 *Macromolecules* **2008**, *41*, 3250–3253.
- 579 (19) Leclercq, L.; Schmitzer, A. R. Supramolecular Encapsulation of  
580 1,3-bis(1-adamantyl)imidazolium Chloride by  $\beta$ -Cyclodextrins: To-  
581 wards Inhibition of C(2)-H/D Exchange. *J. Phys. Org. Chem.* **2009**, *22*,  
582 91–95.
- 583 (20) Gonsior, N.; Hetzer, M.; Kulicke, W. M.; Ritter, H. First Studies  
584 on the Influence of Methylated  $\beta$ -Cyclodextrin on the Rheological  
585 Behavior of 1-Ethyl-3-methyl Imidazolium Acetate. *J. Phys. Chem. B*  
586 **2010**, *114*, 12468–12472.
- 587 (21) Araki, J.; Ito, K. Recent Advances in the Preparation of  
588 Cyclodextrin-based Polyrotaxanes and Their Applications to Soft  
589 Materials. *Soft Matter* **2007**, *3*, 1456–1473.
- 590 (22) Shen, X.; Chen, Q.; Zhang, J.; Fu, P. Chapter 19. Supra-  
591 molecular Structures in the Presence of Ionic Liquids. In *Ionic Liquids:*  
592 *Theory, Properties, New Approaches*; Kokorin, A., Ed.; InTech Europe:  
593 Rijeka, Croatia, 2011; pp 427–482.
- 594 (23) Gao, Y. A.; Li, Z. H.; Du, J. M.; Han, B. X.; Li, G. Z.; Hou, W.  
595 G.; Shen, D.; Zheng, L. Q.; Zhang, G. Y. Preparation and  
596 Characterization of Inclusion Complexes of  $\beta$ -Cyclodextrin with  
597 Ionic Liquid. *Chem.—Eur. J.* **2005**, *11*, 5875–5880.
- 598 (24) Gao, Y.; Zhao, X.; Dong, B.; Zheng, L.; Li, N.; Zhang, S.  
599 Inclusion Complexes of  $\beta$ -Cyclodextrin with Ionic Liquid Surfactants.  
600 *J. Phys. Chem. B* **2006**, *110*, 8576–8581.
- 601 (25) He, Y.; Chen, Q.; Xu, C.; Zhang, J.; Shen, X. Interaction  
602 between Ionic Liquids and  $\beta$ -Cyclodextrin: A Discussion of  
603 Association Pattern. *J. Phys. Chem. B* **2009**, *113*, 231–238.
- 604 (26) Zhang, J.; Shen, X. Multiple Equilibria Interaction Pattern  
605 between the Ionic Liquids  $C_{nm}mPF_6$  and  $\beta$ -Cyclodextrin in Aqueous  
606 Solutions. *J. Phys. Chem. B* **2011**, *115*, 11852–11861.
- 607 (27) Zhang, J.; Shi, J.; Shen, X. Further Understanding of the  
608 Multiple Equilibria Interaction Pattern between Ionic Liquid and  $\beta$ -  
609 Cyclodextrin. *J. Inclusion Phenom. Macrocyclic Chem.* **2014**, *79*, 319–  
610 327.
- 611 (28) François, Y.; Varenne, A.; Sirieix-Plenet, J.; Gareil, P.  
612 Determination of Aqueous Inclusion Complexation Constants and  
613 Stoichiometry of Alkyl(methyl)-methylimidazolium-based Ionic Liquid  
614 Cations and Neutral Cyclodextrins by Affinity Capillary Electro-  
615 phoresis. *J. Sep. Sci.* **2007**, *30*, 751–760.
- 616 (29) Ondo, D.; Tkadlecová, M.; Dohnal, V.; Rak, J.; Kvíčala, J.;  
617 Lehmann, J. K.; Heintz, A.; Ignatiev, N. Interaction of Ionic Liquids  
618 Ions with Natural Cyclodextrins. *J. Phys. Chem. B* **2011**, *115*, 10285–  
619 10297.
- 620 (30) Lipkowitz, K. Applications of Computational Chemistry to the  
621 Study of Cyclodextrins. *Chem. Rev.* **1998**, *98*, 1829–1873.
- 622 (31) Phillips, J. C.; Braun, R.; Wang, W.; Gumbart, J.; Tajkhorshid,  
623 E.; Villa, E.; Chipot, C.; Skeel, R. D.; Kale, L.; Schulten, K. Scalable  
624 Molecular Dynamics with NAMD. *J. Comput. Chem.* **2005**, *26*, 1781–  
625 1802.
- 626 (32) MacKerell, A. D., Jr.; Bashford, D.; Bellott, M.; Dunbrack, R. L.,  
627 Jr.; Evanseck, J. D.; Field, M. J.; Fischer, S.; Gao, J.; Guo, H.; Ha, S.;  
628 et al. All-Atom Empirical Potential for Molecular Modeling and  
629 Dynamics Studies of Proteins. *J. Phys. Chem. B* **1998**, *102*, 3586–3616.
- 630 (33) Liu, Z.; Huan, S.; Wang, W. A Refined Force Field for Molecular  
631 Simulation of Imidazolium-Based Ionic Liquids. *J. Phys. Chem. B* **2004**,  
632 *108*, 12978–12989.
- 633 (34) Jorgensen, W. L.; Chandrasekhar, J.; Madura, J.; Impey, R. W.;  
634 Klein, M. L. Comparison of Simple Potential Functions for Simulating  
635 Liquid Water. *J. Chem. Phys.* **1983**, *79*, 926–935.
- (35) Rodriguez, J.; Elola, M. D. Encapsulation of Small Ionic 636  
Molecules within  $\alpha$ -Cyclodextrins. *J. Phys. Chem. B* **2009**, *113*, 1423– 637  
1428.
- (36) Rodriguez, J.; Semino, R.; Laria, D. Building up Nanotubes: 638  
Docking of “Janus” Cyclodextrins in Solution. *J. Phys. Chem. B* **2009**, 639  
*113*, 1241–1244. 640
- (37) Rodriguez, J.; Elola, M. D.; Laria, D. Ionic Liquid Aqueous 641  
Solutions under Nanoconfinement. *J. Phys. Chem. C* **2012**, *116*, 5394– 642  
5400. 643
- (38) Elola, M. D.; Rodriguez, J. Structure and Dynamics of Nonionic 644  
Surfactants Adsorbed at Vacuum/Ionic Liquid Interfaces. *Langmuir* 645  
**2013**, *29*, 13379–13387. 646
- (39) Betzel, C.; Saenger, W.; Hingerty, B. E.; Brown, G. Topography 647  
of cyclodextrin inclusion complexes, part 20. Circular and flip-flop 648  
hydrogen bonding in  $\beta$ -cyclodextrin undecahydrate: a neutron 649  
diffraction study. *J. Am. Chem. Soc.* **1984**, *106*, 7545–7557. 650
- (40) Hwang, H.; Schatz, G. C.; Ratner, M. A. Steered Molecular 651  
Dynamics Studies of the Potential of Mean Force of a  $Na^+$  or  $K^+$  Ion in a 652  
Cyclic Peptide Nanotube. *J. Phys. Chem. B* **2006**, *110*, 26448–26460. 653
- (41) Darve, E.; Pohorille, A. Calculating Free Energies Using Average 654  
Force. *J. Chem. Phys.* **2001**, *115*, 9169–9183. 655
- (42) Hénin, J.; Chipot, C. Overcoming Free Energy Barriers Using 656  
Unconstrained Molecular Dynamics Simulations. *J. Chem. Phys.* **2004**, 657  
*121*, 2904–2914. 658
- (43) Rodriguez-Gomez, D.; Darve, E.; Pohorille, A. Assessing the 659  
Efficiency of Free Energy Calculation Methods. *J. Chem. Phys.* **2004**, 660  
*120*, 3563–3578. 661
- (44) Cai, W.; Sun, T.; Liu, P.; Chipot, C.; Shao, X. Inclusion 662  
Mechanism of Steroid Drugs into  $\beta$ -Cyclodextrins. Insights from Free 663  
Energy Calculations. *J. Phys. Chem. B* **2009**, *113*, 7836–7843. 664
- (45) Yu, Y.; Chipot, C.; Sun, T.; Shao, X. Spatial Arrangement of  $\alpha$ - 665  
Cyclodextrins in a Rotaxane. Insights from Free-Energy Calculations. *J.* 666  
*Phys. Chem. B* **2008**, *112*, 5268–5271. 667
- (46) Yu, Y.; Chipot, C.; Cai, W.; Shao, X. Molecular Dynamics Study 668  
of the Inclusion of Cholesterol into Cyclodextrins. *J. Phys. Chem. B* 669  
**2006**, *110*, 6372–6378. 670
- (47) He, J.; Chipot, C. J.; Shao, X.; Cai, W. Cyclodextrin-Mediated 671  
Recruitment and Delivery of Amphotericin B. *J. Phys. Chem. C* **2013**, 672  
*117*, 11750–11756. 673
- (48) See note added in proof: Dang, L. X.; Kollman, P. A. Free 674  
Energy of Association of the 18-Crown-6: $K^+$  Complex in Water: A 675  
Molecular Dynamics Simulation. *J. Am. Chem. Soc.* **1990**, *112*, 5716– 676  
5720. 677
- (49) Yoshimura, Y.; Takekiyo, T.; Imai, Y.; Abe, H. High Pressure 678  
Phase Behavior of Two Imidazolium-Based Ionic Liquids, [bmim]- 679  
[BF4] and [bmim][PF6]. In *Ionic Liquids—Classes and Properties*; 680  
Handy, S. T., Ed.; InTech Europe.: Rijeka, Croatia, 2011; pp 171–186. 681
- (50) Uematsu, M.; Franck, E. U. Static Dielectric Constant of Water 682  
and Steam. *J. Phys. Chem. Ref. Data* **1980**, *9*, 1291–1306. 683
- (51) Chowdhary, J.; Ladanyi, B. M. Hydrogen Bond Dynamics at the 684  
Water/Hydrocarbon Interface. *J. Phys. Chem. B* **113**, *13*, 4045–4053. 685