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# Modeling the High-brightness State of the Recurrent Nova T CrB as an Enhanced Masstransfer Event

Wagner Schlindwein 1,2 , Raymundo Baptista , and Gerardo Juan Manuel Luna 4,5 

¹ Instituto Nacional de Pesquisas Espaciais, Avenida dos Astronautas, 1758, São José dos Campos-SP, Brazil; wagner.schlindwein@astro.ufsc.br

² Departamento de Física, Universidade Estadual de Maringá, Avenida Colombo, 5790, Maringá-PR, Brazil

³ Departamento de Física, Universidade Federal de Santa Catarina, Campus Trindade, Florianópolis-SC, Brazil

⁴ Universidad Nacional de Hurlingham (UNAHUR). Laboratorio de Investigación y Desarrollo Experimental en Computación, Avenida Gobernador Vergara 2222,

Villa Tesei, Buenos Aires, Argentina

<sup>5</sup> Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET), Argentina Received 2024 October 21; revised 2025 May 23; accepted 2025 June 4; published 2025 August 5

#### **Abstract**

T Coronae Borealis is the nearest symbiotic recurrent nova. Twice in the last two centuries, in 1866 and 1946, the accreted material ignited on the surface of the white dwarf via runaway thermonuclear fusion reactions and produced a nova eruption. Both eruptions occurred approximately midway through a transient state of high luminosity. A possible explanation of such a state is a dwarf-nova-like outburst, which may arise from a transient increase in the mass-transfer rate of the donor star. We simulate the response of an accretion disk to an event of enhanced mass-transfer that is "interrupted" by a pre-eruption dip associated with the convective phase leading to the thermonuclear runaway. We model the resulting optical light curve using the parameters of the T CrB binary. Our model represents the first attempt to reproduce the transient high-accretion state. The observed brightening can be satisfactorily reproduced by models of an accretion disk with a viscosity parameter  $\alpha = 3$ , an event of enhanced mass-transfer with a duration of  $\Delta t = 15 \, \mathrm{yr}$ , and quiescent and high-state mass-transfer rates of  $2.0 \times 10^{-9} \, M_{\odot} \, \mathrm{yr}^{-1}$  and  $1.9 \times 10^{-7} \, M_{\odot} \, \mathrm{yr}^{-1}$ , respectively, while the pre-eruption dip can be reproduced by the small, accelerated expansion of the inner disk's radius, at an average velocity of  $0.02 \, \mathrm{km \, s^{-1}}$ . Our model is also capable of reproducing the observed changes in color of T CrB throughout the transient event.

*Unified Astronomy Thesaurus concepts:* Stellar accretion disks (1579); Symbiotic binary stars (1674); Recurrent novae (1366); Astronomical simulations (1857); Interacting binary stars (801)

# 1. Introduction

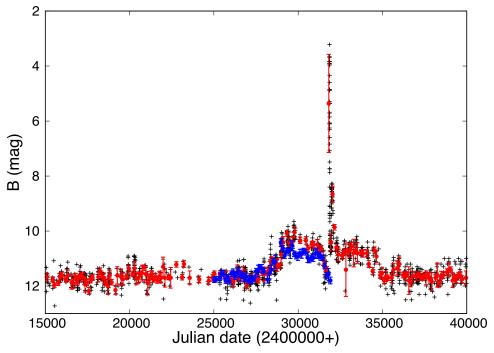
T Coronae Borealis (T CrB) is the nearest symbiotic recurrent nova, at a distance of 916 pc (Gaia Collaboration et al. 2016, 2023). The system contains an M4 III giant (RG, R. Zamanov et al. 2023), which fills its Roche lobe and transfers mass to a massive white dwarf (WD) with  $M_1 \geqslant 1.1 M_{\odot}$  (K. Belczynski & J. Mikolajewska 1998; M. M. Shara et al. 2018; I. Hachisu & M. Kato 2019). This transferred mass forms an accretion disk around the WD with a size of  $89 \pm 19 \, R_{\odot}$  (R. K. Zamanov et al. 2024b). Its two well-recorded outbursts in 1866 and 1946, together with historical eruptions in 1217 and 1787, support a recurrence time of roughly 80 yr (B. E. Schaefer 2023a). During these occasions, the accreted material ignited on the surface of the WD through runaway thermonuclear fusion reactions and produced a nova eruption.

Approximately eight years before the 1866 and 1946 eruptions, the optical brightness of T CrB increased by about 1.5 mag in the *B* band and stayed at that level until about 8 months before the nova eruption. In fact, by studying the years before and after both previous thermonuclear runaways (TNRs), B. E. Schaefer (2010, 2023a) found that T CrB brightening started about 8 yr *before* the eruption and lasted through about 7 yr *after* the eruption, being interrupted for about 1 yr *before* the eruption when the brightness returned to quiescent values (this phase has now been coined as the pre-eruption dip) and 1 yr

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after the eruption until returning to quiescence (see Figure 23 in B. E. Schaefer 2010). From late 2014 until 2022 December, T CrB was in a brightness akin to the similar brightening state that then started to fade and reached a brightness similar to its quiescence level in 2023 October (U. Munari 2023a; R. Zamanov et al. 2023). Figure 1 shows the recent optical behavior of T CrB, overlaid on the light curve from around the time of the 1946 eruption but shifted by -78 yr. The alignment between both light curves is remarkable and most likely the current high-accretion state will lead to the next nova eruption, as it did in the two previous eruptions. A comparison between current and previous brightness behavior has allowed different authors to predict that the next nova eruption will occur within  $2025 \pm 2$  yr (B. E. Schaefer 2019; G. J. M. Luna et al. 2020; R. Zamanov et al. 2023).

There is mounting evidence that this increase in brightness is due to an increase in the accretion rate (G. J. M. Luna et al. 2018; K. Iłkiewicz et al. 2023; B. E. Schaefer 2023a). UV observations during the low-accretion state allowed us to derive accretion rates of  $\dot{M}_{\rm low}=2.0\times10^{-9}\,M_{\odot}\,{\rm yr}^{-1}$  (P. L. Selvelli et al. 1992; V. Stanishev et al. 2004). From the analysis of XMM-Newton observations taken a few months after the start of this state, known as the superactive state after U. Munari et al. (2016), G. J. M. Luna et al. (2018) found a new super-soft component in the X-ray spectrum with a luminosity too low to be due to nuclear burning on the WD's surface, but consistent with the optically thick emission from the boundary layer of the accretion disk, and estimated a lower limit to the accretion rate during the high-brightness state of  $8.5\times10^{-8}\,M_{\odot}\,{\rm yr}^{-1}$ . In addition, the spectroscopic analysis of



**Figure 1.** *B*-magnitude light curves of T CrB during the 1938–1955 brightening state, including the 1946 TNR (black crosses). We include the AAVSO data from the 2004 until 2024 April—brightening state shifted by –78 yr and with a 113 days median filter (blue dots with error bars). The same filter is used for the historical data (red dots with error bars).

the recent high-brightness state by L. Planquart et al. (2025) demonstrates that this state correlates with the bright spot enhancement, and that the increase in bright spot luminosity must originate from either a decrease in the outer disk's radius or an increase in the mass-transfer rate.

Given the recurrent nova nature of T CrB, the ignition of the following nova eruption requires the previous accumulation of a hydrogen-rich envelope of accreted matter,  $M_{\rm ig}$ , onto its WD's surface (e.g., M. Y. Fujimoto 1982; K. J. Shen & L. Bildsten 2009; W. M. Wolf et al. 2013).  $M_{\rm ig}$  depends on  $M_{\rm 1}$  and on the WD mass-accretion rate (as well as on chemical composition, see K. J. Shen & L. Bildsten 2009). A larger WD mass leads to higher accreted envelope temperatures and densities, which allows for the ignition conditions to be reached at lower envelope masses, whereas higher accretion rates lead to higher compressional heating, also resulting in ignition occurring at lower envelope masses.

In the case of T CrB, the envelope mass required to trigger a nova eruption onto a WD of mass  $M_1 = 1.3 M_{\odot}$  fed by a solar composition gas at a quiescent accretion rate of  $2 \times 10^{-9} M_{\odot} \text{ yr}^{-1}$ is  $M_{\rm ig} \simeq 1.1 \times 10^{-5} \, M_{\odot}$  (K. J. Shen & L. Bildsten 2009). The timescale required to accumulate this envelope mass at the quiescent accretion rate is \$\simes 5480\, yr\$, almost two orders of magnitude longer than the observed  $\approx$ 80 yr recurrence time. This implies that there must be a phase of significantly enhanced mass accretion that reduces  $M_{ig}$  and shortens the timescale required to trigger the nova eruption down to the observed recurrence time. Indeed, at a higher mass-accretion rate of  $\simeq 1.7 \times 10^{-7} M_{\odot} \,\mathrm{yr}^{-1}$ the required envelope mass is reduced to  $M_{\rm ig} \simeq 2.6 \times 10^{-6} M_{\odot}$ and the ignition conditions can be reached after only  $\simeq$ 15 yr, which is in good agreement with the full length of the highbrightness state. This reasoning suggests that a high massaccretion phase is key to explain the timings and recurrent nova behavior of T CrB, and sets the motivation for this paper.

Here, we model the observed high-brightness state as an event of enhanced mass-transfer rate from the RG, with the additional requirement that the matter accreted over a time length of  $(80\pm2)$  yr equals the required envelope mass needed to trigger nova eruptions at the observed recurrence interval. The data are described in Section 2. The details of the model and its results are presented in Section 3. The results are discussed in Section 4 and a summary of our conclusions is presented in Section 5.

### 2. Observations

In modeling, we used the historical data set of T CrB compiled by B. E. Schaefer (2023b) that cover the brightness state before and after the 1946 nova eruption, and *BVRI*-band observations from the archive of the American Association of Variable Star Observers (AAVSO) from 2004 until 2024 April. In Figure 1, the historical light curve is shown as black crosses. In order to retain only the long-term trend, we smoothed the historical and AAVSO light curves by applying a median filter with a width of 113 days (half orbital period; red and blue points with error bars in Figure 1, respectively). The historical data include both the brightening that started around 1938 and the nova eruption that occurred in 1946, while the AAVSO data include the current brightening event and were shifted by –78 yr to match the start of the current brightening with that of the 1938 event.

Before the start of its recent high-accretion state, T CrB had average low-accretion state magnitudes of  $B = 11.67 \pm 0.10$  mag,  $V = 10.17 \pm 0.07$  mag,  $R = 9.04 \pm 0.10$  mag, and  $I = 7.52 \pm 0.06$  mag. It is worth noting that we consider the entire period of high-accretion before and after the nova eruption as a single transient, and that the brightness decrease prior to the eruption is caused by another phenomenon (see discussion in Section 4).

#### 3. Model and Results

The 1946 nova eruption occurred during a transient high-accretion state (see Figure 1). A natural explanation for this state is a dwarf-nova-like outburst, where a possible origin of the increase in the accretion rate is an instability in the mass-transfer rate from the donor star leading to an event of mass-transfer increase (mass-transfer instability model, MTIM; G. T. Bath 1972, 1975; G. T. Bath & J. E. Pringle 1981).

MTIM assumes that dwarf nova outbursts are the response of a disk with constant (and high) viscosity to a sudden increase in the mass-transfer rate ( $M_2$ ). Therefore, to model the high-accretion state of T CrB, a high-viscosity is required for a quick response of its accretion disk to the event of enhanced mass-transfer.

We simulate the response of the accretion disk to events of enhanced mass-transfer, in the context of the MTIM, to model the optical light curve of T CrB. We assume the viscosity parameter  $\alpha^6$  to be constant, with a high value ( $\geqslant 1$ ). The reader is referred to W. Schlindwein & R. Baptista (2024) for further details of the calculation of the time evolution of the accretion disk, and to R. Baptista & W. Schlindwein (2022) and W. Schlindwein & R. Baptista (2024) for a discussion of the plausibility of  $\alpha \ge 1$  and its implications. Since we are interested in modeling only the luminosity of the disk, we assume that matter is deposited at its outer edge, uniformly over a radial extent of  $\Delta R = 0.1 R_d$ , where  $R_d$  is the outer disk's radius. We adopted  $\mu = 0.615$  (suitable for a solar abundance of fully ionized gases) and a tidal truncation constant of  $c\omega = 0.01 \text{ rad s}^{-1}$  (Equation (5) from S. Ichikawa & Y. Osaki 1992) which corresponds to a quiescent disk radius of  $R_d \sim 0.74 R_{L_1}$  (where  $R_{L_1}$  is the distance from the WD to the inner Lagrangian point  $L_1$ ), consistent with the value inferred by R. K. Zamanov et al. (2024b). As discussed in Section 2.2 of W. Schlindwein & R. Baptista (2024), since the brightness level during the high-accretion state presents a plateau during maximum (Figure 1), it is appropriate for us to adopt an enhanced mass event with the shape described by:

$$\dot{M}_2 = \dot{M}_2^q + (\dot{M}_2^h - \dot{M}_2^q) \exp\left[-\frac{1}{2} \left(\frac{t - t_e}{b \, \Delta t_e}\right)^n\right],$$
 (1)

where  $\dot{M}_2^q$ ,  $\dot{M}_2^h$ ,  $t_e$ , and  $\Delta t_e$  are the quiescent and high-accretion state mass-transfer rates, the event center instant, and its full width at half-maximum (FWHM), respectively. The addition of the parameter n (which must be even) in the exponent of the exponential argument is used to adjust the plateau of the enhanced mass-transfer event and, as a consequence of this parameter, a term  $b = [2(2 \ln 2)^{1/n}]^{-1}$  was added to ensure that  $\Delta t_e$  is the FWHM. We considered that the disk emits locally as a blackbody. The resulting spectra were convolved with the BVRI passband responses to derive the corresponding magnitudes.

Since the RG contributes significantly to the total luminosity of the system, a good estimate of its magnitudes and variations becomes important for the results of the model. For the V passband, the linear term of the ellipsoidal variability of R. Zamanov et al. (2023) is  $V_{\rm RG} = 10.16$  mag. For the other

Table 1
T CrB Adopted Binary Parameters and Fitted Model Parameters

Parameters	Model I	Model II
(1)	(2)	(3)
Orbital period	5461.65 hr <sup>a</sup>	
$M_1$	$1.37  M_{\odot}^{b}$	$1.29~M_{\odot}$
$R_1$	$0.003~R_{\odot}$	$0.0045~R_{\odot}$
$M_2$	$1.12M_{\odot}^{\ \ b}$	$0.70M_\odot$
$R_2$	$76.5~R_{\odot}$	$64.3R_{\odot}$
Inclination (i)	67° <sup>b</sup>	57 <sup>°</sup> .3
Mass ratio $(q)$	0.82 <sup>b</sup>	0.54
Binary separation (a)	$211.5~R_{\odot}$	$196.2R_{\odot}$
$R_{L_1}$	$110.0~R_{\odot}$	$110.1~R_{\odot}$
$\mu$	0.615	
Distance	916 pc <sup>c</sup>	
$T_2^B$	2967 K	3065 K
$T_2^V$	2910 K	3029 K
$egin{aligned} T_2^B \ T_2^V \ T_2^R \end{aligned}$	2914 K	3056 K
$T_2^I$	3080 K	3277 K
$\eta$	0.6	
$\dot{M}_2$ in quiescence $(\dot{M}_2^q)$	$2.0 \times 10^{-9}  M_{\odot}  \mathrm{yr}^{-1d}$	
$\dot{M}_2$ during event maximum $(\dot{M}_2^h)$	$1.7 \times 10^{-7}  M_{\odot}  \mathrm{yr}^{-1}$	$1.9 \times 10^{-7}  M_{\odot}  \mathrm{yr}^{-1}$
Viscosity parameter ( $\alpha$ )	3.0	
Event duration $(\Delta t_e)$	15 yr	
Plateau parameter (n)	8	

#### Notes.

passbands, we assume an M4 III spectral type for the RG (R. Zamanov et al. 2023) and adopt color indexes of B - V = 1.55 mag, V - R = 1.17 mag and V - I = 2.69 mag (L. H. Aller et al. 1996). The RG is thus by far the dominant light source in the V, R, and I passbands during the lowaccretion state, with  $B_{RG} = 11.71 \text{ mag}$ ,  $R_{RG} = 8.99 \text{ mag}$ , and  $I_{RG} = 7.47$  mag. In order to take the irradiation effect of the accretion luminosity onto the RG into account, we use the irradiation model of J. M. Hameury et al. (2020), adopting the albedo  $\eta = 0.6$ . Their model requires the assumption of an (irradiation free) effective temperature  $T_2$  for the irradiated star. However, the spectrum of the RG is far from that of a blackbody and it is not possible to represent its BVRI magnitudes with a single effective temperature. Therefore, for each passband, we adopted a  $T_2$  value which matches the observed RG brightness at that passband (see Table 1).

U. Munari et al. (2016) used the T CrB IR light curves to infer a temperature increase of the RG heated side at the high-brightness state of  $\sim\!80\,\mathrm{K}$ , or about a 2% increase in comparison to the unirradiated side, implying an irradiating flux of  $\sim\!8\%$  of the intrinsic stellar flux. Using the J. M. Hameury et al. (2020) model to compute the irradiation effect, we find that irradiation by the accretion luminosity increases the surface temperature of the RG heated side by  $\sim\!1\,\mathrm{K}$  and  $\sim\!100\,\mathrm{K}$  in quiescence and in the high-brightness state, respectively, resulting in an RG  $\sim\!0.10\,\mathrm{mag}$  brighter in the *I* passband during the high-brightness state—in good agreement with the brightness increase inferred by U. Munari et al. (2016).

<sup>&</sup>lt;sup>6</sup> The solution is known as the steady α-disk model and is obtained by adopting the prescription of N. I. Shakura & R. A. Sunyaev (1973),  $\nu = \alpha c_s H$ , where α is a dimensionless parameter,  $c_s$  is the speed of sound, and H is the disk's vertical scale height.

<sup>&</sup>lt;sup>a</sup> F. C. Fekel et al. (2000).

<sup>&</sup>lt;sup>b</sup> V. Stanishev et al. (2004).

<sup>&</sup>lt;sup>c</sup> Gaia Collaboration et al. (2023).

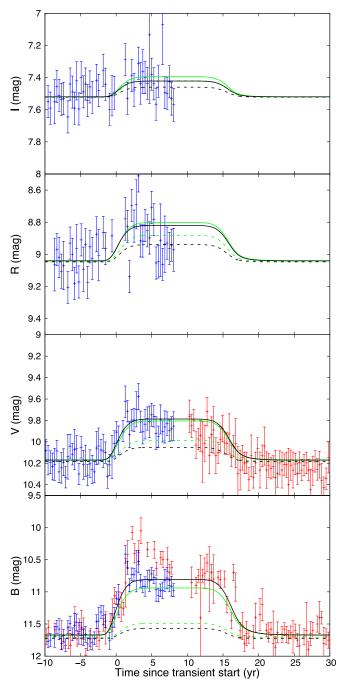
<sup>&</sup>lt;sup>d</sup> P. L. Selvelli et al. (1992), V. Stanishev et al. (2004).

The parameters adopted for our model I simulation are listed in Table 1. The contribution of the WD emission to the BVRI passbands is considered negligible. Interstellar extinction effects were included; we assumed the extinction law of J. A. Cardelli et al. (1989) and adopted E(B-V) =  $0.056 \pm 0.003 \,\mathrm{mag \, kpc^{-1}}$  (E. F. Schlafly & D. P. Finkbeiner 2011). The  $t_e$  and  $\Delta t_e$  values are inferred directly from the historical light curve (Figure 1), while the values of  $\dot{M}_{2}^{q}$  and  $T_{2}$ are obtained by fitting the low-accretion BVRI brightness level. Accordingly, we confirm that the  $\dot{M}_{low}$  value of G. J. M. Luna et al. (2018) (derived from a mean between values from P. L. Selvelli et al. 1992 and V. Stanishev et al. 2004) provides a good description of the T CrB quiescent brightness level. The remaining model parameters were fitted through a set of reduced simulations optimized for this purpose.  $\alpha \geqslant 1$  are required in order to match the observed transient decline timescale in T CrB, whereas for  $\alpha > 3$  the differences in the decline rate are small compared to the uncertainties of the data.

The best-fit *BVRI* light curves corresponding to model I are shown in Figure 2. Note that these light curves are the sum of the brightness of the simulated accretion disk plus the contribution from the irradiated RG companion. The high-accretion state is dominated directly by the accretion disk outburst in the *B* and *V* passbands, but by the resulting RG irradiation effects in the *R* and *I* passbands. The inferred accretion rate during the high-accretion state is  $1.7 \times 10^{-7} M_{\odot} \, \text{yr}^{-1}$ , twice the lower limit derived by G. J. M. Luna et al. (2018).

For a WD of mass  $1.37\,M_\odot$ , the mass of the accreted envelope required for a nova eruption ignition is  $M_{\rm ig} \simeq 10^{-6}\,M_\odot$  for accretion rates  $\simeq 7 \times 10^{-8}\,M_\odot$  yr<sup>-1</sup> (K. J. Shen & L. Bildsten 2009). Considering that the recurrence time of the nova eruption in T CrB is  $\sim 80$  yr, that for about 15 yr the system is in a high-accretion rate state, and that for the remainder of the time it is in a quiescent state accreting at a rate of  $2.0 \times 10^{-9}\,M_\odot$  yr<sup>-1</sup>, the accretion rate required at the high-accretion state is  $\simeq 5.8 \times 10^{-8}\,M_\odot$  yr<sup>-1</sup>. This upper limit is  $\sim 3\times$  smaller than inferred by model I and would result in the system being  $\sim 0.2$  mag fainter than model I in the V passband during the high-accretion state, with the accretion disk and the RG being, respectively,  $\sim 0.75$  mag and  $\sim 0.13$  fainter than in model I. The WD mass in T CrB is quite uncertain, and this discrepancy suggests that the WD mass choice for model I might be overestimated, prompting us to obtain additional constraints on  $M_1$ .

A diagram of the high-accretion state mass-transfer rate  $\dot{M}_{2}^{h}$ required to reach the corresponding  $M_{ig}$  value at the end of the recurrence interval is plotted as a function of WD mass in Figure 3. The relationship  $M(M_1)$  was estimated using the curves from K. J. Shen & L. Bildsten (2009), assuming a value of  $80 \pm 2$  yr for the nova eruption recurrence interval, a time spent in the high-accretion rate state of  $14 \pm 1$  yr, and the quiescence accretion rate of  $2.0 \times 10^{-9} M_{\odot} \, \text{yr}^{-1}$  (G. J. M. Luna et al. 2018). The limit above which steady nuclear burning occurs, i.e., there are no longer recurrent nova eruptions, comes from the expression  $\dot{M}(\text{crit}) \approx 2.3 \times 10^{-7} (M_1/M_{\odot} - 0.19)^{3/2} M_{\odot} \text{ yr}^{-1}$ (B. Warner 1995). The lower limit for  $\dot{M}$  comes from G. J. M. Luna et al. (2018). Consistent model solutions are along the solid line; solutions below and to the left (above and to the right) of this line imply recurrence intervals longer (shorter) than 80 yr. With this constraint in mind, the range of possibilities for  $M_1$  becomes reasonably narrow, between 1.27 and 1.35  $M_{\odot}$ . Lower  $M_1$  values put the system in the steady nuclear burning



**Figure 2.** Simulation results with model I (green solid curve) and model II (black solid curve) parameters. The points with error bars are the same as in Figure 1 for *B* band and analogous for the other bands. The green and black dashed curves are the contribution from the irradiated red giant companion to models I and II, respectively.

region with no recurrent nova events, while higher  $M_1$  values lead to nova recurrence intervals shorter than observed. Thus, the  $M_1 = 1.37 \, M_{\odot}$  and  $\dot{M}_2^h = 1.7 \times 10^{-7} \, M_{\odot} \, \mathrm{yr}^{-1}$  solution of model I is not self-consistent because it implies a recurrence interval shorter than observed.

Aside from the WD mass, the inclination is another poorly constrained binary parameter which significantly influences the results of the T CrB simulations. Tests were conducted with the intent of characterizing the effects of  $M_1$  and i in the T CrB simulations. A smaller primary mass implies a fainter accretion disk while the irradiation effect decreases, since  $T_{2,\text{irr}}$ 

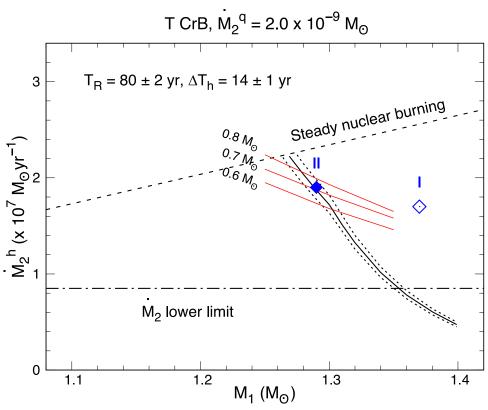


Figure 3. Diagram of accretion rate vs. WD mass for T CrB. The upper black dashed line represents the limit above which steady nuclear burning occurs. The lower limit in  $\dot{M}$  (from G. J. M. Luna et al. 2018) is indicated by the black dashed–dotted line. The black solid and dotted lines mark the relationship  $\dot{M}$  ( $M_1$ ) from the envelope mass that produces a nova eruption, where  $T_R = 80 \pm 2$  yr is the assumed value of the nova eruption recurrence interval, and  $\Delta T_h = 14 \pm 1$  yr is the time spent in the high-accretion state. The red solid lines indicate the relationship  $\dot{M}$  ( $M_1$ ) adopting  $M_2 = 0.6$ , 0.7, and 0.8  $M_{\odot}$  in the T CrB primary mass function of F. C. Fekel et al. (2000). Open and filled blue diamonds mark the solutions for models I and II, respectively.

depends on  $M_1^{0.25}$  and  $R_1^{-0.25}$ . On the other hand, a smaller inclination implies that the apparent disk brightness increases while the irradiation effect remains unchanged. Therefore, with a less massive WD, a higher mass-transfer rate is required to describe the transient; whereas with a smaller inclination, a lower rate is necessary.

We can use Figure 3 as a guide to estimate not only  $M_1$  but also the inclination of T CrB with a relatively small uncertainty range. To obtain the binary parameter set for this test, we adopted the T CrB primary mass function of F. C. Fekel et al. (2000), where the other model parameters  $(q, a, R_{L_1}, R_2, T_2)$  were modified to be consistent with the new values of  $M_1$  and i. With this constraint, the binary inclination must be in the range  $45^{\circ} \lesssim i \lesssim 70^{\circ}$  because the system is noneclipsing.

This exercise leads to model II, with  $M_1 = 1.29 \, M_\odot$ ,  $i = 57^{\circ}.3$ , and a best-fit mass-accretion rate at the high-accretion state of  $\dot{M}_2^h = 1.9 \times 10^{-7} \, M_\odot \, \mathrm{yr}^{-1}$ . The parameters adopted for the model II simulation are listed in Table 1, and its position is marked as a blue filled diamond in Figure 3. It results in a quiescent disk radius of  $R_d \sim 0.70 \, R_{L_1}$  (in good agreement with the value inferred by R. K. Zamanov et al. 2024b), while the irradiation by the accretion luminosity increases the surface temperature of the RG heated side by  $\sim 0.5 \, \mathrm{K}$  and  $\sim 70 \, \mathrm{K}$  in quiescence and in the high-accretion state, respectively, resulting in an RG  $\sim 0.06 \, \mathrm{mag}$  brighter in the I passband during the high-accretion state. The major contribution to the high-accretion state in model II comes from the accretion disk outburst even in the I passband. Since in

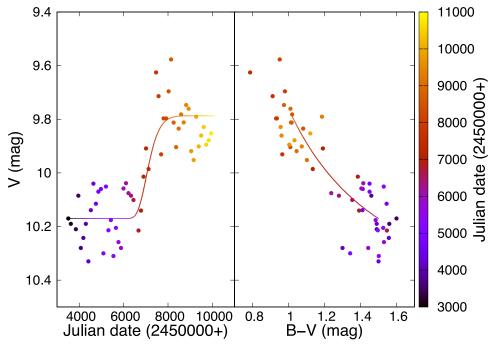
model II the radius of the RG is considerably smaller, larger  $T_2$  values are required in order to obtain the same observed flux.

The best-fit BVRI light curves corresponding to model II are shown in Figure 2. Model II provides a better description of the observations than model I, while consistently falling onto the  $\dot{M}(M_1)$  relationship of Figure 3. Model II is bluer than model I. This is due to the fact that the amplitude of the RG irradiation effect is smaller in this model, thus requiring a more pronounced modulation of the brightness of the accretion disk.

Figure 4 shows the smoothed version of the AAVSO V-passband light curve and the corresponding color–magnitude diagram. The statistical uncertainties of the (B-V) color are typically around 0.18 mag. In quiescence,  $(B-V) \simeq 1.5$ ; T CrB becomes bluer during the high-accretion state, with a  $(B-V) \simeq 1.0$ . The predicted color variations of model II are shown as a solid line in the right-hand panel of Figure 4, and provide a good description of the observed color variations for the rise to the high-accretion state.

A. Schwarzenberg-Czerny (1981) shows that chromospheric emission is relevant for accretion rates  $\dot{M} > 10^{-8}\,M_\odot\,{\rm yr}^{-1}$ , such as those inferred for the high-accretion state of T CrB, with a predicted increase in V-passband brightness by  $\sim 0.2$  mag for an accretion disk with  $\dot{M} = 10^{-7}\,M_\odot\,{\rm yr}^{-1}$  and  $i = 60^\circ$ . While the inclusion of chromospheric emission is beyond the scope of the present paper, one might expect it would allow for a best-fit model with lower  $\dot{M}_2^h$  value and corresponding larger  $M_1$  and i values.

It is worth noting that the shape of the enhanced mass event is simple, set by one  $\dot{M}_2$  value during quiescence and another



**Figure 4.** Left-hand: T CrB light curve in the V band. Right-hand: Color variations across the most recent high-accretion state of T CrB. The dots are the AAVSO data and the solid line is the result of the simulations of model II, while the color-coding represents the time.

in the high-accretion state; these values should correspond to an average  $\dot{M}_2$  over the period. In the real case, the event is expected to show fluctuations and morphologies throughout the transient.

#### 4. Discussion

### 4.1. Are there Alternative Explanations for the Highbrightness State?

Here, we address two alternative explanations for the 15 yr long high-brightness state of T CrB, namely whether it could be the consequence of a dwarf nova outburst powered by the thermal-viscous disk instability or the result of a steady nuclear burning phase at the WD's surface.

The disk-instability model (DIM) assumes that matter accumulates in a low-viscosity disk ( $\alpha_c \sim 0.01$ ) during quiescence, with gas temperature and surface density  $\Sigma$  progressively increasing everywhere, until a critical surface density is reached at some radius, bringing the disk into a higher viscosity ( $\alpha_h \sim 0.1-0.2$ ) regime where the accumulated matter quickly accretes onto the WD (e.g., J.-P. Lasota 2001). The mass-transfer rate,  $\dot{M}_2$ , remains constant during the whole outburst cycle. For the case of T CrB, we may estimate  $\dot{M}_2$  from the envelope mass that needs to accumulate onto the WD's surface in order to trigger the next nova eruption and from the recurrent nova timescale,

$$\dot{M}_2(\text{DIM}) = \frac{M_{\text{ig}}}{T_R} = \frac{2.57 \times 10^{-6} M_{\odot}}{80 \text{ yr}}$$
$$= 3.2 \times 10^{-8} M_{\odot} \text{ yr}^{-1}. \tag{2}$$

In this scenario,  $\dot{M}_{\rm low}=2\times10^{-9}\,M_{\odot}\,{\rm yr}^{-1}$  becomes the residual mass accretion onto the WD in quiescence. Accordingly,  $\dot{M}_{\rm low}\ll\dot{M}_2$ , and the effective rate at which matter accumulates in the disk is  $\dot{M}_{\rm accum}=\dot{M}_2-\dot{M}_{\rm low}=3\times10^{-8}\,M_{\odot}\,{\rm yr}^{-1}$ . Over a quiescence interval of  $T_q=(65\pm3)\,{\rm yr}$ , the disk accumulates a mass of  $\Delta M_{\rm disk}=(1.95\pm0.09)\times10^{-6}M_{\odot}$ . For an outburst

mass-accretion rate of  $\dot{M}_{\rm out} = \dot{M}_2^h = 1.9 \times 10^{-7} \, M_{\odot} \, {\rm yr}^{-1}$ , it takes  $T_{\rm out} = (10.3 \pm 0.5) \, {\rm yr}$  to dump the accumulated matter onto the WD. This predicted DIM outburst duration is significantly shorter than the overall length of the high-brightness state at the  $5\sigma$  confidence level, indicating that not enough mass could be accumulated in the accretion disk during the quiescence period to sustain a DIM outburst for the observed duration.

On the other hand, the nova eruption occurs roughly halfway through the high-brightness state phase, probably ejecting not only the WD envelope mass but also the whole accretion disk mass in the process. Given that the highbrightness state resumes after the end of the T CrB nova eruption, this poses a double problem for the DIM scenario. First, it is hard to explain how a critical surface density condition which takes about 65 yr to occur previous to the nova eruption can repeat itself right after the short nova eruption. Second, the maximum amount of disk mass that could accumulate after the disk's disruption (assuming that the disk starts refilling just after nova maximum) would account for an outburst duration (at the  $\dot{M}_{\rm out}$  rate) of  $\leq 60$  days, two orders of magnitude shorter than the observed 7 yr length of the high-brightness state after the nova eruption. This makes the DIM scenario a nonviable explanation for the highbrightness state in T CrB.

The alternative explanation of the high-brightness state as the consequence of a steady nuclear burning phase at the WD's surface also has several problems. First, in order for steady nuclear burning to occur at the surface of a  $M_1 = 1.29 \, M_{\odot}$  WD, the mass-accretion rate needs to be  $\dot{M}_{\rm burn} \geq 2.3 \times 10^{-7} \, M_{\odot} \, {\rm yr}^{-1}$  (see Figure 3),  $\geq 20\%$  larger than inferred from the modeling of the observations. The resulting amplitude of the high-brightness state as well as the magnitude of the irradiation effect would be systematically larger than observed. Second, the predicted luminosity from steady H-burning at the surface of a  $M_1 = 1.29 \, M_{\odot}$  WD is  $L_{\rm nuc} \simeq 24 \times 10^3 \, L_{\odot}$  (W. M. Wolf et al. 2013), which is a factor of  $\simeq 30$  larger than the inferred

luminosity of the accretion disk at the high-brightness state,  $L_{\rm disk} = 8.3 \times 10^2 L_{\odot}$ , implying that T CrB should be  $\simeq 3.7 \, {\rm mag}$ brighter than observed in the blue. Third, the strong variability observed in soft X-ray observations during the high-brightness state as well as the inferred small area of the corresponding blackbody emitting region derived from spectral modeling indicates that this emission is not powered by H-burning at the WD's surface (G. J. M. Luna et al. 2018). Fourth, there would be no explanation for why the mass-accretion rate suddenly increases by a factor  $\simeq 100$  from  $\dot{M}_{low}$  to  $\dot{M}_{burn}$  some 8 yr before the nova eruption and why would it go back to  $\dot{M}_{low}$  about 7 yr after the nova eruption (other than assuming it is an enhanced mass-transfer event from the RG). Finally, the transition between the steady and unsteady nuclear burning regimes is very sharp, making these two possibilities mutually excludent (B. Paczynski 1983; W. M. Wolf et al. 2013). Steady nuclear burning consumes the hydrogen-rich envelope mass while removing the envelope degeneracy essential for the TNR, thereby preventing a nova eruption to occur while the system is in a steady H-burning phase —whereas in T CrB the nova eruption is superimposed on the high-brightness state. All these discrepancies make the steady nuclear burning scenario also a nonviable explanation for the high-brightness state in T CrB.

### 4.2. The High-brightness State and the Nova Eruption

The basic hypothesis of our modeling is that the high-brightness state is a unique event that starts 8 yr before and lasts until 7 yr after the T CrB nova eruption, and that the decline in brightness observed  $\simeq 1$  yr before the eruption (the "pre-eruption dip," B. E. Schaefer et al. 2023) is part of the eruption itself (see next section).

During the nova event, the accretion disk is probably ejected together with the envelope accumulated onto the WD's surface. At an expansion velocity of  $\simeq 4000 \, \mathrm{km \, s^{-1}}$  (D. B. Mclaughlin 1946; R. F. Sanford 1946), the ejecta have expanded beyond the binary less than a day after the onset of the eruption. From this moment onwards, the RG is presumably able to restore mass transfer at the high-accretion rate,  $\dot{M}_2^h$ , and to re-establish the accretion disk on a timescale of  $\leqslant 400$  days. This is a higher limit to the timescale for the system to return to the previous high-brightness state because irradiation of the RG by the hot and extended primary may temporarily increase the mass-transfer rate beyond  $\dot{M}_2^h$  and accelerate the re-establishment of the accretion disk.

The characteristics of the T CrB nova eruption (e.g., B. E. Schaefer 2010) are reminiscent of those observed in DQ Her (D. B. McLaughlin 1960; B. Warner 1995) and FH Ser (M. F. Bode 1982), where the initial decline is interrupted by a transition phase (marked by a deep minimum of amplitude ≥4 mag and duration of 2–3 months), followed by a brightness increase and recovery of the previous decline rate (leading to a secondary maximum). In FH Ser, the brightness minimum coincides with an excess IR emission, indicating that the visual minimum is caused by the formation of absorbing dust grains that reradiate the intercepted energy in the IR while the bolometric luminosity remains constant (M. F. Bode 1982; B. Warner 1995). Similarly, in T CrB, the secondary maximum of 1946 coincides with the rise of a shell spectrum, implying the formation of an optically thick envelope that absorbs and converts the UV radiations from the hot primary in increased visible flux (P. L. Selvelli et al. 1992). In DQ Her and FH Ser, the ejected envelope shows an elongated geometry

with an equatorial belt and polar blobs (E. R. Mustel & A. A. Boyarchuk 1970; J. B. Hutchings 1972); optical imaging of T CrB also shows a bipolar structure (R. E. Williams 1977). In addition, the cousin, fast recurrent nova RS Oph shows a clear transition phase (identified as a "posteruption dip" by B. E. Schaefer 2010) starting  $\simeq$ 70 days and lasting until  $\sim$ (450 -500) days after the onset of its eruption. Spectropolarimetric monitoring of its 2021 eruption (Y. Nikolov et al. 2023) shows that dust grains roughly aligned with the binary orbital plane were present in RS Oph more than 80 days after the onset of the eruption (i.e., during its transition phase), indicating that dust grains also form in low-mass, high-velocity ejecta of recurrent novae similar to T CrB. Indeed, a recent statistical study of dust formation in novae finds that 17% of very fast novae form dust grains (A. Chong et al. 2025). Having recurrent, fast nova eruptions with a transition phase caused by dust grain formation in 2 (RS Oph and T CrB) out of ≃10 known recurrent novae is consistent with their statistics.

Thus, the primary and the secondary observed maxima of T CrB might not be two separate events demanding a challenging and unusual explanation (R. F. Webbink et al. 1987) but two phases of a unique nova eruption event. If this interpretation is correct, the decline phase ends about 400 days after the start of the T CrB nova eruption (see Figure 21 of B. E. Schaefer 2010), when the accretion disk is already back to the high-brightness state (and the H-rich envelope for the next eruption starts to accumulate on the WD's surface). In favor of this interpretation, we note that the minimum of the transition phase does not correspond to the high-brightness state; at this phase, T CrB is fainter in the B band and brighter in the V band than during the high-brightness state that precedes the 1946 nova eruption, with  $(B-V)_h \simeq +0.5$  mag and  $(B-V)_t \simeq +1.0$  mag, respectively in the high-brightness state and during the transition phase (see Figure 23 of B. E. Schaefer 2010).

An alternative interpretation of the observed secondary maximum of T CrB is that it is caused by irradiation of the RG by a cooling, hot and extended WD (but with constant radius, U. Munari 2023b). In this scenario, the heating of the inner face of the RG (up to  $\simeq$ 7800 K) will likely increase its mass-transfer rate and help to shorten the timescale for the reestablishment of the accretion disk, ensuring that T CrB is back at the high-brightness state by the end of the overall nova decline phase.

# 4.3. On the Pre-eruption Dip

If there is a unique 15 yr long event of enhanced mass accretion around the nova eruption, then what explains the brightness decline over the  $\simeq (1-2)$  yr previous to the nova eruption? Here, we put forward an explanation for the preeruption dip based on the observations.

Recent observations indicate that the pre-eruption brightness decline of T CrB is much more pronounced in the blue than in the red (U. Munari 2023a; K. A. Stoyanov et al. 2025), leading B. E. Schaefer et al. (2023) to suggest that the brightness decline is the result of enhanced absorption by dust grains from a short and anticipated event of mass ejection. However, the lack of evidence for enhanced IR emission (C. E. Woodward et al. 2023) and the fact that the amplitude of the ellipsoidal modulation from the distorted RG remains constant along the brightness decline phase (B. E. Schaefer et al. 2023) indicate that it is the accretion disk which is fading

in brightness (by a factor of  $\simeq 100$ , in order to bring it back close to its quiescent brightness level).

There are two possible ways to decrease the accretion disk's luminosity: one is by decreasing the mass-transfer rate and the other is by increasing the inner disk's radius. A reduction in mass-accretion rate by a factor  $\simeq 100$  (from  $1.9 \times 10^{-7} M_{\odot} \, \mathrm{yr}^{-1}$  back to  $2 \times 10^{-9} M_{\odot} \, \mathrm{yr}^{-1}$ ) results in brightness variations of approximately the same magnitude across the BVRI passbands —in contradiction with the observations. On the other hand, an increase in inner disk's radius by the same factor leads to a color-dependent brightness variation, more pronounced in the B-passband and of progressively lower amplitude with increasing wavelength—which is in good agreement with the color changes observed during the pre-eruption dip. This is the consequence of the fact that increasing the inner disk's radius selectively eliminates the hottest and bluest inner disk regions. Furthermore, increasing the inner disk's radius by a factor  $\simeq 100$ also increases the volume of a geometrically thin, equatorial boundary layer by a comparable amount, allowing it to become optically thin during the pre-eruption dip-again in good agreement with the observations (K. A. Stoyanov et al. 2025). Thus, the observed brightness changes during the pre-eruption dip favor the interpretation that it is caused by an expanding inner disk radius.

In addition, assuming that the Doppler line broadening is caused by the Keplerian rotation of gas in the accretion disk, the half width at zero intensity (HWZI) of the emission lines provides a useful estimate of the inner disk's radius and allow us to further test the idea that the pre-eruption dip is the consequence of an expanding inner disk radius. For example, the temperatures of the opaque steady disk at the highbrightness state are sufficiently low to allow the formation of hydrogen emission lines  $(T \le 10,000 \text{ K})$  for  $R \ge 1.06 R_{\odot}$ , corresponding to Keplerian velocities of  $v_{\phi} \leq 485 \,\mathrm{km \, s}^{-1}$ . Accordingly, the observed width of the Balmer lines during the high-brightness state is  $HWZI \le 500 \text{ km s}^{-1}$  (U. Munari et al. 2016; R. K. Zamanov et al. 2024b), which is in good agreement with this estimate. If the mass-transfer rate is decreased by a factor  $\simeq 100$ , the systematic reduction of accretion disk temperatures at all radii allows the extension of the hydrogen line emitting region down to  $R \ge 0.22 R_{\odot}$ , corresponding to significantly higher Keplerian velocities,  $v_{\phi} \leq 1050 \,\mathrm{km \, s^{-1}}$ . However, spectroscopy at the minimum of the pre-eruption dip (at 2023 October, R. K. Zamanov et al. 2024b) shows that the width of the H $\alpha$  line has instead reduced to  $HWZI \simeq (230-250) \,\mathrm{km \, s}^{-1}$ , corresponding to an inner disk radius for hydrogen emission of  $R_{\rm in} \simeq (3.9-4.6) R_{\odot}$ , which is a factor of  $\simeq 20$  times larger than predicted by the decreasing mass-transfer rate scenario. This suggests that there is a significant increase in the inner disk's radius from the highbrightness state to the pre-eruption dip. Assuming that the inner disk's radius at the high-brightness state equals the WD's radius and taking  $R_{\rm in}$  as an upper limit to the inner disk radius at 2023 October, we infer an upper limit to the average expansion velocity of  $v_{\rm exp} < (0.13-0.16)\,{\rm km\,s}^{-1}$  along the  $\simeq$ 8 months from the start to the minimum of the pre-eruption dip (from 2023 February to 2023 October, U. Munari 2023a; R. K. Zamanov et al. 2024b).

We further tested the idea of such a slowly expanding inner disk radius by simulating the evolution of the accretion disk of model II with a variable inner radius, at a fixed mass-transfer rate  $\dot{M}_2^h$ . Two cases were considered. In the first case, the inner

disk's radius increases from  $R_{\rm in} = R_{\rm WD} = 0.0045 \, R_{\odot}$  up to a few  $R_{\odot}$  at constant acceleration, corresponding to an average expansion velocity  $v_{\rm exp}$  over a 2 yr time interval. In the second case, the inner disk's radius expands at a constant velocity  $v_{\rm exp}$  during the same time interval. The results are compared to the observations of the pre-eruption dip in Figure 5. The observed brightness decline in the BVRI passbands is reasonably well reproduced by the model with accelerated inner disk expansion. A small average expansion velocity of  $v_{\rm exp} = 0.02 \, {\rm km \, s^{-1}}$  provides the best fit to the observational data, in agreement with the upper limit estimated from the observations.

The above observational picture indicates that the decline in accretion disk luminosity associated to the pre-eruption dip is not caused by a decrease in mass-transfer rate but by a significant, slow increase in the inner disk's radius during this time. What could cause the slow inner disk radius expansion?

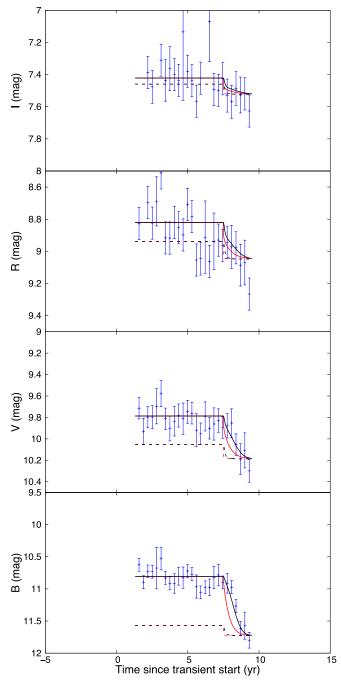
The sequence of events that leads to a nova eruption can be described by three phases (e.g., D. Prialnik 1986; K. J. Shen & L. Bildsten 2009; W. M. Wolf et al. 2013). The pre-nova accretion phase ends when the accumulated envelope mass reaches the ignition conditions. The convection phase starts with the onset of nuclear reactions at the base of the accreted envelope. Since the gas is degenerate, the H-burning region spreads rapidly both inwards and outwards, the nuclear luminosity  $L_{\text{nuc}}$  rises exponentially, temperature gradients increase, and the H-burning region becomes convectively unstable. The timescale for the development of convection throughout the accreted envelope (i.e., the duration of the convection phase) is short compared to the thermal timescale. Therefore, the envelope is out of thermal equilibrium; its bolometric luminosity remains almost constant ( $L_{\rm bol} \sim 10^{-2} L_{\odot}$ ), while  $L_{\text{nuc}}$  increasingly exceeds  $L_{\text{bol}}$  along this phase (e.g., D. Prialnik 1986). The end of the convection phase sets the start of the explosion phase, with the TNR on a fully convective envelope leading to its fast expansion and significant increase in luminosity, which is identified as the nova eruption. The duration of the convection phase is 20-100 times shorter than that of the preceding accretion phase (D. Prialnik 1986; K. J. Shen & L. Bildsten 2009). For T CrB, the accretion phase lasts about 80 yr, this leads to an estimated length of (0.8-4.0) yr, which is in good agreement with the observed  $\simeq (1-2)$  yr duration of the pre-eruption dip. Hence, the pre-eruption dip occurs during the convection phase in T CrB.

We suggest that the inferred expansion of the inner disk's radius is connected to the lack of thermal equilibrium and the development of strong convection in the accreted envelope during this phase, in two possible scenarios. We first note that, at the onset of the convection phase on top of a high-mass WD fed at high-accretion rates, the gas is partially degenerate, even at the base of the envelope  $(T_b \simeq 3 \times 10^7 \, \text{K})$  and  $\rho_b \simeq 10^3 \, \text{g cm}^3$ , e.g., K. J. Shen & L. Bildsten 2009), and gas pressure is sensitive to temperature. According to the first law of thermodynamics, the additional heat provided to each layer across the accreted envelope drives changes in their temperature and density at rates (R. Kippenhahn & A. Weigert 1990),

$$\frac{dq}{dt} = c_{\rho} \frac{dT}{dt} + c_{T} \frac{d\rho}{dt} \,, \tag{3}$$

where

$$c_{\rho} = \left(\frac{\partial u}{\partial T}\right)_{\rho} > 0,\tag{4}$$



**Figure 5.** Simulation results with expansion of the inner radius with constant acceleration (black solid curve) and constant velocity (red solid curve). The points with error bars are the same as in Figure 1 for *B* band and analogous for the other bands. The black and red dashed curves are the contribution from the irradiated red giant companion in the models with constant acceleration and constant velocity, respectively.

$$c_T = \left(\frac{\partial u}{\partial \rho}\right)_T - \frac{P}{\rho} < 0 , \qquad (5)$$

 $c_{\rho}$  and  $c_{T}$  are, respectively, the specific heats at constant density and temperature, u is the internal energy per mass, and P is the total pressure. A dq/dt > 0 implies dT/dt > 0 (because  $c_{\rho} > 0$ ) and  $d\rho/dt < 0$  (because  $c_{T} < 0$ ). Thus, the first possible scenario is that the increasing excess heat deposited at the accreted envelope during the convection phase continuously

increases temperature (leading to pressure unbalance, loss of hydrostatic equilibrium, and expansion) and decreases density (i.e., direct expansion), driving the envelope into slow (but accelerated) expansion at roughly constant bolometric luminosity, while convection spreads and efficiently transports excess nuclear energy further upwards. If the inner disk's radius coincides with the surface of the accreted envelope, the expansion of the envelope leads to the progressive increase of the inner disk's radius and to the continuous decrease of the accretion disk's luminosity, even if the mass-accretion rate remains constant during the process.

If this scenario is correct, why is there no report of envelope expansion during the convection phase in nova eruption simulations? Numerical simulations of nova eruptions are computationally very demanding (e.g., J. José et al. 2020) and, for computational feasibility, most numerical simulations of nova eruptions have been performed with 1D codes, with two relevant limitations. First, hydrostatic equilibrium is imposed throughout the accreted envelope during the convection phase, until the relative pressure unbalance exceeds a threshold (usually  $dP/P > 10^{-5}$ ) and the simulation switches to full hydrodynamic calculations in order to follow the explosion phase (e.g., D. Prialnik 1986; S. A. Glasner et al. 1997; M. Zingale et al. 2002; J. José et al. 2020, and references therein). By design, these simulations are unable to identify and to account for a slow accretion envelope expansion during the convection phase. While this choice is computationally convenient and justified by the focus on the ensuing TNR, it leads to the unrealistic behavior of an accretion envelope that remains static for most of the convective phase and suddenly expanding at already significant velocities  $v_{\rm exp} \simeq (10^1 - 10^2) \, {\rm km \, s^{-1}}$ . Signs that imposing hydrostatic equilibrium throughout the convection phase leads to an incomplete physical description and that envelope expansion does occur appear when 1D nova eruption simulations are used as a starting point to 2D full hydrodynamic simulations. J. Casanova et al. (2018) reported that forcing the initial 1D model to be in hydrostatic equilibrium after mapping into 2D imposes a restriction on the portion of the envelope that can be computed, since the density dramatically decreases and produces numerical underflow (see also M. Zingale et al. 2002)—suggesting that the 1D model envelope is undersized for its physical conditions (i.e., there is unaccounted expansion in the 1D model). In addition, 1D modeling is further limited by the use of the mixing-length theory (MLT) of convection, which cannot account for either mass flux (i.e., envelope expansion, J. José et al. 2020) or strong mixing at coreenvelope interface (J. Casanova et al. 2011). Furthermore, 3D simulations suggest that strong turbulence and mixing do occur at the core-envelope interface and that the resulting convective velocities are systematically larger (by factors 2–3) than those obtained assuming MLT (J. José et al. 2020), driving significant dredge-up of CO or ONeMg material from the

<sup>&</sup>lt;sup>7</sup> This is also true in the case of isobaric expansion, where the increase in temperature is compensated by a matching decrease in density (meaning envelope expansion) in order to keep pressure constant.

The volumetric densities at the inner radius of a steady opaque disk with  $\alpha=3$  and  $\dot{M}_2^h$  are  $\rho_d<10^{-9}~{\rm g~cm^{-3}}$ , at least two orders of magnitude lower than those at the surface of a B0 main-sequence star of  $R=6~R_\odot$  (e.g., E. Böhm-Vitense 1992), indicating that while the expanding atmosphere of the primary star has  $R\leqslant20~R_\odot$ , it will be dense enough to prevent the inner disk regions lagging behind and extending inwards of the expanding atmosphere.

WD's core into the H-burning envelope (which increases the rate of nuclear energy generation) and efficient transport of excess nuclear energy to upper, less degenerate envelope layers—both of which may contribute to envelope expansion during the convection phase.

An alternative scenario to explain the inferred increase of the inner disk's radius is related to the possible development of a strong, transient magnetic field during the convection phase. J. Casanova et al. (2016) suggested that there may be sufficient time during the vigorous convection phase to build a fast dynamo and a strong magnetic field, which could then be advected together with the ejecta during the ensuing nova eruption. If this is the case, the magnetospheric radius increases with magnetic field strength along the convection phase, disrupting the accretion disk at progressively larger radii and leading to the continuous decrease of the accretion disk's luminosity, even if the mass-accretion rate remains constant during the process. For a magnetic WD, the magnetospheric radius inside which magnetic pressure exceeds ram pressure and the accretion disk is disrupted is given by (J. Frank et al. 2002),

$$R_M \simeq 5.1 \times 10^8 \, \dot{M}_{16}^{-2/7} (M_1/M_\odot)^{-1/7} \mu_{30}^{4/7} \, \text{cm},$$
 (6)

where  $\dot{M}_{16}$  is the mass-accretion rate in units of  $10^{16}\,\mathrm{g\,s^{-1}}$ ,  $\mu_{30}$ is the magnetic moment (= $B_{WD}R_{WD}^3$ ) in units of  $10^{30} \,\mathrm{G\,cm}^3$ , and  $B_{\rm WD}$  is the WD's surface magnetic field. For the highbrightness state of T CrB,  $\dot{M}_{16} = 1200$  and  $R_M = 1.73 \times$  $10^5 B_{\rm WD}^{4/7}$  cm. Thus, in order for  $R_M$  to increase from  $\leqslant R_{\rm WD}$  up to  $\simeq 100 R_{\rm WD}$ ,  $B_{\rm WD}$  needs to increase from  $\leq 5 \times 10^5 \,\rm G$  up to  $1.6 \times 10^9$  G. The larger field corresponds to a magnetic moment of  $\mu \simeq 5 \times 10^{34} \,\mathrm{G} \,\mathrm{cm}^3$ , comparable to those of strong field polars (e.g., B. Warner 1995). The corresponding fundamental frequency for cyclotron emission is  $f_{\rm cyc} = 4.5 \times 10^{15} \, \rm Hz$  ( $\lambda_{\rm cyc} = 66.7 \, \rm nm$ ). The predictions from this scenario can be observationally tested: enhanced EUV and soft X-ray emission with cyclotron humps (in the range 19  $-190 \,\mathrm{eV}$  for the first 10 cyclotron harmonics), and linear and circular polarization (and possibly X-ray variability at the WD's rotation period) associated with the pre-eruption dip in T CrB. However, none of these have been detected during the current dip. Soft X-rays were not detected, while near-UV emission fainted (G. J. M. Luna et al. 2025, in preparation) and intrinsic optical polarization was absent (Y. Nikolov 2025, private communication). We thus do not favor this scenario.

If the pre-eruption dip is a general consequence of the convection phase, why is there no evidence of pre-eruption dips on all nova? What is special about T CrB?

T CrB is the only (recurrent) nova whose eruption starts while the system is in a state of enhanced mass accretion, with its disk luminosity being about 100 times brighter than in quiescence. Perhaps the lack of detection of pre-eruption dips in novae is the effect of an observational bias, which will be reduced with the new all-sky surveys. For example, given that all other recurrent nova go into eruption while their accretion disks are at a much lower brightness level, their pre-eruption dip may easily be diluted in the brightness of the RG companion and in the typical  $\simeq 1$  mag brightness variations that affect their light curves (B. E. Schaefer 2010). Moreover, with accretion rates of  $\simeq 10^{-10} - 10^{-9} \, M_{\odot} \, \text{yr}^{-1}$ , small accretion disks, and subsolar companions, quiescent classical novae are

intrinsically fainter than T CrB and are beyond the reach of visual observations and of most amateur astronomers, which has prevented well sampled photometric monitoring of their pre-eruption stage. Furthermore, because of their much longer accretion phase, their convection phase is expected to last about 1-2 centuries; there is no comprehensive and precise photometry of pre-eruption novae over this large amount of time. Nevertheless, R. K. Zamanov et al. (2024a) has reported the tantalizing detection of a pre-eruption dip in RS Oph (although the authors arrived at a different interpretation about its origin than the one we put forward here). Finally, detailed optical observations during the intereruption phases of a recurrent nova with a short recurrence period, and thus with a short convection phase, such as RN M31N 2008-12a (M. J. Darnley et al. 2014) would provide a clear-cut test for the scenario proposed above.

### 4.4. Which Came First, the Chicken or the EGG?

B. E. Schaefer (2023b) raised the interesting issue that "The existence of the pre-eruption high-state presents a mystery as to why the system brightens before the eruption," and then concluded that "So we are left with no explanation for the enigma as to why the high-state anticipates the eruption by 10 yr, just as we have no explanation for the cause or physical mechanism of the high-state existence." This apparent enigma is a consequence of an inversion of the relevance of the events in T CrB.

As remarked in Section 1, without a phase of enhanced mass-accretion, T CrB would be a classical nova with a much longer interval between successive eruptions (≈5480 yr). The best explanation for the high-brightness state (Section 4.1) is that it corresponds to the crucial phase of enhanced massaccretion which determines the much shorter recurrence interval of the T CrB nova eruptions. It is thus correct to say that the TNRs of T CrB are powered by accretion events. Indeed, the matter accumulated onto the WD's surface during the 15 yr long enhanced accretion phase responds to 95% of  $M_{ig}$ , indicating that the probability that the ignition conditions be reached (and lead to the nova eruption) during the highbrightness state is also 95%. This provides a natural explanation for why the nova eruption is superimposed on the high-brightness state. In other words, it is the increased mass-accretion phase during the high-brightness state (the cause) that drives the nova eruption (the consequence), underscoring previous suggestions by G. J. M. Luna et al. (2020) and R. Zamanov et al. (2023), and solving the apparent enigma raised by B. E. Schaefer (2023b).

Concerning the recurrence of the enhanced mass-accretion events, a possible explanation for the sudden increases in  $\dot{M}_2$  required by MTIM involves the interaction of starspots with the inner Lagrangian point  $L_1$ . While the passage of starspots in front of the  $L_1$  point can significantly reduce  $\dot{M}_2$  (M. Livio & J. E. Pringle 1994; A. R. King & J. K. Cannizzo 1998), events of enhanced  $\dot{M}_2$  may occur when there are no starspots transiting  $L_1$  (J. M. Hameury & J. P. Lasota 2014).

A possible mechanism through which the high-accretion state develops and repeats itself every  $\sim\!80\,\mathrm{yr}$  is as follows. A starspot-free region on the secondary that periodically passes in front of  $L_1$  as seeing from the WD would enhance the accretion through  $L_1$ . Let us assume that  $P_{\mathrm{spot}}$  is the period of the starspot-free region, which is slightly larger than the orbital period  $P_{\mathrm{orb}}$ , then the recurrence time can be determined from

the beat period between both,  $1/P_{\rm rec}=1/P_{\rm orb}-1/P_{\rm spot}$ . Defining  $\epsilon=(P_{\rm spot}-P_{\rm orb})/P_{\rm orb}$  as the relative difference between the orbital period and the period of the starspot-free region, we find that  $\epsilon = P_{\rm orb}/(P_{\rm rec} - P_{\rm orb})$ . Although of different spectral type than the secondary in T CrB, there is evidence of starspots on the secondary of SS Cyg, a wellknown dwarf nova (N. A. Webb et al. 2002). In the case of SS Cyg, where  $P_{\text{orb}} = 6.6 \,\text{hr}$  and the dwarf nova outburst recurs on a characteristic timescale of  $P_{\rm rec} \simeq 40 \, {\rm days} \simeq 960 \, {\rm hr}$ , we find  $\epsilon = 0.007$ . In the case of T CrB, with  $P_{\rm orb} = 227.5$  days,  $P_{\rm rec} = 80 \, {\rm yr} = 29{,}220 \, {\rm days}$ , we find  $\epsilon = 0.008$ . This suggests that while in the case of SS Cyg a shift of 0.7% between the starspot and orbital periods can explain its dwarf nova outburst recurrence timescale, in the case of T CrB a comparable shift could explain the recurrence time of the high-accretion state. Although appealing, this mechanism calls for further observations to be accepted, but offers a path to explain the recurrence of the high-accretion state during which the TNR happens. A search for starspot-free regions on the surface of the RG, their evolution with time, and possible correlation with the highbrightness state may help to elucidate if the proposed scenario is viable.

### 5. Conclusions

The observed T CrB brightness variations during the high-accretion state can be satisfactorily reproduced by models of an enhanced mass-transfer event of duration  $\Delta t_e=15$  yr onto a high-viscosity accretion disk with  $\alpha=3$ . The best-fit, self-consistent model has an inferred WD mass  $M_1=1.29\,M_\odot$ , an inclination  $i=57^{\circ}.3$ , and quiescent and high-accretion mass-transfer rates, respectively, of  $2.0\times10^{-9}\,M_\odot\,{\rm yr}^{-1}$  and  $1.9\times10^{-7}\,M_\odot\,{\rm yr}^{-1}$ . This model also provides a good description of the color variations of T CrB throughout the transient.

The pre-eruption dip occurs during the convection phase that precedes the TNR in T CrB and is best described by a slow, accelerated expansion of the inner disk's radius at an average velocity of  $0.02\,\mathrm{km\,s^{-1}}$  over a 2 yr timescale. We suggest that this expansion is connected to the lack of thermal equilibrium and the development of strong convection in the accreted envelope during this phase, in two possible scenarios: (1) the slow expansion of the accreted envelope itself (pushing the inner disk's radius progressively outwards) and (2) the progressive disruption of the inner disk regions by the magnetosphere of a transient magnetic field. However, this last scenario does not seem to be favored by the current observational data.

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*Note added in proof.* The recent claim by J. Merc et al. (2025) that the forthcoming nova eruption in T CrB might be

delayed when compared to the predictions does not challenge our proposed scenarios, given that when both current and previous high-brightness states are compared, on average the one that started in 2014 has been fainter, implying lower accretion rates and larger ignition mass, therefore resulting in a longer time to reach ignition from the start of the high-brightness state as well as a subsequent longer convection phase. We also remark that the inferred expansion of the inner disk radius during the pre-eruption dip phase leads to a sequence of decrease in UV flux (because of the reduced disk luminosity) followed by a transient increase in X-ray flux (because the expanding boundary layer becomes optically thin), which is consistently the time reversed behavior expected for the boundary layer at the onset of dwarf nova outbursts (see, e.g., Figure 1 of M. R. Schreiber et al. 2005).

### **ORCID iDs**

Wagner Schlindwein https://orcid.org/0000-0002-7095-4147 Raymundo Baptista https://orcid.org/0000-0001-5755-7000 Gerardo Juan Manuel Luna https://orcid.org/0000-0002-2647-4373

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