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The potential for detecting life as do don't know it by fractal complexity analysis

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Complete List of Authors:	Azúa-Bustos, Armando; Pontificia Universidad Catolica de Chile, Departamento de Genetica Molecular y Microbiologia Vega Martínez, Cristian; Pontificia Universidad Catolica de Chile, Departamento de Astronomía y Astrofísica
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Manuscripts

Review

1 **The potential for detecting “life as we don’t know it” by fractal complexity**

2 **analysis**

3 Armando Azua-Bustos^{1,2*} Cristian Vega-Martínez³

4

5 ¹Pontificia Universidad Católica de Chile, Faculty of Biological Sciences,
6 Department of Molecular Genetics and Microbiology, Santiago, Chile. Centro de
7 Estudios Generales, Universidad de los Andes, Santiago, Chile.³ Instituto de
8 Astrofísica de La Plata (CCT La Plata, CONICET - UNLP). *To whom
9 correspondence should be addressed.

10 E-mail: ajazua@uc.cl

11

12 **Running title:** detecting life by Fractal Complexity

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17

18 Abstract

19 Finding life in the Universe entirely different to the one evolved on Earth
20 elsewhere is probable. This is a significant constraint for life-detecting
21 instruments that were sent and may be sent elsewhere in the solar system, as how
22 could we detect life as “we don’t know it”? How could we detect something that
23 we have no prior knowledge of its composition or how it looks like? Here we
24 argue that disregarding the type of lifeform that could be envisioned, all must
25 share in common the attribute of being entities that decrease their internal entropy
26 at the expense of free energy obtained from its surroundings. As entropy
27 quantifies the degree of disorder in a system, any envisioned lifeform must have a
28 higher degree of order than its supporting environment. Here we show that by
29 using fractal mathematics analysis alone, one can readily quantify the degree of
30 entropy difference (and thus, their structural complexity) of living processes
31 (lichen growths and plant growing patterns in this case) as distinct entities
32 separate from its similar abiotic surroundings. This approach may allow the
33 possible detection of unknown forms of life based on nothing more than entropy
34 differentials of complementary data sets. Future explorations in the solar system,
35 like Mars or Titan, may incorporate this concept in their mission planning in order
36 to detect potential endemic lifeforms.

37

38 **Introduction**

39 There is a chance of finding life “as we don’t know it” elsewhere in the Universe.
40 These lifeforms may be entirely different from life that evolved on Earth; not
41 using water as a solvent, DNA/RNA as informational molecules, etc., thus
42 reflecting an independent origin of life (Davies *et al.* 2009). This is a significant
43 constraint not only for life-detecting instruments sent, and to be sent to different
44 bodies of the solar system, but also for life-signature detecting techniques to be
45 applied onto more distant exoplanets.

46 Life evolves against entropy, keeping the information gained and increasing it
47 (Avery 2003). As Erwin Schrödinger stated (1945), “life feeds on negative
48 entropy”. Thus, as lifeforms become more complex, their entropy decreases
49 (Crutcheld & Young 1989). Death causes the opposite effect; that is, the
50 quantitative symmetry in the long term between the entropy of the lifeform and its
51 surrounding environment.

52 Although a universally accepted definition for complexity has not been reached so
53 far it may yet be stated that life is a complex adaptive system. As such, it contains
54 interdependent constituents that interact nonlinearly, possessing a structure that
55 spans several scales (Baranger 2011).

56 Thus, one should be able to detect entropy differences (and thus levels of
57 complexity) between lifeforms and the environments where they thrive (Kleidon
58 2010). It then may be expected that extraterrestrial lifeforms will also have lower
59 entropy states in comparison with similar abiotic phenomena found in their
60 environments. In fact, Lovelock proposed that in order to find signs of life, “one
61 must look for a reduction or a reversal of entropy” (Lovelock 1979). On Earth,
62 even the simplest of microorganisms show a high degree of complexity
63 (Passalacqua *et al.* 2009).

64 One mathematical tool that allows an objective quantification of complexity is
65 fractal geometry analysis. Fractal geometry analysis can readily analyze the
66 complexity of different structures, in particular of those spanning several scales. It
67 has been previously shown that fractal geometry better approaches the complexity
68 of many life related phenomena at different scales, from tree distribution in forests
69 to neural activity patterns (Losa 2009). This is estimated by calculating the fractal
70 dimension “D”, a statistical quantity that indicates the degree of completeness in
71 which a fractal structure appears to fill a data space as finer and finer scales are
72 analyzed. In general, an object may be called a “fractal” if its D value exceeds its
73 topological dimension. Consequently, different D values identify different levels
74 of complexity.

75 Fractal geometry analysis may then be applied to the examination of interesting
76 candidates elsewhere in the Universe to check whether a higher order of
77 complexity, compared with environmental features of its system, may be
78 indicative of unknown lifeforms, and potentially, also of abiotic processes altered
79 by life processes. This approach has the advantage of requiring no prior
80 information of the potential lifeform to be analyzed. For the analysis of such
81 candidates, a proof of concept needs to be developed, along a proper analytical
82 technique, both of which we describe here.

83

84 **Material and Methods**

85

86 *Model systems*

87 We chose two different biotic-abiotic model pairs for our analyses, which in
88 addition covered two different orders of magnitude.

89 At the microscopic level, we analyzed lichen covered rocks in the high Andes
90 Mountains near Santiago, Chile. Here the aim was to compare the structure of
91 lichen growths with the structure of the rock where it develops, in order to see if we
92 could detect a higher complexity associated to the lichen growth in relation to its
93 abiotic surroundings.

94 At the macroscopic level, we analyzed *Tillandsia* shrub growing patterns on sand
95 dunes of the Atacama Desert. In these dunes, the Bromeliad *Tillandsia landbeckii*
96 self-organize in characteristic growth bands of shrubs in order to maximize the
97 interception of fogs (Borthagaray *et al.* 2010), creating banding patterns that from
98 above, appear very similar to geologically banding structures. Here the aim was to
99 compare *Tillandsia* banding patterns with geological banding patterns of similar
100 inter-band distances, in order to see if we could detect a higher complexity
101 associated to the *Tillandsia* banding in comparison of that of similar bandings of
102 geological origin.

103

104 *Images*

105 High resolution photographs of lichen covered rocks were taken at the Andes
106 Mountains near Santiago, Chile (FIG. 1A). For the analysis of lichens and rock
107 surfaces, we analyzed 20 bare rocks images (FIG 2A) and 110 lichen images (FIG
108 2B). The lower number of bare rocks surfaces analyzed was due to the scarcity of
109 unequivocally naturally bare rock surfaces immediately adjacent to lichen
110 colonized areas.

111 Geological bandings patterns in the vicinity of areas covered by *Tillandsia* bands
112 were obtained by downloading 30 images (FIG. 2C) from Google Earth. Care was

113 taken to consider that the inter-band distance of geological bandings was about 10
114 meters, which is the mean inter-band distance measured for *Tillandsia* banding
115 growths. 33 *Tillandsia* bandings images (FIG. 2D) were also downloaded from
116 Google Earth. *Tillandsia* covered sites, which are found near the City of Iquique
117 at the Atacama Desert of Chile, were visited as to confirm their biological origin
118 and independency of geological processes (FIG. 1B). This was also confirmed for
119 the banding patterns of geological nature.

120 In addition, we selected 24 banding patterns images (FIG. 2E) taken by the HiRise
121 camera onboard of the Mars Reconnaissance Orbiter at Meridiani Planum on
122 Mars. These banding patterns are thought to have formed through the
123 accumulation of sediments transported by flowing water. The number of images
124 analyzed in this case corresponded to images with similar inter-band distances to
125 the bandings of Earthly origin.

126 In all cases the images were cropped in order to ensure the analysis of just the
127 phenomena of interest (FIG. 2).

128

129 *Development of FrAn, a Fractal Analysis tool*

130 The box-counting method is one of many methods developed for fractal analysis
131 (Soille and Rivet, 1996). It works by covering a set of data (an image in this case)

132 with “boxes” (squares) and then evaluating how many “boxes” are needed to re-
133 describe the data set completely in a metric space. Repeating this measurement
134 with boxes of decreasing sizes results in a logarithmical function of box size (x-
135 axis) and number of boxes needed to cover the pixels image dataset (y-axis) (FIG.
136 3). The slope of this function is referred as the *box dimension*, which is a
137 considered to be a good approximation of the fractal dimension (Soille and Rivet,
138 1996).

139 The software we used for our analyses, “FrAn” (for **F**ractal **A**nalyzer), was
140 created using as a reference a previous program (HarFa), a software that was
141 compiled to perform harmonic and wavelet analysis of digitized images and
142 calculations of their fractal parameters based on the box counting technique
143 (Harfa, 2010). Using this software as an example, we created a new algorithm that
144 also uses the box counting technique, incorporating a new and critical parameter
145 for our aims, the fractal excess (FE) (defined in detail below).

146

147 *Image data analysis*

148 Using FrAn, we first estimated the fractal dimension of the sets images of lichens-
149 colonized and uncolonized Andean rock surfaces: the images were first trimmed
150 in order to consider unequivocally fully colonized and fully uncolonized

151 selections (FIG. 2). FrAn then transforms these images into grey scale versions,
152 and then to black and white images (FIG. 4). The grey scale to black and white
153 transformation is performed for all possible threshold (T) values (256 in total),
154 where $\bar{X} - 1.5\sigma < T < \bar{X} + 1.5\sigma$, where \bar{X} is the mean intensity of all pixels and σ the
155 standard deviation of all pixel intensities. The importance of the thresholding
156 process may be understood if it is considered that the strength of the signal (the
157 brightness and contrast of the image as determined by the intensity value for each
158 pixel) has a direct effect on the amount of information that can be extracted from
159 any particular image (FIG. 5). In practice, this means that every sample image was
160 analyzed at least seven times in the range of -1.5σ and 1.5σ . In addition, to every
161 image analyzed, a “null model” was created, which corresponded to the same
162 image data set, but randomized (FIG. 2F).

163 Then, the Minkowski–Bouligand dimension (or box dimension) was calculated; In
164 $N(\varepsilon) = D_{\text{box}} \ln(1/\varepsilon) + K$, where ε is the box length, N is the number of different
165 boxes of size ε , and K is an arbitrary constant. This was done for all image
166 analyzed and their null counterparts.

167 After these analyses the computation of the Fractal Excess (FE) was then
168 calculated. The FE is defined as the difference between the fractal spectrum of the
169 sample image fractal spectrum and its null model. Therefore, the incorporation of

170 a null model for each of the samples being analyzed guarantees a true estimation
171 of the complexity of the analyzed images.

172 Thus, the final output of the image data analysis is a curve of the entire spectra of
173 FE values for each threshold situation. As a result, a low FE value indicates a high
174 fractal dimension and correspondingly, a higher complexity of the sample being
175 analyzed. In turn, high FE values indicate a low fractal dimension, and thus, a
176 lower complexity of the sample.

177 All analysis were performed with a Hewlett Packard cluster composed by 62 Intel
178 Titanium II processors and a total of 48 GB of RAM available at the Center for
179 bioinformatics of the Faculty of Biological Sciences of the Pontificia Universidad
180 Católica de Chile. Using this processing power, mean analysis time for each
181 image selection was about 20 minutes. FrAn is available on request.

182

183 **Results**

184 Figure 6 shows that the Fractal Excess spectrum curve for all lichen images
185 analyzed is unique, and different to the Fractal Excess spectrum curve for all bare
186 rock surface images. Bare rock samples show higher FE values than lichen FE
187 values, the latter being lower and closer to the x axis.

188 Larger distances between both curves are observed at the positive range of the
189 spectra, although appreciable distances can also be seen at the negative range of
190 the. FE minima also reflect these differences, with bare rock surface being 0.26
191 and Lichen being 0.18 (Figure 7). At both ends of the FE spectra maxima also
192 follow the same pattern, with lichen maxima being lower than bare rock surface
193 values. This result provides good evidence that biotic processes do have a higher
194 complexity than the environment where they occur.

195 Repeating these analyses in another order of scale show a similar trend. We
196 processed images of banding vegetation patterns of *Tillandsia* shrubs growing on
197 the Atacama Desert, comparing them with geological structures of similar
198 appearance, inter-band distance and size in the surrounding area.

199 As can be seen in Figure 8, the FE curve profile of vegetation patterns is readily
200 separated from similarly looking geological banding structures. Similarly to the
201 results obtained with lichen growth analysis, *Tillandsia* growing patterns show a
202 curve with lower values than similar abiotic phenomena, thus revealing the higher
203 complexity associated to living phenomena. As for FE minima, they also reflect
204 these differences, with geological banding patterns being 0.28 and *Tillandsia*
205 banding patterns being 0.20 (FIG. 7).

206 Interestingly, when similar geological banding patterns found in Meridiani
207 Planum on Mars were analyzed, its curve showed a distinctive profile, between
208 those from geological and biological banding patterns on Earth (FIG. 8).

209

210 **Discussion**

211 As a proof of concept of our approach, we focused on two extreme environments
212 as models, which in addition represent two scales of size (FIG. 1).

213 First, we analyzed lichens growing on rocks at high altitude on the Andes
214 Mountains of Chile. Lichens are important drivers of biogeochemistry and the
215 first lifeforms to colonize barren environments (Cornelissen *et al.* 2007). Seen
216 from the point of view of an alien civilization, lichens may not be at first
217 recognized as living entities, a hypothetical scenery that emulate a situation in
218 which humans explore an extraterrestrial environment. Hence, we set to determine
219 whether the complexity of lichens could be differentiated from the similarly
220 looking rock background where they grow. By using FrAn we show that indeed,
221 the complexity structure of bare rocks and lichens differ and are readily separable
222 (FIG. 6). Lichen samples have lower FE values than Bare rock samples, the
223 former being closer to the x axis, thus reflecting their higher complexity and

224 entropy. Minima values from both curves reflect this same difference, with the
225 value of lichen minima being much lower than that of bare rock minima (FIG. 7).

226 In addition, we found that thresholding is useful as a “dial” for extracting the
227 maximum of information for the analyzed images. For the case of the lichen
228 model, thresholding in the range of 0 and 1.5 gives the better resolution.

229 Thus, although we have the experimental advantage of “knowing” that lichens are
230 living entities, just by analyzing high definition images alone, and with the aid of
231 fractal geometry, we could readily differentiate them as distinct higher entropy
232 entities from its similar abiotic surroundings. By analyzing seasonal time series,
233 further spatial and temporal patterns changes in size and or structure
234 (tridimensional for example) could be incorporated as well.

235 In order to test our hypothesis at a larger scale, we applied our analysis to banded
236 vegetation patterns of *Tillandsia* species growing on the Atacama Desert,
237 comparing them with geological banding structures of similar appearance found
238 in the area. Similarly to the case of lichen analysis, *Tillandsia* banding growths
239 also showed lower values than those of similar geological banding patterns, thus
240 confirming their higher complexity. Analog to the case of the lichen model, curve
241 minima also reflect these differences, with *Tillandsia* values being lower than
242 geological values (FIG. 8). In this case, thresholding in the range of -1.5 and -0.5
243 gave a better resolution.

244

245 The *Tillandsia* banding pattern analysis results show that even from afar, life can
246 be distinguished as a distinctive entropy process, distinct from similar abiotic
247 processes.

248 The curve behavior of Mars banding patterns with lower FE values than of Earth
249 abiotic banding patterns but higher than biotic banding patterns remains puzzling
250 for now. As the shapes of the curves of Earth and Mars banding patterns are
251 different, but have similar minima, one may speculate if this could be either
252 reflecting differences in the geological processes that gave rise to both structures
253 or (more interestingly) some limited influence of life processes in the genesis of
254 Mars strata?

255 It is important to note that our analysis allows the estimation of the complexity of
256 datasets being analyzed, (images in this case) but as in practice the input data for
257 the FrAn software are pixel intensity numerical values, any type of data can be
258 fitted as well. Thus, future examination of extraterrestrial features could be
259 fractally analyzed with our method at different informational layers; high
260 resolution images, thermal images, elemental and isotopic compositions, pH, etc.
261 In this way, complementary fractal data values could be then overlaid in a matrix
262 to calculate a Lifeform Probability Index (LPI) for extant or past life related
263 phenomena based on their entropy measurements analysis.

264 Finally, a number of applications may be envisioned for the approach presented
265 here; rovers on distant planets could be “taught” to use the LPI with the aid of
266 artificial intelligence as a way to tag features that human experience intuitively
267 classify as “interesting”. Potential fossil structures could be compared with this
268 method, in order to appraise its true biological origin, both on Earth or elsewhere
269 in the Solar System. Radio signals from potential extraterrestrial civilizations
270 could as well be analyzed in search of fractal patterns, as use of fractal
271 mathematics may be considered as a marker of advanced technological
272 development.

273

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283 analysis of our data.

284

285

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340

341

342

343 **Figure legends**

344

345 **Figure 1.-** Sites used as models. A.- Lichen colonized rocks at the Andes
346 Mountains near Santiago. B- *Tillandsia* banding growths on sand dunes at the
347 Atacama Desert near Iquique, Chile.

348

349 **Figure 2.-** Cropped images samples. A, bare rock surface. B, lichen colonized
350 rock surface. C, Atacama Desert geological bands. D, *Tillandsia* banding growths.
351 E, Mars geological bands. F, the same image of E, after being randomized (null
352 model).

353

354 **Figure 3.-** A, The Box-counting technique applied in a theoretical fractal set (E).
355 B, Plotting the box number ($N(e)$) that includes one part of the fractal set (E) at
356 the very least, versus the size of the box (e). D, the fractal dimension, is the slope
357 of the straight fitted line. Modified from Rodríguez-Pascua *et al.*, 2003.

358

359 **Figure 4.-** Image data transformation process. High definition color images were
360 taken of colonized and uncolonized rocks, and areas of the images where only-

361 colonized and only-uncolonized surfaces were cut and stored. These subsets were
362 then transformed to gray scale and then to black and white images, this last format
363 being the input of the fractal analysis.

364

365 **Figure 5.-** Threshold importance on subsequent data analysis. As the threshold of
366 the black and white image has a direct impact on the amount of information than
367 can reconstruct the original color image, all threshold values between 0 and 256
368 were taken into account for subsequent fractal analysis.

369

370 **Figure 6.-** Fractal Excess (FE) curves of lichen colonized and bare rock surfaces.
371 Shaded areas for each curve correspond to the standard error of the means.

372

373 **Figure 7.-** Fractal excess minimum statistical analysis. Fractal excess minima of
374 the two models shown were separately analyzed by t student test and one-way
375 ANOVA (Tukey's Multiple Comparison post test) respectively. Means with
376 different letters are significantly different ($P < 0.05$; $a > b$).

377

378 **Figure 8.-** Fractal Excess curves of different banding processes on Earth and on
379 Mars. Shaded areas for each curve correspond to the standard error.

Proof For Review

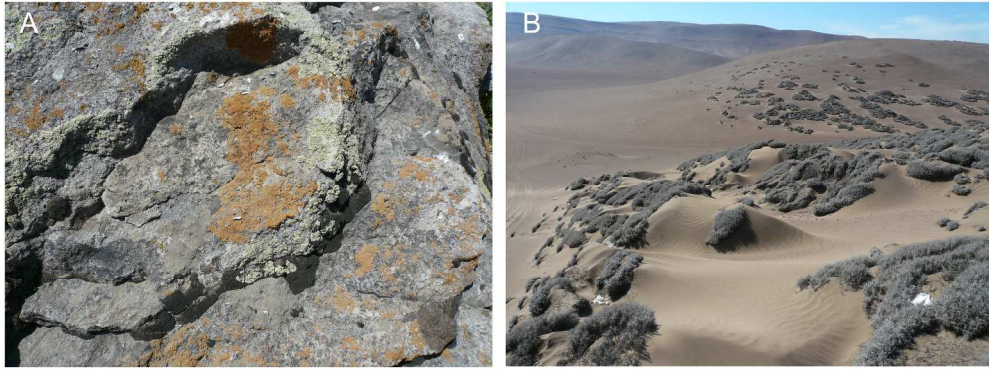


Figure 1.- Sites used as models. A.- Lichen colonized rocks at the Andes Mountains near Santiago. B- Tillandsia banding growths on sand dunes at the Atacama Desert near Iquique, Chile.
453x172mm (199 x 199 DPI)

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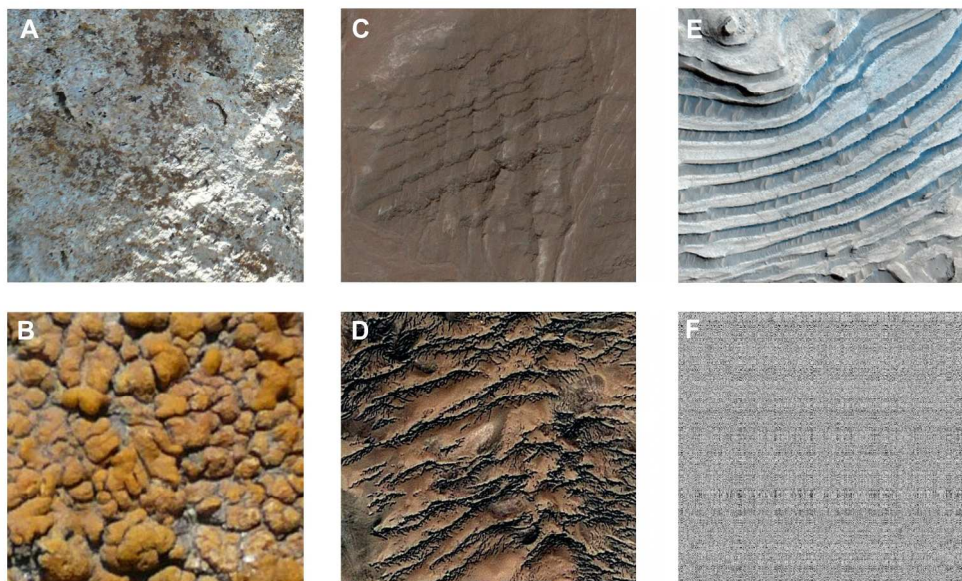


Figure 2.- Cropped images samples. A, bare rock surface. B, lichen colonized rock surface. C, Atacama Desert geological bands. D, Tillandsia banding growths. E, Mars geological bands. F, the same image of E, after being randomized (null model).
382x231mm (200 x 200 DPI)

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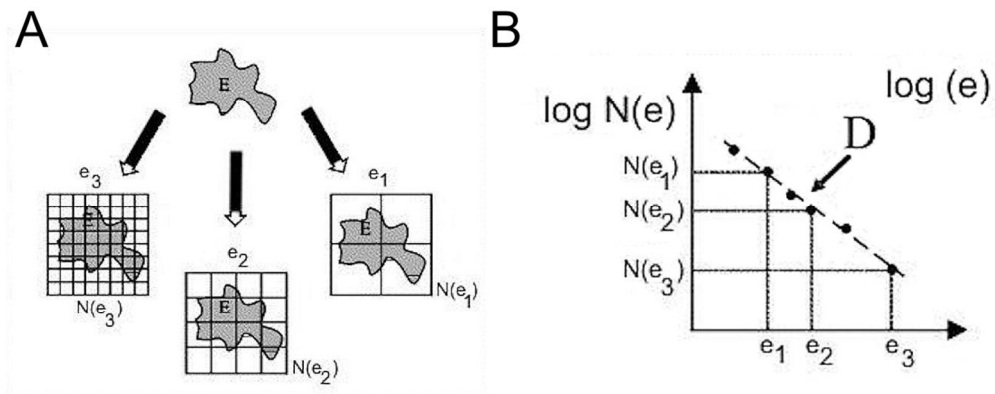


Figure 3.- A, The Box-counting technique applied in a theoretical fractal set (E). B, Plotting the box number ($N(e)$) that includes one part of the fractal set (E) at the very least, versus the size of the box (e). D, the fractal dimension, is the slope of the straight fitted line. Modified from Rodríguez-Pascua et al., 2003.
169x71mm (200 x 200 DPI)

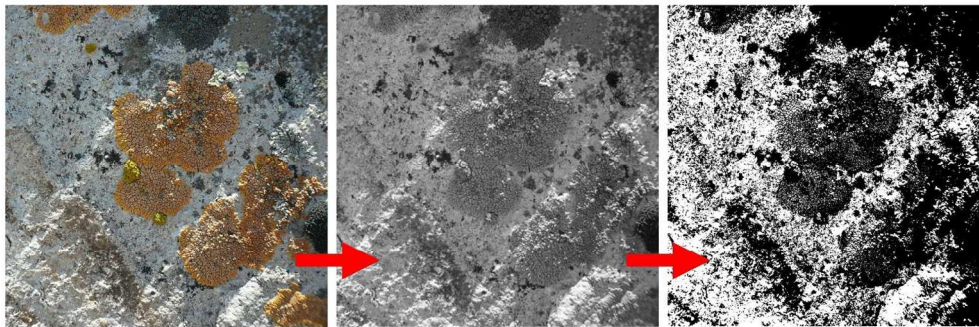


Figure 4.- Image data transformation process. High definition color images were taken of colonized and uncolonized rocks, and areas of the images where only-colonized and only-uncolonized surfaces were cut and stored. These subsets were then transformed to gray scale and then to black and white images, this last format being the input of the fractal analysis.

201x68mm (200 x 200 DPI)

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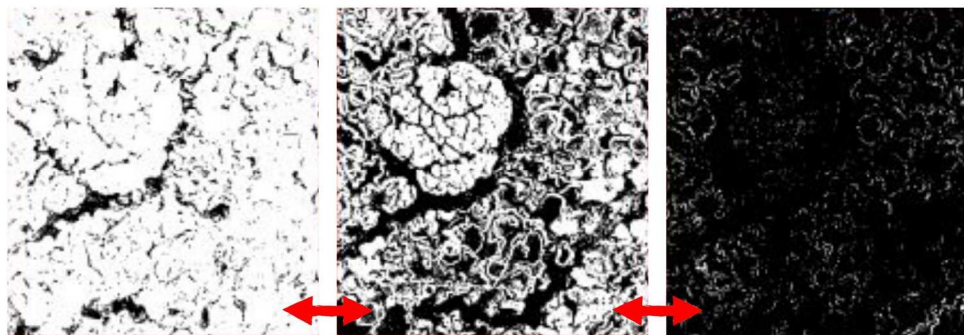


Figure 5.- Threshold importance on subsequent data analysis. As the threshold of the black and white image has a direct impact on the amount of information that can reconstruct the original color image, all threshold values between 0 and 256 were taken into account for subsequent fractal analysis.
252x91mm (200 x 200 DPI)

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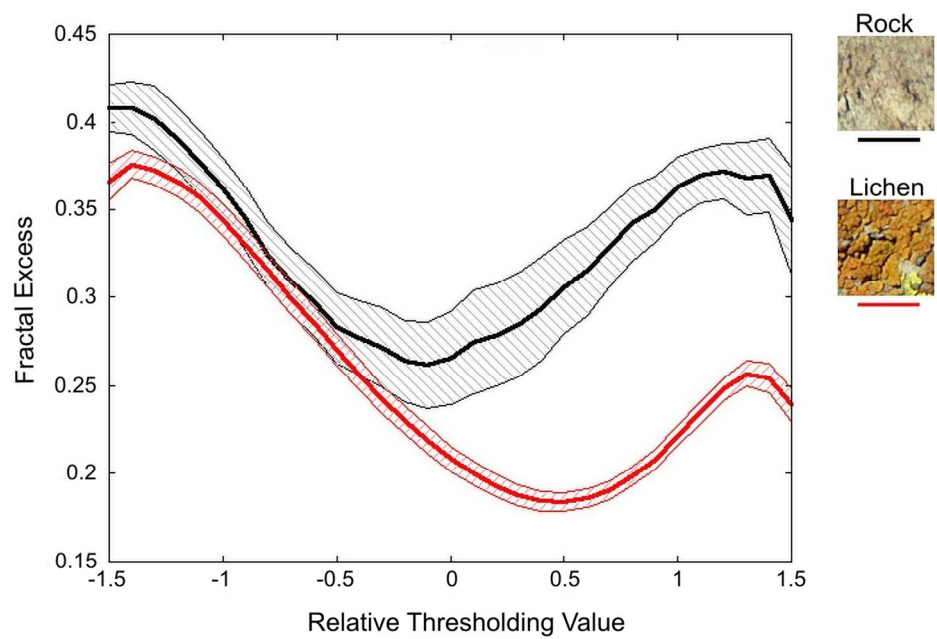


Figure 6.- Fractal Excess (FE) curves of lichen colonized and bare rock surfaces. Shaded areas for each curve correspond to the standard error of the means.
192x126mm (199 x 199 DPI)

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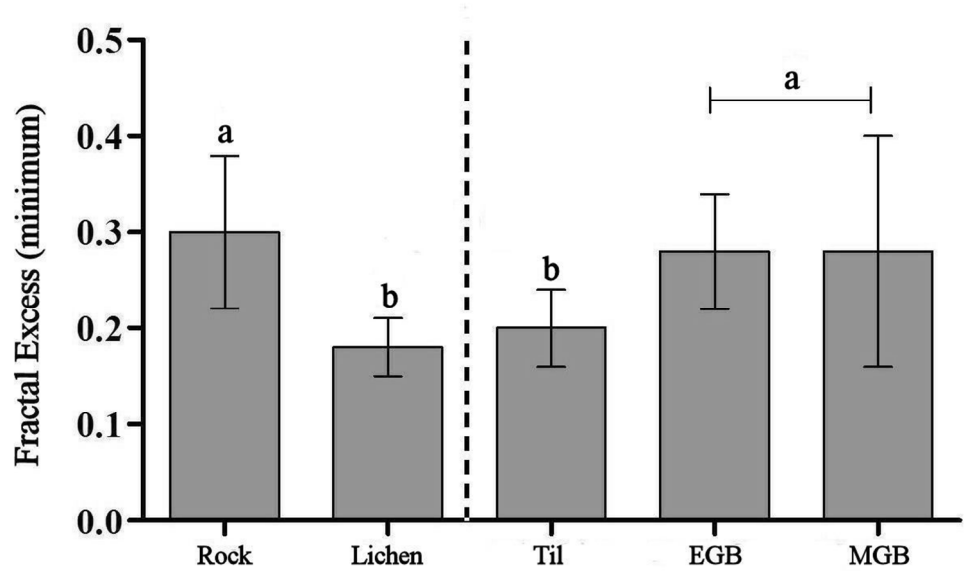


Figure 7.- Fractal excess minimum statistical analysis. Fractal excess minima of the two models shown were separately analyzed by t student test and one-way ANOVA (Tukey's Multiple Comparison post test) respectively. Means with different letters are significantly different ($P < 0.05$; $a > b$).
105x65mm (300 x 300 DPI)

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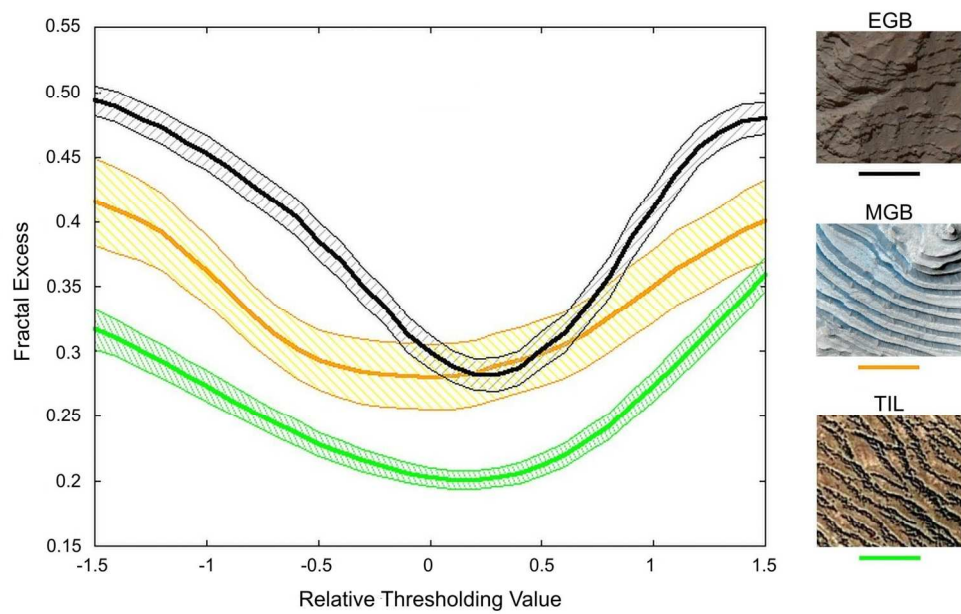


Figure 8.- Fractal Excess curves of different banding processes on Earth and on Mars. Shaded areas for each curve correspond to the standard error.
233x148mm (199 x 199 DPI)