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# Density Functional Study on the Geometric Features and Growing Pattern of  $B_nP_m$  Clusters with  $n = 1-4$ ,  $m = 1-4$ ,  $n + m \leq 5$

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The bonding features of  $B_nP_m$  clusters ( $n = 1-4$ ,  $m = 1-4$ ,  $n +$  $m \leq 5$ ) are studied within the framework of the density functional theory following a systematic growing mechanism. Some stable geometries are found to agree well with results reported previously in the literature. Other geometries are found to be more stable than structures reported elsewhere for small B/P aggregates. To the best of our knowledge, stable geometries for  $BP_4$  are reported for the first time. It is found that small B/P clusters with up to five atoms tend to grow mainly toward nonlinear bidimensional structures. The existence of  $B$ -B and  $B$ -P bonds seems to be of importance for the relative stability of clusters as they grow. The growing patterns could be explained mainly in terms of electrophilic attacks of B atoms to  $B$ -B and  $B$ -P bonds. It is found that the growing is in general accompanied by geometry reorganization and atomic charge rearrangements. Electrophilic attacks of  $P$  atoms to  $B$ -B bonds seems to be a good alternative to grow for aggregates with many B atoms. Atomic charges derived from molecular electrostatic potentials are useful to understand the growing paths followed in terms of electrophilic or nucleophilic attacks. © 2012 Wiley Periodicals, Inc.

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## Introduction

Boron and phosphorus compounds are considered systems of interest in solid-state physics and chemistry because of their potential use as refractory materials. The few experimental studies found so far are focused in obtaining stable structures by means of vapor deposition and in characterizing them by spectroscopic techniques.<sup>[1,2]</sup>

Theoretical studies, conversely, are focused in studying stabilities, equilibrium structures, and vibrational modes of small binary clusters. Linguerri and coworkers<sup>[3]</sup> studied different electronic states of BP, BP<sup>+</sup>, BP<sup>-</sup>, B<sub>2</sub>P<sub>2</sub>, (B<sub>2</sub>P<sub>2</sub>)<sup>+</sup>, and (B<sub>2</sub>P<sub>2</sub>)<sup>-</sup> using the CCSD method and a cc-pVQZ basis set. Qu and coworkers<sup>[4]</sup> investigated the electronic structures and stabilities of (BP)<sub>n</sub> aggregates, where  $n = 2-4$ , using the hybrid exchange-correlation B3LYP functional and 6-31G(d) and 6-  $311++G(2d)$  basis sets. Shi et al.<sup>[5]</sup> used the CCSD(T)/6- $311+G(d)/B3LYP/6-311+G(d)$  level of theory to study structures, potential energy surfaces, growth patterns, and stabilities of planar  $B_nP$  clusters, with  $n = 1$ –7. Burrill and Grein<sup>[6]</sup> studied structural properties of  $X_2Y_2$  (X = B, Al, Ga; Y = N, P, As) aggregates using both the B3LYP and MP2 methods with a 6-311+G(3df) basis set. Gan et al.<sup>[7]</sup> used the full (CI) and CCSD(T) methodologies with cc-pVTZ correlation consistent basis sets to investigate the properties of groups III/V diatomic molecules BN, BP, AlN, and AlP.

Clusters of  $B_nP_m$  stoichiometry (n = 1–4, m = 1–4, n + m  $\leq$ 5) are studied in this work within the framework of the density functional theory, paying special attention to the form in which clusters grow when new atoms are added up. To the best of our knowledge, this is the first work in which a systematic investigation of the growing features of both two-dimensional (2D) and 3D B/P clusters is carried out. Moreover, geometric parameters, atomization energies, and electron spin multiplicities are also reported for the more stable clusters of each size.

## Computational Methods

 $B_nP_m$  clusters (n = 1–4, m = 1–4, n + m  $\leq$  5) are studied in this work using tools from the density functional theory.<sup>[8-10]</sup> The three-parameter hybrid exchange-correlation B3LYP functional is used.<sup>[10-12]</sup> Correlation-consistent basis sets of triple-ζ quality, augmented with polarization functions are used for both B and  $P^{[13,14]}$ 

Geometry optimizations are performed using the heteronuclear diatomic aggregate, BP, as a starting point. Then, both B and P atoms are added up one at a time to form larger clusters with a maximum of five atoms. As every new atom could enter on-top, bridge or hollow sites, various starting geometries are considered for optimization of every new cluster size. The growing pattern is constructed according to the increase

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observed for the atomization energy per atom, which is defined as

$$
E_{\text{atom}} = \frac{nE_{\text{B}} + mE_{\text{P}} - E_{\text{B}_n\text{P}_m}}{n + m}
$$

where  $E_{\text{B}_{n}P_{m}}$  is the total electronic energy of the corresponding conformer and  $E_B$  and  $E_P$  are the electronic energy of the atoms in their ground state. In this way, every cluster formed by N atoms is a candidate to grow only if its atomization energy per atom is greater than that of the aggregate formed by  $N-1$  atoms from which it originates.

Geometry optimizations are performed without symmetry constraints. As the electron spin multiplicity remains fixed during the calculations, a series of geometry optimizations with varying multiplicities is performed for every cluster until the atomization energy per atom reaches its maximum value. The Hessian matrix of the total electronic energy with respect to nuclear coordinates is calculated and diagonalized to verify whether the optimized geometries are true minima or saddle points on the potential energy surface of the clusters.

To rationalize the growing pattern of  $B_nP_m$  clusters, both atomic charges derived from molecular electrostatic potentials (MEP-derived atomic charges) and spin densities (SD) per atom are calculated for every conformer. It was recently demonstrated that MEP-derived atomic charges reproduce very well the sites susceptible both to electrophilic and nucleophilic attacks that can be observed in MEP surfaces.<sup>[15]</sup> Moreover, MEP-derived atomic charges allow a quantitative ordering of those sites. SD surfaces are also very well described by the SD per atom.[15] These facts indicate that both MEP-derived atomic charges and SD per atom could be used instead of the corresponding molecular surfaces, retaining all their quantitative features at the same time. MEP-derived atomic charges are obtained according to the scheme proposed by Singh and Kollman and Merz<sup>[16,17]</sup> and SD are generated through an NBO analysis<sup>[18]</sup> performed on open-shell systems.

All calculations in this work are performed with the Gaussian 03 package, $[19]$  whereas all figures are produced with the aid of the gOpenMol program.<sup>[20,21]</sup>

## Results and Discussion

#### Geometries and atomization energies

Table 1 shows the results for BP and the  $BP_2$  and  $B_2P$  triatomic clusters and Figure 1 shows their equilibrium geometries. As can be seen from the table, BP is characterized by a triplet ground state, in good agreement with results obtained by other authors.<sup>[3-5,7]</sup> The most stable  $BP_2$  cluster is characterized by a doublet electronic state, whereas the  $B_2P$  ground state, conformer 4, presents a triangular geometry, in agreement with results reported in Ref. [5]. A close examination to the topological features of the triatomic clusters suggests that their relative stability in energy could be associated to the formation of B-P and B-B bonds. In line with that suggestion, the P-P bond could be the responsible of the low atomization energy in conformer 3.

Table 1. Atomization energies,  $E_{at}$  in eV/at, spin multiplicities,  $M_{S}$ , and symmetry for the stable B/P diatomic and triatomics found in this work.







Figure 1. Equilibrium geometries of the stable diatomic and triatomics found for B/P aggregates. White and gray circles are boron and phosphorus atoms, respectively. Numbers in parenthesis are the cluster labels, see text and Table 1. Equilibrium bond distances are indicated in A˚.

In the case of the tetratomic clusters, two stable conformers are obtained for  $BP_3$  and  $B_3P_5$ , whereas six stable conformers are found for  $B_2P_2$ , see Table 2 and Figure 2. Two aggregates that show rhombus-like geometries, 6 and 14, are BP<sub>3</sub> and B<sub>3</sub>P



ground states, respectively. Less stable tetratomic species, 7 and 15, are found at about 0.35 eV/at lower in energy than the corresponding ground states. Interestingly, conformers 6





Figure 2. Equilibrium geometries of the stable tetratomics found for B/P aggregates. White and gray circles are boron and phosphorus atoms, respectively. Numbers in parenthesis are the cluster labels, see text and Table 2. Equilibrium bond distances, r, are indicated in  $\AA$  and bond angles, a, and torsion angles, d, are shown in degrees, respectively. Bond angles not shown are equal to 180°. Torsion angles are not provided in the case of planar aggregates.

and 7 are characterized by a singlet electronic state, whereas conformers 14 and 15 exhibit a triplet electronic state. This fact is in disagreement with results reported in Ref. [5], in which a singlet electronic state is predicted to be the ground state of  $B_3P$ . The six stable species of  $B_2P_2$  are characterized by a triplet electronic state. A linear aggregate, conformer 8, is found to be the ground state of  $B_2P_2$ . It is worth mentioning that a rhombus-like structure, similar to that of conformer 11, is reported as the more stable isomer in Refs. [3, 4, 6]. Conformer 11 is 0.24 eV/at lower in energy than conformer 8 in this work. A close examination of the topological features of the tetratomic clusters suggests that their relative stability depends on the number of  $B-P$  and  $B-B$  bonds, see conformers 8, 9, and 14. Interestingly, conformer 6 is one of the more stable tetratomic clusters and presents two P-P bonds, see Figure 2. However, a detailed inspection to the geometric features of that conformer shows that the  $P-P$  bonds are considerably longer than  $P-P$  bonds in other tetratomic aggregates like  $7$ , 10, or 13, in which the P-P distance range from 1.91 to 2.05 Å. Incidentally, atomization energies of these three conformers are much lower than the atomization energy of the most stable tetratomic aggregates. These findings seem to suggest that  $P-P$  bond distances shorter than 2.05  $\AA$  contribute to decrease the relative stability of small B/P aggregates.

Table 3 lists the stable conformations found for the different pentatomic clusters studied in this work. Figures 3–5 show their corresponding equilibrium geometries. Eight stable conformers are found for  $B_2P_3$ , nine and five stable species are obtained for  $B_3P_2$  and for  $B_4P$ , respectively, and four stable structures are achieved for  $BP_4$ . The ground state of  $B_2P_3$ , conformer 16, is characterized by a doublet electronic state and a 3D structure with a slightly distorted trapezoidal geometry, see Figure 3. Interestingly, all stable  $B_2P_3$  conformers present nonlinear equilibrium structures and only conformers 17 and 23 show 2D geometries. The ground state of  $B_3P_2$ , conformer 24, is found to be a doublet electronic state and its equilibrium geometry is characterized by a slightly distorted 2D trapezoid, see Figure 4. Conformer 27 is the only linear  $B_3P_2$  conformer, whereas conformers 28, 31, and 32 are the only 3D structures. Despite the similar equilibrium geometries of conformers 31 and 32, it is worth noting that they originate from different starting structures. All stable B<sub>4</sub>P clusters adopt 2D structures, see Figure 5. Conformer 33 becomes the  $B_4P$ ground state, being characterized by a doublet electronic state, in agreement with Ref. [5]. Finally, conformer 38 is found to be the ground state of  $BP_4$ . It is characterized by a doublet electronic state and a 3D equilibrium geometry. Conformer 39 also presents a 3D equilibrium geometry, whereas conformers 40 and 41 are characterized by planar structures. The four stable  $BP_4$  conformers exhibit very low atomization energies. It is worth emphasizing that to the best of our knowledge this is the first report of stable  $BP_4$  pentatomic aggregates. It is interesting to mention that conformers 33 and 24, the pentatomic species with the higher atomization energies, are dominated





Table 3. Atomization energies,  $E_{at}$  in eV/at, spin multiplicities,  $M_s$ , and

by  $B$ —B and  $B$ —P bonds. A second set of pentatomic clusters, with atomization energies ranging from 3.50 to 3.25 eV/at, consists of conformers 16–18, 25–29, and 34–37. These species are mainly dominated by B-P bonds, with a minor contribution from  $B$ -B bonds. In the few cases in which  $P$ -P bonds are also present, the bond distances are larger than 2.05 Å, thus reinforcing the proposed argument that short  $P-P$  bonds could be responsible for the lower relative stability of B/P aggregates.

#### The growing patterns of  $B-P$  clusters

Growing patterns are studied taking the BP diatomic cluster as starting point. Seeking for simplicity, only those aggregates lying up to 0.15 eV below the ground state of every cluster size are considered as potential candidates to grow. According to the Maxwell–Boltzmann distribution, such a difference is equivalent to a contribution of the given conformer of about 5% to every cluster property measured at a temperature of 600 K.

It can be seen from Table 4 that conformer 2, the most stable BP<sub>2</sub> species, originates as a consequence of a nucleophilic attack to the B atom in the diatomic cluster. Conversely, the most stable  $B_2P$  aggregate, conformer **4**, is formed after an electrophilic attack to the  $B-P$  bond in the diatomic cluster. The other conformers, 3 and 5, lie above the threshold of 0.05 eV/at (0.15 eV/ 3 atoms) and are not considered as candidates to grow. It is interesting to note that a considerable electronic charge rearrangement takes place when conformer 2 is formed. The two P atoms become sites susceptible of nucleophilic attacks, whereas the central B atom becomes a site susceptible of electrophilic attacks. When conformer 4 is formed, an appreciable charge transfer occurs from the P atom in the diatomic species to the incoming B atom. As a consequence of that, the P atom becomes a site susceptible of nucleophilic attacks, whereas the B atoms become sites susceptible both of electrophilic and nucleophilic attacks. Interestingly, all triatomic aggregates exhibit a decrease in the electron spin multiplicity with respect to the diatomic aggregate, indicating that electrons tend to pair each other during the growing. This finding is consistent with the decrease in the SD per atom observed in 2 and 4.

It can be seen from Table 2 that the ground states of  $BP_{3}$ ,  $B_2P_2$ , and  $B_3P$ , conformers 6, 8, and 14, respectively, are separated by low-lying excited states by more than 0.04 eV/at, the threshold arbitrarily imposed before. Thus, only those three tetratomic clusters are considered as candidates for growing from the most stable triatomic aggregates. The comparison of equilibrium geometries of conformers 2 and 6, see Figures 1 and 2 and Table 5, suggests that the growing occurs through an electrophilic attack of the incoming P atom to the B atom in 2. However, the final MEP-derived atomic charges on conformer 6 would indicate whether a quite different growing mechanism or an important charge rearrangement during growing. Conformer 8 is able to grow both from 2 and 4. The criterion of an increase in the atomization energy seems to favor the  $2 \rightarrow 8$  route. Moreover, a close inspection to the three structures involved on the growing suggests that 8 grows from conformer 2 as a consequence of an electrophilic attack of a B atom to a  $B-P$  bond, which becomes completely broken in the final conformer giving place to a new  $B-P$ bond and to a brand new B-B bond. Conversely, it is argued that a  $B-P$  bond in 4 is broken due to an electrophilic attack by a P atom and an important geometry rearrangement leads to a new B-P bond. Thus, both arguments seem to favor the  $2 \rightarrow 8$  growing path, mainly due to the formation of a B-B bond. Conformer 14 grows from 4 as a consequence of an electrophilic attack of a B atom to a  $B$ -B bond. MEP-derived atomic charges confirm the mechanism above. SD per atom values show that unpaired electrons tend to remain localized into P atoms in conformer 8 and into B atoms in 14. Conformer 6 exhibits a closed-shell electronic configuration.

Only pentatomic clusters 16, 17, 24, and 33 are candidates to grow according to their atomization energies. Low-lying excited states lie above the 0.03 eV/at threshold arbitrarily imposed in this work. Conformers 38–41 are excluded from this study on growing patterns due to their low atomization energies. It is worth noting that 17 is the only excited state within the 0.03 eV/at threshold from the  $B_2P_3$  ground state, conformer 16. Conformer 16 could grow whether from conformer 6 or from conformer 8. A close examination to the equilibrium structures and MEP derived atomic charges, Figures 2 and 3 and Table 6, indicates that the  $6 \rightarrow 16$  route involves an electrophilic attack of a B atom to a  $P-P$  bond followed by an important atom reorganization and atomic charge rearrangement, which leads to an increase in the number of  $B-P$  bonds, the formation of an additional  $B-P$  bond





Figure 3. Equilibrium geometries of the stable  $B_2P_3$  pentatomic aggregates. White and gray circles are boron and phosphorus atoms, respectively. Numbers in parenthesis are the cluster labels, see text and Table 3. Equilibrium bond distances, r, are indicated in Å and bond angles, a, and torsion angles, d, are shown in degrees, respectively. Bond angles not shown are equal to 180°. Torsion angles are not provided in the case of planar aggregates.



Figure 4. Equilibrium geometries of the stable  $B_3P_2$  pentatomic aggregates. White and gray circles are boron and phosphorus atoms, respectively. Numbers in parenthesis are the cluster labels, see text and Table 3. Equilibrium bond distances, r, are indicated in Å and bond angles, a, and torsion angles, d, are shown in degrees, respectively. Bond angles not shown are equal to 180°. Torsion angles are not provided in the case of planar aggregates.



P atom to a  $B-P$  bond originates conformer 17 from 8. Thus, it is proposed that conformer 17 grows from conformer 8 after an important atomic charge rearrangement takes place. Conformer 24 could grow from 8 or from 14. It can be seen from Figures 2 and 4 that the  $8 \rightarrow 24$  route can be described as an initial electrophilic attack of a B atom to the  $B\rightarrow B$ bond followed by a geometry distortion that leads to the formation of four new bonds with an important rearrangement of MEPderived atomic charges on the B atoms. Conversely, the growing of 24 from 14 occurs as a consequence of an electrophilic attack of a P atom to a  $B$ -B bond followed by a rearrangement of the atomic charges. The criterion of maximum increase in the atomization energy favors the growing of conformer 24 from 8. Conformer 33 grows from 14 after an electrophilic attack of a B atom to a B-B bond followed by an important MEP-derived atomic charges rearrangement, even involving the P atom, which is the farthest one from the site of the attack. Interestingly, the four pentatomic species considered are characterized by a doublet electronic state. In conformers 16, 17, and 24, the unpaired electron is mainly localized on P atoms, whereas in 33 the unpaired electron is almost equally distributed between the P atom and the B atoms in the aggregate.

Figure 5. Equilibrium geometries of the stable  $B_4P$  and  $BP_4$  pentatomic aggregates. White and gray circles are boron and phosphorus atoms, respectively. Numbers in parenthesis are the cluster labels, see text and Table 3. Equilibrium bond distances, r, are indicated in  $\AA$  and bond angles, a, and torsion angles, d, are shown in degrees, respectively. Bond angles not shown are equal to 1800. Torsion angles are not provided in the case of planar aggregates.

and a decrease in the number of P-P bonds. The  $8 \rightarrow 16$ route, conversely, is formed after an electrophilic attack of a P atom to a B-P bond followed by an increase in the number of  $B-P$  bonds and the formation of a  $P-P$  bond. Both the change in the number of  $P-P$  bonds in the different routes and the criterion of maximum increase in the atomization energy seem to favor the  $6 \rightarrow 16$  growing path. Conformer 17 could grow whether from conformer 6 or from conformer 8. Although the maximum increase in the atomization energy is observed for the  $6 \rightarrow 17$  growing route, it can be deduced from the equilibrium structures, see Figures 2 and 3, that two bonds should be broken at least to go from 6 to 17, suggesting that non-negligible energy barriers could be involved in the growing process. Instead, a simple electrophilic attack of a

Table 4. MEP-derived atomic charges, in units of |e|, and SD per atom as obtained from NBO calculations (see text) in atomic units and in parenthesis, for the stable B/P diatomic and triatomics found in this work.





Table 5. MEP-derived atomic charges, in units of  $|e|$ , and SD per atom as obtained from NBO calculations (see text) in atomic units and in parenthesis, for the stable B/P tetratomics found in this work.



\n- $$
0
$$
  $1 \rightarrow 4 \rightarrow 14 \rightarrow 33$
\n- $1 \rightarrow 4 \rightarrow 14 \rightarrow 24$
\n- $1 \rightarrow 2 \rightarrow 8 \rightarrow 24$
\n

It can be deduced from the paths above and the preceding discussion that the growing mechanism in small  $B-P$  aggregates is dominated by electrophilic attacks of B atoms to  $B$ -B and  $B$ -P bonds. The exceptions are the  $14 \rightarrow 24$  path, which is characterized by an electrophilic attack of a P atom to a B-B bond and the  $1 \rightarrow 2$  path, which is described as a nucleophilic attack of a P atom to a B atom. Changes in electron spin multiplicities and electron localization during growing are difficult to rationalize.

Table 6. MEP-derived atomic charges, in units of |e|, and SD per atom as obtained from NBO calculations (see text) in atomic units and in parenthesis, for the stable B/P pentatomics found in this work.



The previous analysis indicates that five patterns could describe the form in which small  $B-P$  clusters grow, namely, 1  $\rightarrow$  2  $\rightarrow$  6  $\rightarrow$  16, 1  $\rightarrow$  2  $\rightarrow$  8  $\rightarrow$  17, 1  $\rightarrow$  2  $\rightarrow$  8  $\rightarrow$  24, 1  $\rightarrow$  4  $\rightarrow$  14  $\rightarrow$  24, and 1  $\rightarrow$  4  $\rightarrow$  14  $\rightarrow$  33. The first two growing paths show an increase in the atomization energy of about 1.60 eV/at when passing from 1 to 16 and to 17. Conversely, the last three growing patterns exhibit an increase in the atomization energy of about 1.90 eV/at when passing from 1 to 24 and to 33. According to these differences, it is proposed as the most probable growing paths for small  $B-P$  clusters are

## **Conclusions**

Geometric features of  $B_nP_m$  ( $n = 1-4$ ,  $m = 1-4$ ,  $n + m \le 5$ ) were studied in this work within the framework of the density functional theory. The growing pattern of the most stable aggregates was rationalized with the aid of useful tools obtained from calculations.

Present results indicate that small clusters formed by B and P tend to adopt bidimensional geometries in most cases. The most stable structures found for  $B_2P$ ,  $B_3P$ , and  $B_4P$  agree quite well with results reported previously. For  $B_2P_2$ , a linear



geometry is found to be more stable than the rhombus-like structure reported previously elsewhere. Several stable geometries for  $BP_4$  are reported for the first time. It is proposed that the higher atomization energies are closely related to the existence both of B-P and of B-B bonds, whereas short P-P bonds are responsible for the relative lower atomization energies.

The growing pattern of small B/P clusters is governed mainly by electrophilic attacks of an incoming B atom to  $B-P$ or B-B bonds present in the aggregate of smaller size. The electrophilic attack of an incoming P atom to a  $B$ -B bond seems to be an alternative for growing when clusters are saturated with B atoms. It was found that atomic charges derived from MEPs are useful to describe the growing patterns whether in terms of nucleophilic or in terms of electrophilic attacks. Conversely, changes in electron multiplicity are difficult to rationalize.

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Keywords: B/P clusters  $\cdot$  growing pattern  $\cdot$  density functional theory

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