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Improving Pre-movement Pattern Detection with Filter Bank Selection

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Abstract.

Objective: Pre-movement decoding plays an important role in detecting the onsets of actions using low-frequency electroencephalography (EEG) signals before the movement of an upper limb. In this work, a binary classification method is proposed between two different states.

Approach: The proposed method, referred to as filter bank standard task-related component analysis (FBTRCA), is to incorporate filter bank selection into the standard task-related component analysis (STRCA) method. In FBTRCA, the EEG signals are first divided into multiple sub-bands which start at specific fixed frequencies and end frequencies that follow in an arithmetic sequence. The STRCA method is then applied to the EEG signals in these bands to extract canonical correlation patterns. The minimum redundancy maximum relevance feature selection method is used to select essential features from these correlation patterns in all sub-bands. Finally, the selected features are classified using the binary support vector machine classifier. A convolutional neural network (CNN) is an alternative approach to select canonical correlation patterns.

Results: Three methods were evaluated using EEG signals in the time window from two seconds before the movement onset to one second after the movement onset. In the binary classification between a movement state and the resting state, the FBTRCA achieved an average accuracy of 0.8968 ± 0.0847 while the accuracies of STRCA and CNN were 0.8228 ± 0.1149 and 0.8828 ± 0.0917 , respectively. In the binary classification between two actions, the accuracies of STRCA, CNN, and FBTRCA were 0.6611 ± 0.1432 , 0.6993 ± 0.1271 , 0.7178 ± 0.1274 , respectively. Feature selection using filter banks, as in FBTRCA, produces comparable results to STRCA.

Significance: The proposed method provides a way to select filter banks in pre-movement decoding, and thus it improves the classification performance. The improved pre-movement decoding of single upper limb movements is expected to provide people with severe motor disabilities with a more natural, non-invasive control of their external devices.

Keywords: Brain Computer Interface, Movement Detection, Pre-movement Decoding, Standard Task-Related Component Analysis, Filter Bank Selection

1. Introduction

Movements of the human limbs lead to potential changes on the human scalp, which can be observed with non-invasive brain-computer interface-based electroencephalography (EEG) signals [1,2]. In previous studies on movement detection with EEG signals, motor imagery (MI) is one of the most frequently used brain activities in the motor cortex [3–5]. When the limbs begin moving, the power of EEG signals in alpha rhythm (frequency range: $8 \sim 12$ Hz) and beta rhythm (frequency range: $13 \sim 30$ Hz) shows an upward or downward trend, which is called event-related desynchronization/synchronization [6]. When humans imagine a movement of the left or right limb, the power changes in the left/right half of the scalp. However, these power changes in MI occur after the limb moves, which implies that in MI analysis movement can only be detected after the onset of the imagined movement [6]. Looking at the

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brain activity through the movement-related cortical potential (MRCP), the movement of human limbs or the resting state before the movement onset can be evaluated. Hence, MRCP is expected to help enhance the restoration of useful motor functions and reduce the time delay of movement detection [7, 8].

MRCP is a type of low-frequency EEG signal (frequency range: $0.5\sim 10\text{ Hz}$) acquired in the motor cortex [9–11]. MRCP analysis is applied to EEG signals located around the movement onset. The readiness potential (RP) section is the stage that starts from 2 seconds before the onset and ends on the onset [12], while the movement monitoring potential (MMP) section is the stage that starts on the onset and ends 1 second after that [12]. The pre-movement patterns decoded from the RP section in MRCP signals cannot be observed directly. Grand average MRCP is a way to visualize the pre-movement patterns (Figure 1). In grand average MRCP, EEG signals acquired from the motor cortex are averaged across trials. The grand average MRCP of the upper limb movement shows an increase followed by a rapid decrease around the onset compared to the relatively steady grand average MRCP of the resting state. The pre-movement patterns are the features extracted from the RP section based on the grand average MRCP [13, 14].

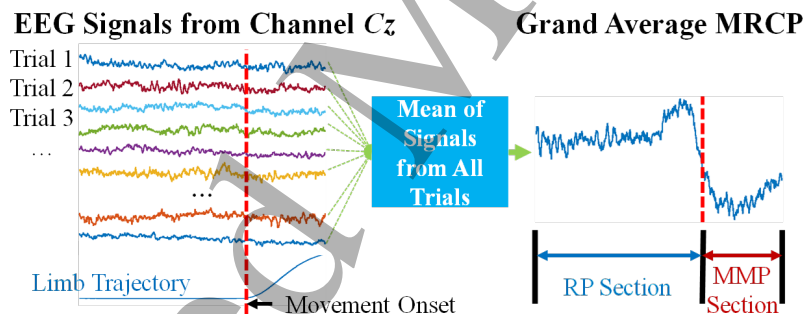


Figure 1. The concept of grand average MRCP. Multiple trials are obtained for MRCP analysis in the EEG paradigm by repeating the same limb movement. Therefore, EEG signals have three dimensions (channel, time and trial). Since the grand average MRCP is obtained by averaging all the trials, it has two dimensions (channel and time). In this figure, channel C_z is used as an example. The movement onset is the onset of the action when the limb begins to move. The grand average MRCP of the action shows an increase followed by a decrease around the movement onset.

By analyzing the grand average MRCP, some previous works focused on the binary classification between a movement state and the resting state or the binary classification between two actions. For instance, Jeong *et al.* proposed the subject-dependent and section-wise spectral filtering method (SSSF) to extract the amplitude features in MRCP and successfully solved the two-class problem between movement and resting states [15]. This method uses the mean amplitude of MRCP signals in both RP and MMP sections as the features. To optimize the selected features, Jeong *et al.* adopted a cross-validation and testing method to select the best frequency range for each subject. Ofner *et al.* proposed the discriminative spatial pattern method (DSP) [16], which calculates

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a linear discriminant analysis classifier for every time step. It was shown that the accuracy increases as the time point approaches the onset of the action in both the RP and MMP sections. Mammone *et al.* proposed the deep convolutional neural network (DCNN) [14], which decodes pre-movement patterns from time-frequency maps of EEG signals at the source level. Duan *et al.* proposed a pre-movement pattern decoding method, the standard task-related component analysis (STRCA) [13] consisting of the task-related component analysis (TRCA) spatial filter and the canonical correlation pattern (CCPs) features. All the methods mentioned above, except for the subject-dependent and section-wise spectral filtering method, are also a solution to the binary classification between two actions. In Table 1, the binary classification results of each method are given.

Table 1. Binary Classification Results in Pre-movement Decoding

Method	Movement vs Resting	Movement vs Movement
STRCA [13]	0.8287 ± 0.1101	0.5970 ± 0.1424
DCNN [14]	0.9030 ± 0.0560	0.6247 ± 0.0070
SSSF [15]	0.7300 ± 0.0783	-
DSP [16]	0.8500 ± 0.0500	0.4400 ± 0.0700

Although STRCA has a very concise structure, it faces the frequency range selection problem when decoding pre-movement patterns in MRCP analysis. In both the SSSF and DCNN methods, the frequency characteristics of the EEG signals is considered when optimizing the two classification methods. The frequency characteristics are optimized by either using filter bank selection with cross-validation and testing or by constructing a time-frequency map [14, 15]. Considering this, it can be seen that STRCA could be further improved with the filter bank technique.

Filter bank selection aims to solve the feature selection problem among various sub-bands in the frequency domain. It is widely used to analyze brain activity such as in MI and in steady-state visually evoked potential (SSVEP). In SSVEP analysis, the canonical correlation analysis method is a classical method used for detecting stimulus frequencies [17]. Canonical correlation analysis can measure the similarity between EEG signals and the reference signals, and many methods in SSVEP analysis have been developed based on this technique [18–20]. Filter bank canonical correlation analysis was proposed to incorporate harmonic and fundamental frequency components, which improved the detection of standard canonical correlation analysis in SSVEP [21]. Without the filter bank technique, the canonical correlation analysis faces the problem of selecting frequency components. In MI analysis, the common spatial pattern method is the most classical one [22]. The method extracts the logarithm-variance features from the EEG signals filtered by the spatial filter, and it shows a varying accuracy among the sub-bands in alpha (8~12 Hz) and beta (13~30 Hz) rhythms [3, 23]. Filter bank common spatial pattern is an advanced MI analysis method that was developed

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by combining the common spatial pattern method and the filter bank technique [24]. The method is able to avoid sub-band selection, thus achieving better and more stable accuracies than the common spatial pattern method.

In both MI and SSVEP analysis, the filter bank technique uses a feature selection method to optimize the extracted common spatial pattern features or the canonical correlation features in each sub-band. The optimal frequency range of the filter bank varies among the subjects due to individual differences. The feature selection method overcomes the frequency range selection problem and enables the classification to achieve a stable and accurate result. When applying the filter bank technique to STRCA, there are three problems to tackle:

- (1) The frequency range setting is unknown, so it is unclear how the starting and stopping frequencies of the sub-bands in the filter bank technique can be selected;
- (2) The feature selection method for STRCA is undetermined;
- (3) The feature arrangement is unclear when applying the feature selection method on STRCA features extracted from all sub-bands.

This study aims to analyze how to incorporate the filter bank technique into STRCA. Two steps are adopted for the improvement of the STRCA method in this work: firstly, three feature range settings are compared to decide how to select the frequency range of each sub-band in pre-movement decoding; secondly, a new filter bank TRCA (FBTRCA) method is proposed to decode the pre-movement patterns for the binary classification between a movement state and the resting state or between two actions.

FBTRCA consists of four steps: frequency bank division, spatial filtering, feature selection and classification. In the first step, the EEG signals are bandpassed into multiple sub-bands in the low-frequency domain. In the second step, canonical correlations are extracted from each of these sub-bands by the STRCA method. In the third stage, a feature selection algorithm is used to select the essential features from the features of all bands automatically. In the fourth step, a classifier is used to classify the selected features. This paper presents a selection of feature selection methods and classifiers for use in FBTRCA, and recommends suitable feature selection and classifiers for MRCP-based brain-computer interface.

In Section 2, the EEG dataset and the data pre-processing mechanism used are introduced, and the proposed FBTRCA method is described. In Section 3, the proposed method is analysed in terms of the frequency range settings, the feature selection and when compared to other methods. In Section 4, the FBTRCA design and workings in pre-movement decoding is discussed. Finally, Section 5 contains the conclusions for this study.

To facilitate the understanding of the contents in this work, the abbreviations are given in Table 2.

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Table 2. Descriptions of Abbreviations

Abbreviation	Full Name	Description
EEG MRCP MI SSVEP	Electroencephalograph Movement-Related Cortical Potential Motor Imagery Steady State Visual-Evoked Potential	Multi-channel signals acquired from the surface of brain scalp. A kind of brain activity related to pre-movement. A kind of brain activity related to movement. A kind of brain activity evoked by visual stimulus.
RP MMP	Readiness Potential Movement Monitoring Potential	EEG signals in the two-second window before the movement onset. EEG signals in the one-second window after the movement onset.
CCA FBCCA CSP FBCSP SSSF	Canonical Correlation Analysis Filter Bank Canonical Correlation Analysis Common Spatial Pattern Filter Bank Common Spatial Pattern Subject-dependent and section-wise spectral filtering	A basic classification method in SSVEP [17]. A method that optimizes CCA by filter bank selection [21]. A basic classification method in MI [22]. A method that optimizes CSP by filter bank selection [24]. A binary classification method for movement and resting states [15].
STRCA FBTRCA	Standard Task-Related Component Analysis Filter Bank Tasked-Related Component Analysis	A binary classification method for movement and resting states [13]. The method that optimizes STRCA by filter bank selection.
TRCA CCP	Task-Related Component Analysis Canonical Correlation Pattern	The spatial filter used in STRCA [13]. The extracted features in STRCA [13].
CNN MIQ MAXREL MINRED MRMR QPFS CIFE CMIM MRMTR	Convolutional Neural Network Mutual Information Quotient Maximum Relevance Minimum Redundancy Minimum Redundancy Maximum Relevance Quadratic Programming Feature Selection Conditional Infomax Feature Extraction Conditional Mutual Information Minimization Maximum Relevance Minimum Total Redundancy	A feature selection method consists of convolutional layers. A feature selection method based on mutual information [25]. A feature selection method based on mutual information [26]. A feature selection method based on mutual information [26]. A feature selection method based on mutual information [26]. A feature selection method based on mutual information [26]. A feature selection method based on mutual information [27]. A feature selection method based on mutual information [28]. A feature selection method based on mutual information [29]. A feature selection method based on mutual information [30].
SVM LDA NN	Support Vector Machine Linear Discriminant Analysis Neural Network	A binary classifier A binary classifier A binary classifier

2. Material and Method

2.1. Dataset Description

There are two public datasets used in this work, namely dataset I and dataset II [16, 31] ‡. Both datasets follow an offline acquisition paradigm in which a trial lasts five seconds. At the start of a trial, the computer screen displays a cross and emits a beeping sound. The computer screen then shows a cue that indicates the required movement or resting two seconds later. When the cue occurs, the subjects implement movements or remain at rest.

The EEG signals are acquired from 11 channels with active electrodes. These channels are located around the motor cortex. According to the 10/20 international system, 5 out of the 11 electrodes are located at the centre of the motor cortex: FC_z , C_3 , C_z , C_4 , CP_z ; while the remaining 6 electrodes are located surrounding the motor cortex: F_3 , F_z , F_4 , P_3 , P_z , P_4 . The EEG signals are filtered with an 8-order Chebyshev bandpass filter from 0.01 Hz to 200 Hz. The sample rate of the EEG signals is 512 Hz, and the signals are downsampled to 256 Hz considering the computational load. A notch filter at 50 Hz is applied to avoid the influence of power line interference.

There are two main differences between the two datasets.

Firstly, dataset I contains signals related to hand movement trajectories acquired using a glove sensor. The onsets of the actions can be located with the movement

‡ <http://bnci-horizon-2020.eu/database/data-sets>,

Dataset I : 25. Upper limb movement decoding from EEG (001-2017) [16];

Dataset II: 26. Attempted arm and hand movements in persons with spinal cord injury (001-2019) [31].

trajectories of the limb. Dataset II, on the other hand, does not contain information about limb movement trajectories.

Secondly, both datasets have different actions and number of subjects. Dataset I consists of 7 states with 15 subjects. These states include the resting state *rest* and 6 actions: *elbow flexion*, *elbow extension*, *supination*, *pronation*, *hand close* and *hand open*. For each action, 60 trials were acquired during the signal acquisition. Dataset II, on the other hand, consists of EEG signals from 9 subjects. Each subject was asked to implement 5 actions, including *supination*, *pronation*, *hand open*, *palmar grasp* and *lateral grasp*. Each action has 72 trials.

In dataset I, the onset can be located from the hand trajectory when the movement is executed. However, the onset cannot be located in dataset II. Therefore, different processing procedures were adopted in the two datasets.

2.1.1. Pre-processing in Dataset I The STRCA method has been evaluated on dataset I in previous studies [13]. Here, we adopt the same pre-processing procedure. In dataset I, the hand movement trajectory is used to locate the movement onsets of the actions. The 1-order difference of the trajectory is taken, and then the 1-order Savitzky-Golay finite impulse response smoothing filter is used to smooth the signals. The length of the time window in the smoothing filter is set to 31. The starting value of the trajectory is subtracted from the trajectory in each trial. The approximate range of the onsets of the actions is the three-second time window with a one-second delay after the cue.

The two motions related to elbow movement, which are *elbow flexion* and *elbow extension*, lead to an increase in the amplitude of the hand trajectory. The trajectory is first changed into the absolute value. The hand trajectories are normalized by dividing them by the maximal absolute value. The location where the normalized trajectory is larger than the threshold of 0.05 is regarded as the movement onset. In trials that contain heavy noise contamination, the onsets of these actions cannot be located, and therefore these are manually removed.

For the other four states, the approximate range of the onset shrinks to a two-second time window with a one-second delay after the cue. The hand trajectory has a lower amplitude and is heavily influenced by noise. In these trials, trajectories are first normalized by dividing them by the maximal absolute value of each trajectory. The function $f(x) = a * \exp(-(\frac{x-b}{c})^2) + d$ is used to fit the smoothed and normalized trajectories by tuning the parameters a, b, c, d . The symbol 'exp' denotes the exponential function. Trials that fulfil $a < 0.05, c > 100$ and $d > 10$ are rejected. The onsets of the actions are determined by a threshold criterion, as the bias d is removed from the fitted function $f(x)$ and the onset is set to the location where the value of $f(x)$ is larger than 0.1.

For the signals in the resting state, the amplitude of the hand trajectory is supposed to be steady and have a small variance. The trials are rejected if the variances of the trajectories are greater than the set threshold of 0.02. The trajectories in the resting state have no movement onset. A fake onset is set to 2.5 s following the beeping sounds.

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In Table 3, the number of trials after eliminating the rejected ones is given. The number of trials of these motions is averaged among all trials in dataset I and is rounded to an integer in the table.

Table 3. Average Number of Trials Across Subjects After Trial Rejection

Motion	<i>elbow flexion</i>	<i>elbow extension</i>	<i>supination</i>	<i>pronation</i>	<i>hand close</i>	<i>hand open</i>	<i>resting</i>
Number	60	59	52	51	56	55	59

The EEG signals can be divided into the RP and MMP sections with the located onsets or fake onsets. The features extracted from the RP section are the pre-movement patterns. In dataset I, we analyze the classification in two cases. In the first case, the EEG signals are from the RP section, and the results are used to analyze the performance of the proposed method in pre-movement decoding. In the second case, the EEG signals are from the RP and MMP sections. In Figure 1, the grand average MRCP shows an increasing trend, so therefore we assume that the EEG signals from both RP and MMP sections may improve the performance compared to the EEG signals from only the RP section.

2.1.2. Pre-processing in Dataset II The onsets of the actions in dataset II cannot be located by movement trajectory. Here, we adopt the same processing procedure in motor imagery as in [32]. EEG signals are extracted from the two-second time window after the cue. The onset is located within this time window, but the precise location is unknown.

Dataset II has five trial-based actions. Compared to the resting state of dataset I, the EEG signals in the resting state are not trial-based. Subjects were asked to have a long-duration rest after acquiring the EEG signals of the actions. The resting state for dataset II is generated by dividing the long-duration resting-state EEG signals into multiple trials. Each trial lasts 2 seconds, and there are 72 trials for each subject in total.

The data obtained was denoted as $\mathbf{X} \in \mathbb{R}^{N_c \times N_s \times N_t}$ or $X(t) \in \mathbb{R}^{N_c \times N_t}$, $t = 1, \dots, N_s$, where N_c is the EEG channel number, N_s is the sample time and N_t is the number of trials. Before the binary classification tasks, EEG signals were normalized by z-score normalization. When evaluating STRCA and the proposed FBTRCA methods with this dataset, 10-fold cross-validation was applied, and the classification performance was calculated as the mean of these 10 folds. The binary classification was implemented between two motions, *e.g.* *elbow flexion* vs *elbow extension* and *elbow flexion* vs *resting* in dataset I. Therefore, dataset I has 21 motion pairs, while dataset II has 15 motion pairs.

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2.2. Filter Bank Task-Related Component Analysis

2.2.1. *Standard Task-Related Component Analysis* STRCA is used to classify the EEG signals between a movement state and the resting state with MRCP signals in the RP section [13]. The method consists of two components: (1) spatial filter TRCA and (2) CCP features. The extracted features are classified with the linear discriminated analysis (LDA) classifier. Figure 2 illustrates the structure of STRCA.

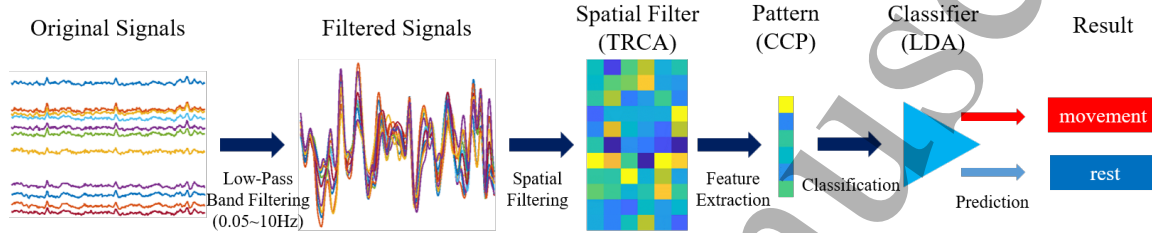


Figure 2. The structure of STRCA consists of the spatial filter TRCA and the extracted CCP features.

TRCA: The spatial filter of TRCA is designed by maximizing the reproducibility during the task [33]. In multichannel EEG signals, the training set is supposed to be $X^k(t) \in \mathbb{R}^{N_c \times N_t}$, where k refers to the class of the EEG signals, $k = 1, 2$. $X(t)$ consists of two kinds of signals: (1) task-related signals $s(t) \in \mathbb{R}$ and (2) task-unrelated noise $n(t) \in \mathbb{R}$. The relationship between $X(t)$, $s(t)$ and $n(t)$ is expressed by:

$$X_{i,j}^k(t) = a_{1,i,j}^k s(t) + a_{2,i,j}^k n(t), \quad i = 1, \dots, N_c, \quad j = 1, \dots, N_t. \quad (1)$$

$y(t)$ is the linear sum of EEG signals $X(t)$, and is defined as:

$$y_j^k(t) = \sum_{i=1}^{N_c} w_i^k X_{i,j}^k(t), \quad j = 1, \dots, N_t. \quad (2)$$

In TRCA, the task-related signal $s(t)$ is recovered from $y(t)$. The ideal solution is difficult to calculate but can be approached by maximizing the inter-trial covariance. The covariance C_{j_1, j_2}^k between the j_1 -th trial and the j_2 -th trial can be computed using:

$$C_{j_1, j_2}^k = Cov(y_{j_1}^k(t), y_{j_2}^k(t)) = \sum_{i_1, i_2}^{N_c} w_{i_1}^k w_{i_2}^k Cov(X_{i_1, j_1}^k(t), X_{i_2, j_2}^k(t)). \quad (3)$$

The covariances of all the trials are summed to obtain a combination of all trials:

$$\begin{aligned} \sum_{\substack{j_1, j_2=1 \\ j_1 \neq j_2}}^{N_t} C_{j_1, j_2}^k &= \sum_{\substack{j_1, j_2=1 \\ j_1 \neq j_2}}^{N_t} Cov(y_{j_1}^k(t), y_{j_2}^k(t)) \\ &= \sum_{\substack{j_1, j_2=1 \\ j_1 \neq j_2}}^{N_t} \sum_{i_1, i_2=1}^{N_c} w_{i_1}^k w_{i_2}^k Cov(X_{i_1, j_1}^k(t), X_{i_2, j_2}^k(t)) = \mathbf{w}^T S^k \mathbf{w}. \end{aligned} \quad (4)$$

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To avoid infinite solutions of \mathbf{w} , the variance of $y_j^k(t)$ is constrained to 1:

$$\begin{aligned} \sum_{j_1, j_2=1}^{N_t} C_{j_1, j_2}^k &= \sum_{j_1, j_2=1}^{N_t} Cov(y_{j_1}^k(t), y_{j_2}^k(t)) \\ &= \sum_{j_1, j_2=1}^{N_t} \sum_{i_1, i_2=1}^{N_c} w_{i_1}^k w_{i_2}^k Cov(X_{i_1, j_1}^k(t), X_{i_2, j_2}^k(t)) = \mathbf{w}^T Q^k \mathbf{w}. \end{aligned} \quad (5)$$

The constrained spatial filter can be obtained by maximizing the generalized eigenvalue equation J , which is expressed as:

$$J = \frac{\mathbf{w}^T S^k \mathbf{w}}{\mathbf{w}^T Q^k \mathbf{w}}. \quad (6)$$

Eigenvectors are obtained by solving the generalized eigenvalue problem. The eigenvectors with the largest eigenvalues are selected as the eigenvectors that are to be used in the spatial filter. Three eigenvectors are adopted in TRCA. These eigenvectors from two classes are then combined into the TRCA spatial filter. The TRCA spatial filter that we obtained is $W \in \mathbb{R}^{N_c \times 6}$.

CCP: Using the training set of EEG data, $\mathbf{X}^k \in \mathbb{R}^{N_c \times N_s \times N_t}$, $k = 1, 2$, we can obtain the CCP templates $\hat{X}^k = \sum_{j=1}^{N_t} \mathbf{X}^k / N_t \in \mathbb{R}^{N_c \times N_s}$, $k = 1, 2$ for each of the two classes. The EEG signal of the trial from which we aim to extract features is $X \in \mathbb{R}^{N_c \times N_s}$. Given the TRCA spatial filter W , we extract the CCP after the EEG signals are transformed with W . Three kinds of correlation coefficients are considered in STRCA:

(1) Correlation coefficients between filtered signals:

$$X_k = \hat{X}^k; X_* = X; \quad (7)$$

$$\rho_{1,k} = corr(X_*^T W, X_k^T W), \quad k = 1, 2; \quad (8)$$

(2) Correlation coefficients between filtered signals with a canonical correlation analysis projection:

$$X_k = \hat{X}^k; X_* = X; \quad (9)$$

$$[A_k, B_k] = cca(X_*^T W, X_k^T W) \quad (10)$$

$$\rho_{2,k} = corr(X_*^T W B_k, X_k^T W B_k), \quad k = 1, 2; \quad (11)$$

(3) Correlation coefficients between the distances of filtered signals:

$$\hat{X}_k = \hat{X}^k - \hat{X}^{3-k}; X_* = X - \hat{X}^{3-k}; \quad (12)$$

$$[A_k, B_k] = cca(X_*^T W, X_k^T W) \quad (13)$$

$$\rho_{3,k} = corr(X_*^T W A_k, X_k^T W A_k), \quad k = 1, 2. \quad (14)$$

In the above equations, canonical correlation analysis is used to optimize the correlation between the templates \hat{X}^k and X . The function symbols *corr* and *cca* indicate the calculation process of the correlation coefficient and the process of CCA analysis, respectively. For each trial, we can obtain six features, which are referred to as CCP features in the following section.

2.2.2. *Filter Bank TRCA* This study proposes an FBTRCA method to enhance pattern decoding in MRCP analysis. Figure 3 shows the flowcharts of the proposed method, which consists of three major procedures: (1) filter bank analysis, (2) CCP feature extraction and (3) feature selection.

First, in the filter bank technique, the sub-bands are decomposed with multiple filters that have different pass-bands. In this study, the bandpass filter used for extracting sub-band components from the original EEG signals was an 8-order infinite impulse Butterworth filter.

STRCA is then applied to each sub-band separately, resulting in six CCP features. The number of sub-bands is denoted as m , such that the number of CCP features extracted from all sub-bands is $6 \times m = 6m$. The essential features are extracted from the $6m$ features in all sub-bands using one of the feature arrangement types. The feature arrangement type refers to the arrangement of the $6m$ CCP features when the feature selection method is applied.

Finally, the selected essential features are classified with the binary classifier. This study compares two classifiers, including the LDA and the support vector machine (SVM).

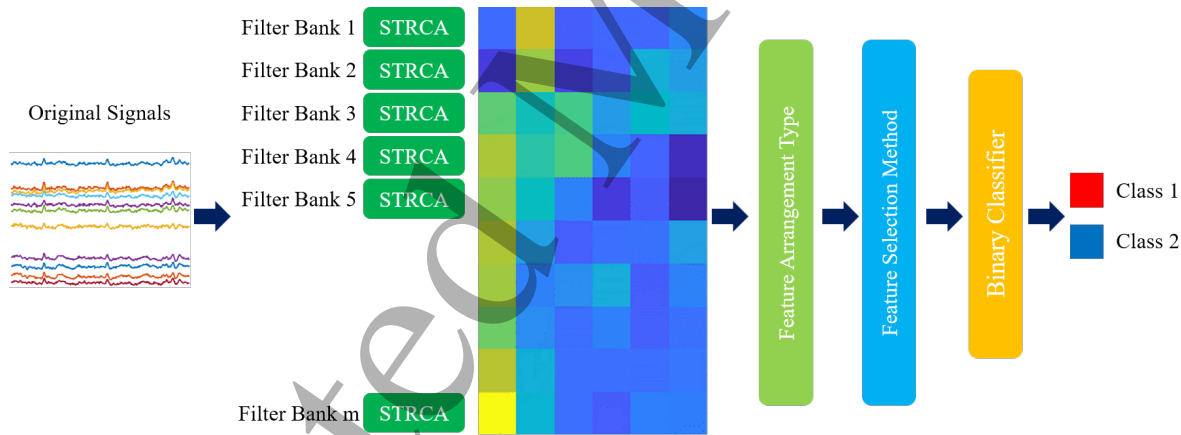


Figure 3. The structure of FBTRCA. CCP features are extracted from EEG signals using various filter banks, and a total of $6 \times m$ features are obtained. Then, feature selection methods are used to extract the essential features. A binary classifier is used to classify the selected essential features and predict the state of the EEG signals (movement or resting).

2.2.3. *Frequency Range Settings* In the decomposition of sub-bands, the decomposed EEG signals and classification accuracies vary with different frequency range settings of the filters. In the MI analysis, the frequency range of the filter banks was equipped with equally spaced bandwidths in alpha and beta rhythms, *e.g.* $4 \sim 8$ Hz, $8 \sim 12$ Hz, ..., $36 \sim 40$ Hz [32]. In the SSVEP analysis, the frequency range of the filter banks started at $n \times 8$ Hz and ended at a fixed frequency, *e.g.* $8 \sim 88$ Hz, $16 \sim 88$ Hz, ..., $80 \sim 88$ Hz, $n = 1, 2, \dots, 10$ [21].

Improving Pre-movement Pattern Detection with Filter Bank Selection 12

In MRCP analysis, the frequency range setting is undetermined. Considering that MRCP signals are a type of EEG signal with low frequencies, the maximum high cut-off frequency is set to 10 Hz. Three frequency arrangement settings are compared, including M_1 , M_2 and M_3 .

(1) M_1 Figure 4(a): The frequency range setting in M_1 is similar to that in FBCSP but with different low cut-off and high cut-off frequencies. The sub-bands in M_1 are equipped with equally spaced bandwidths.

(2) M_2 Figure 4(b): The frequency range setting in M_2 corresponds to the harmonic frequency bands. The high cut-off frequency is twice as high as the low cut-off frequency.

(3) M_3 Figure 4(c): The frequency range setting in M_3 is similar to the best setting in FBCCA. One of the two ends of the sub-bands is a fixed value. The low cut-off is fixed because the MRCP signals are in a low-frequency band. The high cut-off frequencies are arranged as an arithmetic sequence.

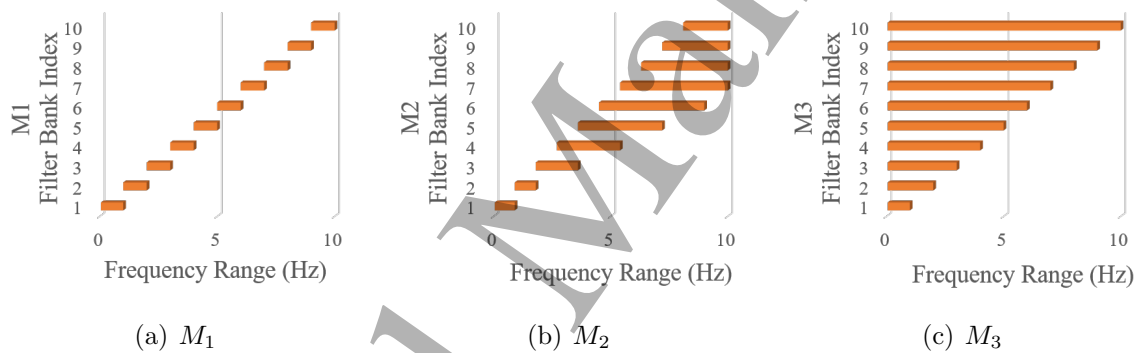


Figure 4. Frequency range settings of sub-bands for the filter bank design. M_1 : sub-bands with equally spaced bandwidths (e.g. 0.05 ~1 Hz, 1~2 Hz, ..., 9~10 Hz).; M_2 : sub-bands whose stopping frequency is twice as high as the starting frequency (e.g. 0.05~0.9 Hz, 0.9~1.8 Hz, 1.8~3.6 Hz, ..., 8.1~10 Hz).; M_3 : sub-bands that start at a fixed frequency (e.g. 0.05~1 Hz, 0.05~2 Hz, ..., 0.05~10 Hz). Considering that the MRCP are EEG signals with low frequencies, the maximum frequency of the range is set to 10Hz. In this figure, the number of filter banks is 10 ($m=10$).

2.2.4. Feature Arrangement Types From each of the sub-bands, six CCP features are extracted. The total number of features is therefore $6 \times m = 6m$. When selecting essential features from these using feature selection methods, there are two feature arrangement types that were used (Figure 5).

Type 1: The feature selection method is applied individually to each feature in the CCP. The feature selection method selects K_1 essential features out of m features, and is applied six times. In the end, $6 \times K_1$ essential features are selected in total. The maximum value of K_1 is 100.

Type 2: The feature selection method is applied to all six features in CCP simultaneously. The feature selection method is applied only once, and K_2 essential features are selected from $6 \times m$ features. The maximum value of K_2 is $6 \times m = 600$.

Improving Pre-movement Pattern Detection with Filter Bank Selection

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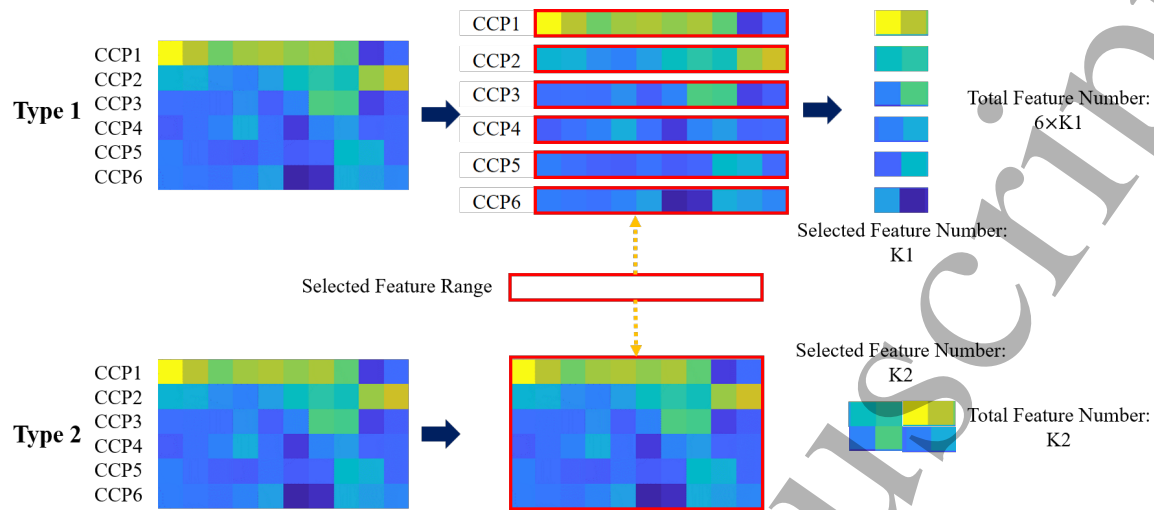


Figure 5. There are two arrangements that were used when selecting the features across these filter banks. Type 1: a feature selection method was applied to each feature in CCP respectively. Type 2: a feature selection method was applied to all six features in CCP simultaneously.

278 *2.2.5. Feature Selection Methods* Mutual-information-based approaches are a popular
 279 feature selection paradigm in data mining. In the FBCSP method of MI analysis,
 280 feature selection based on mutual information plays a significant role in optimizing the
 281 CSP features in all sub-bands. This study compares eight mutual-information-based
 282 feature selection methods to find a suitable one for selecting CCP features in multiple
 283 sub-bands. The compared feature selection methods include:

- 284 (1) Mutual Information Quotient (MIQ) [25]
- 285 (2) Maximum Relevance (MAXREL) [26]
- 286 (3) Minimum Redundancy (MINRED) [26]
- 287 (4) Minimum Redundancy Maximum Relevance (MRMR) [26]
- 288 (5) Quadratic Programming Feature Selection (QPFS) [27]
- 289 (6) Conditional Infomax Feature Extraction (CIFE) [28]
- 290 (7) Conditional Mutual Information Minimization (CMIM) [29]
- 291 (8) Maximum Relevance Minimum Total Redundancy (MRMTR) [30]

292 *2.2.6. Binary Classifiers* In STRCA, two binary classifiers have been compared,
 293 including the linear discriminate analysis (LDA) and the support vector machine (SVM).
 294 Because the number of features of STRCA is fixed, the simple LDA classifier shows the
 295 best performance among the three classifiers explored in [13]. In the proposed FBTRCA
 296 method, however, there are more than six features, and the number of features changes
 297 due to the feature selection settings. As a result, the kernel-based SVM classifier may
 298 show better performance when dealing with hyper-dimension features. Therefore, the
 299 two classifiers are also compared in this work.

4
5 300 *2.3. Benchmark Method*

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7 301 The convolutional neural network (CNN) is used universally for feature selection.
8 302 A neural network can be adjusted to an unknown function by backpropagation. The
9 303 convolution unit in CNN can capture the local features of given inputs and thus select
10 304 the essential features. Considering that the size of the EEG dataset is small, the CNN
11 305 method with a simple architecture is used as the benchmark method for feature selection.

12 306 In the CNN architecture, the CCP features are the input of the neural network
13 307 and are regarded as a 6-channel image. The height and width of the images are the
14 308 numbers of the low cut-off frequencies and the high cut-off frequencies, respectively. A
15 309 two-dimensional convolution layer is used to extract essential features from these CCP
16 310 features. This convolution layer has 24 filters, each of size 3×3 . A batch norm layer
17 311 and a ReLu layer are used to normalize the output of the convolution layer. A 2×2 max
18 312 pool layer with stride 2 follows the ReLu layer. Finally, a full-connect neural network
19 313 with a hidden size of 50 is used as the binary classifier. The output of the hidden layer
20 314 is normalized with the batch norm. The network is trained with an Adam optimizer
21 315 with a learning rate of 0.001. The maximum training epoch is set to 200.

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28 316 *2.4. Performance Measurement*

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30 317 In binary classification, accuracy, F1-score and cross-entropy loss are three prevalent
31 318 measurements for classification performance. In the classification task, the model will be
32 319 tested after training. There are four outcomes in the testing result: true positive (TP),
33 320 true negative (TN), false positive (FP) and false negative (FN) [34]. The definitions of
34 321 these four outcomes for the binary classification are given as

35 322 TP = the number of cases is correctly identified as one class;

36 323 FP = the number of cases is incorrectly identified as one class;

37 324 TN = the number of cases is correctly identified as the other class;

38 325 FN = the number of cases is incorrectly identified as the other class.

39 326 The accuracy measures the ratio of the correctly predicted trials in the testing set,
40 327 and is calculated through the following expression:

$$41 \quad Accuracy = \frac{TP + TN}{TP + TN + FP + FN}. \quad (15)$$

42 328 In the calculation of F1-score, two measurements are considered: precision and
43 329 recall. The precision is defined as

$$44 \quad Precision = \frac{TP}{TP + FP}, \quad (16)$$

45 330 whereas the recall is defined as

$$46 \quad Recall = \frac{TP}{TP + FN}. \quad (17)$$

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59 331 F1-score is given by combining both precision and recall:
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$$F1 = \frac{2 \times Precision \times Recall}{Precision + Recall}. \quad (18)$$

Both the two classes have an F1-score, which are therefore denoted as $F1_1$ and $F1_2$. The macro-average F1-score (macroAVG) is used as a measurement which balances the F1-scores of the two classes:

$$macroAVG = 0.5 \times (F1_1 + F1_2). \quad (19)$$

Cross-entropy loss refers to the contrast between two random variables. It shows how accurate the classification model is by defining the difference between the estimated probability and the true label. The higher the difference between the two label outputs, the higher the loss. The cross-entropy loss is defined as

$$CrossEntropy = L(\mathbf{y}, \mathbf{t}) = -\sum_{k=1}^2 \mathbf{t}_k \ln(\mathbf{y}_k), \quad (20)$$

where \mathbf{t} is the true label and \mathbf{y} is the estimated probability. When measuring the classification performance of FBTRCA, the estimated probability is replaced with the predicated label of FBTRCA.

For the performance evaluation, 10-fold cross-validation is used. For each of the subjects and motion pairs, the accuracy, macroAVG and cross-entropy are averaged across 10 folds to get the mean and the deviation. When presenting the classification performance of the motion pairs, we average the means and the deviations of all the subjects. The final evaluation scores for each method are obtained by averaging the means and deviations across all subjects and motion pairs. We also use the two-side t -test to measure the improvement from STRCA to FBTRCA. The p -value is measured from the results of the 10 folds, for each of the subjects and motion pairs.

3. Results

The proposed FBTRCA method is evaluated with the two datasets. EEG signals are divided into the RP and MMP sections in the first dataset, while in the second dataset, the signals are in the two-second time window after the cue. The result analysis is carried out in three cases: when the EEG signals are from (1) the RP section in dataset I, (2) both the RP and MMP sections in dataset I, and (3) the two-second time window after the cue in dataset II. The performance of the classification methods is evaluated by 10-fold cross-validation.

This study aims to incorporate the filter bank technique into STRCA and thus propose a new methodology, FBTRCA. Three steps are necessary to achieve this goal:

- (1) decide on the frequency range settings;
- (2) evaluate the parameters K1 and K2 in the two types of feature arrangements;
- (3) compare results achieved through FBTRCA against the benchmark.

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In the first step, the properties of each filter bank will be determined, including the number of filter banks and their individual frequency ranges. The second step will evaluate K1 and K2 for each mutual-information-based feature selection method. The effects of LDA and SVM on FBTRCA are also compared in the second step. In the third step, the best performance of the FBTRCA method is compared to those achieved by the CNN and STRCA methods in the three cases presented above.

3.1. Analysis of the Frequency Range Settings

STRCA is applied to filter banks in three different settings: M_1 , M_2 and M_3 . Figure 6 shows the classification accuracies of each filter bank in the three settings. The performance is evaluated with the binary classification between the movement and resting states in the RP section of dataset I. The mean of the 6 (actions) \times 15 (subjects) \times 10 (folds) accuracies is taken to evaluate the classification performance.

In setting M_1 , the accuracy decreases to 0.5 as the filter bank index increases. Similarly, the accuracy of the M_2 setting follows the same trend. The STRCA fails to solve the binary classification of the EEG signals in the sub-bands without low frequencies. Therefore, the two frequency range settings are not suitable for the combination of STRCA and the filter bank technique. In the M_3 setting, however, the accuracies in the filter banks are acceptable.

The main difference between M_3 and either M_1 or M_2 is that the frequency ranges of the filter banks in M_3 cover the sub-bands at low frequencies. The sub-bands at low frequencies maintain the information necessary for STRCA.

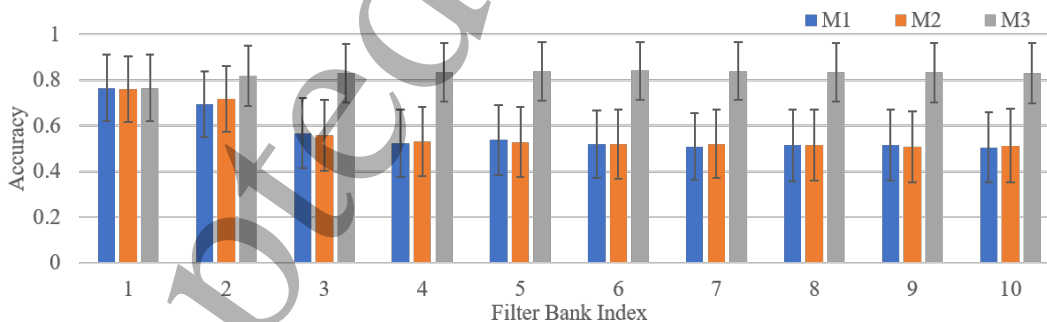


Figure 6. Classification accuracies of STRCA in three frequency range settings. In both the M_1 and M_2 settings, the accuracies decrease as the filter bank index increases, as the STRCA cannot tell the difference between the actions and the resting state. In the M_3 setting, the accuracy remains stable with an acceptable range. This means that M_3 is the only acceptable frequency arrangement setting among the three.

In the sight of these results, the M_3 frequency range setting is adopted with modifications in the design of the filter banks for the proposed FBTRCA method. The low cut-off frequency is shifted slightly from 0.5 Hz to 0.05 Hz with step 0.05 Hz, and the high cut-off frequency remains the same as that in M_3 . The total adopted number of sub-bands is 10 \times 10.

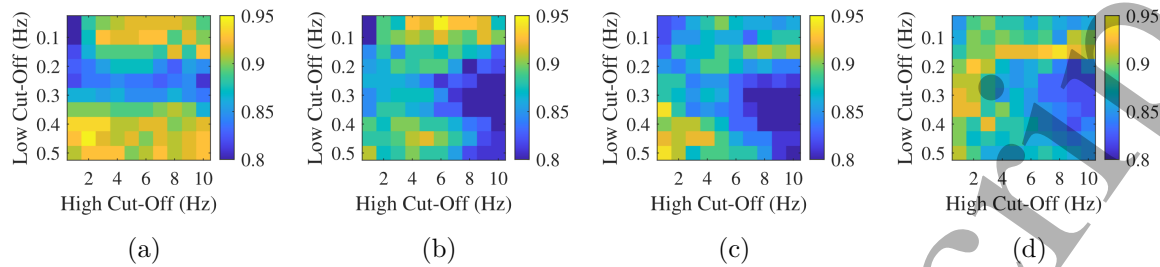


Figure 7. Average classification accuracies of STRCA in different sub-bands. (a) Subject 1, *elbow flexion vs resting state*; (b) Subject 1, *elbow extension vs resting*; (c) Subject 2, *elbow flexion vs resting*; (d) Subject 2, *elbow extension vs resting*. For different subjects or actions, the sub-band that has the best classification performance differs. Indeed, this is the reason why it is necessary to incorporate the filter bank technique in STRCA and develop the proposed FBTRCA method.

In Figure 7, the classification accuracies of STRCA in these sub-bands are given. The sub-bands with the highest accuracy vary for different subjects and actions. It is hard to decide on a suitable sub-band for STRCA, and for this reason, FBTRCA is proposed to solve this problem.

3.2. Analysis on Feature Selection Methods

After applying STRCA to 100 sub-bands, 6×100 CCP features are extracted. Then, feature selection methods select the essential features with a certain feature arrangement type. These essential features are classified with binary classifiers. In Figure 8, the classification performances of eight mutual-information-based feature selection methods are compared on two feature arrangement types. The essential features are classified with the LDA classifier and the SVM classifier (linear kernel). The statistics shown in Figure 8 are the average accuracies across subjects and motion pairs in the RP section of dataset I. The motion pairs include both (1) the binary classification between two actions and (2) the binary classification between a movement state and the resting state.

The results in Figure 8 are analyzed from three different perspectives: (1) binary classifiers, (2) comparison among the mutual-information-based feature selection methods, and (3) parameter searching on K1 and K2.

SVM and LDA are both basic binary classifiers used in machine learning. LDA casts the features into two classes through a linear projection, while SVM converts the features into hyper-space using a linear kernel and then casts the features in hyper-space into two classes. Because of the kernel, SVM is more efficient than LDA when tackling complicated features. In Figure 8, it can be seen that SVM has a better classification performance than LDA. The accuracies of LDA decrease sharply in Figure 8(a) and 8(c), and the best accuracy of LDA in Figure 8(a) is slightly lower than the accuracy of SVM in Figure 8(b). Therefore, the SVM classifier is better in the classification of FBTRCA.

In Figure 8, eight feature selection methods based on mutual information are

Improving Pre-movement Pattern Detection with Filter Bank Selection

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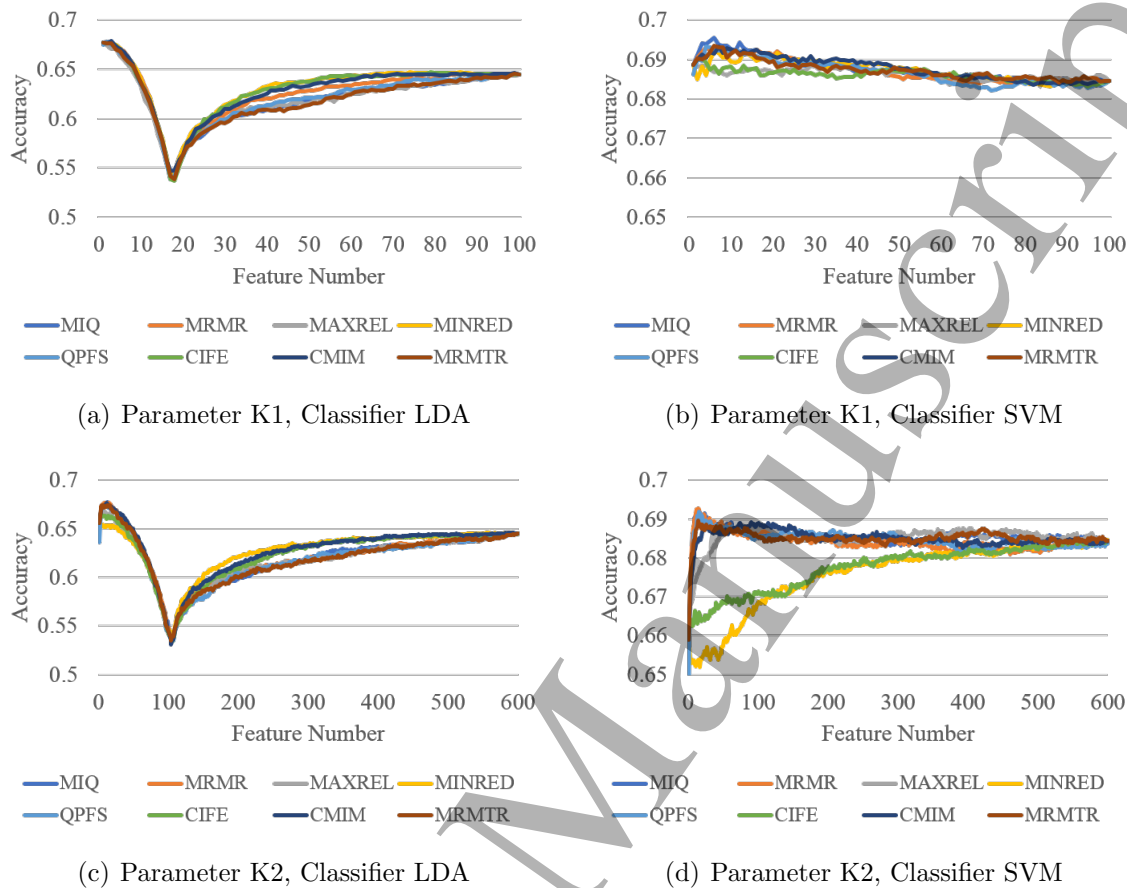


Figure 8. Tuning the K1 and K2 parameters with the LDA and SVM classifiers.

416 compared. These methods have similar accuracies except for MINRED (yellow line)
 417 and CIFE (green line). The accuracies of the other six methods have a similar (1) best
 418 accuracy and (2) changing trend. In the following analysis, the MRMR method is used
 419 as the feature selection method based on mutual information.

420 The ranges of K1 and K2 are 0~100 and 0~600, respectively. Despite their
 421 difference in range, their best accuracies are the same in Figure 8(b) and Figure 8(d).
 422 There is no significant difference between the two feature arrangement types when
 423 selecting essential features using methods based on mutual information.

424 To conclude on the above three points, the best procedure for the FBTRCA method
 425 has three steps. First, EEG signals are divided into 10×10 low-frequency banks
 426 according to the M_3 frequency range setting. Second, the feature selection method
 427 MRMR is used to select essential features. Finally, the selected essential features are
 428 classified using the SVM classifier. The number of selected essential features is about

429 15.

3.3. Comparison against Benchmarks

CNN is a universal feature selection method based on machine learning. The proposed FBTRCA method is compared against the STRCA and the CNN methods. The structure of the CNN model is given in Section 2.3. The input of the CNN method is $6 \times 10 \times 10$ CCP features, which include CCP features in 10×10 low-frequency filter banks. The input of the STRCA is the EEG signals in $0.05 \sim 10$ Hz.

A comparison between the STRCA, CNN and FBTRCA methods can be made using the accuracy, macroAVG and cross-entropy loss measurements, which are averaged across all subjects and all folds. In Figure 9, the results for the two cases in the dataset I are given, where the classification methods are applied to EEG signals in the RP section or to both the RP and MMP sections. The x-axis refers to the motion pairs, and the abbreviations are short for the names of actions. For example, 'EF' is short for 'elbow flexion'. Figure 10 presents the classification results of dataset II. The classification methods are applied to the EEG signals in the two-second time window after the cue. Overall, it can be observed that the FBTRCA method outperforms the STRCA and CNN methods in both datasets. To better present the classification performance, we list the detailed accuracies for all subjects and motion pairs in the datasets I and II (Table 4-15). The detailed accuracies are results averaged from accuracies of ten folds of cross-validation. The mean and the deviation are listed in two separate tables.

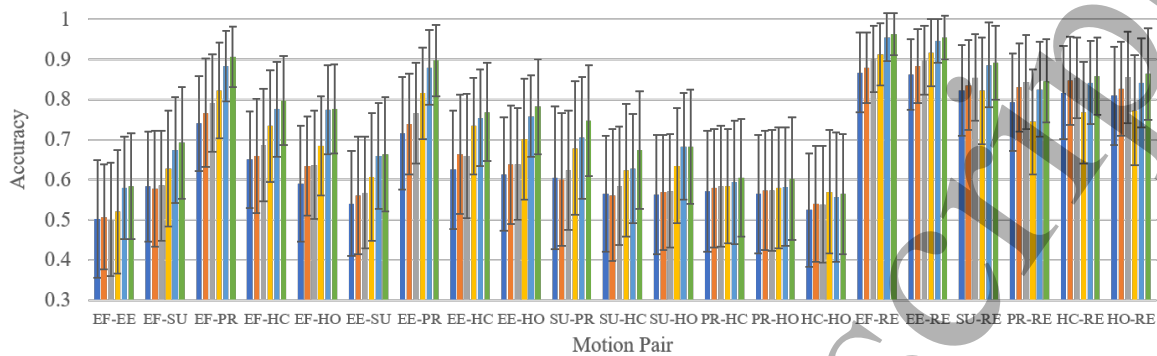
In dataset I, the binary classification is evaluated on the EEG signals in the RP section. The binary classification between actions and the resting state reflects whether the subjects want to move their limbs or stay at rest. The meaning of pre-movement decoding is to detect the movement intention before the limb moves. FBTRCA can improve the performance of pre-movement decoding compared to the previous STRCA method. When EEG signals in both RP and MMP sections are used, all three classification methods show an improved performance compared to the results for signals in only the RP section. The EEG signals are also different between the two states in the MMP section.

During the acquisition of EEG signals in dataset II, the limb movement trajectories were not recorded, and thus the onsets of actions cannot be located precisely. The two-second time window after the cue is taken in the classification evaluation. Within this time window, the subjects begin to move their limbs. Therefore, the two-second time window covers part of both the RP and MMP sections. Although the onsets cannot be located in dataset II, the FBTRCA still improves the classification performance.

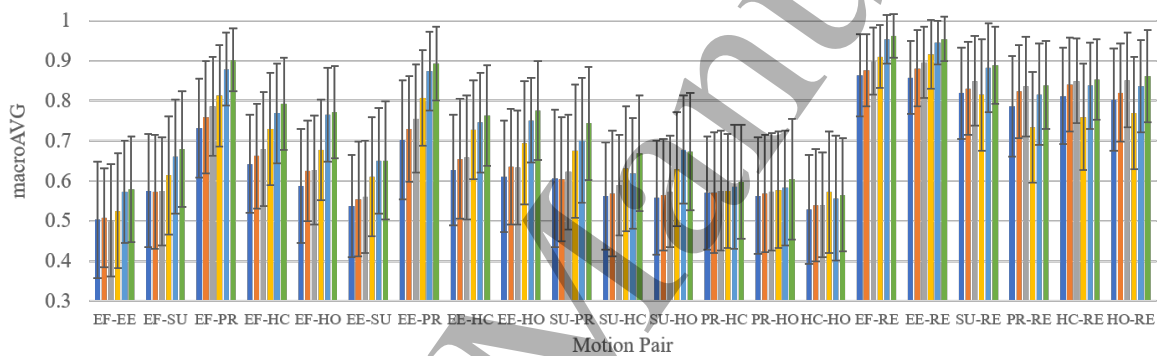
We also present the p -values of two-side t -test between the STRCA method and the FBTRCA method (Table 16-18). The p -values are calculated from the accuracies of ten folds, for each subject and each motion pair. In the three tables, the p -values are highlighted if the value is smaller than 0.1. In the dataset I (RP+MMP section), there is at least one subject that FBTRCA shows significant improvement than STRCA ($p < 0.1$), except for the classification between *pronation* and *hand close* or between *pronation* and *hand open*.

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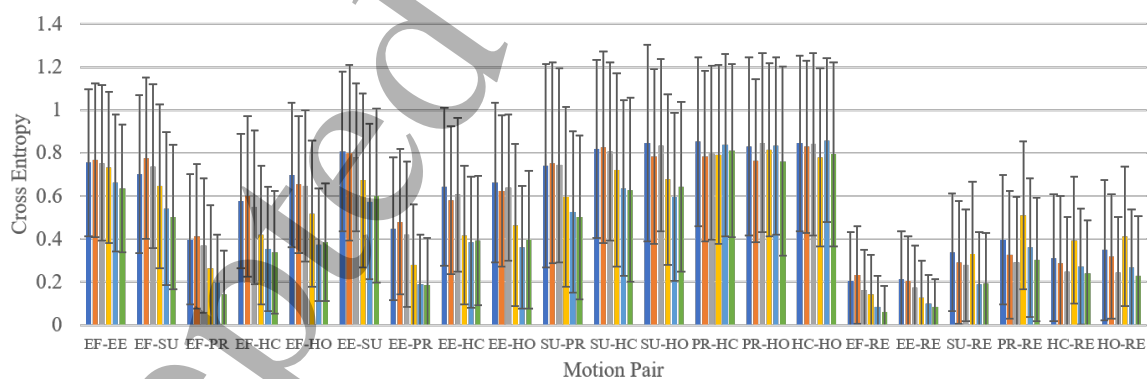
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(a) Dataset I, Accuracy

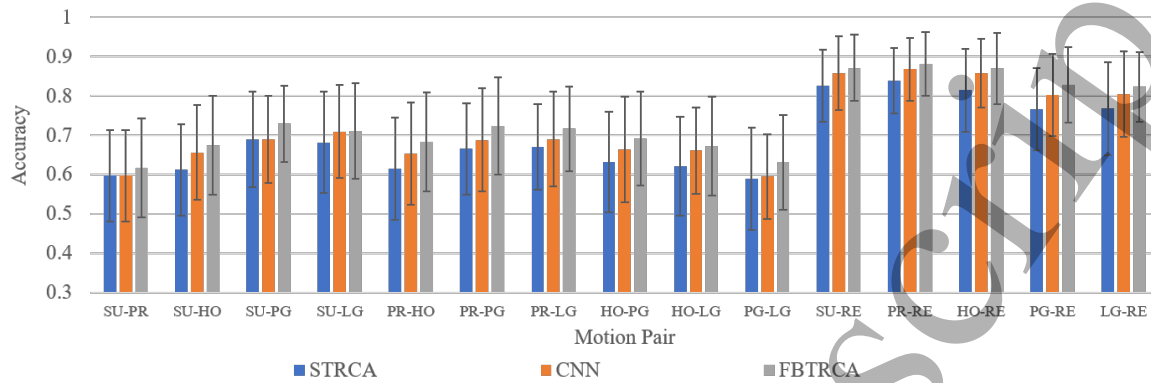


(b) Dataset I, MacroAVG

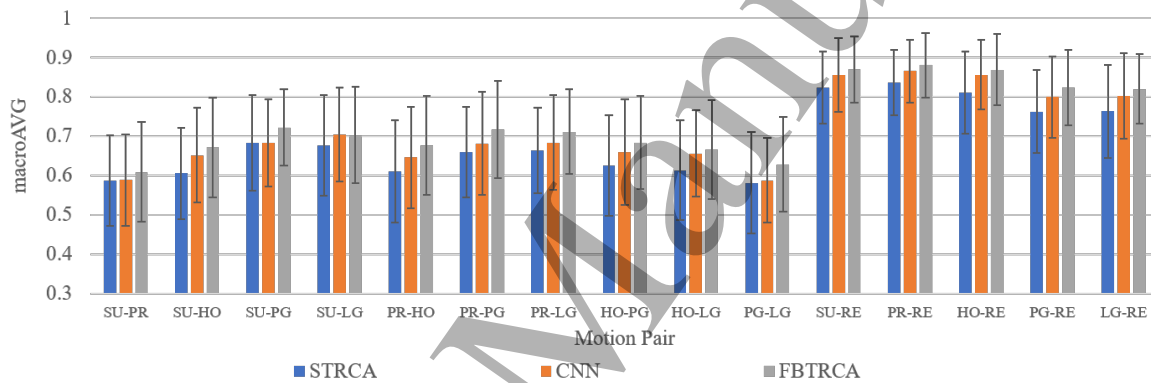


(c) Dataset I, Cross Entropy

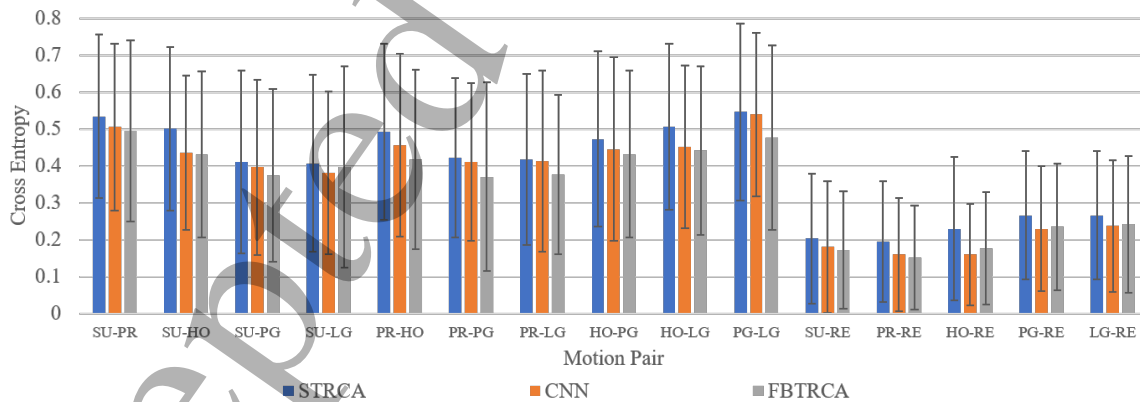
Figure 9. Accuracy, macroAVG and cross-entropy loss comparison in dataset I. Three methods including STRCA, CNN and FBTRCA are compared. The classification is evaluated in either the RP section or both the RP and MMP sections. The accuracies are averaged across all subjects and all folds. The x-label represents the motion pair in which the binary classification is applied. The abbreviations of these states are used in the figures to facilitate the presentation; for example, 'EF' is short for the movement state *elbow flexion*. Figure 9(a), Figure 9(b) and Figure 9(c) each refer to one of the three measurements respectively.



(a) Dataset II, Accuracy



(b) Dataset II, MacroAVG



(c) Dataset II, Cross Entropy

Figure 10. Accuracy, macroAVG and cross-entropy loss comparison in dataset II. Three methods including STRCA, CNN and FBTRCA are compared. The classification is evaluated in the two-second time window after the cue. The other settings of this figure are the same as those presented in Figure 9.

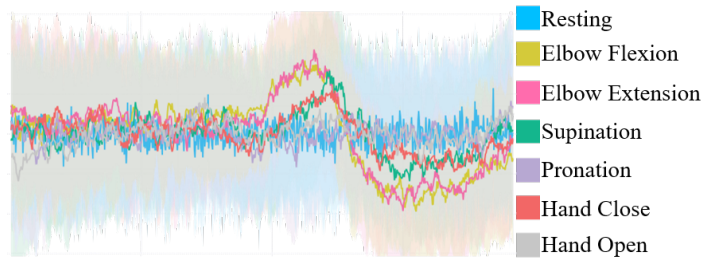


Figure 11. The grand average MRCPs of multiple motions.

471 In summary, the proposed FBTRCA method incorporates the filter bank technique
 472 into the basic STRCA method, thus presenting a comparable classification performance
 473 to STRCA in pre-movement decoding.

474 4. Discussion

475 In this study, we proposed a new pre-movement decoding method, FBTRCA. This
 476 method is developed by incorporating filter bank selection on the STRCA method. In
 477 comparison to MI signals, MRCP signals have the advantage that the movement patterns
 478 can be observed before the movement onset. FBTRCA is designed to extract features
 479 from the grand average MRCP, which contains information about the movement in
 480 MRCP signals. FBTRCA consists of three modules: the spatial filter TRCA, the CCPs
 481 features and the low-frequency bands. The associations between these and the grand
 482 average MRCP are detailed below. To better explain the relationship between FBTRCA
 483 and grand average MRCP, the grand average MRCP of multiple actions in channel C_z
 484 is presented in Figure 11.

485 The spatial filter is a linear transformation of multi-channel EEG signals. It
 486 plays the role of channel selection and thus optimizes the spatial characteristic of EEG
 487 signals. Our previous work pointed out that SSVEP and MRCP signals have similar
 488 spatial distributions, and the STRCA method was proposed by comparing the effects
 489 of different spatial filters for MRCP signals [13]. The spatial filter TRCA showed a
 490 better performance when compared to other spatial filters. Among the compared spatial
 491 filters, the discriminative canonical pattern matching is a spatial filter that maximizes
 492 the inter-class covariance and minimizes the intraclass covariance. However, even the
 493 performance of this filter was worse than TRCA. Therefore, the spatial filtering does
 494 not maximize the intraclass covariance in this work. As given in Section 2.2.1, TRCA
 495 searches for the projection matrix that maximizes the covariance of each trial in each
 496 class. The ideal spatial filter transforms the EEG signals of all trials into a single trial
 497 so that the covariances among these trials are maximized. The grand average MRCP
 498 is the mean of all the trials in each class. We assume that the ideal single trial is the
 499 grand average MRCP, although there might be some biases. The EEG signals of all the
 500 trials in each class approach the grand average MRCP of each class during the spatial

filtering. Because the inter-trial noises are not correlated, the noise components in EEG signals have lower eigenvalues. The noises are removed from the signals by taking the eigenvectors of the three maximum eigenvalues in the spatial filtering.

In Figure 11, the grand average MRCPs of multiple motions are different. In the binary classification, the class of an EEG trial is determined by the distances between the EEG trial and the two grand average MRCPs. The goal is to quantify the relationship between the EEG signals of each trial and the grand average MRCPs of two classes after the spatial filtering. CCPs are in fact used to measure the similarity between EEG signals and the grand average MRCPs. In the calculation of CCPs, three types of correlation coefficients are used to measure the similarity between EEG signals and the grand average MRCPs; these include (1) the correlation between EEG signals and the grand average MRCP, (2) the canonical correlation between EEG signals and the grand average MRCP, and (3) the canonical correlation between two differences, including the difference between EEG signals and the grand average MRCP and the difference between two grand average MRCPs. Because the three coefficients are measuring the similarity between EEG signals and the grand average MRCP and there are two grand average MRCPs, the number of total CCP features is six.

However, because the differences between the two motions are reflected in their grand average MRCP signals, the similarity between their grand average MRCP signals limits their classification performance. For instance, the classification between *elbow flexion* and *resting* has a high accuracy, but the classification between *elbow flexion* and *elbow extension* achieves an unsatisfactory performance.

The grand average MRCP plays an important role in STRCA and FBTRCA. But the calculation procedure is simple, which is the same as the procedure of the CCP templates given in Section 2.2.1. In the training set, the EEG signals of each trial are labelled. The grand average MRCP can be established simply by averaging EEG trials belonging to the same class. Calculating the grand average MRCP with the training set and using the grand average MRCP as a template can be derived from [35–37]. Their grand average MRCP was extracted from the surrogate channel in the training set. In our work, the template is extracted from the channels in the motor cortex. The number of channels in the grand average MRCP is then minimized by the task-related component analysis.

When applying filter bank selection to STRCA, the EEG signals are divided into several frequency ranges. As shown in Figure 12(a), the low cut-offs of these frequency ranges are small, while the high cut-offs are sorted in an arithmetic sequence. In MRCP analysis, the grand average MRCP shows an increase followed by a decrease around the movement onset. The grand average MRCP is a low-frequency signal. Figure 12(b) illustrates the power spectrum of the grand average MRCP. As the frequency increases, the time window with high power (yellow part) becomes narrow. Therefore, it is necessary to maintain the low-frequency components, as then the increasing high cut-off of filter banks can introduce more subtle features. For example, in Figure 12(a), the 0.5~3 Hz component reflects how the grand average MRCP changes. As the high

Improving Pre-movement Pattern Detection with Filter Bank Selection

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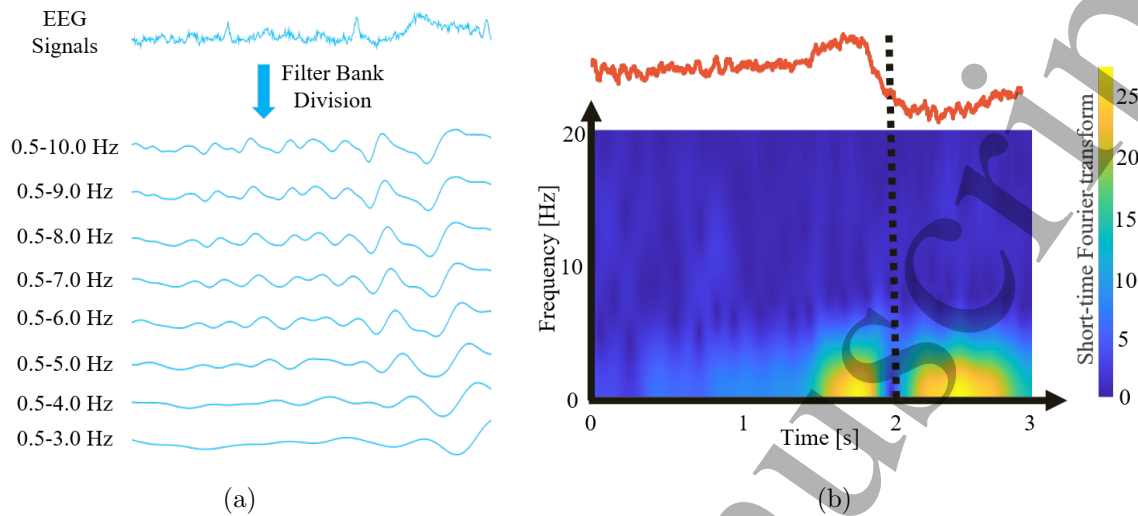


Figure 12. Frequency characteristics of MRCP signals. (a) Low-frequency components of MRCP signals in the RP section (M_3). (b) Power spectrum of the grand average MRCP in both RP and MMP sections, calculated by the short-time Fourier transform.

cut-off increases to 10 Hz , more local trends are introduced.

The Figure 12(a) can be used to explain why the frequency range setting M_3 is better than the other two settings. The correlation coefficients measure the similarity of the unlabeled trial and the grand average MRCPs. As mentioned above, the classification of STRCA and FBTRCA depends on the differences between two grand average MRCPs. The most discriminant features in the grand average MRCP are the increase and decrease around the movement onset (Figure 11). Reflected in Figure 12(a), the increase and decrease are located in the extremely low-frequency bands (0.5~3 Hz), which indicates the global trend of MRCP signals. When the high cut-off frequency increases, more subtle features are introduced. In the frequency range settings, M_1 and M_2 , the global trend of MRCP signals is removed in the filtering and only subtle or local features are kept. It leads to the results that the increase and decrease trends are removed, and the differences of the increase and decrease between two motions cannot be further analyzed and distinguished in STRCA and FBTRCA. Therefore, the frequency range setting M_3 is used in the analysis of MRCP signals.

In the frequency range setting M_3 of Figure 4, the filter bank 10 (*e.g.*, 0.05~10 Hz) covers the ranges of the rest filter banks and thus contains the information from other frequency bands. However, the other filter banks are still important in the signal processing. This can be explained by the classification accuracies in multiple filter banks. In Figure 7, the average classification accuracies of multiple filter banks are presented. When the low cut-off of the filter bank is fixed to a small value, the accuracy of STRCA changes as the high cut-off frequency increases in an arithmetic sequence. The best accuracies among these bands are different among subjects and motion pairs. A possible reason is the influence of noise in the frequencies greater than the best frequency, and

the insufficient information in the frequencies smaller than the best frequency. The best frequency bands cannot be determined directly by giving a certain frequency range. The filter bank selection across these frequency bands in the proposed FBTRCA is necessary when tackling this problem. Therefore, although the filter bank 10 covers all the other filter banks, the other filter banks are still necessary. The filter bank 10 may be influenced by undetected noises and is not in the best frequency range.

During the development of the FBTRCA method, the processing capabilities in SSVEP and MI are considered. This includes the canonical correlation coefficients in SSVEP and the feature selection on filter banks in MI.

SSVEP also uses canonical correlations as features for classification, but there are some differences. In SSVEP, there are two kinds of templates when calculating the correlation coefficients [33]. The first template is the CCP template averaged across trials in each class. The second template is the sinusoidal function. Because the visual stimulus in SSVEP has a specific frequency, the similarity between EEG signals and the sinusoidal function with a specific frequency can predict the frequencies of visual stimuli. Compared to SSVEP, MRCP has a natural drawback: the templates cannot be measured with frequencies. As shown in Figure 11, the differences between the grand average MRCPs of a motion pair are different. For example, the differences between the grand average MRCPs of *elbow flexion* and *elbow extension* is smaller compared to the differences between *elbow flexion* and *supination*. We cannot measure how much smaller the differences are, but they can be measured by the frequencies of visual stimuli in SSVEP. Therefore, it is difficult to classify the MRCP signals by adopting the maximum value of correlation coefficients as in SSVEP. The coefficients calculated in STRCA are used as features for further improvement by feature selection.

In Section 3, the classification results between EEG signals in the RP section and the RP+MMP sections are compared. The EEG signals in RP+MMP show an improvement over those in only the RP section. The reason is that the grand average MRCPs also show the differences between the two actions in the MMP section. Similarly to the result analysis of dataset II, it is not necessary to locate the onset of the action and divide the EEG signals into RP and MMP sections if one is only considering the classification of two classes. The classification results in the RP section indicate whether this method works in pre-movement decoding. The classification results in both the RP and MMP sections reflect the best classification performance that this method can achieve.

The feature selection methods we used are based on mutual information instead of similarity or sparse learning [38]. Mutual information is preferred in this case because it has shown to have good performances previously in FBCSP. Mutual information is also used in MI analysis when selecting features from filter banks. Because of the efficiency of mutual information in feature selection on filter banks, feature selection methods based on mutual information were first considered. Compared to feature selection with CNN, the feature selection based on mutual information achieved better performance, as shown in Figure 9. Compared to mutual information, sparse learning is suitable in the feature selection from both multiple filter banks and time windows [32].

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Traditional EEG processing methods have three key points, spectral, spatial and temporal. The proposed FBTRCA method is associated with one point of the traditional method, spectral, *i.e.*, filter banking. According to our research experience on MRCP signals, FBTRCA and STRCA cannot well deal with the spatial optimization. The spatial filtering in STRCA and FBTRCA work as unrelated-components rejection. The introduce of more channels will lead to a decrease of the classification performance of STRCA and FBTRCA. The temporal characteristic used in FBTRCA and STRCA is the correlation, which measures the similarity of two time series. It can be further improved in future work. Besides, the STRCA and FBTRCA can only be used in the binary classification limiting to the scheme of STRCA. Migrating the two binary classification methods to the multi-class classification task is also an important work. In MRCP signals, the grand average MRCP is a special concept in EEG processing, which averages across all trials belonging to a class. However, averaging is a simple approach to finding the center points of all trials and inevitably introduces unexpected influences like outlier points. It is also possible to find a hyper-space that casts the trials to the discriminant points.

5. Conclusion

The proposed FBTRCA method incorporates the filter bank technique and solves the unstable accuracy problem. There are four steps in FBTRCA. First, EEG signals are divided into multiple sub-bands in the low-frequency domain. Second, CCP features are extracted from these sub-bands with the STRCA method. Then, the minimum redundancy maximum relevance method is used to optimize and select the CCP features. Finally, the selected features are classified with the SVM binary classifier. When decoding the pre-movement pattern in the RP and MMP section, the average accuracy increases from 0.8228 ± 0.1149 (STRCA) to 0.8968 ± 0.0847 (FBTRCA) in the binary classification between the actions and the resting state; the average accuracy increases from 0.6611 ± 0.1432 (STRCA) to 0.7178 ± 0.1274 (FBTRCA) in the binary classification between two actions.

6. Code availability

The code of this work is freely available here: <https://github.com/plustar/Movement-Related-Cortical-Potential>.

7. Acknowledgement

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Improving Pre-movement Pattern Detection with Filter Bank Selection

Table 4. Mean of Classification Accuracies of Dataset I (RP) Across Ten Folds (Movement vs Movement)

Subject	Method	Motion Pair																Average
		EF-EE	EF-SU	EF-PR	EF-HC	EF-HO	EE-SU	EE-PR	EE-HC	EE-HO	SU-PR	SU-HC	SU-HO	PR-HC	PR-HO	HC-HO		
1	STRCA	0.5167	0.6000	0.7545	0.6364	0.5818	0.4400	0.6273	0.6091	0.4636	0.7333	0.6556	0.5333	0.5400	0.5600	0.5800	0.5888	
	CNN	0.5083	0.6600	0.8636	0.6091	0.6545	0.6500	0.7455	0.5727	0.4636	0.6667	0.6222	0.5556	0.5400	0.5700	0.5200	0.6135	
	FBTRCA	0.5333	0.6800	0.8455	0.7091	0.6182	0.6000	0.8000	0.8000	0.4818	0.7222	0.6667	0.6111	0.6000	0.5700	0.5200	0.6366	
2	STRCA	0.5300	0.5700	0.7500	0.5500	0.4700	0.5600	0.7500	0.5100	0.4800	0.6800	0.5700	0.4600	0.6300	0.6300	0.5000	0.5760	
	CNN	0.5300	0.5500	0.7900	0.4800	0.5000	0.5500	0.8000	0.5400	0.6100	0.7400	0.4900	0.5200	0.5900	0.4800	0.5853		
	FBTRCA	0.5700	0.5800	0.8400	0.5100	0.4800	0.6500	0.8300	0.4800	0.6200	0.7200	0.5500	0.5100	0.6100	0.6300	0.5000	0.6053	
3	STRCA	0.4000	0.5700	0.7000	0.8455	0.7900	0.6900	0.6700	0.8909	0.7800	0.6000	0.6556	0.6125	0.6444	0.6500	0.6778	0.6784	
	CNN	0.4250	0.6400	0.6900	0.8364	0.8200	0.6500	0.7000	0.8818	0.8200	0.5750	0.6111	0.6875	0.6222	0.5125	0.6556	0.6751	
	FBTRCA	0.4583	0.5500	0.7700	0.8545	0.8400	0.6100	0.8100	0.9000	0.8400	0.5750	0.6778	0.6750	0.6444	0.6250	0.7000	0.7020	
4	STRCA	0.4417	0.6000	0.8364	0.7750	0.6686	0.5000	0.8364	0.7250	0.7000	0.7600	0.6727	0.6500	0.5727	0.5900	0.5455	0.6579	
	CNN	0.5667	0.5091	0.8636	0.7917	0.7273	0.5182	0.8636	0.7750	0.8091	0.7800	0.6727	0.7100	0.5727	0.5900	0.6863		
	FBTRCA	0.5500	0.4818	0.9182	0.8083	0.7545	0.5636	0.8545	0.8167	0.7818	0.8600	0.8091	0.7300	0.6000	0.6200	0.6182	0.7178	
5	STRCA	0.6273	0.4727	0.7000	0.5727	0.4818	0.6900	0.7500	0.5800	0.6000	0.6600	0.5500	0.6000	0.6300	0.5300	0.5500	0.5936	
	CNN	0.4636	0.5727	0.7091	0.5636	0.5818	0.5600	0.7100	0.6700	0.5700	0.5400	0.5700	0.5300	0.6000	0.6000	0.5700	0.5874	
	FBTRCA	0.5091	0.5182	0.6909	0.5455	0.5909	0.6500	0.7200	0.6400	0.6200	0.5700	0.6000	0.5300	0.5900	0.6200	0.5200	0.5943	
6	STRCA	0.5833	0.6545	0.9333	0.6636	0.8182	0.5000	0.8111	0.6000	0.7091	0.6000	0.5700	0.5800	0.5875	0.6000	0.6000	0.6540	
	CNN	0.5683	0.6182	0.8667	0.6909	0.7818	0.5545	0.7889	0.6182	0.7455	0.5750	0.5800	0.5400	0.6625	0.6250	0.6523		
	FBTRCA	0.5083	0.7000	0.9222	0.7000	0.8091	0.5455	0.8000	0.6182	0.7273	0.5625	0.5400	0.5800	0.7000	0.5750	0.5900	0.6591	
7	STRCA	0.5167	0.6000	0.7091	0.6182	0.5000	0.4545	0.7364	0.6364	0.6091	0.6900	0.5400	0.5300	0.5700	0.5400	0.5100	0.5840	
	CNN	0.5500	0.5818	0.7091	0.5909	0.6182	0.5364	0.8000	0.6818	0.6182	0.6000	0.5200	0.5900	0.5600	0.5300	0.5200	0.6004	
	FBTRCA	0.5500	0.6273	0.7727	0.6000	0.6182	0.5000	0.7818	0.6455	0.5636	0.6700	0.5100	0.5400	0.5300	0.5300	0.5300	0.6046	
8	STRCA	0.5083	0.6545	0.7636	0.6364	0.6545	0.4818	0.7364	0.5364	0.5636	0.5400	0.5100	0.5800	0.5300	0.5200	0.4100	0.5744	
	CNN	0.5083	0.6364	0.7818	0.6545	0.7000	0.5273	0.7000	0.4900	0.6000	0.4900	0.4700	0.5000	0.5500	0.4600	0.4400	0.5778	
	FBTRCA	0.5250	0.6091	0.7818	0.6818	0.7000	0.5182	0.7727	0.6364	0.6818	0.5200	0.5200	0.5200	0.5600	0.4800	0.4500	0.5971	
9	STRCA	0.5583	0.6545	0.7455	0.7000	0.5727	0.6000	0.6845	0.6182	0.6364	0.6000	0.4800	0.6500	0.4900	0.5800	0.4800	0.5947	
	CNN	0.5000	0.6091	0.7273	0.6455	0.5545	0.5727	0.6909	0.6455	0.5455	0.4600	0.4900	0.5900	0.5900	0.7200	0.5907		
	FBTRCA	0.5667	0.6455	0.7545	0.7000	0.5727	0.5727	0.7091	0.6818	0.6182	0.5000	0.4600	0.6300	0.5100	0.6000	0.5000	0.6014	
10	STRCA	0.4417	0.4273	0.5833	0.6909	0.4818	0.5091	0.6750	0.6636	0.5727	0.6273	0.5900	0.5300	0.5455	0.4909	0.5400	0.5579	
	CNN	0.4250	0.4364	0.5750	0.7273	0.4545	0.5273	0.6333	0.7727	0.6364	0.6818	0.6400	0.6100	0.5273	0.4727	0.6400	0.5840	
	FBTRCA	0.4583	0.4818	0.6083	0.7182	0.4455	0.4818	0.6750	0.7636	0.5545	0.6364	0.6800	0.5200	0.5364	0.4909	0.5900	0.5761	
11	STRCA	0.4400	0.6500	0.7333	0.5400	0.4900	0.5400	0.5444	0.4400	0.5600	0.4778	0.4800	0.6100	0.5222	0.5444	0.5100	0.5388	
	CNN	0.5700	0.4800	0.8222	0.5700	0.6000	0.5300	0.7111	0.5900	0.5700	0.5556	0.5600	0.6000	0.5667	0.5778	0.5300	0.5889	
	FBTRCA	0.4900	0.5800	0.8000	0.5900	0.4800	0.5200	0.7000	0.7000	0.5200	0.5444	0.5400	0.6000	0.5333	0.5667	0.5000	0.5656	
12	STRCA	0.5455	0.5600	0.6900	0.7091	0.6091	0.5333	0.6889	0.6400	0.6100	0.5625	0.5111	0.6111	0.5111	0.4778	0.4600	0.5813	
	CNN	0.5727	0.6500	0.8000	0.7182	0.6818	0.5222	0.6889	0.6000	0.7000	0.5875	0.4333	0.6333	0.4778	0.5667	0.4500	0.6055	
	FBTRCA	0.4909	0.5900	0.7900	0.7091	0.7273	0.5444	0.7444	0.6900	0.6800	0.6500	0.5111	0.6333	0.6444	0.5333	0.4800	0.6279	
13	STRCA	0.5083	0.6000	0.6909	0.5545	0.5000	0.4818	0.6909	0.6273	0.5818	0.4600	0.5200	0.4700	0.5300	0.6600	0.5100	0.5590	
	CNN	0.4250	0.5455	0.7636	0.6909	0.5273	0.4818	0.7545	0.7091	0.5000	0.4900	0.5300	0.4800	0.5900	0.5500	0.5200	0.5705	
	FBTRCA	0.3917	0.5727	0.7636	0.6818	0.5364	0.6091	0.7182	0.6636	0.5364	0.5300	0.5700	0.4900	0.5400	0.6100	0.4900	0.5602	
14	STRCA	0.4833	0.5900	0.7700	0.6455	0.5455	0.5300	0.8200	0.6636	0.6091	0.6125	0.6000	0.5222	0.6444	0.6000	0.4400	0.6051	
	CNN	0.5583	0.6200	0.8600	0.7000	0.6182	0.5200	0.7800	0.6636	0.6182	0.6500	0.6000	0.4889	0.6444	0.6667	0.5200	0.6345	
	FBTRCA	0.5417	0.6200	0.8500	0.7818	0.6273	0.5000	0.7700	0.6364	0.5636	0.7000	0.6556	0.5333	0.5889	0.6556	0.4100	0.6289	
15	STRCA	0.4455	0.5556	0.7400	0.6200	0.6900	0.6900	0.7364	0.6364	0.7364	0.5778	0.5667	0.5000	0.6200	0.4900	0.5600	0.6110	
	CNN	0.4909	0.5667	0.6800	0.6200	0.6800	0.7000	0.7182	0.6273	0.7636	0.6111	0.5667	0.5222	0.5700	0.5600	0.6164		
	FBTRCA	0.4455	0.5889	0.7000	0.6500	0.7000	0.7200	0.7727	0.6909	0.7273	0.3889	0.6000	0.5333	0.5800	0.4700	0.6200	0.6265	
Average	STRCA	0.5031	0.5833	0.7400	0.6505	0.5899	0.5407	0.7152	0.6251	0.6141	0.6054	0.5648	0.5626	0.5712	0.5642	0.5249	0.5970	
	CNN	0.5074	0.5784	0.7668	0.6593	0.6339	0.5600	0.7390	0.6358	0.6002	0.5617	0.5685	0.5626	0.5789	0.5728	0.5401	0.6112	
	FBTRCA	0.5059	0.5884	0.7872	0.6827	0.6340	0.5730	0.7639	0.6649	0.6411	0.6233	0.5927	0.5757	0.5845	0.5718	0.5345	0.6216	

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Table 5. Deviation of Classification Accuracies of Dataset I (RP) Across Ten Folds (Movement vs Movement)

Subject	Method	Motion Pair															Average
		EF-EE	EF-SU	EF-PR	EF-HC	EF-HO	EF-SU	EE-PR	EE-HC	EE-HO	SU-PR	SU-HC	SU-HO	PR-HC	PR-HO	HC-HO	
1	STRCA	0.1610	0.1700	0.0614	0.1134	0.1973	0.0966	0.1088	0.1548	0.1385	0.1673	0.1330	0.1366	0.1578	0.1174	0.1874	0.1401
	CNN	0.1087	0.1179	0.0643	0.2102	0.0959	0.1434	0.0717	0.1717	0.1629	0.1386	0.1304	0.1171	0.2011	0.1418	0.1549	0.1392
	FBTRCA	0.1427	0.1229	0.0862	0.1472	0.0392	0.1054	0.1032	0.1728	0.1548	0.1677	0.1386	0.0944	0.2261	0.1252	0.2044	0.1434
2	STRCA	0.2111	0.1160	0.2014	0.1650	0.1767	0.1075	0.1958	0.1969	0.2098	0.1476	0.2111	0.1350	0.0949	0.1418	0.1633	0.1649
	CNN	0.1418	0.2068	0.1197	0.1874	0.1700	0.1581	0.0667	0.1955	0.1969	0.1506	0.2132	0.0789	0.1729	0.1663	0.1687	0.1596
	FBTRCA	0.1636	0.1549	0.1075	0.2132	0.1874	0.1780	0.1160	0.1687	0.1549	0.0632	0.2635	0.1197	0.1792	0.1252	0.1563	0.1568
3	STRCA	0.1511	0.0675	0.1054	0.0614	0.1287	0.0876	0.1337	0.0939	0.1398	0.2267	0.0973	0.1811	0.1640	0.1419	0.1330	0.1275
	CNN	0.1441	0.1174	0.1449	0.1032	0.1033	0.1269	0.1247	0.0862	0.1317	0.1972	0.1907	0.1587	0.1405	0.1376	0.1693	0.1384
	FBTRCA	0.1375	0.1354	0.1059	0.0636	0.0516	0.1524	0.0994	0.0904	0.1174	0.1208	0.2369	0.1581	0.1261	0.1179	0.1054	0.1213
4	STRCA	0.2153	0.1150	0.0939	0.1182	0.1289	0.1303	0.1118	0.1245	0.1289	0.1713	0.1150	0.1354	0.1606	0.1287	0.0857	0.1309
	CNN	0.1024	0.1067	0.1154	0.1195	0.1212	0.1289	0.0883	0.1364	0.0904	0.1317	0.1828	0.1101	0.1359	0.1197	0.1050	0.1196
	FBTRCA	0.1427	0.0614	0.0796	0.1245	0.1359	0.1342	0.0977	0.1405	0.1150	0.1506	0.1385	0.1494	0.1828	0.1317	0.1197	0.1269
5	STRCA	0.1450	0.1118	0.1216	0.0748	0.1488	0.1333	0.1080	0.1476	0.1563	0.1713	0.1269	0.1333	0.1059	0.1337	0.1581	0.1318
	CNN	0.1512	0.1289	0.1197	0.1197	0.1227	0.1350	0.1663	0.1252	0.2058	0.1430	0.2058	0.1160	0.1247	0.1155	0.1703	0.1433
	FBTRCA	0.1150	0.1216	0.1615	0.1485	0.1437	0.1179	0.1317	0.1265	0.1932	0.1337	0.1333	0.0949	0.1197	0.1229	0.1874	0.1368
6	STRCA	0.1470	0.1592	0.0777	0.1606	0.1485	0.1372	0.1054	0.1369	0.0717	0.1748	0.1252	0.1619	0.1565	0.1419	0.1764	0.1387
	CNN	0.1097	0.1649	0.1021	0.1300	0.1434	0.1684	0.0820	0.1533	0.1197	0.1581	0.1687	0.1075	0.1768	0.1398	0.1414	0.1549
	FBTRCA	0.1544	0.1548	0.0750	0.1359	0.1385	0.0796	0.1366	0.1757	0.1286	0.1350	0.1430	0.1619	0.1467	0.1972	0.1197	0.1388
7	STRCA	0.0946	0.0878	0.1197	0.1118	0.1437	0.1964	0.1512	0.1286	0.1216	0.1853	0.1838	0.1567	0.1252	0.1647	0.1197	0.1394
	CNN	0.1192	0.1067	0.1592	0.1674	0.0835	0.1738	0.1342	0.1500	0.0939	0.1247	0.0789	0.2025	0.0966	0.1059	0.1989	0.1330
	FBTRCA	0.0896	0.0796	0.1500	0.1227	0.1032	0.1372	0.1227	0.1629	0.1138	0.1252	0.1792	0.1075	0.0949	0.1337	0.1494	0.1248
8	STRCA	0.1641	0.2204	0.1671	0.1286	0.1342	0.0862	0.1985	0.1385	0.1533	0.2011	0.1101	0.1814	0.1567	0.1398	0.1524	0.1555
	CNN	0.1732	0.1545	0.1878	0.1197	0.1054	0.1533	0.1966	0.1425	0.1434	0.1969	0.1265	0.1829	0.1716	0.1649	0.1476	0.1549
	FBTRCA	0.1669	0.1138	0.1777	0.1372	0.0748	0.1606	0.1780	0.1355	0.1372	0.1619	0.1317	0.2098	0.1265	0.1135	0.1080	0.1422
9	STRCA	0.1364	0.1907	0.0835	0.1138	0.1606	0.0878	0.1592	0.1271	0.1355	0.1886	0.1687	0.1434	0.1449	0.1751	0.1619	0.1451
	CNN	0.0962	0.1359	0.1545	0.1450	0.1289	0.1717	0.1150	0.1985	0.2227	0.1647	0.2284	0.1663	0.1449	0.1687	0.0789	0.1541
	FBTRCA	0.1349	0.1684	0.1663	0.1425	0.1246	0.1289	0.0939	0.1289	0.1472	0.1054	0.2413	0.1337	0.2183	0.1054	0.1247	0.1475
10	STRCA	0.0686	0.1359	0.1361	0.1557	0.1289	0.1497	0.1270	0.1289	0.1054	0.1985	0.1792	0.1567	0.1603	0.1300	0.1265	0.1392
	CNN	0.1386	0.1197	0.1270	0.1286	0.1050	0.1592	0.1721	0.1071	0.1917	0.1780	0.1578	0.1524	0.1858	0.1649	0.1265	0.1476
	FBTRCA	0.1128	0.1359	0.1245	0.1170	0.0904	0.1054	0.1493	0.1150	0.1684	0.1818	0.1619	0.1932	0.1512	0.1369	0.0994	0.1362
11	STRCA	0.1578	0.0707	0.1405	0.1265	0.1524	0.1174	0.1330	0.1506	0.2271	0.1576	0.1549	0.2183	0.1576	0.1848	0.1197	0.1513
	CNN	0.1059	0.1619	0.1589	0.1889	0.1563	0.1337	0.1673	0.1663	0.1418	0.2160	0.2066	0.1563	0.1105	0.1721	0.1418	0.1590
	FBTRCA	0.1524	0.1751	0.1721	0.1524	0.1549	0.1549	0.1177	0.1687	0.1687	0.1223	0.1506	0.1333	0.1021	0.1848	0.1764	0.1524
12	STRCA	0.2010	0.1430	0.1853	0.0939	0.1359	0.1463	0.2271	0.2366	0.1370	0.1693	0.1073	0.0944	0.2042	0.1288	0.1430	0.1569
	CNN	0.1821	0.1650	0.1247	0.1385	0.1500	0.1054	0.1874	0.1247	0.0667	0.1324	0.1430	0.1576	0.0915	0.1772	0.0707	0.1845
	FBTRCA	0.2151	0.2378	0.1449	0.1533	0.1714	0.0973	0.1660	0.1449	0.1687	0.1936	0.1405	0.1391	0.0876	0.1721	0.1549	0.1592
13	STRCA	0.1776	0.1926	0.1150	0.1385	0.1071	0.1821	0.0878	0.1684	0.1067	0.1713	0.1619	0.1337	0.1160	0.1647	0.1101	0.1422
	CNN	0.1429	0.1870	0.2019	0.1227	0.1197	0.2187	0.1054	0.1118	0.1831	0.1969	0.1398	0.1398	0.1729	0.1650	0.1619	0.1574
	FBTRCA	0.1419	0.1870	0.1497	0.1618	0.1572	0.1488	0.1088	0.1425	0.1000	0.2214	0.1059	0.1449	0.2119	0.1370	0.1101	0.1486
14	STRCA	0.0657	0.1197	0.0483	0.1246	0.1660	0.1494	0.1033	0.1054	0.2012	0.1713	0.1829	0.1486	0.2082	0.1673	0.1713	0.1422
	CNN	0.0883	0.1687	0.1075	0.0963	0.1385	0.1398	0.1033	0.1870	0.1408	0.2189	0.1194	0.1076	0.1048	0.1048	0.1989	0.1433
	FBTRCA	0.0708	0.1229	0.0850	0.1067	0.1450	0.1155	0.1160	0.1212	0.2134	0.1687	0.0973	0.1148	0.1963	0.0973	0.1524	0.1282
15	STRCA	0.1000	0.1656	0.1075	0.1229	0.1197	0.1524	0.1512	0.1660	0.0796	0.1640	0.1105	0.1080	0.1476	0.1449	0.1174	0.1305
	CNN	0.1150	0.1430	0.1398	0.1476	0.1135	0.0816	0.1088	0.1738	0.1227	0.1309	0.1523	0.1054	0.1952	0.1838	0.1337	0.1318
	FBTRCA	0.1246	0.1660	0.1333	0.1434	0.1853	0.1476	0.1071	0.1434	0.1355	0.2163	0.1829	0.1021	0.1476	0.1636	0.1549	0.1502
Average	STRCA	0.1464	0.1377	0.1176	0.1206	0.1452	0.1307	0.1401	0.1470	0.1408	0.1777	0.1445	0.1483	0.1507	0.1470	0.1442	0.1424
	CNN	0.1313	0.1446	0.1352	0.1416	0.1234	0.1465	0.1260	0.1487	0.1476	0.1652	0.1637	0.1428	0.1477	0.1484	0.1442	0.1438
	FBTRCA	0.1377	0.1425	0.1280	0.1380	0.1352	0.1309	0.1229	0.1454	0.1478	0.1512	0.1630	0.1371	0.1545	0.1376	0.1415	0.1409

Table 7. Deviation of Classification Accuracies of Dataset I (RP) Across Ten Folds (Movement vs Resting)

Subject	Method	Motion Pair										Average	
		EF-RE	EE-RE	SU-RE	PR-RE	HC-RE	HO-RE	HO-RE	HO-RE	HO-RE	HO-RE		
1	STRCA	0.1032	0.0977	0.1430	0.1567	0.1229	0.1350	0.1264					
	CNN	0.0963	0.0963	0.0820	0.1033	0.0949	0.0943	0.0945					
	FBTRCA	0.0748	0.0575	0.0586	0.1101	0.0919	0.0876	0.0801					
2	STRCA	0.1265	0.0843	0.1197	0.0994	0.1197	0.0994	0.1082					
	CNN	0.1398	0.0738	0.0699	0.1174	0.1370	0.0994	0.1062					
	FBTRCA	0.1101	0.0738	0.0632	0.1059	0.0972	0.1398	0.0983					
3	STRCA	0.1192	0.0351	0.0699	0.1059	0.0904	0.1430	0.0939					
	CNN	0.0805	0.0439	0.1197	0.1155	0.1300	0.0843	0.0957					
	FBTRCA	0.0829	0.0583	0.0816	0.1549	0.0977	0.1033	0.0965					
4	STRCA	0.0796	0.0963	0.0816	0.0876	0.0671	0.1160	0.0880					
	CNN	0.0796	0.0636	0.0738	0.1179	0.0857	0.2011	0.1036					
	FBTRCA	0.0835	0.0883	0.0919	0.1054	0.1134	0.2111	0.1156					
5	STRCA	0.1703	0.1563	0.1509	0.1287	0.1650	0.1647	0.1560					
	CNN	0.0789	0.0789	0.1101	0.1370	0.1155	0.1135	0.1058					
	FBTRCA	0.1246	0.1287	0.1449	0.1287	0.0919	0.1160	0.1224					
6	STRCA	0.0583	0.0562	0.0904	0.0915	0.1088	0.1067	0.0853					
	CNN	0.0439	0.0439	0.1000	0.0820	0.0748	0.0977	0.0737					
	FBTRCA	0.0583	0.0430	0.0742	0.1177	0.1170	0.1000	0.0850					
7	STRCA	0.1115	0.0786	0.0575	0.0878	0.1188	0.1150	0.0940					
	CNN	0.1270	0.1054	0.1088	0.0614	0.1342	0.1472	0.1140					
	FBTRCA	0.0896	0.0861	0.0939	0.1088	0.1286	0.1289	0.1060					
8	STRCA	0.0703	0.0896	0.0796	0.1485	0.0767	0.0977	0.0937					
	CNN	0.1043	0.1125	0.1000	0.1150	0.0904	0.0862	0.1014					
	FBTRCA	0.0810	0.0766	0.1150	0.0883	0.1118	0.1032	0.0960					
9	STRCA	0.1142	0.0708	0.1938	0.2019	0.1227	0.1118	0.1359					
	CNN	0.0583	0.1669	0.1868	0.0857	0.0982	0.1138	0.1183					
	FBTRCA	0.0883	0.1329	0.1154	0.1359	0.1385	0.0904	0.1169					
10	STRCA	0.0636	0.0671	0.0699	0.1197	0.1430	0.1033	0.0944					
	CNN	0.0857	0.0835	0.0966	0.1425	0.1135	0.1430	0.1108					
	FBTRCA	0.0636	0.0717	0.0949	0.1227	0.0675	0.1174	0.0896					
11	STRCA	0.1197	0.1174	0.1398	0.1391	0.1370	0.1370	0.1317					
	CNN	0.0675	0.1549	0.1350	0.1660	0.0966	0.1252	0.1242					
	FBTRCA	0.0949	0.1197	0.1033	0.1640	0.1252	0.1370	0.1240					
12	STRCA	0.0963	0.1197	0.1288	0.1309	0.1179	0.2119	0.1343					
	CNN	0.1000	0.1524	0.1410	0.0876	0.1524	0.2025	0.1393					
	FBTRCA	0.0671	0.1229	0.1576	0.1171	0.1075	0.1494	0.1203					
13	STRCA	0.0861	0.0791	0.1300	0.1300	0.1663	0.0575	0.1081					
	CNN	0.1024	0.0966	0.1342	0.1289	0.1118	0.0904	0.1107					
	FBTRCA	0.0805	0.0998	0.1790	0.0835	0.0904	0.0963	0.1049					
14	STRCA	0.0896	0.0829	0.1174	0.1080	0.1197	0.1212	0.1065					
	CNN	0.0615	0.0583	0.1269	0.1075	0.1050	0.0636	0.0871					
	FBTRCA	0.0900	0.0861	0.1398	0.0943	0.1000	0.1071	0.1029					
15	STRCA	0.0796	0.0878	0.1317	0.0857	0.0671	0.1150	0.0945					
	CNN	0.0939	0.0615	0.0904	0.0717	0.1032	0.0963	0.0877					
	FBTRCA	0.0767	0.0861	0.1054	0.1032	0.1032	0.1150	0.0983					
Average	STRCA	0.0992	0.0879	0.1136	0.1214	0.1159	0.1223	0.1101					
	CNN	0.0880	0.0928	0.1123	0.1093	0.1095	0.1172	0.1049					
	FBTRCA	0.0844	0.0888	0.1079	0.1160	0.1054	0.1202	0.1038					

Improving Pre-movement Pattern Detection with Filter Bank Selection

Table 8. Mean of Classification Accuracies of Dataset I (RP+MMP) Across Ten Folds (Movement vs Movement)

Subject	Method	Motion Pair															Average
		EF-EE	EF-SU	EF-PR	EF-HC	EF-HO	EE-SU	EE-PR	EE-HC	EE-HO	SU-PR	SU-HC	SU-HO	PR-HC	PR-HO	HC-HO	
1	STRCA	0.4917	0.6700	0.8273	0.7182	0.5909	0.5800	0.7273	0.7273	0.6000	0.8111	0.7111	0.6333	0.6000	0.6200	0.6600	0.6645
	CNN	0.5417	0.6900	0.9091	0.7636	0.7364	0.6400	0.9000	0.7909	0.7364	0.9111	0.7778	0.7556	0.5800	0.6500	0.6300	0.7342
	FBTRCA	0.5500	0.7100	0.9273	0.8091	0.7273	0.6900	0.9182	0.8364	0.7545	0.9222	0.8000	0.7889	0.5900	0.6900	0.6500	0.7576
2	STRCA	0.5300	0.5700	0.8700	0.6000	0.5200	0.5600	0.8100	0.6100	0.4900	0.7400	0.4900	0.5500	0.6400	0.6700	0.5000	0.6100
	CNN	0.5100	0.6500	0.9100	0.5700	0.5000	0.6300	0.8600	0.5300	0.6300	0.7600	0.5200	0.6100	0.7000	0.7200	0.4500	0.6353
	FBTRCA	0.5900	0.6500	0.9400	0.5700	0.5600	0.6100	0.8900	0.6100	0.6600	0.7700	0.5900	0.5900	0.7100	0.7400	0.4200	0.6600
3	STRCA	0.5083	0.7000	0.7500	0.8364	0.7600	0.5800	0.7400	0.9273	0.8400	0.5500	0.6444	0.7000	0.5333	0.6500	0.7111	0.6954
	CNN	0.6917	0.8100	0.7900	0.9455	0.9200	0.7400	0.8400	0.9455	0.9600	0.7125	0.7333	0.8000	0.6000	0.5500	0.6333	0.7781
	FBTRCA	0.7333	0.8500	0.8500	0.9273	0.9100	0.7700	0.8500	0.9545	0.9600	0.6875	0.8000	0.7875	0.5889	0.7000	0.6333	0.8002
4	STRCA	0.5583	0.6182	0.9545	0.8833	0.8000	0.5818	0.9273	0.8500	0.7818	0.9000	0.8455	0.8500	0.5900	0.5700	0.6000	0.7541
	CNN	0.5833	0.7091	0.9909	0.9417	0.8455	0.7000	0.9636	0.9167	0.8545	0.9800	0.9091	0.9400	0.6000	0.6300	0.6273	0.8128
	FBTRCA	0.6417	0.7000	0.9727	0.9500	0.8686	0.6909	0.9636	0.9250	0.8818	0.9800	0.9545	0.9500	0.6000	0.6700	0.6455	0.8260
5	STRCA	0.5818	0.5909	0.8182	0.6818	0.6545	0.7100	0.9100	0.8500	0.8000	0.5900	0.6000	0.6000	0.5700	0.5100	0.5800	0.6698
	CNN	0.6182	0.7364	0.8455	0.8091	0.7727	0.7700	0.9600	0.8800	0.7900	0.6000	0.5700	0.4900	0.6200	0.5000	0.5300	0.7008
	FBTRCA	0.5818	0.6273	0.9091	0.8000	0.7273	0.7300	0.9700	0.8400	0.8300	0.6400	0.5300	0.5000	0.5700	0.5600	0.5600	0.6917
6	STRCA	0.5000	0.6000	0.9333	0.7364	0.8364	0.5455	0.9333	0.6945	0.8091	0.6625	0.5900	0.7100	0.6750	0.6250	0.6400	0.6967
	CNN	0.6250	0.6273	0.9333	0.8182	0.8727	0.6091	0.9111	0.6636	0.8545	0.6625	0.5500	0.6900	0.6125	0.5625	0.6200	0.7075
	FBTRCA	0.6083	0.7091	0.9667	0.7727	0.8818	0.6091	0.9222	0.6900	0.8545	0.7000	0.4800	0.6700	0.6875	0.6000	0.6200	0.7121
7	STRCA	0.4917	0.6182	0.8455	0.7091	0.6909	0.5545	0.8636	0.7182	0.7091	0.6300	0.5500	0.5500	0.5900	0.5200	0.4900	0.6354
	CNN	0.5583	0.6455	0.9364	0.7455	0.8455	0.5273	0.8909	0.7364	0.7091	0.6200	0.6000	0.6100	0.6200	0.5000	0.5800	0.6756
	FBTRCA	0.5417	0.6636	0.9364	0.7636	0.6909	0.5818	0.8909	0.7364	0.7000	0.6800	0.5800	0.7000	0.6600	0.5200	0.4900	0.6670
8	STRCA	0.4583	0.6182	0.8545	0.7727	0.7000	0.5636	0.8818	0.6727	0.6455	0.7700	0.6400	0.7000	0.5000	0.5500	0.5300	0.6572
	CNN	0.4917	0.6545	0.9455	0.7455	0.7818	0.6000	0.9364	0.6727	0.7455	0.8500	0.5800	0.6300	0.5500	0.5200	0.5500	0.6836
	FBTRCA	0.4917	0.7364	0.9364	0.8000	0.7727	0.6364	0.9273	0.7273	0.7636	0.8600	0.7000	0.6800	0.5400	0.6100	0.5300	0.7141
9	STRCA	0.7083	0.7973	0.8364	0.7636	0.7545	0.6455	0.7818	0.7364	0.7273	0.6400	0.4900	0.5600	0.5700	0.6200	0.5900	0.6767
	CNN	0.8417	0.8182	0.9455	0.7818	0.8091	0.6909	0.8909	0.8091	0.8091	0.5900	0.4800	0.7300	0.5400	0.7100	0.5700	0.7344
	FBTRCA	0.8917	0.7545	0.9455	0.8364	0.8091	0.6909	0.8909	0.7727	0.8273	0.6200	0.4500	0.7000	0.5800	0.7000	0.6600	0.7462
10	STRCA	0.5167	0.5364	0.7250	0.8545	0.6455	0.5545	0.6583	0.7818	0.7636	0.6545	0.6800	0.7200	0.6545	0.4636	0.5600	0.6513
	CNN	0.5083	0.6000	0.7250	0.8091	0.7636	0.5909	0.7917	0.8364	0.6182	0.7636	0.8200	0.7200	0.6000	0.5818	0.5200	0.6832
	FBTRCA	0.4833	0.6000	0.7750	0.8545	0.7364	0.6000	0.7583	0.8455	0.7636	0.6636	0.8000	0.7000	0.6455	0.5455	0.6100	0.6921
11	STRCA	0.4900	0.6600	0.6889	0.6100	0.5800	0.6700	0.7000	0.5700	0.5700	0.6444	0.6700	0.6200	0.5111	0.5778	0.4900	0.6035
	CNN	0.5100	0.6900	0.7667	0.6100	0.6600	0.5900	0.7111	0.6500	0.5800	0.6333	0.5800	0.7200	0.5000	0.6000	0.4400	0.6161
	FBTRCA	0.5300	0.7100	0.8000	0.7000	0.6700	0.6200	0.8000	0.6700	0.6400	0.6444	0.6700	0.7500	0.5522	0.5556	0.3800	0.6441
12	STRCA	0.5636	0.6100	0.7900	0.7182	0.7364	0.6333	0.7778	0.6700	0.7100	0.6250	0.5667	0.5889	0.5667	0.4344	0.5400	0.6361
	CNN	0.6545	0.5600	0.8900	0.7909	0.7818	0.7222	0.8889	0.6600	0.8100	0.6625	0.4667	0.7000	0.5333	0.4889	0.4900	0.6733
	FBTRCA	0.6636	0.6500	0.9200	0.7818	0.8000	0.6778	0.9111	0.7400	0.8400	0.8000	0.7000	0.7444	0.6222	0.5444	0.5100	0.7270
13	STRCA	0.5083	0.5929	0.7636	0.6909	0.5182	0.5445	0.8182	0.7455	0.6636	0.6100	0.6200	0.4600	0.5300	0.6400	0.5200	0.6156
	CNN	0.4500	0.5727	0.8455	0.7182	0.6636	0.6455	0.8182	0.6273	0.6818	0.5900	0.6200	0.5300	0.5700	0.5000	0.6399	0.6999
	FBTRCA	0.5250	0.6273	0.8818	0.8182	0.6636	0.6545	0.9091	0.8182	0.6818	0.6500	0.7000	0.5900	0.5200	0.5500	0.5700	0.6773
14	STRCA	0.5250	0.6100	0.8900	0.7545	0.6818	0.6400	0.8300	0.8000	0.6000	0.6750	0.5889	0.6444	0.5556	0.6556	0.4800	0.6621
	CNN	0.6000	0.6900	0.9400	0.8727	0.8000	0.7636	0.9500	0.7636	0.7455	0.7500	0.5889	0.6667	0.6667	0.6889	0.4900	0.7223
	FBTRCA	0.6250	0.7000	0.9300	0.8545	0.8727	0.6100	0.9300	0.8273	0.7727	0.8000	0.6556	0.6556	0.6000	0.7444	0.4700	0.7365
15	STRCA	0.3727	0.7000	0.7900	0.6800	0.8000	0.7300	0.8727	0.6909	0.8091	0.6778	0.6667	0.6333	0.6600	0.5800	0.6600	0.6882
	CNN	0.5182	0.6889	0.8700	0.7200	0.8500	0.8200	0.8818	0.6364	0.7636	0.6333	0.6333	0.6444	0.6200	0.4600	0.6400	0.6920
	FBTRCA	0.4455	0.7222	0.9500	0.7000	0.8600	0.7500	0.9091	0.7182	0.8545	0.7444	0.6667	0.6222	0.6600	0.5500	0.5800	0.7155
Average	STRCA	0.5203	0.6280	0.8225	0.7340	0.6846	0.6069	0.8155	0.7336	0.7013	0.6787	0.6235	0.6347	0.5831	0.5798	0.5701	0.6611
	CNN	0.5829	0.6748	0.8829	0.7761	0.7735	0.6591	0.8796	0.7540	0.7586	0.7049	0.6282	0.6832	0.5942	0.5574	0.5574	0.6993
	FBTRCA	0.5935	0.6940	0.9094	0.7959	0.7697	0.6651	0.8967	0.7748	0.7856	0.7441	0.6718	0.6866	0.6064	0.6187	0.6187	0.7178

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Table 9. Deviation of Classification Accuracies of Dataset I (RP+MMP) Across Ten Folds (Movement vs Movement)

Subject	Method	Motion Pair																Average
		EF-EE	EF-SU	EF-PR	EF-HC	EF-HO	EE-SU	EE-PR	EE-HC	EE-HO	SU-PR	SU-HC	SU-HO	PR-HC	PR-HO	HC-HO		
1	STRCA	0.1819	0.0949	0.1629	0.1170	0.1560	0.2044	0.1355	0.1134	0.1671	0.2098	0.1500	0.1391	0.1247	0.1033	0.1713	0.1487	
	CNN	0.1483	0.0876	0.0857	0.1150	0.1572	0.1430	0.0962	0.0862	0.0904	0.0703	0.0907	0.1366	0.1317	0.1269	0.1337	0.1108	
	FBTRCA	0.0805	0.1287	0.0575	0.0904	0.1134	0.0994	0.1000	0.1271	0.0963	0.0715	0.1366	0.1105	0.1449	0.1197	0.1650	0.1108	
2	STRCA	0.1947	0.1703	0.1337	0.1633	0.1135	0.1265	0.1663	0.1101	0.2424	0.1350	0.1853	0.1434	0.1713	0.1494	0.1414	0.1564	
	CNN	0.1197	0.1252	0.0876	0.1947	0.1333	0.1160	0.1350	0.1160	0.1252	0.1265	0.1969	0.1229	0.1563	0.1229	0.2068	0.1437	
	FBTRCA	0.0876	0.1780	0.0699	0.2111	0.1350	0.1197	0.1101	0.1101	0.2221	0.2003	0.2025	0.1729	0.1370	0.0966	0.1753	0.1489	
3	STRCA	0.2058	0.1247	0.1269	0.0575	0.1350	0.1687	0.1713	0.0939	0.1075	0.1687	0.1721	0.1344	0.1021	0.1419	0.1753	0.1391	
	CNN	0.1182	0.0894	0.0738	0.0636	0.0632	0.1174	0.1075	0.0469	0.0516	0.1868	0.1589	0.1467	0.1829	0.1882	0.1486	0.1169	
	FBTRCA	0.1230	0.1434	0.1080	0.0575	0.0876	0.1252	0.1080	0.0479	0.0966	0.1792	0.1366	0.1324	0.0915	0.1467	0.1177	0.1134	
4	STRCA	0.1524	0.1032	0.0643	0.1125	0.1342	0.1828	0.0575	0.1097	0.1434	0.0816	0.1289	0.1354	0.1372	0.1889	0.1067	0.1226	
	CNN	0.0962	0.0575	0.0287	0.0562	0.0862	0.1138	0.0469	0.1039	0.1067	0.0422	0.0742	0.0516	0.1376	0.1160	0.1000	0.0811	
	FBTRCA	0.1364	0.1216	0.0439	0.0703	0.0694	0.1497	0.0636	0.0917	0.1054	0.0422	0.0773	0.0707	0.1300	0.1160	0.1170	0.0933	
5	STRCA	0.1227	0.1278	0.1286	0.1154	0.1472	0.1524	0.1101	0.1179	0.1414	0.1595	0.2404	0.1944	0.1418	0.1524	0.1033	0.1467	
	CNN	0.1954	0.1512	0.1054	0.0796	0.1500	0.1252	0.0516	0.0919	0.0738	0.1563	0.1494	0.1101	0.1317	0.1033	0.1494	0.1216	
	FBTRCA	0.1828	0.0796	0.0742	0.1032	0.1286	0.0949	0.0675	0.1975	0.0949	0.1265	0.1252	0.1944	0.1567	0.1075	0.1647	0.1205	
6	STRCA	0.1800	0.1300	0.0574	0.1938	0.1342	0.1355	0.0777	0.1592	0.1246	0.1773	0.1729	0.1370	0.1054	0.1768	0.1955	0.1438	
	CNN	0.0982	0.1890	0.0777	0.1134	0.0977	0.0862	0.1148	0.1138	0.0977	0.1672	0.1269	0.0994	0.1376	0.1693	0.1989	0.1259	
	FBTRCA	0.1182	0.1808	0.0537	0.1437	0.1216	0.1054	0.0750	0.1973	0.0878	0.1344	0.1814	0.1337	0.1215	0.2555	0.1229	0.1355	
7	STRCA	0.1687	0.1592	0.1138	0.1592	0.1150	0.1938	0.0982	0.1088	0.1271	0.2058	0.1841	0.1509	0.1370	0.1874	0.1287	0.1492	
	CNN	0.1043	0.1170	0.0748	0.1271	0.0862	0.1408	0.0835	0.1738	0.0717	0.1687	0.1414	0.1197	0.1687	0.1155	0.1663	0.1240	
	FBTRCA	0.1195	0.1138	0.0748	0.1300	0.1369	0.0878	0.0835	0.1170	0.1425	0.1476	0.1398	0.1767	0.2221	0.1476	0.1197	0.1306	
8	STRCA	0.1375	0.1032	0.0977	0.1372	0.1289	0.1118	0.0748	0.0977	0.1246	0.1160	0.2119	0.1247	0.1247	0.1337	0.1352	0.1255	
	CNN	0.1544	0.1472	0.0777	0.1342	0.1067	0.1216	0.1369	0.0835	0.1434	0.0919	0.1252	0.1252	0.1650	0.2098	0.1344	0.1344	
	FBTRCA	0.1072	0.1684	0.0748	0.1118	0.1071	0.1545	0.0939	0.1545	0.1369	0.0843	0.1155	0.1814	0.1174	0.1729	0.1418	0.1282	
9	STRCA	0.1128	0.1603	0.1408	0.1227	0.1359	0.1385	0.0878	0.1512	0.1818	0.4430	0.1370	0.1265	0.1494	0.1932	0.1853	0.1444	
	CNN	0.0917	0.0606	0.0636	0.1150	0.0904	0.1150	0.0835	0.1000	0.1088	0.2283	0.1549	0.1418	0.1265	0.1370	0.1829	0.1200	
	FBTRCA	0.0883	0.1216	0.0469	0.1271	0.1317	0.1342	0.0904	0.0835	0.0516	0.1814	0.1354	0.1563	0.1619	0.1155	0.1578	0.1192	
10	STRCA	0.1459	0.1000	0.1364	0.1300	0.1170	0.1841	0.1208	0.0767	0.1369	0.1907	0.1317	0.1814	0.1408	0.1088	0.1265	0.1352	
	CNN	0.1270	0.1300	0.1472	0.1738	0.1149	0.1154	0.0982	0.1118	0.0977	0.2001	0.1229	0.1434	0.1369	0.1814	0.1398	0.1259	
	FBTRCA	0.1561	0.1369	0.0883	0.1067	0.1000	0.1434	0.0998	0.0963	0.1227	0.1770	0.1414	0.0943	0.1246	0.1714	0.1595	0.1279	
11	STRCA	0.2283	0.1506	0.1463	0.2079	0.1033	0.2452	0.1576	0.2058	0.1494	0.2082	0.1636	0.1476	0.1494	0.1148	0.1595	0.1672	
	CNN	0.1969	0.0876	0.1223	0.1197	0.1578	0.1287	0.1304	0.1900	0.1476	0.1892	0.1751	0.1317	0.1757	0.1673	0.2171	0.1558	
	FBTRCA	0.1636	0.1197	0.1148	0.1563	0.1494	0.1476	0.1366	0.2003	0.1578	0.1366	0.1829	0.2369	0.0915	0.1656	0.1033	0.1509	
12	STRCA	0.1032	0.1969	0.1101	0.1684	0.0904	0.1288	0.1571	0.1494	0.1449	0.1318	0.2124	0.1486	0.1772	0.1889	0.2011	0.1540	
	CNN	0.1271	0.1713	0.0994	0.1717	0.0878	0.1907	0.1283	0.1647	0.1663	0.1672	0.1366	0.0915	0.1073	0.1370	0.1407	0.1193	
	FBTRCA	0.0963	0.2369	0.0632	0.1434	0.1032	0.2250	0.1148	0.1430	0.1350	0.0874	0.1288	0.0915	0.1304	0.1610	0.2234	0.1389	
13	STRCA	0.1329	0.1928	0.1369	0.1227	0.1216	0.1317	0.0958	0.1118	0.1821	0.2234	0.1135	0.1838	0.1494	0.1506	0.1687	0.1478	
	CNN	0.0805	0.1870	0.0862	0.1450	0.0963	0.1317	0.0857	0.1355	0.0904	0.1287	0.1476	0.2312	0.1337	0.1581	0.1751	0.1342	
	FBTRCA	0.1574	0.1890	0.0862	0.0606	0.1216	0.1472	0.0857	0.1355	0.1071	0.2273	0.1195	0.1729	0.1317	0.1900	0.1418	0.1380	
14	STRCA	0.1115	0.1197	0.0876	0.1606	0.1231	0.1578	0.0823	0.1032	0.1434	0.1787	0.1818	0.0703	0.2095	0.1223	0.1549	0.1338	
	CNN	0.1165	0.1595	0.0699	0.0767	0.1032	0.1197	0.0527	0.1150	0.1197	0.1768	0.1576	0.0973	0.1656	0.1148	0.1449	0.1193	
	FBTRCA	0.1318	0.1054	0.0675	0.1067	0.1150	0.1101	0.0675	0.0796	0.0982	0.1581	0.1610	0.1223	0.1829	0.1177	0.2111	0.1223	
15	STRCA	0.1385	0.1818	0.1370	0.1229	0.1054	0.1252	0.1150	0.1067	0.1450	0.1610	0.0907	0.1391	0.1430	0.1398	0.1647	0.1344	
	CNN	0.1488	0.2082	0.1160	0.0919	0.0972	0.1317	0.0748	0.1134	0.0977	0.1288	0.1177	0.1554	0.1874	0.2366	0.1506	0.1371	
	FBTRCA	0.1938	0.2045	0.0707	0.1054	0.0966	0.1509	0.0742	0.1512	0.1150	0.1391	0.1481	0.1405	0.1075	0.1900	0.1033	0.1327	
Average	STRCA	0.1545	0.1440	0.1187	0.1394	0.1260	0.1591	0.1139	0.1210	0.1508	0.1660	0.1651	0.1438	0.1422	0.1518	0.1544	0.1432	
	CNN	0.1282	0.1319	0.0877	0.1185	0.1109	0.1312	0.0930	0.1200	0.1019	0.1359	0.1331	0.1282	0.1538	0.1473	0.1613	0.1271	
	FBTRCA	0.1295	0.1485	0.0730	0.1150	0.1141	0.1330	0.0914	0.1232	0.1180	0.1408	0.1419	0.1458	0.1368	0.1516	0.1487	0.1274	

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Table 10. Mean of Classification Accuracies of Dataset I (RP+MMP) Across Ten Folds (Movement vs Resting)

Subject	Method	Motion Pair									Average
		EF-RE	EE-RE	SU-RE	PR-RE	HC-RE	HO-RE	HO-RE	HO-RE	HO-RE	
1	STRCA	0.8636	0.8545	0.8444	0.7300	0.7700	0.8000	0.8104	0.8000	0.8104	
	CNN	0.9545	0.9000	0.9333	0.8700	0.8400	0.9200	0.9030	0.9200	0.9030	
	FBTRCA	0.9727	0.9273	0.9444	0.8700	0.8500	0.9200	0.9141	0.9200	0.9141	
2	STRCA	0.9300	0.9100	0.8600	0.7700	0.8400	0.8200	0.8550	0.8200	0.8550	
	CNN	0.9500	0.9100	0.8800	0.8300	0.8500	0.7900	0.8600	0.7900	0.8600	
	FBTRCA	0.9900	0.9400	0.9000	0.8500	0.8800	0.8700	0.9050	0.8700	0.9050	
3	STRCA	0.9333	0.9417	0.8000	0.7600	0.7545	0.8200	0.8349	0.8200	0.8349	
	CNN	0.9583	1.0000	0.9000	0.8900	0.8364	0.8700	0.9091	0.8700	0.9091	
	FBTRCA	0.9583	1.0000	0.9000	0.8900	0.8091	0.9000	0.9096	0.9000	0.9096	
4	STRCA	0.9545	0.9273	0.9400	0.7800	0.8000	0.8100	0.8686	0.8100	0.8686	
	CNN	0.9727	0.9636	1.0000	0.8800	0.8818	0.8600	0.9264	0.8600	0.9264	
	FBTRCA	0.9909	0.9636	1.0000	0.8700	0.8909	0.8800	0.9326	0.8800	0.9326	
5	STRCA	0.8636	0.9400	0.7500	0.7000	0.7400	0.7400	0.7889	0.7400	0.7889	
	CNN	0.9364	0.9600	0.8200	0.7800	0.8300	0.8100	0.8561	0.8100	0.8561	
	FBTRCA	0.9364	0.9800	0.8100	0.7900	0.8100	0.8100	0.8561	0.8100	0.8561	
6	STRCA	0.9833	0.9833	0.8273	0.9000	0.8455	0.8273	0.8944	0.8273	0.8944	
	CNN	1.0000	1.0000	0.9455	0.9111	0.9364	0.8545	0.9412	0.8545	0.9412	
	FBTRCA	0.9917	1.0000	0.9455	0.8889	0.9273	0.8818	0.9392	0.8818	0.9392	
7	STRCA	0.8417	0.8750	0.7009	0.6545	0.6686	0.6364	0.7437	0.6364	0.7437	
	CNN	0.9417	0.8583	0.7636	0.7091	0.6818	0.6636	0.7697	0.6636	0.7697	
	FBTRCA	0.9417	0.8917	0.8455	0.7182	0.6818	0.7091	0.7980	0.7091	0.7980	
8	STRCA	0.9750	0.9667	0.9364	0.8091	0.8545	0.9000	0.9069	0.9000	0.9069	
	CNN	1.0000	0.9833	0.9000	0.8545	0.9273	0.9545	0.9366	0.9545	0.9366	
	FBTRCA	0.9917	0.9833	0.9455	0.8545	0.9182	0.9455	0.9398	0.9455	0.9398	
9	STRCA	0.9000	0.8833	0.6909	0.7455	0.6364	0.7182	0.7624	0.6364	0.7624	
	CNN	0.9750	0.9750	0.8455	0.8000	0.8091	0.8636	0.8780	0.8636	0.8780	
	FBTRCA	0.9833	0.9750	0.8455	0.8273	0.8455	0.8364	0.8555	0.8364	0.8555	
10	STRCA	0.9000	0.9364	0.8100	0.7636	0.7100	0.8300	0.8250	0.8300	0.8250	
	CNN	0.9273	0.9364	0.9000	0.8000	0.8100	0.8700	0.8739	0.8700	0.8739	
	FBTRCA	0.9364	0.9636	0.9200	0.8636	0.8500	0.8900	0.9039	0.8900	0.9039	
11	STRCA	0.8200	0.8400	0.8300	0.6889	0.7300	0.6500	0.7598	0.6500	0.7598	
	CNN	0.8900	0.8800	0.8800	0.7778	0.8500	0.7800	0.8430	0.7800	0.8430	
	FBTRCA	0.9300	0.9300	0.8600	0.7556	0.8600	0.8400	0.8626	0.8400	0.8626	
12	STRCA	0.9273	0.9300	0.8444	0.6667	0.7900	0.6700	0.8047	0.6700	0.8047	
	CNN	0.9091	0.9000	0.9111	0.8000	0.8500	0.8000	0.8617	0.8000	0.8617	
	FBTRCA	0.9455	0.9200	0.8889	0.7556	0.8600	0.8400	0.8683	0.8400	0.8683	
13	STRCA	0.9250	0.9250	0.7545	0.6909	0.7545	0.7909	0.8068	0.7909	0.8068	
	CNN	0.9583	0.9750	0.8273	0.7727	0.7636	0.8455	0.8571	0.8455	0.8571	
	FBTRCA	0.9750	0.9667	0.8455	0.8909	0.8182	0.8727	0.8948	0.8727	0.8948	
14	STRCA	0.9500	0.9333	0.8300	0.7000	0.8364	0.7636	0.8356	0.7636	0.8356	
	CNN	0.9833	0.9833	0.8700	0.8100	0.9364	0.9091	0.9154	0.9091	0.9154	
	FBTRCA	0.9833	0.9750	0.9300	0.8400	0.9000	0.8455	0.9123	0.8455	0.9123	
15	STRCA	0.9182	0.9167	0.8200	0.8091	0.7818	0.8182	0.8440	0.8182	0.8440	
	CNN	0.9727	0.9667	0.9200	0.9000	0.8818	0.8273	0.9114	0.8273	0.9114	
	FBTRCA	0.9818	0.9667	0.9400	0.8818	0.9364	0.8727	0.9299	0.8727	0.9299	
Average	STRCA	0.9124	0.9175	0.8219	0.7446	0.7672	0.7730	0.8228	0.7730	0.8228	
	CNN	0.9553	0.9461	0.8864	0.8257	0.8412	0.8412	0.8828	0.8412	0.8828	
	FBTRCA	0.9672	0.9589	0.9014	0.8364	0.8558	0.8609	0.8968	0.8609	0.8968	

Table 11. Deviation of Classification Accuracies of Dataset I (RP+MMP) Across Ten Folds (Movement vs Resting)

Subject	Method	Motion Pair										Average
		EF-RE	EE-RE	SU-RE	PR-RE	HC-RE	HO-RE	HO-RE	HO-RE	HO-RE	HO-RE	
1	STRCA	0.0773	0.1300	0.1304	0.1252	0.0823	0.1414	0.1414	0.1414	0.1414	0.1414	0.1144
	CNN	0.0643	0.0904	0.0777	0.0949	0.0966	0.0789	0.0789	0.0789	0.0789	0.0789	0.0838
	FBTRCA	0.0614	0.0939	0.0586	0.0949	0.0972	0.1033	0.1033	0.1033	0.1033	0.1033	0.0849
2	STRCA	0.0675	0.0738	0.0966	0.1160	0.1430	0.1317	0.1430	0.1317	0.1430	0.1317	0.1047
	CNN	0.1080	0.0738	0.1135	0.0949	0.1563	0.1101	0.1094	0.1101	0.1101	0.1094	0.0758
	FBTRCA	0.0316	0.0516	0.0816	0.0707	0.1033	0.1160	0.1160	0.1160	0.1160	0.1160	0.0758
3	STRCA	0.0766	0.0686	0.1633	0.1075	0.1488	0.1135	0.1488	0.1135	0.1488	0.1135	0.1130
	CNN	0.0589	0.0000	0.0943	0.1197	0.1118	0.0949	0.0949	0.0949	0.0949	0.0949	0.0799
	FBTRCA	0.0708	0.0000	0.0943	0.1197	0.1246	0.0943	0.0943	0.0943	0.0943	0.0943	0.0839
4	STRCA	0.0479	0.0939	0.0516	0.1476	0.1342	0.1449	0.1342	0.1449	0.1342	0.1449	0.1033
	CNN	0.0439	0.0636	0.0000	0.1229	0.1054	0.1350	0.1054	0.1350	0.1054	0.0785	0.0785
	FBTRCA	0.0287	0.0767	0.0000	0.1059	0.0575	0.1874	0.0575	0.1874	0.0575	0.1874	0.0760
5	STRCA	0.1071	0.0699	0.1900	0.1633	0.1174	0.1578	0.1174	0.1578	0.1174	0.1343	
	CNN	0.1359	0.0699	0.1317	0.1135	0.0949	0.0994	0.0994	0.0994	0.0994	0.1075	
	FBTRCA	0.0963	0.0422	0.1370	0.1370	0.0994	0.1729	0.0994	0.1729	0.0994	0.1141	
6	STRCA	0.0351	0.0351	0.1684	0.0973	0.1138	0.1450	0.1138	0.1450	0.1138	0.0991	
	CNN	0.0000	0.0000	0.0767	0.0876	0.0614	0.1227	0.0614	0.1227	0.0614	0.0581	
	FBTRCA	0.0264	0.0000	0.0636	0.0907	0.0939	0.1054	0.0939	0.1054	0.0939	0.0633	
7	STRCA	0.0998	0.1128	0.1359	0.1408	0.1488	0.1545	0.1488	0.1545	0.1488	0.1321	
	CNN	0.0791	0.0791	0.1557	0.1197	0.1437	0.1359	0.1437	0.1359	0.1437	0.1188	
	FBTRCA	0.0562	0.0966	0.1606	0.1246	0.1437	0.0835	0.1437	0.0835	0.1437	0.1109	
8	STRCA	0.0403	0.0583	0.0439	0.1088	0.0878	0.1246	0.0878	0.1246	0.0878	0.0773	
	CNN	0.0000	0.0000	0.0904	0.0878	0.0575	0.0643	0.0575	0.0643	0.0575	0.0559	
	FBTRCA	0.0264	0.0351	0.0469	0.0767	0.0904	0.0767	0.0904	0.0767	0.0904	0.0587	
9	STRCA	0.1097	0.0896	0.1497	0.1539	0.1485	0.1572	0.1485	0.1572	0.1485	0.1337	
	CNN	0.0403	0.0562	0.1717	0.1858	0.1629	0.0773	0.1629	0.0773	0.1629	0.1157	
	FBTRCA	0.0351	0.0562	0.1054	0.1385	0.1289	0.1118	0.1289	0.1118	0.1289	0.0960	
10	STRCA	0.0796	0.0963	0.1595	0.1434	0.1197	0.1160	0.1197	0.1160	0.1197	0.1191	
	CNN	0.0717	0.0614	0.1054	0.1649	0.0876	0.1160	0.0876	0.1160	0.0876	0.1011	
	FBTRCA	0.0748	0.0469	0.1033	0.1372	0.0707	0.0994	0.0707	0.0994	0.0707	0.0887	
11	STRCA	0.0919	0.1350	0.1494	0.1366	0.1418	0.2273	0.1418	0.2273	0.1418	0.1470	
	CNN	0.0994	0.0919	0.1033	0.1171	0.1354	0.1135	0.1354	0.1135	0.1354	0.1101	
	FBTRCA	0.0675	0.0675	0.0699	0.1148	0.1265	0.1174	0.1265	0.1174	0.1265	0.0939	
12	STRCA	0.1032	0.0823	0.1304	0.1048	0.1370	0.1213	0.1370	0.1213	0.1370	0.1213	
	CNN	0.0606	0.0667	0.1148	0.1261	0.0527	0.2000	0.0527	0.2000	0.0527	0.1035	
	FBTRCA	0.0469	0.0632	0.1171	0.0876	0.1075	0.1776	0.1075	0.1776	0.1075	0.1000	
13	STRCA	0.0615	0.0829	0.1289	0.1300	0.1359	0.0963	0.1359	0.0963	0.1359	0.1059	
	CNN	0.0439	0.0403	0.1385	0.1303	0.0878	0.1138	0.0878	0.1138	0.0878	0.0924	
	FBTRCA	0.0403	0.0430	0.1138	0.0835	0.0958	0.1227	0.0958	0.1227	0.0958	0.0832	
14	STRCA	0.0703	0.0766	0.1636	0.1333	0.1472	0.0767	0.1472	0.0767	0.1472	0.1113	
	CNN	0.0351	0.0351	0.0949	0.0994	0.0748	0.0958	0.0748	0.0958	0.0748	0.0725	
	FBTRCA	0.0351	0.0403	0.1059	0.1075	0.0671	0.0862	0.0671	0.0862	0.0671	0.0737	
15	STRCA	0.0904	0.0556	0.1229	0.1512	0.1067	0.1134	0.1067	0.1134	0.1067	0.1067	
	CNN	0.0439	0.0430	0.1135	0.1000	0.1216	0.1088	0.1216	0.1088	0.1216	0.0885	
	FBTRCA	0.0383	0.0430	0.0843	0.0748	0.0748	0.0878	0.0748	0.0878	0.0748	0.0672	
Average	STRCA	0.0772	0.0840	0.1323	0.1306	0.1275	0.1376	0.1275	0.1376	0.1275	0.1149	
	CNN	0.0590	0.0538	0.1055	0.1177	0.1034	0.1177	0.1034	0.1177	0.1034	0.0917	
	FBTRCA	0.0491	0.0504	0.0895	0.1043	0.0988	0.1162	0.0988	0.1162	0.0988	0.0847	

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Table 12. Mean of Classification Accuracies of Dataset II Across Ten Folds (Movement vs Movement)

Subject	Method	Motion Pair															Average
		SU-PR	SU-HO	SU-PG	SU-LG	PR-HO	PR-PG	PR-LG	HO-PG	HO-LG	PG-LG						
1	STRCA	0.6000	0.5571	0.6429	0.5286	0.5857	0.6286	0.5857	0.6000	0.5929	0.5929	0.5929	0.5914				
	CNN	0.5357	0.7071	0.6286	0.5857	0.6000	0.6000	0.6000	0.6429	0.6571	0.6429	0.6100					
	FBTRCA	0.4929	0.6571	0.6643	0.6143	0.6429	0.6571	0.6071	0.6643	0.6429	0.6571	0.5857	0.6229				
2	STRCA	0.5571	0.6571	0.6500	0.7286	0.5714	0.7071	0.6214	0.5714	0.5786	0.5143	0.6157					
	CNN	0.5500	0.6571	0.6286	0.7714	0.6714	0.7071	0.6857	0.5571	0.5286	0.6314						
	FBTRCA	0.5643	0.7000	0.6929	0.7000	0.6429	0.7071	0.7000	0.6500	0.6643	0.5143	0.6536					
3	STRCA	0.5071	0.5857	0.7000	0.6786	0.6286	0.6571	0.6214	0.5786	0.5500	0.6071	0.6114					
	CNN	0.5643	0.6500	0.7214	0.7286	0.6429	0.7143	0.6786	0.6500	0.6071	0.6143	0.6571					
	FBTRCA	0.5857	0.7571	0.7500	0.6929	0.6643	0.7357	0.6929	0.6500	0.6500	0.6714	0.6850					
4	STRCA	0.6214	0.7571	0.7786	0.8214	0.7071	0.7571	0.7643	0.6786	0.7357	0.6214	0.7243					
	CNN	0.6643	0.8143	0.8143	0.8214	0.7714	0.8143	0.8214	0.7357	0.7500	0.6786	0.7686					
	FBTRCA	0.6571	0.8500	0.8429	0.8929	0.8286	0.8214	0.8429	0.7143	0.7786	0.7286	0.7957					
5	STRCA	0.7286	0.6143	0.7571	0.7214	0.7214	0.7357	0.8143	0.7286	0.6929	0.6357	0.7150					
	CNN	0.7071	0.6929	0.7714	0.8000	0.6929	0.7643	0.8643	0.6929	0.6571	0.6357	0.7279					
	FBTRCA	0.7357	0.6786	0.8071	0.7429	0.7571	0.7929	0.8214	0.7429	0.6571	0.6643	0.7429					
6	STRCA	0.5571	0.5857	0.8143	0.7143	0.5357	0.6929	0.7143	0.7929	0.6500	0.6500	0.6707					
	CNN	0.5643	0.5786	0.7714	0.7429	0.6071	0.7214	0.6357	0.8214	0.7143	0.6807	0.6807					
	FBTRCA	0.6071	0.5500	0.8214	0.7429	0.6143	0.7929	0.6857	0.7929	0.6786	0.7000	0.6986					
7	STRCA	0.5500	0.5000	0.5357	0.5571	0.5143	0.5429	0.5357	0.5214	0.5429	0.4500	0.5250					
	CNN	0.5500	0.5429	0.4929	0.5786	0.5643	0.5429	0.5643	0.5571	0.6214	0.5071	0.5521					
	FBTRCA	0.5929	0.5286	0.5357	0.6000	0.6000	0.5871	0.5143	0.5929	0.5571	0.5643	0.5643					
8	STRCA	0.6357	0.7214	0.6214	0.6857	0.6500	0.5643	0.6143	0.5714	0.6429	0.5929	0.6300					
	CNN	0.5714	0.7286	0.6929	0.7071	0.6786	0.5714	0.6357	0.6429	0.6714	0.5357	0.6436					
	FBTRCA	0.6500	0.7643	0.6929	0.7786	0.7643	0.6500	0.6857	0.7143	0.6857	0.5643	0.6950					
9	STRCA	0.6143	0.5286	0.7071	0.7000	0.6214	0.7000	0.7571	0.6429	0.6000	0.6357	0.6507					
	CNN	0.6643	0.5357	0.6857	0.6500	0.6500	0.7571	0.7286	0.6786	0.7143	0.6643	0.6729					
	FBTRCA	0.6500	0.6071	0.7571	0.6357	0.6643	0.7429	0.7929	0.6500	0.6571	0.6714	0.6829					
Average	STRCA	0.5968	0.6119	0.6897	0.6817	0.6151	0.6651	0.6698	0.6317	0.6206	0.5889	0.6371					
	CNN	0.5968	0.6563	0.6897	0.7095	0.6532	0.6881	0.6905	0.6643	0.6611	0.5952	0.6605					
	FBTRCA	0.6151	0.6770	0.7294	0.7111	0.6865	0.7175	0.7048	0.6857	0.6667	0.6294	0.6823					

Table 13. Deviation of Classification Accuracies of Dataset II Across Ten Folds (Movement vs Movement)

Subject	Method	Motion Pair										Average
		SU-PR	SU-HO	SU-PG	SU-LG	PR-HO	PR-PG	PR-LG	HO-PG	HO-LG	PG-LG	
1	STRCA	0.1075	0.0878	0.1280	0.1355	0.1157	0.2043	0.1338	0.1223	0.1431	0.1906	0.1367
	CNN	0.1271	0.1139	0.1054	0.1313	0.1622	0.1313	0.1127	0.1065	0.1107	0.1213	0.1213
	FBTRCA	0.1324	0.0999	0.1216	0.1075	0.1347	0.1338	0.0967	0.1169	0.0825	0.1460	0.1172
2	STRCA	0.1054	0.1421	0.0979	0.1205	0.0891	0.1035	0.0955	0.1782	0.1188	0.1536	0.1205
	CNN	0.1617	0.1536	0.0811	0.0878	0.1021	0.1235	0.1075	0.1608	0.1643	0.1219	0.1219
	FBTRCA	0.1149	0.1677	0.1216	0.0940	0.1429	0.1446	0.1251	0.1280	0.1216	0.1251	0.1285
3	STRCA	0.1035	0.1205	0.0878	0.1315	0.1460	0.1251	0.1119	0.1559	0.1262	0.1129	0.1221
	CNN	0.1188	0.1280	0.0979	0.0811	0.1065	0.1388	0.1758	0.1324	0.1078	0.1021	0.1189
	FBTRCA	0.1338	0.1176	0.0907	0.1349	0.1119	0.1067	0.1306	0.1088	0.1595	0.1223	0.1217
4	STRCA	0.0757	0.1223	0.0979	0.0907	0.1407	0.0838	0.1169	0.1078	0.1013	0.1067	0.1044
	CNN	0.0828	0.1075	0.0904	0.1271	0.1677	0.1075	0.1129	0.0894	0.0694	0.1057	0.1057
	FBTRCA	0.0878	0.1366	0.0738	0.0907	0.0904	0.1024	0.0999	0.1214	0.0786	0.0563	0.0938
5	STRCA	0.0999	0.1127	0.1150	0.1485	0.0979	0.0894	0.0768	0.0999	0.1013	0.1280	0.1109
	CNN	0.0855	0.0894	0.0878	0.1608	0.1262	0.1216	0.0855	0.1349	0.1205	0.1235	0.1136
	FBTRCA	0.1119	0.1438	0.0678	0.1513	0.1436	0.1088	0.0772	0.0838	0.1436	0.1651	0.1197
6	STRCA	0.1251	0.1205	0.1513	0.1010	0.1852	0.0828	0.1010	0.0855	0.1280	0.1139	0.1194
	CNN	0.0855	0.1088	0.1107	0.1223	0.1552	0.1188	0.1366	0.1315	0.1166	0.0919	0.1178
	FBTRCA	0.1357	0.1169	0.1129	0.1075	0.1475	0.1280	0.1127	0.1324	0.1129	0.1380	0.1245
7	STRCA	0.1719	0.1117	0.1271	0.1338	0.1460	0.1176	0.1357	0.1431	0.1587	0.1349	0.1380
	CNN	0.1508	0.1313	0.1324	0.1035	0.1324	0.1475	0.0919	0.1421	0.1216	0.1446	0.1298
	FBTRCA	0.1508	0.1313	0.0772	0.1550	0.0768	0.1407	0.1380	0.1067	0.0811	0.1139	0.1141
8	STRCA	0.1188	0.0979	0.1169	0.1355	0.0855	0.1595	0.0964	0.1166	0.1214	0.1013	0.1150
	CNN	0.0891	0.1157	0.1169	0.1088	0.1271	0.1388	0.1631	0.1429	0.0602	0.1176	0.1176
	FBTRCA	0.1407	0.1067	0.0828	0.1366	0.1169	0.1559	0.1223	0.1065	0.1355	0.1280	0.1232
9	STRCA	0.1313	0.1269	0.1324	0.1572	0.1651	0.0738	0.1127	0.1468	0.1355	0.1235	0.1305
	CNN	0.1390	0.1357	0.1756	0.1595	0.1139	0.1223	0.0999	0.1725	0.1166	0.0955	0.1331
	FBTRCA	0.1366	0.1024	0.1176	0.1665	0.1349	0.0904	0.0919	0.1280	0.0999	0.0690	0.1137
Average	STRCA	0.1154	0.1158	0.1214	0.1282	0.1301	0.1155	0.1090	0.1285	0.1260	0.1295	0.1220
	CNN	0.1156	0.1204	0.1109	0.1191	0.1292	0.1312	0.1207	0.1348	0.1098	0.1200	0.1200
	FBTRCA	0.1271	0.1248	0.0962	0.1271	0.1222	0.1202	0.1105	0.1147	0.1128	0.1182	0.1174

Table 15. Deviation of Classification Accuracies of Dataset II Across Ten Folds (Movement vs Resting)

Subject	Method	Motion Pair									Average
		SU-RE	PR-RE	HO-RE	PG-RE	LG-RE	HO-RE	PG-RE	LG-RE	Average	
1	STRCA	0.0952	0.0955	0.1508	0.0979	0.0964	0.1072	0.0964	0.1072	0.1072	0.1072
	CNN	0.1235	0.0757	0.0772	0.1013	0.1013	0.0969	0.1013	0.0969	0.0969	0.0969
	FBTRCA	0.0673	0.0999	0.1013	0.0999	0.1119	0.0961	0.1119	0.0961	0.0961	0.0961
2	STRCA	0.0602	0.0527	0.0602	0.0678	0.1139	0.0710	0.1139	0.0710	0.0710	0.0710
	CNN	0.0452	0.0588	0.0625	0.0842	0.1067	0.0715	0.1067	0.0715	0.0715	0.0715
	FBTRCA	0.0369	0.0499	0.0527	0.0476	0.0476	0.0470	0.0476	0.0470	0.0470	0.0470
3	STRCA	0.0772	0.0825	0.1127	0.1271	0.1347	0.1068	0.1347	0.1068	0.1068	0.1068
	CNN	0.0940	0.0482	0.1119	0.1260	0.1205	0.1001	0.1260	0.1001	0.1001	0.1001
	FBTRCA	0.0940	0.0369	0.1067	0.1010	0.0476	0.0773	0.1010	0.0773	0.0773	0.0773
4	STRCA	0.0952	0.0583	0.1013	0.0904	0.0894	0.0869	0.0894	0.0869	0.0869	0.0869
	CNN	0.0955	0.0588	0.0673	0.0768	0.0710	0.0739	0.0710	0.0739	0.0739	0.0739
	FBTRCA	0.0482	0.0563	0.0710	0.0583	0.0753	0.0618	0.0753	0.0618	0.0618	0.0618
5	STRCA	0.0753	0.0855	0.1054	0.1139	0.0967	0.0954	0.0967	0.0954	0.0954	0.0954
	CNN	0.0607	0.0964	0.1010	0.0855	0.0855	0.0858	0.0855	0.0858	0.0858	0.0858
	FBTRCA	0.0772	0.0940	0.0772	0.0894	0.1021	0.0880	0.1021	0.0880	0.0880	0.0880
6	STRCA	0.0952	0.0678	0.1054	0.1010	0.1431	0.1025	0.1431	0.1025	0.1025	0.1025
	CNN	0.0452	0.0842	0.0625	0.0786	0.1117	0.0764	0.1117	0.0764	0.0764	0.0764
	FBTRCA	0.1013	0.1021	0.0855	0.0757	0.1188	0.0967	0.1188	0.0967	0.0967	0.0967
7	STRCA	0.1545	0.1523	0.1179	0.0738	0.1506	0.1298	0.1506	0.1298	0.1298	0.1298
	CNN	0.1665	0.0955	0.1407	0.1470	0.1396	0.1379	0.1470	0.1396	0.1379	0.1379
	FBTRCA	0.1719	0.1710	0.1119	0.0999	0.1421	0.1394	0.1421	0.1394	0.1394	0.1394
8	STRCA	0.1054	0.0710	0.0828	0.1608	0.1226	0.1085	0.1226	0.1085	0.1085	0.1085
	CNN	0.1313	0.0828	0.0891	0.0967	0.0710	0.0942	0.0967	0.0710	0.0942	0.0942
	FBTRCA	0.1107	0.0625	0.0878	0.1205	0.0878	0.0939	0.1205	0.0878	0.0939	0.0939
9	STRCA	0.0678	0.0842	0.1054	0.1117	0.1223	0.0983	0.1223	0.0983	0.0983	0.0983
	CNN	0.0825	0.1157	0.0811	0.1349	0.1168	0.1168	0.1349	0.1168	0.1168	0.1168
	FBTRCA	0.0602	0.0838	0.0738	0.1407	0.1013	0.0920	0.1407	0.1013	0.0920	0.0920
Average	STRCA	0.0918	0.0833	0.1047	0.1049	0.1189	0.1007	0.1189	0.1007	0.1007	0.1007
	CNN	0.0938	0.0796	0.0882	0.1040	0.1086	0.0948	0.1040	0.1086	0.0948	0.0948
	FBTRCA	0.0853	0.0841	0.0853	0.0925	0.0927	0.0880	0.0925	0.0927	0.0880	0.0880

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Table 16. P -value between STRCA and FBTRCA calculated by two-side t -test (Dataset I-RP)

Motion	Subject															Average
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	
EF-EE	0.8093	0.6415	0.3785	0.2014	0.0586	0.2806	0.4291	0.8244	0.8923	0.6945	0.4803	0.5653	0.1221	0.0723	1.0000	0.4967
EF-SU	0.2434	0.8720	0.6809	0.0102	0.3955	0.5256	0.4762	0.6485	0.9113	0.3812	0.2564	0.7364	0.7517	0.5872	0.6585	0.5423
EF-PR	0.0142	0.2285	0.1558	0.0499	0.8885	0.7486	0.3082	0.8163	0.8789	0.6733	0.3553	0.1955	0.2388	0.0186	0.4697	0.4027
EF-HC	0.2317	0.6445	0.7486	0.5469	0.6103	0.5914	0.7331	0.4545	1.0000	0.6631	0.4351	1.0000	0.0750	0.0170	0.6215	0.5582
EF-HO	0.6556	0.9036	0.2691	0.1422	0.1127	0.8890	0.0489	0.3618	1.0000	0.4746	0.8859	0.1047	0.5530	0.2557	0.7776	0.4956
EE-SU	0.0023	0.1879	0.1672	0.2962	0.3860	0.2912	0.5560	0.5362	0.5872	0.6432	0.7486	0.8437	0.1041	0.6215	0.6601	0.4421
EE-PR	0.0019	0.2809	0.0161	0.7031	0.5843	0.8409	0.4700	0.6713	0.3630	1.0000	0.0126	0.5402	0.5452	0.3220	0.5427	0.4596
EE-HC	0.8070	0.7187	0.8279	0.1401	0.3419	0.7992	0.8914	0.1201	0.3606	0.0838	0.2778	0.5759	0.6085	0.5979	0.4419	0.5062
EE-HO	0.7851	0.1068	0.3125	0.1515	0.8020	0.7007	0.3140	0.0860	0.7771	0.7756	0.6601	0.3219	0.3388	0.6300	0.8569	0.5079
SU-PR	0.8837	0.4410	0.7618	0.1825	0.2068	0.5979	0.7805	0.8093	1.0000	0.9161	0.3045	0.2962	0.4393	0.2649	0.8984	0.5855
SU-HC	0.8569	0.8535	0.7869	0.0277	0.4017	0.6237	0.7160	0.8558	0.8323	0.2540	0.3913	1.0000	0.4246	0.4077	0.6278	0.6040
SU-HO	0.1558	0.3924	0.4218	0.2257	0.1929	1.0000	0.8697	0.5025	0.7507	0.9003	0.9030	0.6809	0.7521	0.8536	0.4872	0.6059
PR-HC	0.5001	0.7587	1.0000	0.7272	0.4391	0.1145	0.4311	0.6432	0.8120	0.8977	0.8536	0.0739	0.8973	0.5470	0.5520	0.6165
PR-HO	0.8558	1.0000	0.6733	0.6126	0.1346	0.7486	0.8832	0.4915	0.7606	1.0000	0.7911	0.4246	0.4700	0.3760	0.7756	0.6665
HC-HO	0.5025	1.0000	0.6837	0.1356	0.7033	0.8837	0.7450	0.9069	0.7606	0.3388	0.8837	0.7676	0.6893	0.6839	0.3419	0.6418
EF-RE	0.2743	0.3581	0.3760	0.4645	0.1513	1.0000	0.8558	0.0145	0.2878	0.5305	0.1150	0.1589	0.1964	0.8379	0.4453	0.4044
EE-RE	0.6182	0.1753	0.0062	0.6652	0.1769	0.7142	0.6565	0.6601	0.3077	0.7730	0.3581	0.5872	0.6837	0.5165	0.6733	0.5048
SU-RE	0.1892	0.1194	0.2546	0.6132	0.3765	0.8086	1.0000	0.3177	0.6164	0.4313	0.2895	0.4987	0.5241	0.4973	0.7120	0.4832
PR-RE	0.2030	0.3955	0.8681	0.8201	1.0000	1.0000	0.5452	0.4163	0.3018	0.0594	0.0247	0.3306	0.0179	0.2846	0.6733	0.4627
HC-RE	0.4206	0.4228	0.2945	0.8297	0.2564	1.0000	0.6215	0.4073	0.0166	0.8437	0.7372	0.0913	0.5510	0.5872	0.4925	0.5048
HO-RE	0.3388	0.2134	0.2963	1.0000	0.8770	0.5628	0.1515	0.6906	0.1785	0.4291	0.1201	0.1302	0.2163	0.3860	1.0000	0.4394
Average	0.4452	0.5102	0.4752	0.4069	0.4332	0.7010	0.5944	0.5159	0.6379	0.6078	0.4707	0.4725	0.4381	0.4459	0.6528	0.5205

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Table 17. *P*-value between STRCA and FBTRCA calculated by two-side *t*-test (Dataset I-RP+MMP)

Motion	Subject															Average
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	
EF-EE	0.3664	0.3858	0.0082	0.2139	1.0000	0.1291	0.4543	0.5530	0.0008	0.6278	0.6578	0.0379	0.8010	0.0835	0.3471	0.3778
EF-SU	0.4391	0.3180	0.0225	0.1221	0.5530	0.1387	0.4721	0.0747	0.6733	0.2507	0.4218	0.6862	0.6753	0.0913	0.8003	0.3826
EF-PR	0.0838	0.1597	0.0739	0.4697	0.0687	0.1964	0.0490	0.0499	0.0320	0.3433	0.0750	0.0046	0.0329	0.2675	0.0041	0.1274
EF-HC	0.0676	0.7264	0.0024	0.1294	0.0266	0.6394	0.4123	0.6319	0.2095	1.0000	0.2883	0.3750	0.0087	0.1184	0.7007	0.3558
EF-HO	0.0382	0.4825	0.0086	0.1929	0.2546	0.4376	1.0000	0.1869	0.3741	0.0782	0.1346	0.1597	0.0155	0.0021	0.2011	0.2378
EE-SU	0.1433	0.3760	0.0104	0.1615	0.7287	0.2564	0.6900	0.2434	0.1184	0.5456	0.5874	0.5944	0.1268	0.6278	0.7507	0.3974
EE-PR	0.0021	0.2208	0.1080	0.1964	0.1589	0.7486	0.5120	0.2468	0.0083	0.0587	0.1468	0.0439	0.0382	0.0082	0.4118	0.1936
EE-HC	0.0579	1.0000	0.4240	0.1145	0.8451	0.5049	0.7231	0.3579	0.5197	0.1194	0.2853	0.2986	0.2069	0.5165	0.6468	0.4414
EE-HO	0.0208	0.1194	0.0172	0.0925	0.5843	0.3381	0.8820	0.0586	0.1116	1.0000	0.3219	0.0525	0.7886	0.0056	0.4474	0.3240
SU-PR	0.1422	0.6991	0.0943	0.0131	0.4474	0.6005	0.5402	0.0626	0.7873	0.9132	1.0000	0.0026	0.6961	0.1150	0.3349	0.4299
SU-HC	0.1828	0.2643	0.0381	0.0340	0.4247	0.1820	0.6864	0.4419	0.5197	0.0652	1.0000	0.1069	0.1356	0.3968	1.0000	0.3652
SU-HO	0.0126	0.5803	0.1597	0.0531	0.2650	0.5172	0.7886	0.7771	0.0410	0.7606	0.1580	0.0114	0.1206	0.8061	0.8609	0.3942
PR-HC	0.8705	0.3263	0.2163	0.8808	1.0000	0.8086	0.4075	0.4697	0.8875	0.8802	0.8180	0.4351	0.8756	0.6195	1.0000	0.6997
PR-HO	0.1785	0.2295	0.4486	0.1707	0.4077	0.8020	1.0000	0.4286	0.2758	0.2188	0.7313	0.2188	0.2557	0.1150	0.6924	0.4116
HC-HO	0.8957	0.2858	0.2593	0.3760	0.7486	0.7873	1.0000	1.0000	0.3750	0.4474	0.0838	0.7559	0.4822	0.9052	0.2095	0.5741
EF-RE	0.0026	0.0203	0.4583	0.0544	0.1278	0.5560	0.0129	0.2878	0.0345	0.3065	0.0069	0.6182	0.0453	0.1964	0.0553	0.1855
EE-RE	0.1686	0.3061	0.0150	0.3553	0.1387	0.1510	0.7269	0.4486	0.0134	0.4313	0.0756	0.7642	0.1753	0.1451	0.2635	0.2271
SU-RE	0.0401	0.3306	0.1108	0.0017	0.4286	0.0525	0.4230	0.6601	0.0156	0.0838	0.5724	0.4331	0.1118	0.1221	0.0203	0.2271
PR-RE	0.0114	0.0789	0.0199	0.1346	0.1985	0.7947	0.2986	0.2945	0.2266	0.1285	0.2527	0.0544	0.0007	0.0187	0.1897	0.1801
HC-RE	0.0624	0.4825	0.3858	0.0645	0.1673	0.0965	0.7842	0.1278	0.0035	0.0051	0.0442	0.2199	0.2418	0.2295	0.0015	0.1944
HO-RE	0.0439	0.3794	0.1036	0.3624	0.3568	0.3487	0.2069	0.3388	0.0623	0.2301	0.0305	0.0424	0.1145	0.0378	0.2447	0.1935
Average	0.1824	0.3701	0.1419	0.1997	0.4253	0.4336	0.5748	0.3686	0.2519	0.4045	0.3663	0.2817	0.2833	0.2585	0.4265	0.3313

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Table 18. P -value between STRCA and FBTRCA calculated by two-side t -test (Dataset II)

Motion	Subject									Average
	1	2	3	4	5	6	7	8	9	
SU-PR	0.0624	0.8859	0.1592	0.3428	0.8820	0.4029	0.5607	0.8090	0.5585	0.5182
SU-HO	0.0287	0.5452	0.0047	0.1267	0.2806	0.5096	0.6065	0.3618	0.1449	0.2899
SU-PG	0.7033	0.3968	0.2263	0.1145	0.3624	0.9061	1.0000	0.1323	0.3836	0.4695
SU-LG	0.1346	0.5617	0.8132	0.0951	0.7530	0.5480	0.5165	0.1443	0.3864	0.4392
PR-HO	0.3222	0.1964	0.5470	0.0338	0.5241	0.3079	0.1177	0.0225	0.5330	0.2894
PR-PG	0.7157	1.0000	0.1482	0.1419	0.2158	0.0527	0.7829	0.2401	0.2605	0.3953
PR-LG	0.6864	0.1318	0.2057	0.1235	0.8379	0.5579	0.7304	0.1642	0.4474	0.4317
HO-PG	0.2451	0.2723	0.2504	0.4956	0.7331	1.0000	0.2218	0.0104	0.9089	0.4597
HO-LG	0.3510	0.1283	0.1375	0.3045	0.8992	0.6031	0.8027	0.4660	0.2973	0.4433
PG-LG	0.9261	1.0000	0.2378	0.0117	0.6706	0.3886	0.0556	0.5867	0.4351	0.4791
SU-RE	0.0011	1.0000	0.2100	0.4558	0.3087	0.6319	0.1352	0.1567	0.8061	0.3784
PR-RE	0.4246	0.3630	0.1510	0.5843	0.2295	0.5872	0.2160	0.0282	0.8513	0.3817
HO-RE	1.0000	0.1753	0.0068	0.7193	0.2418	0.2593	0.1427	0.0543	0.3061	0.3195
PG-RE	0.0925	0.4240	0.0514	0.2237	0.0425	0.2263	0.0093	1.0000	0.2725	0.2602
LG-RE	0.1099	0.1171	0.1313	0.1929	0.1656	0.8108	0.2069	0.3082	0.6747	0.3019
Average	0.3869	0.4799	0.2187	0.2444	0.4764	0.5195	0.4050	0.2990	0.4844	0.3905

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