# Virial masses of late type galaxies from the SDSS DR16

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### ABSTRACT

Motivated by the challenges of calculating the dynamical masses of late-type galaxies (LTGs) and the enormous amount of data from the Sloan Digital Sky Survey (SDSS), we calculate virial masses of a sample of approximately 126,000 LTGs from the sixteenth data release of the SDSS. The virial mass estimations were made considering Newtonian mechanics, virial equilibrium and velocity dispersion from stars and gas. The procedure gave as a result seven mass estimations for each galaxy. The calculated masses were calibrated using a sample of spiral galaxies with velocity rotation curves. Considering the results from the calibration, we find that the correlation between virial and dynamical (rotation curve) masses is stronger for high inclination values. Therefore the calibration relies more on the available data for higher inclination angle galaxies. We also show that if we have a heterogeneous sample of galaxies one must take into consideration the size and colour of these galaxies by using the following variables: Sersic index n, concentration index and colour of the stars. For relatively smaller and bluer LTGs the gas velocity dispersion provides a more consistent mass calculation, while for LTGs that are relatively larger and redder the stellar velocity dispersion provides a better correlated mass calculation.

**Key words:** Galaxies: fundamental parameters. Galaxies: photometry, distances and redshifts.

#### **1 INTRODUCTION**

The determination of the masses of galaxies has been an interesting problem ever since galaxies were identified as very large conglomerations of stars and gas in the universe (see Burbidge & Burbidge 1975; Fich & Tremaine 1991; Courteau et al. 2014). At present there are three

\* E-mail: alberto.nigoche@academicos.udg.mx eduardo.delafuente@academicos.udg.mx main methods that allow the calculation of galactic masses, namely:

(i) Dynamical or virial masses. The dynamical or virial masses are determined recurring to dynamical methods which in turn use the rotation curves or the velocity dispersion of gas or stars in galaxies. It is important to mention at this point that all these methods presuppose that Newtonian gravitation is valid at all scales in the universe; if this were not the case, then the determinations obtained from these methods would be flawed. The dynamical mass

determinations for LTGs are usually derived from their rotation curves. Early attempts to determine the masses of galaxies using this method were undertaken by Scheiner (1899), Slipher (1914), Pease (1918), and Opik (1922), in which he inferred a value for the mass of M31. Some time later there were attempts at determining the mass of the Milky Way by Kapteyn & van Rhijn (1922), Oort (1932b), and Oort (1932a). Determinations of the M31 total mass using velocities determined from absorption lines were made by Babcock (1939), Mayall (1950), and Lallemand et al. (1960). With the measurement of rotation curves further away from the centre of LTGs, and the discovery that these remain flat out to large radii, early suggestions of the existence of a non-luminous massive component were put forward. Rubin & Ford (1970) were the first to obtain a rotation curve for M31 out to  $120' (\sim 27 \ kpc)$  in which they noticed how it remains flat out to a large distance from the centre. Using HI, Roberts & Whitehurst (1975) confirmed the flatness of the M31 rotation curve out to  $170' (\sim 38 \ kpc)$ . The flatness of rotation curves in all galaxy types is a well-established fact (Faber & Gallagher 1979; Rubin et al. 1985; Sofue & Rubin 2001, among others). There have also been mass determination of LTGs using the emission lines of  $H\alpha$ , CO and HI. A reasonable agreement between determinations performed with these different lines is found (see Sofue & Rubin 2001; Simon et al. 2003, 2005; Spekkens & Sellwood 2007)), and also from measurements made with the [OII], [OIII],  $H\beta$ and [SII] lines (Courteau & Sohn 2003). At some point the question of whether the gas rotation curve really represented the total mass of the galaxy arose. There is likely evidence that the gas rotation curves represent the gas distribution within the optical disk of galaxies (see Cayatte et al. 1994; Mathewson et al. 1992; Courteau 1997; Catinella et al. 2007, among others).

To determine the mass of an elliptical galaxy using the virial theorem, three things are needed:

• Distance of the galaxy from the Sun

• the line-of-sight velocity dispersion of the stars in the centre

• the distribution of light projected on the plane of the sky from which we can derive the potential energy

The first determination of a velocity dispersion was for M32 by Minkowsky (1954), later Burbidge et al. (1961c) and Burbidge et al. (1961b) reevaluated the value of the velocity dispersion and in Burbidge et al. (1961a) they obtained the velocity dispersion for NGC 3379. Velocity dispersions for 12 additional galaxies were obtained by Minkowsky (1961). For the determination of the potential energy of a spheroidal galaxy we refer to Poveda (1958) where a full discussion is given. It was shown by de Vaucouleurs (1963) and Poveda (1958) that the potential energy is given by:

$$\Omega = -0.33 \frac{GM^2}{R'} \tag{1}$$

where R' is the radius that contains half of the total light

of the galaxy, this radius is called the 'effective' radius, G is the constant of Universal Gravitation and M represents the mass. All the quantities in equation (1) are in cgs units.

The dynamical masses of Gas-Poor Galaxies (ETGs) have been determined from molecular gas observations by Sage et al. (2007) and Young et al. (2011), from ionised gas observations by Bertola et al. (1984), Fisher (1997) and Sarzi et al. (2006) and from neutral gas observations by Knapp et al. (1985), Morganti et al. (2006), and di Serego Alighieri et al. (2007) among others. King & Minkowski (1966) measured rotation in the inner regions of two giant ellipticals in the Virgo cluster, NGC 4621 (E3) and NGC 4697 (E5).

(ii) Luminous masses. Luminous masses of galaxies are determined measuring the total luminosity of galaxies and assuming a specific mass to light (M/L) ratio which would imply a value for the mass. The (M/L) does not have a universal value and its determination is central to the calculation of galaxy masses using this method. The (M/L)ratio may depend on a variety of factors such as the way the galactic mass is assembled (De Lucia et al. 2007), the different Spectral Energy Distributions (SED) of galaxies (Walcher et al. 2011) and (Conroy 2013), the different mix of Stellar Populations (SPs). Oort (1926) and Baade (1944) recognized the presence of at least two different SPs in our galaxy. For a comprehensive review on SPs see Greggio & Renzini (2011). The different SPs are superposed in a galaxy, and each has a different Star Formation Rate (SFR) which must also be considered and which evolves with time (Sandage 1986), (MacArthur et al. 2004). Another factor is the Initial Mass Function (IMF; see Salpeter 1955; Scalo 1986; Kroupa 2001; Chabrier 2003) which tells us how the mass is distributed in a galaxy at the beginning of the lives of its stars.

The types of stars in a galaxy -hence their masscan be calculated using stellar population synthesis models. There are optimised population synthesis models (see Spinrad & Taylor 1971; Faber 1972; O'Connell 1976; Pickles 1985; Bica & Alloin 1986; MacArthur et al. 2009, among others) and Evolutionary population synthesis models (see Tinsley 1972; Tinsley & Gunn 1976; Renzini & Voli 1981; Bruzual A. 1983, among others). In summary, determining the M/L ratio for a galaxy could be a very complicated problem, however once it is determined, the galactic mass can be calculated straightforwardly from its measured luminosity and distance.

(iii) Mass determination using relativistic light bending by gravitational lenses. This method would give us a crude value for the mass of a single galaxy because in order to bend light gravitationally it is necessary to have a very large mass such as that of a cluster of galaxies and the mass of an individual galaxy would correspond to the average value of the mass for each galaxy in the cluster.

The first attempt to detect the weak gravitational bending of light by a massive object was conducted by Tyson et al. (1984) with a not very definitive result, the first real detec-

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tion was achieved by Brainerd et al. (1996). Mass measurements for galaxies in the Sloan Digital Sky Survey (SDSS) were achieved by McKay et al. (2002) and Prada et al. (2003). Dark matter was detected by Kaiser & Squires (1993) and lensing produced by clusters of galaxies was detected by Tyson et al. (1990), and Fahlman et al. (1994). There have been a number of searches for spiral lens galaxies by Féron et al. (2009), Sygnet et al. (2010) and Treu et al. (2011).

The Hubble Space Telescope (HST) has been used to take data on weak lensing galaxies for a few tens of ETGs with  $0.1 \leq z \leq 0.8$  see (Gavazzi et al. 2007), (Auger et al. 2010), (Lagattuta et al. 2010).

There is also what is called Strong Gravitational Lensing. There is a multitude of papers that have either tried to detect it or have detected it and in so doing, one of their byproducts has been the measurement of masses of clusters of galaxies. Papers such as those by Bertin et al. (1992), Saglia et al. (1992), Loewenstein & White (1999), Keeton (2001), and Padmanabhan et al. (2004) to mention a few.

There have been a few strong lensing surveys such as SLACS (Sloan Lens ACS) Bolton et al. (2004), Bolton et al. (2005), Bolton et al. (2006), Bolton et al. (2008),Schneider (2006), Koopmans et al. (2006), Treu et al. (2006), Treu et al. (2009), Gavazzi et al. (2007),Treu (2010), Auger et al. (2011) and Newton et al. (2011) among others.

In order to apply the first two methods (dynamics, luminosity) it is necessary to know the distance at which the galaxy in question is located. The further away this galaxy is, the larger the uncertainties in the distance determination, and therefore the larger the uncertainties in its mass.

In the case of LTGs, they contain different structures (bulge, disk, spiral arms) with different levels of importance that make it difficult to calculate the dynamical or the virial mass properly because the tracers of these structures are different. The best way to obtain the dynamical mass of LTGs is using the rotation curves but the present-day technology is not good enough to obtain these rotation curves for relatively distant LTGs. Besides the amount of time to obtain the rotation curves of LTGs is relatively high. At the present time, we can find in the literature photometric and spectroscopic information of thousands of galaxies from different surveys, but this information is not sufficient to obtain the rotation curves due to the previously mentioned problems. However, the SDSS contains more than one hundred thousand LTGs with photometric and spectroscopic information that can be used to obtain their virial masses through the velocity dispersion of gas and/or stars. This work is devoted to using this valuable information from the SDSS and obtaining virial mass estimations of LTGs with the lowest possible uncertainties. To achieve this goal we will use a subsample of SDSS LTGs with measured rotation curves from the literature to obtain their dynamical mass and compare it with the virial mass estimation from the velocity dispersion. This comparison will permit us to calibrate the virial masses, tak-

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ing into account the importance of the different structures that constitute the LTGs.

This work is organized as follows: In section 2 we present our sample of galaxies and the method by which it was selected. Section 3 presents the formal definition of dynamic and virial masses. In section 4 we calculate the virial masses of the galaxies in our sample. In section 5 we calculate the dynamical masses of a subsample of galaxies which have rotation curves determined in the literature. Section 7 presents the comparison of the virial and dynamical masses. In section 8 we discuss our findings and finally in section 9 we present our conclusions.

### 2 THE SAMPLE OF LTGS

We extract a sample of LTGs -exponential brightness profilefrom the SDSS DR16 (York et al. 2000; Blanton et al. 2003) with photometric and spectroscopic information. The basic required parameters to achieve the goals of this work are size and velocity dispersion from stars and gas. The main selection criterion used to quantify the brightness profile was the SDSS fracDeV parameter. The fracDeV parameter is equivalent to the Sersic (1968) index n, n = 1 corresponds to fracDeV = 0 while n = 4 corresponds to fracDeV =1. Galaxies with fracDeV < 0.5 are relatively well adjusted by a exponential profile. Since the photometric errors are lower in g and r filters and the spectroscopic errors are lower for velocity dispersion greater than 60 km/s, we take into account this information to obtain the sample of LTGs. The resultant sample with  $fracDeV_g < 0.5$ ,  $fracDeV_r < 0.5$ and stellar  $\sigma > 60 \ km/s$  -according to SDSS nomenclaturecontains 126 815 galaxies. These galaxies are distributed in a redshift interval 0.00 < z < 0.35 and within a magnitude range  $\Delta m \sim 10 \ mag$ .

# 2.1 Correction of the photometric and spectroscopic data

Once we have compiled the galaxy sample, we must correct both the photometric and the spectroscopic data. We here list the performed corrections (see Nigoche-Netro et al. 2015):

• Seeing and Extinction corrections: we use the seeingcorrected parameters in the total magnitude and effective radius as well as the extinction corrections by employing the respective SDSS pipelines on the data (see York et al. 2000; Blanton et al. 2003, and references therein).

• K correction: We use the values obtained from the following formulae (Nigoche-Netro et al. 2008):

$$k_g(z) = -5.261 z^{1.197},\tag{2}$$

$$k_r(z) = -1.271 z^{1.023},\tag{3}$$

• Cosmological dimming correction: We follow Jørgensen et al. (1995a) where the effective surface brightness ( $< \mu_e >$ ) is corrected by subtraction of 10 log(1+z), being z the redshift relative to the CMB.

• Evolution correction: We apply the evolution correction from Nigoche-Netro et al. (2008) utilising:

$$ev_g(z) = +1.15z,$$
 (4)

$$ev_r(z) = +0.85z,$$
 (5)

• Effective radius correction to the rest reference frame: We follow Hyde & Bernardi (2009) to correct colour gradients where the mean effective radius is smaller at longer wavelengths by using:

$$r_{e,g,rest} = \left[\frac{(1+z)\lambda_g - \lambda_r}{\lambda_g - \lambda_r}\right] (r_{e,g,obs} - r_{e,r,obs}) + r_{e,r,obs},$$
(6)

with  $\lambda_g = 4686$ Å, and  $\lambda_r = 6165$ Å.

• Aperture correction to the velocity dispersion: The aperture correction is significant because it avoids dependencies on distance and instruments used in calculating the spectral parameters. Following Jørgensen et al. (1995b), we determine the ratio between the velocity dispersion values  $(\sigma_{SDSS})$  and the corrected velocity dispersion  $(\sigma_e)$  or velocity dispersion inside  $\mathbf{r}_e$  as:

$$\log\left(\frac{\sigma_{SDSS}}{\sigma_e}\right) = -0.065\log\left(\frac{r_{ap}}{r_e}\right) - 0.013\left[\log\left(\frac{r_{ap}}{r_e}\right)\right]^2,$$
(7)

where  $r_{ap} = 1.5$  arcsec for the SDSS case (York et al. 2000; Blanton et al. 2003).

Finally, the errors in the photometric and spectroscopic variables were obtained from the errors given in the SDSS, which were in turn propagated by considering the mathematical expressions of each of the corrections listed above.

### 3 THE MASS ESTIMATIONS OF THE LTGS

We assume Newtonian dynamics and that the velocity dispersion is due to the gravitational potential well. The LTGs mass estimates are made using data for stars and gas obtained from the SDSS DR16. These estimates will be calibrated later by means of a sample of galaxies for which we have measured rotation curves.

We have defined the virial masses as those masses that are obtained using the velocity dispersion of the gas or of the stars in the galaxies, while the dynamical masses would be those masses obtained by means of the rotation curves. It is important to stress that this nomenclature is used as a means to differentiate the method by which the masses are obtained, however both mass-values are due to the gravitational potential of the galaxy in question and are derived using Newtonian dynamics.

### 4 THE VIRIAL MASS FROM THE STARS OF LTGS.

We have made seven estimates of the total virial mass  $(\mathbf{M}_{\mathbf{Virial}})$  (see section 4.1) considering the following equation (Poveda 1958):

$$\mathbf{M}_{\mathbf{Virial}} \sim K \frac{r_e \sigma_e^2}{G},$$
 (8)

where  $r_e$  and,  $\sigma_e$  represent the effective radius and the velocity dispersion of stars inside  $r_e$ , respectively, Gis the gravitational constant and K is the proportion or scale factor. Historically, the scale factor has been considered constant, for example, for the de Vaucouleurs profile case Cappellari et al. (2006) found K = 5.9. Further studies have found the scale factor seems to depend on the Sersic index and/or the inclination angle of the galactic plane (Cappellari et al. 2006; Mocz et al. 2012). In this work we will consider both constant and variable scale factor (see section 4.1). This scale factor will be calibrated with the analysis that we will perform in the following sections.

Equation 8 considers an idealized situation and does not take into account possible effects on the mass estimations of LTGs due to environment, shape and velocity dispersion anisotropies.

### 4.1 Calculation of virial masses considering different scale factors and different estimates of the velocity dispersion

As previously mentioned the data for the virial mass estimates for the LTGs have been taken from the SDSS DR16. The data used are: the redshift, the exponential effective radius, the Petrosian radii R90 and R50, the major and minor semi-axes of the galactic disk, the stellar velocity dispersion, the gas velocity dispersion using the  $H_{\alpha}$  line, and the gas velocity dispersion using the average of some of the Balmer lines  $(H_{\alpha}, H_{\gamma}, H_{\beta}, H_{\delta}, H_{\epsilon}, H_{\zeta}, H_{\eta})$ . In what follows we present these estimates.

(i)  $\mathbf{M_{KS}}$ . This mass was calculated using a constant scale factor (K=5.9) and the velocity dispersion of the stars.

(ii)  $\mathbf{M}_{\mathbf{KA}}$ . This mass was calculated using a constant scale factor (K=5.9) and the velocity dispersion of  $H_{\alpha}$ .

(iii)  $\mathbf{M}_{\mathbf{KB}}$ . This mass was calculated using a constant scale factor (K=5.9) and the average of the velocity dispersion of the Balmer lines.

(iv)  $\mathbf{M}_{nS}$ . This mass was calculated using a scale factor as a function of the Sersic index n ( $K = 8.87 - 0.831n + 0.0241n^2$ ) (Cappellari et al. 2006) and the velocity dispersion of the stars.

For the remaining three estimates we considered K as a function of the galactic inclination angle (i) (Mocz et al. 2012) as expressed in the following equations:

$$K = \left(\frac{2.3548}{\sin(i)}\right)^2,\tag{9}$$

$$sin(i) = \sqrt{\frac{1 - (\frac{b}{a})^2}{1 - (0.19)^2}},$$
 (10)

where a and b represent the major and minor semi-axes of the galactic disk.

(v)  $M_{IS}$ . This mass was calculated using a scale factor expressed as a function of the inclination angle (equation 9) and the velocity dispersion of the stars.

(vi)  $\mathbf{M}_{\mathbf{IA}}$ . This mass was calculated using a scale factor expressed as a function of the inclination angle (equation 9) and the velocity dispersion of  $H_{\alpha}$ .

(vii)  $\mathbf{M}_{IB}$ . This mass was calculated using a scale factor expressed as a function of the inclination angle (equation 9) and the average of the velocity dispersion of the Balmer lines.

In table A.1 (appendix A) we show an extract (145 LTGs) of the virial masses catalogue, of the 126 815 LTGs, obtained following the previous procedures. The entire catalogue could be found, in electronic form, in the following link:

### 5 DYNAMICAL MASSES OF A SUBSAMPLE OF LTGS USING ROTATION CURVES

Catinella et al. (2005) presented a long slit spectroscopic study in  $H_{\alpha}$  of 403 non-interacting spiral galaxies using the Palomar Hale 5 m telescope. One of the main objectives of this study was to obtain their rotation curves. In this work we selected all the galaxies from Catinella et al. (2005) which have photometric and spectroscopic information in the SDSS DR16 sample, resulting in a subsample of 145 galaxies. The spectroscopic information includes the stellar velocity dispersion and/or the gas velocity dispersion.

In what follows we present the details of the calculation of the dynamical mass for the 145 Catinella et al. (2005) galaxies using their rotation curves. We make available the results in Table A2.

In order to determine the dynamical masses of the LTGs, a mass component fitting was performed. The mass components were represented by a Miyamoto-Nagai Potential (Miyamoto & Nagai 1975):

$$\phi = \frac{GM}{\sqrt{R^2 + \left[a + (b^2 + z^2)^{1/2}\right]^2}},$$
(11)

where G is the universal gravitational constant and M

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the total mass generating the gravitational field; a and b are two constants representing the scale length and scale height respectively, whereas R and z are the spatial variables.

A disk was set as the main component. Depending on the quality of the kinematic data, a second spherical inner component was included. Additionally, for some objects, an external spherical component was required to account for the flat region of the rotation curves at large radii. The obtained masses were corrected by inclination following the SDSS DR16 data. Respect to the fitting process, the main difficulties came from the deviation from circular motion which is present in almost all LTGs. Other aspects such as the spatial sampling, the radial extension of kinematic data and the rotational center determination were also considered as source of uncertainties. The obtained dynamical masses and their errors are listed in Appendix A (Table A.2).

If we only consider the information on galaxies with relatively small errors (less than 30% in both virial and dynamical mass) and difference between virial and dynamical masses less than three times the dispersion (see Tables 1-6), the sample is reduced to a total of approximately 80 galaxies, with small variations in the total number depending on the subsample selection criteria. We used these subsamples in the following sections to perform the calibration of the virial masses.

### 6 SUBSAMPLES DEFINITION FOR THE COMPARISON OF VIRIAL AND DYNAMICAL MASSES

The estimates of the virial and/or dynamical masses may be dependent on different properties, including the following: absolute magnitude, Sersic index, concentration index, colour (g - r) and galactic inclination angle. So, in order to perform the comparison in an appropriate manner we must consider subsamples with different cuts in the variables mentioned above. The estimation of the variable is described as follows:

• The absolute magnitude was calculated considering the corrected apparent magnitude and the redshift from the SDSS.

• The Sersic index was calculated through a fit to the n vs. R90/R50 from Table 1 in Graham et al. (2005) in filters g and r from the SDSS, and later we took the average of these indices. R90 and R50 are the radii that contain 90% and 50% of the Petrosian flux, respectively.

• The concentration parameter was obtained by averaging the ratio of the Petrosian radii (R90/R50) from the SDSS in the filters g and r.

• The colour g-r was obtained from the g and r corrected magnitudes in the SDSS.

• The average inclination angle was calculated from equation 3 in filters g and r from SDSS.

Table 1.  $BCES_{Bis}$  fit parameters for  $\mathbf{M}_{\mathbf{Virial}}$  vs.  $\mathbf{M}_{\mathbf{Dyn}}$  for LTG samples considering different scale factors and distinct estimates of the velocity dispersion (see Section 4.1). We apply approximately symmetric cuts in the values of absolute magnitude in the g filter  $\mathbf{M}_g$ .

		Slope	Intercept	Correlation coefficient	Dispersion	No. of galaxies
$M_g > -20.2$						
$M_g \leqslant -20.2$	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 1.11 \pm 0.09 \\ 1.11 \pm 0.10 \\ 1.15 \pm 0.19 \\ 1.09 \pm 0.08 \\ 1.08 \pm 0.09 \\ 0.94 \pm 0.08 \\ 1.08 \pm 0.21 \end{array}$	$\begin{array}{c} -0.61 \pm 0.90 \\ -0.51 \pm 1.02 \\ -0.92 \pm 1.89 \\ -0.49 \pm 0.80 \\ -0.34 \pm 1.00 \\ 1.18 \pm 0.81 \\ -0.18 \pm 2.06 \end{array}$	$\begin{array}{c} 0.77\\ 0.71\\ 0.42\\ 0.78\\ 0.71\\ 0.72\\ 0.32\end{array}$	$\begin{array}{c} 0.29 \\ 0.27 \\ 0.30 \\ 0.28 \\ 0.33 \\ 0.27 \\ 0.33 \end{array}$	31 23 31 39 40 33 31
	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 1.16 \pm 0.06 \\ 0.94 \pm 0.06 \\ 0.93 \pm 0.05 \\ 1.17 \pm 0.07 \\ 1.06 \pm 0.07 \\ 0.94 \pm 0.08 \\ 0.95 \pm 0.08 \end{array}$	$\begin{array}{c} -1.39 \pm 0.68 \\ 1.10 \pm 0.60 \\ 1.29 \pm 0.56 \\ -1.62 \pm 0.73 \\ -0.28 \pm 0.75 \\ 1.02 \pm 0.90 \\ 1.10 \pm 0.88 \end{array}$	$\begin{array}{c} 0.74 \\ 0.68 \\ 0.72 \\ 0.72 \\ 0.74 \\ 0.58 \\ 0.62 \end{array}$	$\begin{array}{c} 0.28 \\ 0.29 \\ 0.28 \\ 0.29 \\ 0.25 \\ 0.34 \\ 0.34 \end{array}$	52 47 46 54 53 50 50

**Table 2.**  $BCES_{Bis}$  fit parameters for  $\mathbf{M}_{\mathbf{Virial}}$  vs.  $\mathbf{M}_{\mathbf{Dyn}}$  for LTG samples considering different scale factors and distinct estimates of the velocity dispersion (see Section 4.1). We apply approximately symmetric cuts in the values of Sersic index n.

		Slope	Intercept	Correlation coefficient	Dispersion	No. of galaxies
$n \leqslant 0.8$						
n > 0.8	$M_{\mathrm{KS}}$ $M_{\mathrm{KA}}$ $M_{\mathrm{KB}}$ $M_{\mathrm{IS}}$ $M_{\mathrm{IS}}$ $M_{\mathrm{IA}}$ $M_{\mathrm{IB}}$	$\begin{array}{c} 0.87 \pm 0.05 \\ 0.85 \pm 0.04 \\ 0.94 \pm 0.03 \\ 0.89 \pm 0.04 \\ 0.87 \pm 0.05 \\ 0.83 \pm 0.04 \\ 0.93 \pm 0.03 \end{array}$	$\begin{array}{c} 1.92 \pm 0.52 \\ 2.17 \pm 0.39 \\ 1.13 \pm 0.31 \\ 1.48 \pm 0.49 \\ 1.77 \pm 0.49 \\ 2.28 \pm 0.44 \\ 1.22 \pm 0.33 \end{array}$	$\begin{array}{c} 0.82 \\ 0.86 \\ 0.89 \\ 0.84 \\ 0.82 \\ 0.85 \\ 0.85 \\ 0.85 \end{array}$	$\begin{array}{c} 0.22 \\ 0.24 \\ 0.22 \\ 0.25 \\ 0.26 \\ 0.26 \\ 0.25 \end{array}$	$ \begin{array}{r} 40 \\ 37 \\ 36 \\ 46 \\ 47 \\ 42 \\ 39 \end{array} $
N N N N N N	$M_{\mathrm{KS}}$ $M_{\mathrm{KA}}$ $M_{\mathrm{KB}}$ $M_{\mathrm{IS}}$ $M_{\mathrm{IS}}$ $M_{\mathrm{IA}}$ $M_{\mathrm{IB}}$	$\begin{array}{c} 1.12 \pm 0.04 \\ 0.99 \pm 0.05 \\ 1.02 \pm 0.04 \\ 1.08 \pm 0.04 \\ 1.01 \pm 0.03 \\ 0.94 \pm 0.07 \\ 0.99 \pm 0.08 \end{array}$	$\begin{array}{c} -0.88 \pm 0.42 \\ 0.59 \pm 0.55 \\ 0.41 \pm 0.46 \\ -0.47 \pm 0.39 \\ 0.38 \pm 0.33 \\ 1.14 \pm 0.69 \\ 0.70 \pm 0.80 \end{array}$	$\begin{array}{c} 0.86 \\ 0.79 \\ 0.82 \\ 0.85 \\ 0.87 \\ 0.82 \\ 0.78 \end{array}$	$\begin{array}{c} 0.30 \\ 0.32 \\ 0.30 \\ 0.31 \\ 0.29 \\ 0.34 \\ 0.36 \end{array}$	$ \begin{array}{r} 43\\ 34\\ 41\\ 47\\ 46\\ 41\\ 42 \end{array} $

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**Table 3.**  $BCES_{Bis}$  fit parameters for  $\mathbf{M}_{\mathbf{Virial}}$  vs.  $\mathbf{M}_{\mathbf{Dyn}}$  for LTG samples considering different scale factors and distinct estimates of the velocity dispersion (see Section 4.1). We apply approximately symmetric cuts in the concentration parameter (R90/R50).

		Slope	Intercept	Correlation coefficient	Dispersion	No. of galaxies
$(R90/R50) \leqslant 2.4$						
(R90/R50) > 2.4	$\begin{array}{c} M_{KS} \\ M_{KA} \\ M_{KB} \\ M_{nS} \\ M_{IS} \\ M_{IS} \\ M_{IB} \end{array}$	$\begin{array}{c} 0.93 \pm 0.04 \\ 0.82 \pm 0.04 \\ 0.92 \pm 0.03 \\ 0.97 \pm 0.04 \\ 0.94 \pm 0.04 \\ 0.84 \pm 0.04 \\ 0.89 \pm 0.03 \end{array}$	$\begin{array}{c} 1.23 \pm 0.47 \\ 2.43 \pm 0.38 \\ 1.38 \pm 0.29 \\ 0.66 \pm 0.48 \\ 0.97 \pm 0.48 \\ 2.14 \pm 0.38 \\ 1.51 \pm 0.34 \end{array}$	$\begin{array}{c} 0.84 \\ 0.88 \\ 0.90 \\ 0.85 \\ 0.85 \\ 0.88 \\ 0.86 \end{array}$	$\begin{array}{c} 0.21 \\ 0.21 \\ 0.20 \\ 0.24 \\ 0.25 \\ 0.25 \\ 0.23 \end{array}$	$37 \\ 35 \\ 33 \\ 42 \\ 41 \\ 38 \\ 35 \\ 35$
	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 1.06 \pm 0.03 \\ 0.93 \pm 0.04 \\ 0.95 \pm 0.04 \\ 1.04 \pm 0.03 \\ 0.95 \pm 0.03 \\ 0.89 \pm 0.06 \\ 0.94 \pm 0.07 \end{array}$	$\begin{array}{c} -0.22 \pm 0.32 \\ 1.31 \pm 0.45 \\ 1.09 \pm 0.39 \\ -0.12 \pm 0.35 \\ 0.96 \pm 0.31 \\ 1.67 \pm 0.62 \\ 1.27 \pm 0.69 \end{array}$	$\begin{array}{c} 0.86 \\ 0.81 \\ 0.82 \\ 0.86 \\ 0.86 \\ 0.83 \\ 0.77 \end{array}$	$\begin{array}{c} 0.30 \\ 0.30 \\ 0.31 \\ 0.30 \\ 0.29 \\ 0.33 \\ 0.36 \end{array}$	$46 \\ 35 \\ 44 \\ 51 \\ 52 \\ 45 \\ 46$

**Table 4.**  $BCES_{Bis}$  fit parameters for  $\mathbf{M}_{\mathbf{Virial}}$  vs.  $\mathbf{M}_{\mathbf{Dyn}}$  for LTG samples considering different scale factors and distinct estimates of the velocity dispersion (see Section 4.1). We apply approximately symmetric cuts in the values of color g - r.

		Slope	Intercept	Correlation coefficient	Dispersion	No. of galaxies
$g - r \leqslant 0.6$						
g - r > 0.6	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 0.82 \pm 0.05 \\ 0.81 \pm 0.03 \\ 0.93 \pm 0.04 \\ 0.85 \pm 0.04 \\ 0.82 \pm 0.05 \\ 0.81 \pm 0.03 \\ 0.86 \pm 0.04 \end{array}$	$\begin{array}{c} 2.41 \pm 0.57 \\ 2.54 \pm 0.35 \\ 1.39 \pm 0.37 \\ 1.98 \pm 0.49 \\ 2.37 \pm 0.53 \\ 2.48 \pm 0.34 \\ 2.03 \pm 0.44 \end{array}$	$\begin{array}{c} 0.85 \\ 0.89 \\ 0.85 \\ 0.83 \\ 0.82 \\ 0.89 \\ 0.83 \end{array}$	$\begin{array}{c} 0.24 \\ 0.20 \\ 0.24 \\ 0.27 \\ 0.28 \\ 0.24 \\ 0.26 \end{array}$	$30 \\ 32 \\ 38 \\ 41 \\ 40 \\ 39 \\ 40$
	MKS MKA MKB MIS MIS MIA MIB	$\begin{array}{c} 1.19 \pm 0.04 \\ 0.99 \pm 0.05 \\ 1.07 \pm 0.05 \\ 1.21 \pm 0.04 \\ 1.11 \pm 0.04 \\ 0.93 \pm 0.08 \\ 1.01 \pm 0.08 \end{array}$	$\begin{array}{c} -1.64 \pm 0.45 \\ 0.56 \pm 0.58 \\ -0.11 \pm 0.54 \\ -2.02 \pm 0.46 \\ -0.79 \pm 0.42 \\ 1.24 \pm 0.81 \\ 0.44 \pm 0.79 \end{array}$	$\begin{array}{c} 0.83 \\ 0.76 \\ 0.76 \\ 0.83 \\ 0.84 \\ 0.72 \\ 0.71 \end{array}$	$\begin{array}{c} 0.29 \\ 0.33 \\ 0.35 \\ 0.29 \\ 0.27 \\ 0.36 \\ 0.38 \end{array}$	$54 \\ 38 \\ 39 \\ 52 \\ 53 \\ 44 \\ 41$

**Table 5.**  $BCES_{Bis}$  fit parameters for  $\mathbf{M_{Virial}}$  vs.  $\mathbf{M_{Dyn}}$  for LTG samples considering different scale factors and distinct estimates of the velocity dispersion (see Section 4.1). We apply color cuts considering the lower limit of the red sequence ( $\psi = -0.02667M_r + 0.11333$ ) (Cooper et al. 2010).

		Slope	Intercept	Correlation coefficient	Dispersion	No. of galaxies
$g-r\leqslant \psi$						
$g - r > \psi$	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 0.88 \pm 0.05 \\ 0.87 \pm 0.04 \\ 0.94 \pm 0.04 \\ 0.87 \pm 0.05 \\ 0.83 \pm 0.07 \\ 0.84 \pm 0.05 \\ 0.87 \pm 0.04 \end{array}$	$\begin{array}{c} 1.73 \pm 0.58 \\ 1.91 \pm 0.43 \\ 1.25 \pm 0.39 \\ 1.73 \pm 0.49 \\ 2.22 \pm 0.78 \\ 2.18 \pm 0.56 \\ 1.97 \pm 0.38 \end{array}$	$\begin{array}{c} 0.81 \\ 0.82 \\ 0.82 \\ 0.82 \\ 0.76 \\ 0.82 \\ 0.81 \end{array}$	$\begin{array}{c} 0.27 \\ 0.27 \\ 0.27 \\ 0.28 \\ 0.32 \\ 0.32 \\ 0.27 \end{array}$	48 47 55 59 60 53 56
	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 1.21 \pm 0.03 \\ 0.96 \pm 0.03 \\ 1.02 \pm 0.04 \\ 1.25 \pm 0.03 \\ 1.17 \pm 0.03 \\ 0.93 \pm 0.03 \\ 1.02 \pm 0.05 \end{array}$	$\begin{array}{c} -1.77 \pm 0.43 \\ 0.97 \pm 0.53 \\ 0.39 \pm 0.42 \\ -2.28 \pm 0.47 \\ -1.42 \pm 0.41 \\ 1.24 \pm 0.36 \\ 0.41 \pm 0.51 \end{array}$	$\begin{array}{c} 0.88 \\ 0.84 \\ 0.83 \\ 0.89 \\ 0.89 \\ 0.89 \\ 0.86 \\ 0.82 \end{array}$	$\begin{array}{c} 0.26 \\ 0.27 \\ 0.32 \\ 0.25 \\ 0.26 \\ 0.26 \\ 0.34 \end{array}$	35 23 24 34 33 30 25

Table 6.  $BCES_{Bis}$  fit parameters for  $\mathbf{M}_{\mathbf{Virial}}$  vs.  $\mathbf{M}_{\mathbf{Dyn}}$  for LTG samples considering different scale factors and distinct estimates of the velocity dispersion (see Section 4.1). We apply approximately symmetric cuts in the values of inclination angle *i*.

		Slope	Intercept	Correlation coefficient	Dispersion	No. of galaxies
$i \leqslant 66$						
i > 66	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 1.19 \pm 0.06 \\ 0.97 \pm 0.04 \\ 1.10 \pm 0.05 \\ 1.15 \pm 0.04 \\ 1.07 \pm 0.05 \\ 0.94 \pm 0.06 \\ 1.12 \pm 0.08 \end{array}$	$\begin{array}{c} -1.66 \pm 0.65 \\ 0.79 \pm 0.47 \\ -0.58 \pm 0.49 \\ -1.36 \pm 0.48 \\ -0.47 \pm 0.54 \\ 0.99 \pm 0.66 \\ -0.91 \pm 0.83 \end{array}$	$\begin{array}{c} 0.79 \\ 0.81 \\ 0.83 \\ 0.84 \\ 0.84 \\ 0.81 \\ 0.76 \end{array}$	$\begin{array}{c} 0.32 \\ 0.29 \\ 0.30 \\ 0.30 \\ 0.29 \\ 0.33 \\ 0.36 \end{array}$	$ \begin{array}{r} 43\\ 34\\ 34\\ 46\\ 46\\ 42\\ 38\end{array} $
	$\begin{array}{c} M_{\rm KS} \\ M_{\rm KA} \\ M_{\rm KB} \\ M_{\rm nS} \\ M_{\rm IS} \\ M_{\rm IA} \\ M_{\rm IB} \end{array}$	$\begin{array}{c} 0.92 \pm 0.02 \\ 0.86 \pm 0.04 \\ 0.85 \pm 0.03 \\ 0.92 \pm 0.02 \\ 0.89 \pm 0.02 \\ 0.86 \pm 0.02 \\ 0.85 \pm 0.03 \end{array}$	$\begin{array}{c} 1.37 \pm 0.24 \\ 2.08 \pm 0.38 \\ 2.16 \pm 0.32 \\ 1.25 \pm 0.26 \\ 1.68 \pm 0.26 \\ 2.00 \pm 0.24 \\ 2.17 \pm 0.32 \end{array}$	$\begin{array}{c} 0.90\\ 0.86\\ 0.86\\ 0.89\\ 0.89\\ 0.89\\ 0.89\\ 0.89\\ 0.87\end{array}$	$\begin{array}{c} 0.23 \\ 0.25 \\ 0.24 \\ 0.24 \\ 0.24 \\ 0.24 \\ 0.24 \\ 0.24 \end{array}$	$\begin{array}{c} 40 \\ 36 \\ 43 \\ 47 \\ 47 \\ 41 \\ 43 \end{array}$

### 7 CALIBRATION OF THE DYNAMICAL MASSES OF THE SDSS LTGS SAMPLE

In order to make the comparison between the dynamical and virial masses, we divide the samples in an approximately symmetrical way with respect to the different variables that might affect the estimates of the virial mass (see section 6). In Figure 1 we show a mosaic of the frequency distribution of the mentioned variables with the objective that the reader can visualize where the cuts were performed, dividing the sample approximately equally. Due to the different ways of calculating the masses and the number of variables investigated there are potentially more than 40 graphs that could be presented, but here we only show the graphs of one of the biggest samples ( $\mathbf{M}_{nS}$  sample) to avoid giving redundant information.

Once the cuts are made we perform a linear fit to the data. The coefficients of the fit could be affected significantly by both the choice of independent variables and the fitting method (Isobe et al. 1990). The measurement errors in the variables may induce even bigger biases, as well as correlation in the errors or intrinsic dispersion in the relation. The Bivariate Correlated Errors and Intrinsic Scatter Bisector ( $BCES_{Bis}$ ) method (Isobe et al. 1990; Akritas & Bershady 1996; Nigoche-Netro et al. 2010) is a statistical model that takes into account the different sources of bias mentioned above. Here, we use the  $BCES_{Bis}$  method to calculate the coefficients of the  $\mathbf{M}_{Virial}$  vs.  $\mathbf{M}_{Dyn}$  relationships. The results are as follows:

(i) Absolute magnitude cut in the filter  $g(M_g)$ .

The absolute magnitude cut was made at  $M_g = -20.2$ . In Table 1 and Figure 2 we show the comparison between the virial and dynamical masses for the seven estimates of the virial mass with  $M_g > -20.2$  and  $M_g \leq -20.2$ .

(ii) Sersic index cut.

The cut in the Sersic index n was taken at n = 0.8. In Table 2 and Figure 3 we show the results for the comparison of the virial and dynamical masses for the seven estimates of the virial mass with n > 0.8 and  $n \leq 0.8$ .

(iii) Concentration cut (R90/R50).

The cut in concentration was made at (R90/R50) = 2.4. In Table 3 and Figure 4 we show the results of comparing the virial and dynamical masses for the seven estimates of the virial mass with (R90/R50) > 2.4 and  $(R90/R50) \leq 2.4$ . (iv) Colour *q-r* cut.

The colour cut was taken in two different ways:

- Symmetrical cut in g-r = 0.6. In Table 4 and Figure 5 we show the results for the comparison of virial and dynamical masses for the seven estimates of the virial mass with g-r > 0.6 and g- $r \leq 0.6$ .

- Knowing that the galaxies, including the spiral galaxies, are found in two well differentiated regions on a colourmagnitude diagram (the red sequence on the top part and the blue cloud on the bottom part; see Figure 6) we performed a cut in the colour g-r considering the following lower limit to the red sequence ( $\psi$ ) (Cooper et al. 2010):  $\psi = -0.02667M_r + 0.11333$ 

In Table 5 and in Figure 7 we show the results of the comparison of the virial and dynamical masses for the seven estimates of the virial mass with  $g - r > \psi$  and  $g - r \leq \psi$ .

(v) Cut in inclination angle (i).

The cut in inclination angle was made at  $i = 66^{\circ}$ . In Table 6 and Figure 8 we show the results of the comparison for the virial and dynamical masses for the seven estimates of the virial mass with  $i > 66^{\circ}$  and  $i \leq 66^{\circ}$ .

### 8 DISCUSSION

The comparisons of the virial and dynamical masses from the different samples of LTGs gave the following results:

• When the magnitude is considered in the comparison of subsamples of LTGs we find that the correlation coefficients attain the lowest values and the fit dispersions attain the highest values with respect to the rest of the variables considered in the analysis (Sersic index n, concentration, colour, and angle of inclination).

There are neither substantial differences in the correlation fits nor in the dispersion when we compare samples of faint and bright galaxies (see Figure 2 and Table 1). The method used to make the estimate of the virial mass is of no consequence, that is to say, there are no significant differences whether the virial mass is obtained with a constant K or if it is dependent on the Sersic n index or the inclination angle. It also does not matter whether this virial mass was obtained using the velocity dispersions of the stars or of the gas.

• When we consider the Sersic index n, the correlation is relatively high in all fits (see Table 2). We can see that for  $n \leq 0.8$  the slopes are lower than the slopes for n > 0.8. It is noticeable that for galaxies with  $n \leq 0.8$  the correlation is lower when the virial mass is obtained using the stars compared to when this mass is obtained using the gas. For galaxies with n > 0.8 the opposite occurs. The method by which the virial mass is obtained turns out not to be significant for these results.

• When we consider the LTGs concentration parameter (R90/R50), we can see that for R90/R50 < 2.4 the slopes are lower than the slopes for R90/R50 > 2.4 (see Table 3). We also find a relatively high correlation for all fits. In this case, we observe that the more concentrated LTGs (R90/R50 < 2.4) show a larger correlation, when we use the gas in estimating the virial mass, as opposed to when we use the stars. For the less concentrated galaxies (R90/R50 > 2.4) the opposite occurs. The method by which the virial mass is calculated does not seem to be of much importance for these results.

• When the LTGs color is considered, we can see that for blue galaxies the slopes are lower than the slopes for red galaxies (see Tables 4 and 5). We also find a relatively high correlation in all cases. It can be noticed that for blue galax-



Figure 1. Frequency distribution of the variables that might affect the virial mass estimates for the  $M_{nS}$  sample. The approximately symmetrical cuts on the sample are made at -20.2, 0.8, 2.4, 0.6, 66° for magnitude, Sersic index, concentration, colour and inclination angle, respectively.

ies, the correlation is lower when the virial mass is obtained using the stars compared to when it is obtained by means of the gas. For red galaxies the opposite occurs. The method by which we obtained the virial mass does not seem to be of much consequence for the results above.

• When we take into account the inclination angle of the galaxy, we can see that for smaller inclination angles the slopes are greater than the slopes for larger inclination angles (see Table 6). We also find a clear difference in correlation coefficient and dispersion for samples with smaller inclination angles as compared with samples with larger inclination angles. Again, the method utilized to estimate the virial mass appears not to be of much significance.

The correlation of the fits is larger (lower dispersion) for galaxies with inclination angles  $i > 66^{\circ}$  both when the velocity dispersion of the stars or the velocity dispersion of the gas is used. How the virial mass estimate was made was not significant.

• In general, the fits show a lower correlation (larger dispersion) when the galaxies are separated by luminosity values and larger correlation (lower dispersion) when the galaxies are separated by inclination angle values (see Tables 1-6 and Figures 2-8). In the latter case, the method utilised to make the virial mass estimate is not important, there are no significant differences whether the K factor is taken as a constant or is dependent on the Sersic index n, or the inclination angle. Neither are there important differences if we use the velocity dispersion of the stars or the gas velocity dispersion for the virial mass estimates.

The estimates of virial masses given in this paper must be considered carefully and the results and suggestions given above should be taken into account in terms of the method and parameters used to obtain a better determination of the virial masses. In all cases, the best calibrations for the virial mass are those for which the inclination angle is relatively high ( $i > 66^{\circ}$ ). On the other hand, if you have samples of spiral galaxies with one of the following properties; relatively small Sersic index, relatively small concentration or blue color, it is more appropriate to use the virial mass estimate obtained with the gas velocity dispersion ( $H_{\alpha}$  or the average velocity dispersion of the Balmer lines). For the opposite cases it is better to use the estimate of the virial mass obtained with the velocity dispersion of the stars.

### 9 CONCLUSIONS

Due to the difficulty of calculating the dynamical masses of LTGs and with the objective of using the enormous amount of data from the SDSS, in the present paper we calculate different estimates of the virial mass for LTGs. The assumptions we use include Newtonian dynamics, and virial equilibrium. The data used for calculation are provided by the SDSS dynamical information of each galaxy as represented by its stars and gas. The virial masses were calibrated by comparing them with a subsample of galaxies whose dynamical masses were obtained using their rotation curves. Moreover, we characterized the possible effects that different variables might have on the values of the virial mass estimates. Among the main variables that could affect the estimates of the virial mass we find the following: the scale factor K (see equation 8), the luminosity, the Sersic index n, the concentration index, the colour and the galaxy inclination angle.

The most important results that followed from the comparison of virial and dynamical masses, considering approximately symmetrical cuts in the variables mentioned above, are the following:

• In the case of cuts in luminosity no significant differences in the correlation coefficients of the fits for virial mass versus dynamical mass are found (see Table 1). We also find that the correlation coefficients are relatively low (relatively high dispersion), and that the method utilized to calculate the virial mass has no importance (see section 4.1). Neither are there important differences whether the stars or the gas are used in calculating the virial mass. From the above we conclude that galaxy luminosity is not an adequate variable to use to improve the determination of the virial mass.

• When we perform cuts in the Sersic index n, on the concentration index or on the colour g - r, the fits show a relatively high correlation in all cases (see Tables 2-4). We can see that for lower Sersic index, lower concentration and blue galaxies the slopes of the fits are lower than the slopes for greater Sersic index, greater concentration and red galaxies. It is interesting to note that if the Sersic index and/or the concentration are relatively low or if the color is blue, the correlation is higher if the velocity dispersion of the gas ( $H_{\alpha}$  or the average velocity dispersion of the Balmer lines) are considered. For the opposite cases the correlation is higher if we consider the velocity dispersion of the stars. From this we may conclude that, as we might expect, for the smaller and bluer LTGs (dominated by the disk) the best indicator of the virial mass is the gas, while for larger and redder LTGs (dominated by the bulge), the best virial mass indicator is the stars. The method used to calculate the virial mass is of no consequence, in other words, there are no significant differences whether the virial mass is obtained with a constant K or if it is dependent on the Sersic n index or the inclination angle.

• In the case of cuts in the galactic inclination angle we find a highest correlation in the fits (lower dispersion) as compared to the variables discussed in the previous two items. We also can see that for smaller inclination angles the slopes are greater than the slopes for larger inclination angles. An evidently higher correlation appears for samples of galaxies with a larger inclination angle. In this case no significant differences due to the method used to obtain the virial mass is found. Neither are there significant differences whether the stars or the gas are used in the estimate of the virial mass. From this we may conclude that the better determined virial masses (using indistinctly the gas or the stars) are those for which the inclination angle is relatively high and that the method used for calculating this mass is of no importance, therefore, we may use either a constant Kfactor or a variable one without affecting substantially the estimate of the virial mass. The calibrations we used in this case are those presented in Table 6.

Considering these results and the calibration equation in Tables 1-6, we may conclude that the best calibrations for the virial masses of LTGs are those for galaxies with a relatively high inclination angle. If we have galaxies with relatively low inclination angles or we have samples of galaxies with heterogeneous properties one must take into consideration the size or colour of these galaxies through the use of the following variables: Sersic index n, concentration index or colour. For relatively smaller and bluer LTGs one must use the gas, while for LTGs that are relatively larger and redder one must use the stars.

If the reader wishes to perform their own virial mass estimates; they may use equation 1 and consider the calibration equations given in Tables 1-6 taking into consideration the properties of their sample and the advice given above.

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**Data availability.** The data underlying this article are available in the article and in its online supplementary material.

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Figure 2. Distribution of the logarithmic difference between virial and dynamical mass for two absolute magnitude cuts ( $M_g > -20.2$ ,  $M_g \leq -20.2$ ) and different virial mass estimations. Black continuous lines are BCES<sub>Bis</sub> fits



Figure 3. Distribution of the logarithmic difference between virial and dynamical mass for two Sersic index cuts ( $n \leq 0.8$ , n > 0.8) and different virial mass estimations. Black continuous lines are  $BCES_{Bis}$  fits



Figure 4. Distribution of the logarithmic difference between virial and dynamical mass for two concentration index cuts  $((R90/R50) \leq 2.4, (R90/R50) > 2.4)$  and different virial mass estimations. Black continuous lines are BCES<sub>Bis</sub> fits



Figure 5. Distribution of the logarithmic difference between virial and dynamical mass for two colour cuts  $(g - r \le 0.6, g - r > 0.6)$  and different virial mass estimations. Black continuous lines are BCES<sub>Bis</sub> fits

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Figure 6. Colour-magnitude diagram of the  $M_{nS}$  sample. The black line represents the limit of the red sequence according to Cooper et al. (2010).



Figure 7. Distribution of the logarithmic difference between virial and dynamical mass for two colour cuts considering the Red Sequence limit ( $\psi = -0.02667M_r + 0.11333$ ; Cooper et al. 2010) and different virial mass estimations. Black continuous lines are BCES<sub>Bis</sub> fits.



Figure 8. Distribution of the logarithmic difference between virial and dynamical mass for two inclination angle cuts ( $i \leq 66^{\circ}$ ,  $i > 66^{\circ}$ ) and different virial mass estimations. Black continuous lines are  $BCES_{Bis}$  fits

### 10 APPENDIX A

In Table A.1 we show the virial masses, and some parameters involved in the analysis of this work, of a sub-sample of 145 LTGs from SDSS DR16 with information in Catinella et al. (2005). The virial masses were obtained following the procedure described in section 4. In column 1 we find the galaxy name in SDSS DR16. In column 2 we find the redshift from SDSS DR16. In column 3 we find the absolute magnitude in the g filter, estimated using the apparent magnitude from the SDSS DR16. In column 4 we find the colour g - r from the SDSS DR16. In columns 5 and 6 we find the ratio of the Petrosian radii R90 and R50 from the SDSS DR16 in the g and r filters respectively. In columns 7 and 8 we find the Sersic index n, in the g and r filters respectively, estimated using the procedure described in section 6. In column 9 and 10 we find the galactic inclination angles, in the g and rfilters respectively, estimated using equation 1 from section 4.1. Finally, in columns 11, 12, 13, 14, 15, 16, and 17 we find the logarithmic virial masses  $M_{KS}, M_{KA}, M_{KB}, M_{nS},$  $M_{IS}$ ,  $M_{IA}$ , and  $M_{IB}$  respectively. The entire catalogue of virial masses of 126  $\,699$  LTGs from the SDSS (see section 2) with the same structure of Table A.1, can be found in electronic form in the following link:

It is very important to remark that the previously mentioned masses must be corrected, depending on the necessities of the reader, using Tables 1-6 from section 7 and the advice given in section 9.

In Table A.2 we show the dynamical masses of a subsample of 145 LTGs from Catinella et al. (2005) with photometric and/or spectroscopic information in the SDSS DR16. The dynamical masses were obtained using the rotation curves from Catinnella et al. 2005 as described in section 5. In column 1 we find the galaxy name in the Arecibo General Catalog (AGC). In Column 2 we show other names of the galaxy (NGC, IC, CGCG or MCG). In column 3 we find the SDSS DR16 name. In columns 4 and 5 we find the right ascension and declination, respectively. Finally, in column 6 we find the dynamical mass in solar masses.

SDSS DR16	z	$M_g$	g - r	$R50/R90_{g}$	$R50/R90_{r}$	$n_g$	$n_r$	$i_g$	$i_r$	$M_{KS}$	M <sub>KA</sub>	$M_{KB}$	$M_{nS}$	$M_{IS}$	$M_{IA}$	$M_{IB}$
1237653653447180545	$0.01872 \pm 0.00002$	$-19.05 \pm 0.0065$	$0.08504 \pm 0.0085$	$2.595 \pm 0.2061$	$2.665 \pm 0.0945$	$0.9331 \pm 0.3671$	$1.068 \pm 0.1989$	$78.47 \pm 0.6191$	$84.43 \pm 1.043$	$10.18 \pm 0.0953$	$10.28 \pm 0.0297$	$9.779 \pm 0.0793$	$10.31 \pm 0.0953$	$10.16 \pm 0.0400$	$10.26 \pm 0.0125$	$9.756 \pm 0.0333$
1237652629638873182	$0.03893 {\pm} 0.00002$	$-20.15 \pm 0.0050$	$0.6190 \pm 0.0066$	$2.328 \pm 0.0655$	$2.391 \pm 0.0434$	$0.5865 \pm 0.0589$	$0.6482 \pm 0.0462$	$80.71 \pm 1.326$	$83.48 \pm 1.142$	$10.54 \pm 0.0799$	$10.25 \pm 0.0453$	$10.16 {\pm} 0.0540$	$10.68 \pm 0.0799$	$10.51 \pm 0.0336$	$10.23 \pm 0.0191$	$10.13 \pm 0.0227$
1237652947456360495	$0.01312 {\pm} 0.00001$	$-20.95 \pm 0.0032$	$0.7691 \pm 0.0045$	$2.956 \pm 0.2660$	$3.013 \pm 0.3245$	$1.937 \pm 1.075$	$2.181 \pm 1.480$	$6824 \pm 0.2975$	$68.23 \pm 0.2784$	$11.19 \pm 0.0112$	$11.42 {\pm} 0.0643$	$11.33 {\pm} 0.0495$	$11.28 \pm 0.0112$	$11.22 \pm 0.0045$	$11.45 \pm 0.0254$	$11.36 {\pm} 0.0195$
1237652947993624616	$0.02032 \pm 0.00001$	$-19.86 \pm 0.0041$	$0.3786 \pm 0.0059$	-	-	$0.3278 \pm 11.87$	$0.3402 \pm 16.78$	$49.55 \pm 0.5539$	$49.83 \pm 0.5344$	$9.062 \pm 0.6737$	$9.975 \pm 0.0180$	$9.957 \pm 0.0236$	$9.219 \pm 0.6737$	$9.264 \pm 0.2182$	$10.18 \pm 0.0059$	$10.16 \pm 0.0077$
1237652900753244294	$0.01925 \pm 0.00001$	$-18.89 \pm 0.0042$	$0.3997 \pm 0.0059$	$2.592 \pm 0.1168$	$2.586 \pm 0.1665$	$0.9280 \pm 0.2066$	$0.9170 \pm 0.2899$	$80.57 \pm 0.9919$	$80.70 \pm 1.093$	$9.856 \pm 0.2327$	$9.808 \pm 0.0097$	$9.802 \pm 0.0140$	$9.989 \pm 0.2327$	$9.834 \pm 0.0975$	$9.786 \pm 0.0042$	$9.780 \pm 0.0059$
1237652900753244175	$0.01911 \pm 0.00001$	$-20.56 \pm 0.0028$	$0.8687 \pm 0.0038$	$3.147 \pm 0.6629$	$3.246 \pm 0.7332$	$2.886 \pm 3.976$	$3.543 \pm 5.347$	$71.29 \pm 0.3562$	$70.91 \pm 0.3030$	$11.04 \pm 0.0137$	$10.98 \pm 0.0309$	$10.87 \pm 0.0295$	$11.08 \pm 0.0137$	$11.06 \pm 0.0055$	$10.99 \pm 0.0124$	$10.88 \pm 0.0119$
1237652900753244328	$0.00448 \pm 0.00001$	$-17.15 \pm 0.0079$	$0.1221 \pm 0.0109$	$2.317 \pm 0.0941$	$2.276 \pm 2.277$	$0.5770 \pm 0.0821$	$0.5431 \pm 1.775$	90	90	$10.02 \pm 0.4501$	-	-	$10.17 \pm 0.4501$	$9.983 \pm 0.1924$	$9.731 \pm 0.0090$	-
1237652947993952343	$0.02021 \pm 0.00001$	$-18.91 \pm 0.0073$	$0.4281 \pm 0.0104$	$1.927 \pm 0.0354$	$1.971 \pm 0.0332$	$0.3720 \pm 0.0097$	$0.3851 \pm 0.0105$	$38.76 \pm 0.9533$	$39.21 \pm 0.9607$	$9.927 \pm 0.2006$	$10.09 \pm 0.0322$	$9.971 \pm 0.0427$	$10.08 \pm 0.2006$	$10.30 \pm 0.0536$	$10.45 \pm 0.0088$	$10.34 \pm 0.0115$
1237663782593822774	$0.01798 \pm 0.00001$	$-19.32 \pm 0.0039$	$0.5806 \pm 0.0053$	$2.057 \pm 0.0314$	$2.099 \pm 0.0241$	$0.4162 \pm 0.0129$	$0.4349 \pm 0.0113$	61.93±0.5195	$62.40 \pm 0.4355$	$10.07 \pm 0.0896$	$10.23 \pm 0.0077$	$10.22 \pm 0.0091$	$10.22 \pm 0.0896$	$10.14 \pm 0.0337$	$10.30 \pm 0.0030$	$10.30 \pm 0.0035$
12376662782120750224	$0.01908 \pm 0.00002$ 0.01024 $\pm 0.00001$	-18.99±0.0058 17.08±0.0074	$0.9062 \pm 0.0082$ 0.2800 $\pm 0.0117$	$2.450\pm0.0968$ $2.282\pm0.1256$	$2.693 \pm 0.1221$ 2.502 $\pm 0.1110$	$0.7160 \pm 0.1200$ 0.6282 $\pm 0.1202$	$1.129 \pm 0.2746$ 0.7855 \pm 0.1572	78.52±0.7862 48.55±1.102	46 46±1 240	9.464±0.3898 0.022±0.2582	$10.02 \pm 0.0276$ 0.620 $\pm 0.0241$	9.963±0.0351 0.762±0.0247	9.597±0.3898	$9.449 \pm 0.1621$ 10.15 \pm 0.1122	10.01±0.0115 0.860±0.0070	$9.948 \pm 0.0146$ 0.002 $\pm 0.0081$
1227003183130135334	0.06611±0.00002	-11.55±0.0014 21.08±0.0052	0.5300±0.0117	1 020±0 0251	2.004±0.0200	0.0355±0.1302	0.2059±0.0101	40.00±0.0225	40.40±1.240	10.05±0.0608	$10.023\pm0.0241$	10 20±0 1679	11 10±0.0608	11 21±0.0185	10.20±0.1150	10.65±0.0500
1237663783130824820	0.06646±0.00002	-20.30±0.0076	0.6856±0.0004	2 310+0 1086	2.004±0.0250	0.5709±0.0039	0.7188+0.1270	90	47.05±0.3645	$10.80\pm0.0003$ 10.80±0.1073	$10.03\pm0.3792$ 10.72 $\pm0.0297$	10.59±0.1078	10.94±0.1073	$10.76\pm0.0458$	$10.29\pm0.1130$ $10.69\pm0.0128$	$10.05\pm0.0309$ $10.55\pm0.0146$
1237666338652618892	$0.01771 \pm 0.00002$	$-18.54\pm0.0057$	0.2947±0.0086	$2.0349\pm0.0491$	2.083+0.0443	0.4073±0.0189	$0.4273\pm0.0197$	60 80±0 7683	60 09+0 8447	-	$9.560 \pm 0.0943$	9.887±0.0682	-	10.76	9.648±0.0349	9.975±0.0252
1237663784205680908	$0.03935 \pm 0.00002$	$-19.59 \pm 0.0073$	$0.8128 \pm 0.0092$	$2.571 \pm 0.1674$	$2.626 \pm 0.3213$	$0.8923 \pm 0.2814$	$0.9894 \pm 0.6159$	$82.24 \pm 1.885$	$81.98 \pm 1.317$	$10.61 \pm 0.0629$	$10.72 \pm 0.0568$	$10.22 \pm 0.0848$	$10.74 \pm 0.0629$	$10.58 \pm 0.0265$	$10.70 \pm 0.0239$	$10.19 \pm 0.0357$
1237666339190472839	$0.00581 \pm 0.00003$	$-16.79 \pm 0.0247$	$0.3531 \pm 0.0377$	$2.169 \pm 0.1136$	$2.229 \pm 0.0515$	$0.4707 \pm 0.0653$	$0.5086 \pm 0.0352$	$74.50 \pm 0.7108$	$76.32 \pm 1.600$	$9.917 \pm 0.2808$	-	-	$10.06 \pm 0.2808$	$9.912 \pm 0.1154$	$9.537 \pm 0.0653$	-
1237663784206270641	$0.01266 \pm 0.00002$	$-18.88 \pm 0.0101$	$0.3543 \pm 0.0140$	$2.027 \pm 0.0325$	$2.119 \pm 0.0272$	$0.4043 \pm 0.0122$	$0.4444 \pm 0.0135$	$68.37 \pm 0.6463$	$67.69 \pm 0.6588$	$9.7200 \pm 0.2465$	$9.056 \pm 0.2469$	$9.696 \pm 0.1062$	$9.873 \pm 0.2465$	$9.752 \pm 0.0971$	$9.088 \pm 0.0972$	$9.728 \pm 0.0418$
1237666338116993064	$0.02712 \pm 0.00001$	$-21.86 \pm 0.0027$	$0.7110 \pm 0.0037$	$2.305 \pm 0.0249$	$2.457 \pm 0.0363$	$0.5666 \pm 0.021$	$0.7259 {\pm} 0.0459$	$57.48 \pm 0.3404$	$52.30 \pm 0.2993$	$11.49 \pm 0.0159$	$11.33 {\pm} 0.0688$	$11.26 \pm 0.0609$	$11.64 \pm 0.0159$	$11.63 {\pm} 0.0056$	$11.47 \pm 0.0239$	$11.40 \pm 0.0212$
1237663783132790881	$0.00662 \pm 0.00001$	$-10.29 \pm 0.1984$	$0.5014 \pm 0.2355$	-	-	-	-	60	61.64	$8.892 \pm 0.2247$	-	-	$9.049 \pm 0.2247$	$8.882 \pm 0.1312$	$8.255 \pm 0.1026$	-
1237657189840584856	$0.02590 \pm 0.00001$	$-20.05 \pm 0.0039$	$0.6355 \pm 0.0052$	$2.658 \pm 0.1479$	$2.783 \pm 0.1539$	$1.053 \pm 0.3060$	$1.355 \pm 0.4258$	$74.23 \pm 0.4140$	$73.70 \pm 0.4344$	$10.67 \pm 0.0357$	$10.54 \pm 0.0125$	$10.47 \pm 0.0135$	$10.79 \pm 0.0357$	$10.68 \pm 0.0146$	$10.54 \pm 0.0052$	$10.47 \pm 0.0056$
1237663782597034125	-	-	-	-	-	-	-	81	81	-	-	-	-	-	-	-
1237663782597099527	$0.01547 \pm 0.00001$	$-19.92 \pm 0.0046$	$0.5857 \pm 0.0064$	$2.726 \pm 0.1654$	$2.907 \pm 0.1503$	$1.206 \pm 0.4011$	$1.748 \pm 0.5467$	$76.79 \pm 0.1545$	$74.35 \pm 0.3652$	$10.58 \pm 0.0261$	$8.576 \pm 0.2134$	$10.11 \pm 0.0266$	$10.69 \pm 0.0261$	$10.57 \pm 0.0108$	$8.570 \pm 0.0877$	$10.10 \pm 0.0110$
1237657069546831898	$0.01632 \pm 0.00001$	$-20.29\pm0.0032$	$0.6588 \pm 0.0045$	$3.129 \pm 0.6831$	$3.251 \pm 0.6621$	$2.778 \pm 3.951$	$3.581 \pm 4.878$	70.42±0.1723	68.24±0.2631	$10.76 \pm 0.0149$	$9.511 \pm 0.0005$	$10.72 \pm 0.0733$	$10.79 \pm 0.0149$	$10.78 \pm 0.0059$	$9.535 \pm 0.0005$	$10.74 \pm 0.0291$
1237678880495894618	-	-	-	- 0.062   0.4047	2 110 0 5000	1 007 1 1 744	-	71 22 0 4067	55	11 10 0 0171	-	-	-	-	-	-
1237652000223000057	$0.02639 \pm 0.00001$ $0.01790 \pm 0.00001$	$-21.13\pm0.0029$ $-20.54\pm0.0027$	$0.6943 \pm 0.0040$ $0.6106 \pm 0.0038$	$2.963 \pm 0.4243$ 2 542 $\pm 0.0282$	$2.576\pm0.0246$	$1.967 \pm 1.744$ 0.8446 ± 0.0442	$2.718 \pm 2.833$ 0.9006 $\pm 0.0419$	58 92±0 2779	$71.91\pm0.3381$ 50 30 $\pm0.2631$	$11.12\pm0.0171$ 10.57 $\pm0.0168$	$11.18 \pm 0.0887$ 10.19 $\pm 0.0295$	$11.02\pm0.0701$ 10.29±0.0209	$11.19\pm0.0171$ 10.70±0.0168	$11.13\pm0.0069$ 10.67 $\pm0.0062$	$11.19\pm0.0338$ 10.29 $\pm0.0108$	$11.03\pm0.0283$ 10.39 $\pm0.0077$
1237663783676477669	$0.02131 \pm 0.00001$	-21.03±0.0029	0.9200±0.0038	1.936±0.0116	2.045±0.0240	$0.3745\pm0.0033$	0.4114±0.0114	35.45±0.5561	48.36±0.4421	$10.01 \pm 0.0100$ $10.90 \pm 0.0132$	$11.01\pm0.0230$ 11.01±0.0328	$10.23 \pm 0.0203$ $10.74 \pm 0.0337$	11.05±0.0132	11 21+0 0039	11 32+0 0094	11.05±0.0097
1237657070628503722	$0.07550 \pm 0.00001$	$-21.39\pm0.0057$	$0.6914 \pm 0.0074$	$2.332 \pm 0.1262$	$2.460 \pm 0.1266$	$0.5899 \pm 0.1145$	$0.7288 \pm 0.1610$	78.25±1.1577	$77.89 \pm 0.8764$	$11.39 \pm 0.0444$	-	-	$11.53 \pm 0.0444$	$11.37 \pm 0.0185$	$11.30 \pm 0.0061$	-
1237657584951034038	$0.02349 \pm 0.00002$	$-19.31 \pm 0.0065$	$0.7005 \pm 0.0085$	$2.435 \pm 0.0564$	$2.655 \pm 0.1065$	$0.6974 \pm 0.0672$	$1.047 \pm 0.2188$	$79.35 \pm 1.253$	$78.36 \pm 0.8041$	$10.64 \pm 0.1297$	$10.36 \pm 0.0352$	$10.19 \pm 0.0465$	$10.78 \pm 0.1297$	$10.63 \pm 0.0541$	$10.34 \pm 0.0147$	$10.18 \pm 0.0194$
1237663783142096968	$0.02164 \pm 0.00001$	$-21.20 \pm 0.0035$	$0.6398 {\pm} 0.0048$	$2.478 \pm 0.0817$	$2.622 \pm 0.0953$	$0.7519 \pm 0.1088$	$0.9832 \pm 0.1813$	$69.79 \pm 0.4075$	$67.23 \pm 0.3277$	$11.12 \pm 0.0238$	$11.24 \pm 0.0060$	$11.24 \pm 0.0058$	$11.26 \pm 0.0238$	$11.15 \pm 0.0094$	$11.27 \pm 0.0025$	$11.27 \pm 0.0024$
1237663783142228130	$0.02189 \pm 0.00001$	$-19.13 \pm 0.0064$	$0.4399 \pm 0.0089$	$2.256 \pm 0.0923$	$2.367 \pm 0.0798$	$0.5279 \pm 0.0681$	$0.6239 \pm 0.0797$	$74.13 \pm 0.9235$	$72.58 \pm 0.6751$	$9.964 \pm 0.1655$	$9.974 \pm 0.0165$	$9.990 \pm 0.0191$	$10.11 \pm 0.1655$	$9.968 \pm 0.0674$	$9.978 \pm 0.0068$	$9.995 \pm 0.0079$
1237663783142228165	-	-	-	-	-	-	-	68	68	-	-	-	-	-	-	-
1237657584951230617	$0.02342 \pm 0.00001$	$-20.25 \pm 0.0043$	$0.6541 \pm 0.0058$	$2.312 \pm 0.0315$	$2.451 \pm 0.0496$	$0.5726 \pm 0.0271$	$0.7177 \pm 0.0617$	$78.693 \pm 0.5700$	$79.36 \pm 0.4983$	$10.79 \pm 0.0593$	$10.52 \pm 0.0236$	$10.41 \pm 0.0290$	$10.94 \pm 0.0593$	$10.78 \pm 0.0247$	$10.50 \pm 0.0099$	$10.39 \pm 0.0121$
1237652900767268885	$0.01730 \pm 0.00002$	$-20.31 \pm 0.0051$	$0.5606 \pm 0.0071$	$1.877 \pm 0.2926$	$1.999 \pm 0.2754$	$0.3596 \pm 0.0678$	$0.3941 \pm 0.0947$	$47.69 \pm 0.3971$	$50.68 \pm 0.3523$	$10.48 \pm 0.0777$	$10.19 \pm 0.0225$	$10.16 \pm 0.0277$	$10.63 \pm 0.0777$	$10.68 \pm 0.0250$	$10.40 \pm 0.0073$	$10.37 \pm 0.0089$
1237663784217149628	$0.00948 \pm 0.00002$	$-17.90 \pm 0.0135$	$0.3286 \pm 0.0366$	$2.204 \pm 0.0996$	$2.221 \pm 0.0500$	$0.4923 \pm 0.0634$	$0.5029 \pm 0.0333$	$76.72 \pm 1.524$	$79.60 \pm 4.546$	$10.34 \pm 0.2130$	-		$10.49 \pm 0.2130$	$10.32 \pm 0.0887$	$9.659 \pm 0.0403$	-
1237666300018229273	$0.02267 \pm 0.00001$	-20.58±0.0040	$0.6019 \pm 0.0055$	2.620±0.2286	$2.694 \pm 0.0544$	0.9781±0.4319	$1.133 \pm 0.1228$	76.40±0.5634	78.34±0.4922	$10.14 \pm 0.1150$	$10.67 \pm 0.0498$	$10.33 \pm 0.0713$	$10.26 \pm 0.1150$	$10.13 \pm 0.0476$	$10.66 \pm 0.0207$	$10.32 \pm 0.0954$
1237649964066406405	$0.01891 \pm 0.00001$	$-21.55 \pm 0.0028$	$0.7851 \pm 0.0038$	$2.598 \pm 0.0687$	2.699±0.0967	$0.9387 \pm 0.1232$	$1.142 \pm 0.2203$	73.63±0.3427	70.24±0.3288	$11.37 \pm 0.0140$	8.925±0.7590	$11.01 \pm 0.0641$	$11.50 \pm 0.0140$	$11.38 \pm 0.0057$	$8.936 \pm 0.3064$	$11.02 \pm 0.0259$
1237033388477411043	-	19 59-00 0060	-	- 2.266±69.41	2 456±70 84	-	- 0.7928±80.9997	78 09±0 5516	70	0.427±0.8147	0 152+0 1715	0.065±0.0572	0.520±0.2147	0.408±0.2449	- 0 192±0 0795	- 0.026±0.0242
1237664837535858925	0.01392_0.00001	-18.3810.0000	0.010210.0000	2.300±00.41	2.400110.04	0.0220100.00	0.1230.103.2221	50	50	5.457±0.8147	5.152±0.1115	5.505±0.0515	5.360±0.8147	5.400±0.3442	5.125±0.0125	5.530±0.0242
1237667782809223472				-				72	72	-	-					
1237667782809223502	$0.07771 \pm 0.00001$	$-20.69 \pm 0.0069$	$0.6491 \pm 0.0089$	$2.173 \pm 0.0995$	$2.387 \pm 0.0791$	$0.4733 \pm 0.0579$	$0.6440 \pm 0.0832$	$84.81 \pm 2.920$	$84.15 \pm 2.1211$	$10.67 \pm 0.1342$	$11.15 \pm 0.0176$	$11.10 \pm 0.0183$	$10.81 \pm 0.1342$	$10.64 \pm 0.0568$	$11.12 \pm 0.0076$	$11.07 \pm 0.0079$
1237661086957568117	$0.07600 \pm 0.00002$	$-20.82 \pm 0.0078$	$0.4747 \pm 0.0102$	$2.366 \pm 0.2197$	$2.457 \pm 0.1390$	$0.6227 \pm 0.2187$	$0.7250 \pm 0.1755$	$82.93 \pm 3.013$	$82.03 \pm 2.118$	$10.65 \pm 0.2132$	$10.73 \pm 0.0484$	$10.62 \pm 0.0556$	$10.79 \pm 0.2132$	$10.63 \pm 0.0898$	$10.70 \pm 0.0205$	$10.59 \pm 0.0235$
1237664092898852896	$0.02610 \pm 0.00001$	$-21.39 \pm 0.0029$	$0.6472 \pm 0.0040$	$2.622 \pm 0.3894$	$2.765 \pm 0.3534$	$0.9824 \pm 0.7398$	$1.307 \pm 0.9389$	$72.94 \pm 0.3811$	$70.60 \pm 0.3792$	$11.58 \pm 0.0147$	$11.54 \pm 0.0624$	$11.57 \pm 0.0503$	$11.70 \pm 0.0147$	$11.59 \pm 0.0060$	$11.55 \pm 0.0252$	$11.58 \pm 0.0203$
1237654601019686930	$0.01299 \pm 0.00001$	$-21.42 \pm 0.0034$	$0.8196 \pm 0.0048$	$2.938 \pm 0.0886$	$2.996 \pm 0.0976$	$1.867 \pm 0.3449$	$2.105 \pm 0.4292$	$44.53 \pm 0.2229$	$44.09 \pm 0.2119$	$11.34 \pm 0.0105$	$10.58 \pm 0.0663$	$11.18 \pm 0.0469$	$11.42 \pm 0.0105$	$11.62 \pm 0.0032$	$10.86 \pm 0.0197$	$11.46 \pm 0.0139$
1237664093438214204	-	-	-	-	-	-	-	65	65	-	-	-	-	-	-	-
1237660412649865229	0.00492±0.00001	-17.67±0.0187	0.225±0.0209	2.230±0.0183	2.238±0.0407	0.5096±0.0126	0.5151±0.0286	$40.43 \pm 1.295$	52.19±0.3733	9.327±0.1709	-	-	9.476±0.1709	9.571±0.0527	9.543±0.0060	-
1237071200004108703	$0.04905 \pm 0.00001$ 0.01658 \pm 0.00001	-20.94±0.0036	$0.4661 \pm 0.0048$ 0.5724 $\pm 0.0050$	2.537±0.0473 2.500±0.1272	2.555±0.0412 2.502±0.0772	0.8301±0.0730 0.7042±0.1820	0.8303±0.0629 0.0208±0.1272	49.71±0.3044 \$1.02±0.8628	49.94±0.4331 81.72±0.7184	$10.43 \pm 0.0326$ 10.47 $\pm 0.0050$	$10.41\pm0.0093$ 0.085 $\pm0.0182$	$10.33 \pm 0.0111$ 10.20 $\pm 0.0002$	10.50±0.0526	10.05±0.0171	0.060±0.0032	$10.35 \pm 0.0037$ 10.26 \pm 0.0040
1237650705680235542	0.01748+0.00001	-20.09±0.0034	0.7612±0.0046	2.305±0.1212	2.000+0.0666	0.6747±0.1040	$0.5258\pm0.1372$ 0.6679 $\pm0.0742$	75 58±0.4630	75 11+0 3188	$10.47 \pm 0.0335$ $10.82 \pm 0.0335$	10 75±0 0065	$10.29\pm0.0033$ $10.70\pm0.0076$	10.00±0.0335	$10.45\pm0.0405$ $10.81\pm0.0138$	10.75±0.0028	$10.20\pm0.0040$ 10.70±0.0032
1237660763768029308	$0.04594 \pm 0.00001$	$-20.60 \pm 0.0037$	$0.7064 \pm 0.0048$	$2.121\pm0.0302$	$2.244 \pm 0.0000$ $2.244 \pm 0.0297$	$0.4453 \pm 0.0151$	$0.5188 \pm 0.0211$	65.64±0.6157	$63.91 \pm 0.5043$	$10.81 \pm 0.0476$	$10.83 \pm 0.0101$	$10.80 \pm 0.00108$	$10.96 \pm 0.0476$	$10.87 \pm 0.0183$	$10.88 \pm 0.0040$	$10.85 \pm 0.0043$
1237648720676585591	$0.05616 \pm 0.00001$	$-21.51 \pm 0.0041$	$0.5739 \pm 0.0053$	$1.909 \pm 0.1255$	$1.992 \pm 0.1411$	$0.3674 \pm 0.0323$	$0.3919 \pm 0.0475$	$48.93 \pm 0.6467$	$46.14 \pm 0.5125$	$11.04 \pm 0.0507$	$11.42 \pm 0.0157$	$11.26 \pm 0.0157$	$11.20 \pm 0.0507$	$11.27 \pm 0.0159$	$11.65 \pm 0.0050$	$11.49 \pm 0.0050$
1237648720676585778	$0.08781 \pm 0.00001$	$-22.37 \pm 0.0046$	$0.5505 {\pm} 0.0058$	$2.157 \pm 0.0395$	$2.254 \pm 0.0356$	$0.4640 \pm 0.0219$	$0.5264 \pm 0.0262$	$47.22 \pm 0.7476$	$47.54 \pm 0.5689$	$11.51 \pm 0.0415$	$11.31 \pm 0.0126$	$11.31 \pm 0.0126$	$11.66 \pm 0.0415$	$11.74 \pm 0.0130$	$11.54 \pm 0.0042$	$11.54 \pm 0.0042$
1237665097926115359	$0.01361 \pm 0.00001$	$-20.57 \pm 0.0035$	$0.7689 {\pm} 0.0048$	$2.833 \pm 0.1501$	$2.896 \pm 0.1480$	$1.502 \pm 0.4650$	$1.711 \pm 0.5267$	$71.60 \pm 0.3410$	$72.01 \pm 0.3140$	$11.17 \pm 0.0127$	$10.93 {\pm} 0.0901$	$11.26 \pm 0.0581$	$11.27 \pm 0.0127$	$11.18 {\pm} 0.0052$	$10.94 \pm 0.0364$	$11.27 \pm 0.0235$
1237658493336879239	$0.00683 \pm 0.00001$	$-18.15 \pm 0.0079$	$0.7368 \pm 0.0111$	$2.708 \pm 0.2508$	$2.744 \pm 0.2686$	$1.165 \pm 0.5845$	$1.252 \pm 0.6800$	$78.48 \pm 0.4699$	$77.49 \pm 0.4428$	$9.965 \pm 0.0465$	-	-	$10.08 \pm 0.0465$	$9.950 \pm 0.0193$	$10.41 \pm 0.0100$	-
1237668289080000630	$0.01268 {\pm} 0.00001$	$-18.50 \pm 0.0058$	$0.5313 \pm 0.0080$	$2.158 \pm 0.0306$	$2.225 \pm 0.0302$	$0.4645 \pm 0.0171$	$0.5062 \pm 0.0204$	$68.09 \pm 0.5463$	$67.65 \pm 0.5310$	$10.15 \pm 0.1015$	$9.785 \pm 0.0255$	$9.823 \pm 0.0278$	$10.30 \pm 0.1015$	$10.18 \pm 0.0399$	$9.818 {\pm} 0.0101$	$9.856 \pm 0.0110$
1237658205573808201	$0.01591 \pm 0.00001$	$-21.16 \pm 0.0036$	$0.5144 \pm 0.0051$	$2.323 \pm 0.0172$	$2.458 \pm 0.0302$	$0.5819 \pm 0.0152$	$0.7254 \pm 0.0381$	$62.33 \pm 0.3190$	$62.73 \pm 0.2845$	$10.74 \pm 0.0331$	$10.88 \pm 0.0326$	$10.50 \pm 0.0432$	$10.88 \pm 0.0331$	$10.81 \pm 0.0125$	$10.95 \pm 0.0123$	$10.57 \pm 0.0163$
1237671122692210971	$0.04662 \pm 0.00001$	-20.73±0.0041	$0.5637 \pm 0.0053$	$2.732 \pm 0.3064$	$2.995 \pm 0.3265$	$1.222 \pm 0.7550$	$2.101 \pm 1.434$	86.29±1.977	85.16±1.097	$11.05 \pm 0.0378$	$10.74 \pm 0.0334$	$10.56 \pm 0.0377$	$11.15 \pm 0.0378$	$11.02 \pm 0.0161$	$10.71 \pm 0.0142$	$10.53 \pm 0.0160$
1237668289080983802	0.07255±0.00001	-19.72±0.0137	0.4970±0.0181	2.310±0.2028	$2.340 \pm 0.3146$	0.5705±0.1734	$0.5974 \pm 0.2919$	83.56	82.89	9.286±1.479	8.981±0.3235	10.31±0.0521	9.432±1.479	9.258±0.6236	8.954±0.1365	10.28±0.0223
1237007541753331904 1927651800161291160	$0.02520\pm0.00002$ 0.02127 $\pm0.00001$	$-20.06\pm0.0061$ 20.56 $\pm0.0041$	$0.7851 \pm 0.0082$ 0.6502 $\pm 0.0057$	$2.596 \pm 0.1880$ 1.064 $\pm 0.0016$	2 061±0 0170	0.9346±0.3355 0.2820±0.0040	- 4176±0.0075	90 55.07±0.4297	86.44±0.6861 56.74±0.4200	$11.28 \pm 0.0586$ 10.81 $\pm 0.0522$	$10.81 \pm 0.0819$ 10.70 $\pm 0.0222$	$10.24 \pm 0.1987$ 10.56 $\pm 0.0270$	$11.41\pm0.0586$ 10.07 $\pm0.0522$	$11.24 \pm 0.0250$ 10.05 \pm 0.0184	$10.77 \pm 0.0349$ 10.82 \pm 0.0078	$10.21 \pm 0.0846$ 10.60 \pm 0.005
1237667202650384635	0.02127±0.00001	-19 18±0 0045	0.4665±0.0061	$2542\pm0.0010$ 2542 $\pm0.1177$	2.501±0.0119	0.3325±0.0045	0.7977+0.1156	79 50±0 6931	78 14±0.4200	$10.31\pm0.0322$ 10.15 $\pm0.1186$	9.148+0.0740	9.909+0.0278	$10.97 \pm 0.0322$ 10.29 $\pm 0.1186$	10.14+0.0494	9.132±0.0078	9.892+0.0116
1237664667363246202	$0.04422 \pm 0.00001$	$-21.83 \pm 0.0029$	$0.5348 \pm 0.0038$	$2.576 \pm 0.0757$	$2.635 \pm 0.0655$	$0.8998 \pm 0.1287$	$1.008 \pm 0.1285$	$53.40 \pm 0.4220$	$51.39 \pm 0.3650$	$11.41 \pm 0.0198$	$11.54 \pm 0.1565$	$11.28 \pm 0.1086$	$11.54 \pm 0.0198$	$11.58 \pm 0.0067$	$11.71 \pm 0.0527$	$11.45 \pm 0.0366$
1237667323784527982	$0.05390 \pm 0.00001$	$-19.42 \pm 0.0085$	$0.3108 \pm 0.0122$	$2.075 \pm 0.1211$	$2.339 \pm 0.1569$	$0.4236 \pm 0.0527$	$0.5965 \pm 0.1452$	88	87.71	$11.13 \pm 0.1643$	$10.20 \pm 0.0346$	$10.22 \pm 0.0374$	$11.28 \pm 0.1643$	$11.09 \pm 0.0697$	$10.17 \pm 0.0149$	$10.18 \pm 0.0161$
1237648720686415913	$0.01847 {\pm} 0.00001$	$-21.09 \pm 0.0026$	$0.6883 \pm 0.0036$	$2.957 \pm 0.3331$	$3.004 \pm 0.2552$	$1.943 \pm 1.351$	$2.140 \pm 1.141$	$64.63 \pm 0.3169$	$64.37 \pm 0.2870$	$11.01 \pm 0.0142$	$11.06 \pm 0.0708$	$10.84 \pm 0.0603$	$11.09 \pm 0.0142$	$11.06 \pm 0.0055$	$11.11 \pm 0.0271$	$10.89 \pm 0.0231$
1237648720152625168	$0.02455 {\pm} 0.00001$	$-21.22 \pm 0.0030$	$0.5509 {\pm} 0.0041$	$2.096 \pm 0.0219$	$2.219 \pm 0.0199$	$0.4332 {\pm} 0.0102$	$0.5021 \pm 0.0132$	$60.19 \pm 0.3473$	$59.11 \pm 0.3164$	$11.51 \pm 0.0208$	$11.85 {\pm} 0.0940$	$11.53 {\pm} 0.0638$	$11.66 {\pm} 0.0208$	$11.60 {\pm} 0.0077$	$11.94{\pm}0.0345$	$11.62 \pm 0.0234$
1237650760240005233	$0.04583 {\pm} 0.00002$	$-21.32 \pm 0.0042$	$0.5275 {\pm} 0.0056$	$1.875 {\pm} 0.0228$	$1.942 {\pm} 0.0212$	$0.3591 {\pm} 0.0052$	$0.3762 {\pm} 0.0061$	$61.67 {\pm} 0.6592$	$59.59 {\pm} 0.5459$	$11.11 {\pm} 0.0517$	$10.94{\pm}0.0304$	$10.78 {\pm} 0.0426$	$11.26 {\pm} 0.0517$	$11.20{\pm}0.0191$	$11.02 {\pm} 0.0113$	$10.87 {\pm} 0.0158$
1237661358615035950	$0.00239 \pm 0.00002$	$-17.45 \pm 0.0350$	$0.5572 \pm 0.0495$	$2.561 \pm 0.0839$	$2.636 \pm 0.1070$	$0.8753 \pm 0.1377$	$1.009 \pm 0.2103$	$69.68 \pm 0.3021$	$69.31 \pm 0.3294$	$9.140 \pm 0.0797$	-	-	$9.272 \pm 0.0797$	$9.164 \pm 0.0317$	$9.219 \pm 0.0082$	-
1237674648852627562	$0.02076 \pm 0.00001$	$-20.66 \pm 0.0033$	$0.6051 \pm 0.0045$	$2.214 \pm 0.0167$	$2.309 \pm 0.0128$	$0.4986 \pm 0.011$	$0.5703 \pm 0.0103$	$51.83 \pm 0.3234$	$49.69 \pm 0.2642$	$10.71 \pm 0.0352$	$10.57 \pm 0.0083$	$10.43 \pm 0.0120$	$10.85 \pm 0.0352$	$10.89 \pm 0.0116$	$10.75 \pm 0.0028$	$10.62 \pm 0.0040$
1237657856071827493	0.00327±0.00001	-16.70±0.0220	0.5093±0.0312	2.398±0.2538	$2.488 \pm 0.1876$	0.6562±0.2752	0.7657±0.2564	83.28±1.405	84.58±1.600	$9.065 \pm 1.537$	-	-	$9.206 \pm 1.537$	9.036±0.6488	$9.648 \pm 0.0291$	-
1237671140406657069	$0.02839 \pm 0.00001$ $0.01752 \pm 0.00001$	-21.34±0.0025	$0.5328 \pm 0.0034$ $0.4228 \pm 0.0086$	$2.265 \pm 0.0301$ $2.146 \pm 0.1672$	2.237±0.0227 2.200±0.0628	0.5348±0.0228 0.4585±0.0801	$0.5144 \pm 0.0159$ 0.5704 $\pm 0.0527$	57.82±0.3197	58.58±0.3116	$11.03 \pm 0.0338$ 10.64 $\pm 0.2112$	$11.26 \pm 0.0088$ 10.04 $\pm 0.0227$	$11.25 \pm 0.0090$ 10.08 $\pm 0.0201$	$11.18 \pm 0.0338$ 10.70 $\pm 0.2112$	$11.14 \pm 0.0122$ 10.60±0.0002	$11.37 \pm 0.0032$ 0.000 $\pm 0.0144$	$11.35 \pm 0.0033$ 10.05 $\pm 0.0167$
1237650760778440199	0.01733±0.00001 0.01720+0.00001	-16.85±0.0069	0.4338±0.0080 0.1541+0.0181	2.140±0.1053 2.383+0.1047	2.309±0.0028 2.180±0.1602	0.4363±0.0691 0.6401±0.2020	0.3704±0.0537 0.4832±0.1022	90 80 47+2 961	90 80.08	10.04±0.2112 11.28±0.1826	8 576+0 3765	9.871±0.0406	10.79±0.2112 11.43±0.1896	11.26±0.0766	8.554±0.1578	9.848±0.0172
1201000100110449122	0.01120±0.00001	-10.00110	0.104170.0191	2.303±0.1347	2.100±0.1092	0.0401±0.2029	0.4004T0.1000	00.41 ± 2.001	00.00	**.20±0.1020	0.010T0.0100	0.01120.0400	AL:4010.1020	**.20±0.0700	0.004T0.1019	2.040T0.0119

**Table A1.** Virial masses of a subsample of 145 LTGs from Catinella et al. (2005) with photometric and/or spectroscopic information in the SDSS DR16.

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SDSS DR16	z	$M_g$	g - r	$R50/R90_g$	$R50/R90_r$	$n_g$	$n_r$	$i_g$	$i_r$	$M_{KS}$	$M_{KA}$	$M_{KB}$	$M_{nS}$	$M_{IS}$	$M_{IA}$	$M_{IB}$
1237650760241774845	$0.05816 \pm 0.00002$	$-20.53 \pm 0.0070$	$0.4246 \pm 0.0096$	$1.866 \pm 0.0565$	$2.066 \pm 0.0645$	$0.3571 \pm 0.0126$	$0.4197 \pm 0.0273$	$57.98 \pm 1.2501$	$57.80 \pm 1.145$	$9.673 \pm 1.392$	$10.51 \pm 0.0764$	$10.71 \pm 0.0854$	$9.827 \pm 1.392$	$9.783 \pm 0.5006$	$10.62 \pm 0.0276$	$10.82 \pm 0.0308$
1237650760241905743	$0.07072 \pm 0.00001$	$-21.67 \pm 0.0040$	$0.6604 \pm 0.0052$	$2.384 \pm 0.0543$	$2.500 \pm 0.0445$	$0.6408 \pm 0.0567$	$0.7816 {\pm} 0.0626$	$67.82 \pm 0.6083$	$67.67 \pm 0.5337$	$11.30 \pm 0.0340$	$11.08 \pm 0.0203$	$11.01 \pm 0.0212$	$11.44 \pm 0.0340$	$11.33 {\pm} 0.0134$	$11.11 \pm 0.0081$	$11.05 \pm 0.0084$
1237650760241905753	$0.00525 \pm 0.00001$	$-15.32 \pm 0.0125$	$0.4579 \pm 0.0179$	$2.148 \pm 0.0569$	$2.165 \pm 0.6043$	$0.4594 {\pm} 0.0308$	$0.4687 \pm 0.3437$	$83.70 \pm 1.944$	$81.25 \pm 1.779$	$9.550 \pm 0.4342$	-	-	$9.702 \pm 0.4342$	$9.524 {\pm} 0.1828$	$8.988 {\pm} 0.0320$	-
1237650760241971341	$0.02725 \pm 0.00001$	$-20.12\pm0.0039$	$0.9143 \pm 0.0051$	$2.893 \pm 0.1370$	$2.940 \pm 0.1295$	$1.699 \pm 0.4836$	$1.874 \pm 0.5064$	$74.28 \pm 0.6195$	$75.71 \pm 0.4783$	$10.82 \pm 0.0287$	$10.17 \pm 0.0570$	$10.11 \pm 0.0591$	$10.92 \pm 0.0287$	$10.82 \pm 0.0118$	$10.17 \pm 0.0234$	$10.11 \pm 0.0243$
1237650369407090853	$0.02666 \pm 0.00001$	-20.47±0.0036	$0.6164 \pm 0.0049$	$2.677 \pm 0.2517$	$2.739 \pm 0.2183$	$1.093 \pm 0.5445$	$1.240\pm0.5465$	75.61±0.4543	74.20±0.4063	$11.05 \pm 0.0265$	$10.77 \pm 0.0347$	$10.56 \pm 0.0392$	$11.17 \pm 0.0265$	$11.05 \pm 0.0109$	$10.75 \pm 0.0144$	$10.56 \pm 0.0161$
1237662195961686301	$0.00235 \pm 0.00001$	-17.46±0.0224	0.9756±0.0317	$2.770\pm0.1235$	$2.813 \pm 0.1260$	$1.319 \pm 0.3316$	$1.440\pm0.3729$	69.73±0.2837	70.08±0.2640	9.846±0.0207	-	-	9.959±0.0207	9.867±0.0083	9.790±0.0070	-
1237658491205582919	$0.03519 \pm 0.00001$	-19.89±0.0036	$0.2614 \pm 0.0051$	2.943±0.0662	2.961±0.1002	1.884±0.2603	1.960±0.4101	50.79±0.5725	54.07±0.5458	10.44±0.0978	10.08±0.0039	9.893±0.0076	10.53±0.0978	10.61±0.0329	10.25±0.0017	10.06±0.0028
1237653124470661181 1227664201001225047	$0.02142 \pm 0.00001$ $0.02266 \pm 0.00001$	-21.25±0.0029 20.74±0.0020	0.6397±0.0041	2.817±0.0180 2.885±0.4705	2.884±0.0170 2.700±0.2482	$1.451 \pm 0.0530$ 1.679 $\pm 1.622$	1.669±0.0589	26.20±0.2237 78.06±0.1994	29.16±0.2206 70.86±0.2226	$10.81 \pm 0.0141$ 11.25 $\pm 0.0162$	$10.57 \pm 0.0116$ 11.04 $\pm 0.062$	$10.50\pm0.0118$ 10.02 $\pm0.0524$	$10.91 \pm 0.0141$ 11.26 $\pm 0.0162$	$11.44 \pm 0.0028$ $11.22 \pm 0.0068$	$11.20\pm0.0023$ 11.02 $\pm0.0260$	$11.13 \pm 0.0024$ 10.01 $\pm 0.0210$
1237661960790992019	0.06495±0.00001	-20.43±0.0073	0.5669±0.0091	2.335±0.4705	2.199±0.3482 2.385±0.0757	0.5983+0.1132	0.6417+0.0791	79.60±1.1224	77 95+1 437	10.92+0.0684	11.01±0.0146	$10.95 \pm 0.0524$ $10.97 \pm 0.0153$	11.06±0.0684	10.90±0.0286	$10.99\pm0.0260$	10.91±0.0219
1237664289391116484	$0.05087 \pm 0.00001$	$-19.42\pm0.0010$	$0.3271\pm0.0153$	$2.041 \pm 0.1217$ $2.216 \pm 0.1163$	2.301±0.1195	$0.0900\pm0.1102$ $0.4996\pm0.0765$	$0.5632 \pm 0.0998$	90	90	10.0210.0004	$10.30 \pm 0.0389$	$10.25 \pm 0.0458$	-	10.90	$10.26\pm0.0000$	10.21±0.0198
1237664289391182057	$0.02569 \pm 0.00001$	$-18.66 \pm 0.0081$	$0.6199 \pm 0.0111$	$2.181 \pm 0.1209$	$2.316 \pm 0.0824$	$0.4778 \pm 0.0720$	$0.5757 \pm 0.0716$	90	90	$10.08 \pm 0.3785$	$10.41 \pm 0.0164$	$10.41 \pm 0.0190$	$10.23 \pm 0.3785$	$10.04 \pm 0.1620$	$10.37 \pm 0.0074$	$10.38 \pm 0.0085$
1237661433771261955	-	-	-	-	-	-	-	63	63	-	-	-	-	-	-	-
1237648702966988820	$0.01903 \pm 0.00001$	$-20.36 \pm 0.0040$	$0.6633 \pm 0.0055$	$2.397 \pm 0.0465$	$2.563 \pm 0.0589$	$0.6549 \pm 0.0503$	$0.8779 \pm 0.0970$	$57.11 \pm 0.3213$	$58.77 \pm 0.2956$	$10.46 \pm 0.0443$	$8.685 \pm 0.1248$	$10.21 \pm 0.0158$	$10.60 \pm 0.0443$	$10.57 \pm 0.0156$	$8.795 \pm 0.0449$	$10.32 \pm 0.0057$
1237665441511964722	$0.06461 \pm 0.00002$	$-21.28 \pm 0.0047$	$0.6358 {\pm} 0.0062$	$1.889 \pm 0.0933$	$1.988 \pm 0.3615$	$0.3622 \pm 0.0224$	$0.3906 \pm 0.1202$	$55.81 \pm 0.7264$	$56.79 \pm 0.5862$	$11.10 \pm 0.0492$	$11.12 \pm 0.0988$	$10.72 \pm 0.1129$	$11.26 \pm 0.0492$	$11.23 \pm 0.0174$	$11.25 \pm 0.0349$	$10.84 \pm 0.0399$
1237661149765107752	$0.01375 \pm 0.00001$	$-20.59 \pm 0.0034$	$0.7597 \pm 0.0048$	$2.297 \pm 0.0184$	$2.446 \pm 0.0424$	$0.5602 \pm 0.0152$	$0.7110 \pm 0.0521$	$63.95 \pm 0.2881$	$60.01 \pm 0.2838$	$10.86 \pm 0.0206$	$10.61 \pm 0.2320$	$10.19 {\pm} 0.1952$	$11.00 \pm 0.0206$	$10.93 \pm 0.0078$	$10.69 \pm 0.0870$	$10.26 \pm 0.0732$
1237661971186188446	$0.02387 \pm 0.00002$	$-19.09 \pm 0.0049$	$0.6643 \pm 0.0067$	$2.529 \pm 0.0695$	$2.581 \pm 0.0683$	$0.8249 \pm 0.1053$	$0.9080 \pm 0.1174$	$70.51 \pm 0.5996$	$70.39 \pm 0.5325$	$10.18 \pm 0.0595$	$10.17 \pm 0.0222$	$10.01 \pm 0.0274$	$10.31 \pm 0.0595$	$10.20 \pm 0.0238$	$10.19 \pm 0.0089$	$10.03 \pm 0.0110$
1237667255627087966	$0.05979 \pm 0.00001$	$-22.12\pm0.0030$	$0.7452 \pm 0.0040$	$2.367 \pm 0.0500$	$2.443 \pm 0.0431$	$0.6239 \pm 0.0499$	$0.7073 \pm 0.0524$	$52.71 \pm 0.4345$	$52.94 \pm 0.3619$	$11.55 \pm 0.0211$	$11.71 \pm 0.0989$	$11.59 \pm 0.0850$	$11.69 \pm 0.0211$	$11.71 \pm 0.0072$	$11.87 \pm 0.0335$	$11.76 \pm 0.0288$
1237661970112577674	$0.02538 \pm 0.00002$	-19.13±0.0053	0.7827±0.0069	$2.676 \pm 0.1554$ $2.208 \pm 0.0400$	$2.743 \pm 0.1172$	$1.092 \pm 0.3357$	$1.249 \pm 0.2958$	83.94±1.3636	83.20±0.8948	$10.62 \pm 0.0509$ 10.22 $\pm 0.0604$	$10.36 \pm 0.0290$	$10.25 \pm 0.0350$	$10.74 \pm 0.0509$ 10.47 ± 0.0604	$10.59 \pm 0.0215$ 10.20 ± 0.0262	$10.33 \pm 0.0123$ 10.52 ± 0.0020	$10.22\pm0.0148$ 10.42±0.0048
1237031733087091887	$0.04425 \pm 0.00001$ 0.01072 $\pm 0.00001$	-20.34±0.0042	$0.4482 \pm 0.0037$ 0.4212 $\pm 0.0000$	2.328±0.0400 2.514±0.1501	2.407±0.0452 2.805±0.6574	0.3800±0.0300	1.705±9.220	74.47±0.7391 80.47±0.0116	76.22±0.5817	10.52±0.0094	$10.31\pm0.0091$ 10.40±0.0227	$10.42 \pm 0.0115$ 10.21 $\pm 0.0400$	$10.47 \pm 0.0694$ 10.70 $\pm 0.0748$	$10.52 \pm 0.0283$ 10.57 $\pm 0.0211$	$10.32 \pm 0.0039$ 10.47 $\pm 0.0100$	10.43±0.0048
122767176478602050514	0.02278±0.00002	-13.00±0.0071 20.10±0.0046	0.4213±0.0055	$1.874\pm0.0177$	1.051±0.0374	0.2588±0.0041	0.2788±0.0056	49.28±0.5429	42 20±0 4604	10.42±0.1542	10.45±0.0237	0.872±0.0026	10.58±0.1549	$10.37 \pm 0.0311$ 10.72 $\pm 0.0441$	10.47±0.0100	10.18±0.0268
1237671764249477365	0.08212±0.00001	$-22.34\pm0.0040$	$0.5488\pm0.0055$	$2.281\pm0.0780$	$2.475\pm0.0409$	$0.5385 \pm 0.0041$ $0.5465 \pm 0.0616$	$0.3785 \pm 0.0030$ 0.7485 $\pm 0.0541$	$70.86\pm0.6026$	$72.44\pm0.5587$	$10.43\pm0.1342$ 11.50±0.0371	$11.24\pm0.0339$	11 12±0.0350	$11.64\pm0.0371$	$11.51\pm0.0441$	$11.25\pm0.0137$	$10.13\pm0.0203$ 11 13 $\pm0.0141$
1237648720698867721	$0.00542 \pm 0.00001$	$-18.36 \pm 0.0119$	$0.4469 \pm 0.0160$	$2.018 \pm 0.0172$	$2.120 \pm 0.0247$	$0.4009 \pm 0.0063$	$0.4445 \pm 0.0123$	$58.35 \pm 0.5960$	$58.23 \pm 0.2713$	$9.535 \pm 0.1445$		-	$9.688 \pm 0.1445$	$9.642 \pm 0.0522$	$9.360 \pm 0.0156$	
1237671763175473314	$0.02343 \pm 0.00002$	$-19.48 \pm 0.0053$	$0.6269 \pm 0.0073$	$2.439 \pm 0.1197$	$2.495 \pm 0.0992$	$0.7024 \pm 0.1441$	$0.7745 \pm 0.1377$	90	90	$10.36 \pm 0.1247$	$10.21 \pm 0.0283$	$10.17 \pm 0.0353$	$10.50 \pm 0.1247$	$10.33 \pm 0.0531$	$10.17 \pm 0.0121$	$10.13 \pm 0.0151$
1237664289932640543	$0.04725 \pm 0.00002$	$-18.97 \pm 0.0124$	$0.4851 \pm 0.0166$	$2.638 \pm 0.5595$	$2.519 \pm 0.2228$	$1.014 \pm 1.105$	$0.8097 \pm 0.3290$	82.64	83.12	$10.23 \pm 0.3040$	$10.56 \pm 0.0640$	$10.34 \pm 0.0831$	$10.36 \pm 0.3040$	$10.20 \pm 0.1281$	$10.54 \pm 0.0272$	$10.32 \pm 0.0352$
1237648702972625038	$0.02443 \pm 0.00002$	$-19.65 \pm 0.0054$	$0.7171 \pm 0.0073$	$2.212 \pm 0.0532$	$2.270 \pm 0.0395$	$0.4972 \pm 0.0346$	$0.5381 {\pm} 0.0302$	$59.57 \pm 0.8752$	$58.02 \pm 0.7076$	$10.45 \pm 0.0677$	$10.39 \pm 0.0536$	$9.995 \pm 0.0825$	$10.60 \pm 0.0677$	$10.55 {\pm} 0.0246$	$10.49 {\pm} 0.0195$	$10.10 \pm 0.0300$
1237650761862086739	$0.01342 \pm 0.00001$	$-17.81 \pm 0.0052$	$0.3517 \pm 0.0074$	$2.017 \pm 0.0436$	$2.325 \pm 0.1101$	$0.4006 \pm 0.0159$	$0.5839 {\pm} 0.0982$	$70.90 \pm 0.8044$	$68.82 \pm 0.8068$	$9.581 \pm 0.2929$	$8.968 \pm 0.0826$	$9.539 {\pm} 0.0415$	$9.731 \pm 0.2929$	$9.602 {\pm} 0.1168$	$8.989 {\pm} 0.0330$	$9.560 \pm 0.0166$
1237650761862086708	-	-	-	-	-	0.00	2.00	65	65	-	-	-	-	-	-	-
1237671992947703853	$0.02272 \pm 0.00001$	$-21.74 \pm 0.0027$	$0.7974 \pm 0.0038$	$2.166 \pm 0.5378$	$2.236 \pm 0.3851$	$0.4692 \pm 0.3066$	$0.5136 \pm 0.2685$	$60.64 \pm 0.3767$	$61.13 \pm 0.3292$	$11.55 \pm 0.0169$	$11.51 \pm 0.0603$	$11.44 \pm 0.0511$	$11.70 \pm 0.0169$	$11.63 \pm 0.0063$	$11.59 \pm 0.0224$	$11.53 \pm 0.0190$
1237655499737661514	$0.01435 \pm 0.00001$	-20.79±0.0030	$0.7145 \pm 0.0042$	$2.561 \pm 0.0404$	$2.672 \pm 0.0440$	$0.8754 \pm 0.0662$	$1.084 \pm 0.0943$	63.71±0.3088	63.14±0.2797	$10.45 \pm 0.0217$	$10.71 \pm 0.0224$	$10.38 \pm 0.0251$	$10.58 \pm 0.0217$	$10.51 \pm 0.0083$	$10.77 \pm 0.0085$	$10.45 \pm 0.0095$
1237655499737727088	$0.01328 \pm 0.00001$	$-20.77 \pm 0.0031$	$0.6695 \pm 0.0044$	$2.060 \pm 0.0622$	$2.158 \pm 0.0682$	$0.4173 \pm 0.0259$	$0.4649 \pm 0.0308$	$50.35 \pm 0.2961$	47.05±0.2742	10.88±0.0188	8.780±0.3832	$10.99 \pm 0.0236$	$11.04 \pm 0.0188$	$11.10 \pm 0.0060$	$8.994 \pm 0.1223$	$11.20 \pm 0.0076$
12376622529524531258	- 0.02225+0.00001	10 22±0 0047	-	- 2 242±0 0252	2 272±0.0820	0 5182±0 0251	-	57 80 52±1 002	57 91 62±0 0069	10 20+0 0727	10.20±0.0122	-	10 54±0 0727	- 10 27±0 0200	10.18±0.0052	-
1237667783917174819	$0.02525\pm0.00001$ $0.02661\pm0.00001$	-18 53±0.0047	$0.0113\pm0.0002$ 0.4667 $\pm0.0077$	2.585+0.2109	2.608±0.2781	0.9147+0.3819	$0.0237 \pm 0.0340$ 0.9570 $\pm 0.5114$	77 41+1 284	76 68+1 210	9 849+0 2674	9.917+0.0183	9.934+0.0221	9.980±0.2674	9.837±0.0309	9.906±0.0078	9.922+0.0093
1237664291011887113	$0.02334\pm0.00001$	$-21.40\pm0.0030$	$0.7781 \pm 0.0041$	2.791±0.1435	$2.919\pm0.1397$	$1.376\pm0.4041$	$1.795\pm0.5220$	68.32±0.2687	68 12±0 2739	$11.38\pm0.0161$	$11.23\pm0.0315$	$11.23\pm0.0278$	$11.49\pm0.0161$	11 42+0 0064	$11.26\pm0.0013$	$11.26\pm0.0000000000000000000000000000000000$
1237662225686003729	$0.01893 \pm 0.00001$	$-19.21 \pm 0.0036$	$0.6809 \pm 0.0049$	$3.097 \pm 0.2674$	$3.156 \pm 0.2571$	$2.599 \pm 1.449$	$2.943 \pm 1.572$	$64.69 \pm 0.4104$	$66.27 \pm 0.3846$	$10.24 \pm 0.0257$	$10.24 \pm 0.0081$	$10.16 \pm 0.0095$	$10.30 \pm 0.0259$	$10.29 \pm 0.0100$	$10.29 \pm 0.0032$	$10.21 \pm 0.0037$
1237667783918026937	$0.02774 \pm 0.00001$	$-20.92 \pm 0.0037$	$0.8519 \pm 0.0049$	$2.469 \pm 0.0355$	$2.619 \pm 0.0631$	$0.7399 \pm 0.0461$	$0.9778 \pm 0.1192$	$63.87 \pm 0.3889$	$59.69 \pm 0.3299$	$11.47 \pm 0.0229$	$11.12 \pm 0.0599$	$11.03 \pm 0.0560$	$11.61 \pm 0.0229$	$11.54 \pm 0.0086$	$11.19 \pm 0.0224$	$11.11 \pm 0.0210$
1237654881271152801	$0.00458 \pm 0.00002$	$-18.48 \pm 0.0169$	$0.3798 \pm 0.0239$	$2.439 \pm 0.0505$	$2.379 \pm 0.0107$	$0.7019 \pm 0.0608$	$0.6361 \pm 0.0110$	$81.83 \pm 1.064$	$73.08 \pm 0.3259$	$9.772 \pm 0.1239$	-	-	$9.915 \pm 0.1239$	$9.761 \pm 0.0513$	$9.961 \pm 0.0207$	-
1237655495981990086	$0.02454 \pm 0.00001$	$-20.76 \pm 0.0033$	$0.4636 \pm 0.0045$	$2.194 \pm 0.0403$	$2.079 \pm 0.0234$	$0.4860 \pm 0.0249$	$0.4254 \pm 0.0103$	$54.62 \pm 0.4411$	$54.59 \pm 0.4036$	$10.43 \pm 0.1114$	$10.75 \pm 0.0094$	$10.64 \pm 0.0115$	$10.58 \pm 0.1114$	$10.57 \pm 0.0386$	$10.90 \pm 0.0033$	$10.78 \pm 0.0040$
1237662237477241008	$0.01371 \pm 0.00002$	$-19.32 \pm 0.0062$	$0.6673 \pm 0.0087$	$2.480 \pm 0.1155$	$2.692 \pm 0.1946$	$0.7550 \pm 0.1547$	$1.129 \pm 0.4372$	$78.04 \pm 0.5915$	$78.02 \pm 0.4662$	$10.18 \pm 0.0817$	$9.553 \pm 0.0574$	$10.03 \pm 0.0264$	$10.31 \pm 0.0817$	$10.17 \pm 0.0339$	$9.539 \pm 0.0239$	$10.01 \pm 0.0110$
1237662263240949953	$0.01533 \pm 0.000004$	$-18.31 \pm 0.0044$	$0.2969 \pm 0.0063$	$2.525 \pm 0.1283$	$2.587 \pm 0.1073$	$0.8183 \pm 0.1922$	$0.9193 \pm 0.1875$	90	90	-	$12.25 \pm 0.1240$	$9.586 \pm 0.0268$	-	10.17	$12.21 \pm 0.0529$	$9.550 \pm 0.0115$
1237674601605103640	$0.02473 \pm 0.00001$	-20.99±0.0029	$0.5432 \pm 0.0040$	$1.991 \pm 0.0199$	$2.101 \pm 0.0214$	0.3913±0.0067	$0.4355 \pm 0.1006$	$48.66 \pm 0.3629$	50.41±0.3331	$10.92 \pm 0.0489$	$10.70 \pm 0.0063$	10.67±0.0080	$11.07 \pm 0.0489$	$11.12 \pm 0.0158$	$10.90 \pm 0.0022$	10.87±0.0027
1237662224077815972	$0.04270 \pm 0.00001$ $0.00552 \pm 0.00001$	$-21.38 \pm 0.0031$ 18.08 $\pm 0.0101$	$0.5834 \pm 0.0042$ $0.2785 \pm 0.0142$	$2.232 \pm 0.0332$ 2.407 $\pm 0.1011$	2.380±0.0372 2.222±0.2775	$0.5109 \pm 0.0229$ 0.6657 $\pm 0.2110$	$0.6371 \pm 0.0384$ 0.5100 $\pm 0.1014$	$69.11 \pm 0.4350$ $49.72 \pm 0.5487$	70.21±0.3892 42.05±0.4785	0.882±0.1487	$10.70 \pm 0.0723$	$10.49 \pm 0.0780$	$11.25 \pm 0.0299$ 10.02 $\pm 0.1487$	$11.12\pm0.0119$ 10.18±0.0420	$10.72 \pm 0.0288$ 10.14 $\pm 0.0040$	$10.52 \pm 0.0311$
1237643764034230020	0.00000210.00001	-13.33±0.0101	0.5926±0.0047	2.407±0.1311	2.202±0.2110	0.5842±0.0224	0.3109±0.1914	50.60±0.2824	42.93±0.4785	10.65±0.0220	10 70±0 0505	10.20±0.0750	10.70±0.0220	10.74±0.0122	10.14±0.0045	10 20+0 0270
1237662224615342283	0.02889±0.00001	-19 21+0 0049	0.3347±0.0076	2.432+0.0528	2.508±0.0817	0.6942±0.0624	$0.7046\pm0.1125$	78 20±0 8934	78 03±0 8639	9.952+0.2726	8 793±0 1865	10.10±0.0346	10.09±0.2726	9.938+0.1133	8 779±0 0775	10.09±0.0144
1237674655289966817	$0.05394 \pm 0.00002$	$-21.33 \pm 0.0040$	$0.6596 \pm 0.0052$	$2.162 \pm 0.0462$	$2.156 \pm 0.0307$	$0.4671 \pm 0.0260$	$0.4639 \pm 0.0170$	$64.61 \pm 0.5852$	$65.45 \pm 0.5084$	$11.00 \pm 0.0464$	$10.86 \pm 0.0320$	$10.75 \pm 0.0324$	$11.15 \pm 0.0464$	$11.05 \pm 0.0179$	$10.91 \pm 0.0124$	$10.80 \pm 0.0125$
1237655498670211218	$0.02380 \pm 0.00001$	$-21.30 \pm 0.0031$	$0.6246 \pm 0.0042$	$1.939 \pm 0.0125$	$1.958 \pm 0.0105$	$0.3755 \pm 0.0036$	$0.3809 \pm 0.0032$	$47.36 \pm 0.3902$	$47.79 \pm 0.3384$	$11.14 \pm 0.0257$	$11.06 \pm 0.0751$	$10.86 \pm 0.0690$	$11.29 \pm 0.0257$	$11.37 \pm 0.0081$	$11.29 \pm 0.0235$	$11.09 \pm 0.0216$
1237648704056328322	$0.00576 {\pm} 0.00001$	$-19.31 \pm 0.0145$	$1.082 \pm 0.0171$	$3.019 \pm 0.1780$	$3.179 {\pm} 0.2093$	$2.214 \pm 0.8235$	$3.086 \pm 1.339$	$59.86 \pm 1.717$	$71.52 {\pm} 0.2694$	$10.52 {\pm} 0.0153$	-	-	$10.58 {\pm} 0.0153$	$10.57 {\pm} 0.0067$	$10.25 \pm 0.0049$	-
1237654881276395557	$0.00548 {\pm} 0.00001$	$-18.35 {\pm} 0.0116$	$0.7032 {\pm} 0.0164$	$2.049 {\pm} 0.1103$	$2.129 {\pm} 0.0998$	$0.4131 {\pm} 0.0444$	$0.4495 {\pm} 0.0511$	$72.58 {\pm} 0.4457$	$72.57 {\pm} 0.3983$	$10.09 {\pm} 0.0430$	-	-	$10.25 {\pm} 0.0430$	$10.10{\pm}0.0174$	$9.988 {\pm} 0.0048$	-
1237648704056918077	$0.00554 \pm 0.00001$	$-19.54 \pm 0.0050$	$0.7909 \pm 0.0071$	$2.082 \pm 0.0139$	$2.177 \pm 0.0123$	$0.4271 \pm 0.0062$	$0.4756 \pm 0.0073$	$48.51 \pm 0.2785$	$47.46 \pm 0.2612$	$10.40 {\pm} 0.0164$	-	-	$10.55 \pm 0.0164$	$10.62 \pm 0.0052$	$10.82 \pm 0.0080$	-
1237662305118650412	$0.02942 \pm 0.00001$	$-21.54 \pm 0.0027$	$0.9078 \pm 0.0036$	$3.770 \pm 77.59$	$3.745 \pm 77.90$	-	-	$77.63 \pm 0.1778$	$75.29 \pm 0.3122$	$11.42 \pm 0.0153$	$11.57 \pm 0.0840$	$11.52 \pm 0.0695$	$11.13 \pm 0.0153$	$11.42 \pm 0.0064$	$11.56 \pm 0.0347$	$11.51 \pm 0.0287$
1237667781239636022	0.03746±0.00001	-21.94±0.0023	0.7166±0.0032	$3.028 \pm 0.2211$	$3.178 \pm 0.2155$	2.255±1,041	3.079±1.376	67.19±0.2664	68.15±0.2879	$11.45 \pm 0.0124$	$11.62 \pm 0.0912$	$11.45 \pm 0.0714$	$11.50 \pm 0.0124$	11.48±0.0049	$11.65 \pm 0.0358$	$11.49 \pm 0.0280$
1237008272980754643	0.04618±0.00001	-18.01±0.0136	0.5579±0.0179	2.384±0.1645	2.313±0.1536	0.6408±0.1716	0.8035±0.2245	88.37	84.41	10.96±0.1383	$9.036 \pm 0.2834$	$10.20 \pm 0.0626$	11.10±0.1383	10.93±0.0587	9.024±0.1201	10.17±0.0268
1237651736313528355	$0.00449 \pm 0.00001$ $0.01721 \pm 0.00001$	-19.17±0.0068	0.8389±0.00955 0.2216±0.0068	$2.395 \pm 0.0430$ $2.417 \pm 0.1768$	2.485±0.0580 2.580±0.2508	0.6527±0.0463	$0.7615 \pm 0.0787$ 0.0224 \pm 0.4550	59.23±0.3147	59.17±0.3066	$10.35 \pm 0.0166$ 0.722 \pm 0.0070	e e20±0 1720	-	$10.49 \pm 0.0166$ 0.860 $\pm 0.0070$	10.45±0.0061 0.688±0.4282	10.53±0.0140 8.786±0.0747	10.06±0.0167
1227655602491096626	0.00021±0.00001	-18.04±0.0048	0.5210±0.0008	2.417±0.1108	2.565±0.2556	0.6215±0.2009	0.0144±0.4046	55 15±0 2701	50 20±0 2208	10.00±0.0812	0.030±0.1735	10.10±0.0388	10 14±0 0812	10 12±0 0200	0.922±0.0099	10.0010101
1237655550742298700	$0.03065 \pm 0.00001$	$-21.51 \pm 0.0027$	$0.7833 \pm 0.0036$	$2.903 \pm 0.1762$	$3.065 \pm 0.1529$	$1.734 \pm 0.6356$	$2.434 \pm 0.7770$	$64.43 \pm 0.4319$	$64.49 \pm 0.3343$	$11.53 \pm 0.0118$	-	-	$11.62 \pm 0.0118$	$11.59 \pm 0.0046$	$11.33 \pm 0.0182$	-
1237662302453039177	$0.03107 \pm 0.00001$	$-21.40\pm0.0029$	$0.6500 \pm 0.0039$	$2.938\pm0.4964$	$3.141\pm0.4087$	$1.866 \pm 1.932$	2 850+2 422	$74.82\pm0.4532$	73 73±0 3613	$11.35 \pm 0.0176$	$10.75 \pm 0.0734$	$10.62 \pm 0.0765$	$11.42 \pm 0.0176$	$11.35 \pm 0.0072$	$10.75 \pm 0.0300$	$10.62 \pm 0.0313$
1237654954281468455	$0.02745 \pm 0.00002$	$-20.90 \pm 0.0038$	$0.7251 \pm 0.0052$	$2.151 \pm 0.0307$	$2.314 \pm 0.0265$	$0.4608 \pm 0.0167$	$0.5742 \pm 0.0229$	$64.56 \pm 0.4135$	$66.58 \pm 0.3806$	$10.93 \pm 0.0473$	$10.77 \pm 0.0264$	$10.61 \pm 0.0310$	$11.08 \pm 0.0473$	$10.98 \pm 0.0183$	$10.81 \pm 0.0102$	$10.65 \pm 0.0120$
1237652598487646631	$0.02009 \pm 0.00001$	$-19.87 \pm 0.0044$	$0.8528 \pm 0.0057$	$2.898 \pm 0.3517$	$2.931 \pm 0.2473$	$1.719 \pm 1.257$	$1.840 {\pm} 0.9486$	$80.25 \pm 0.7415$	$86.53 \pm 1.107$	$10.91 \pm 0.0307$	$10.62 \pm 0.0303$	$10.11 \pm 0.0609$	$11.01 \pm 0.0307$	$10.89 {\pm} 0.0130$	$10.60 \pm 0.0128$	$10.08 \pm 0.0257$
1237656567038935144	$0.01263 {\pm} 0.00001$	$-19.95 {\pm} 0.0046$	$0.7910 {\pm} 0.0064$	$2.174 {\pm} 0.3360$	$2.353 {\pm} 0.1881$	$0.4739 {\pm} 0.1962$	$0.6101{\pm}0.1809$	$53.13 {\pm} 0.3387$	$53.74 {\pm} 0.2710$	$10.58 {\pm} 0.0239$	$8.496 {\pm} 0.8907$	$10.42 {\pm} 0.0627$	$10.73 {\pm} 0.0239$	$10.74 {\pm} 0.0082$	$8.653 {\pm} 0.3038$	$10.58 {\pm} 0.0214$
1237652944768008329	$0.01672 {\pm} 0.00001$	$-19.92 \pm 0.0035$	$0.6668 {\pm} 0.0048$	$2.664 \pm 0.0298$	$2.713 {\pm} 0.0235$	$1.066 \pm 0.0626$	$1.175 {\pm} 0.0552$	$57.05 \pm 0.3627$	$53.50 {\pm} 0.3082$	$10.51 {\pm} 0.0263$	$8.438 {\pm} 0.0008$	$10.47 {\pm} 0.0104$	$10.64 {\pm} 0.0263$	$10.65 {\pm} 0.0092$	$8.574 {\pm} 0.0008$	$10.61 {\pm} 0.0037$
1237663457240089137	$0.02044 \pm 0.00001$	$-20.13 \pm 0.0042$	$0.4531 {\pm} 0.0059$	$2.290 \pm 0.03078$	$2.254 \pm 0.0231$	$0.5544 \pm 0.0250$	$0.5262 \pm 0.0170$	$60.29 \pm 0.3979$	$59.92 \pm 0.3734$	$10.15 \pm 0.0794$	$10.14 {\pm} 0.0160$	$10.11 {\pm} 0.0191$	$10.29 \pm 0.0794$	$10.24 \pm 0.0292$	$10.23 \pm 0.0059$	$10.20 \pm 0.0071$
1237663456703545733	$0.01929 \pm 0.00001$	$-20.73 \pm 0.0035$	$0.7256 \pm 0.0048$	$1.959 \pm 0.2705$	$2.072 \pm 0.2610$	$0.3814 \pm 0.0821$	$0.4225 \pm 0.1127$	$53.36 \pm 0.3495$	$55.40 \pm 0.3161$	$10.80 \pm 0.0269$	$10.74 \pm 0.0660$	$10.24 \pm 0.0950$	$10.95 \pm 0.0269$	$10.95 \pm 0.0093$	$10.88 \pm 0.0228$	$10.39 \pm 0.0328$
1237666210347614532	$0.05536 \pm 0.00001$	$-20.13 \pm 0.0061$	$0.5283 \pm 0.0081$	$2.477 \pm 0.1513$	$2.569 \pm 0.1622$	$0.7501 \pm 0.2007$	$0.8889 \pm 0.2714$	87.43	55	$10.96 \pm 0.0604$	$11.32 \pm 0.0060$	$11.29 \pm 0.0058$	$11.10 \pm 0.0604$	$10.93 \pm 0.0257$	$11.29 \pm .0030$	$11.26 \pm 0.0030$
1237666210347745660	$0.01756 \pm 0.00002$	-19.76±0.0059	$0.4868 \pm 0.0081$	$2.242 \pm 0.0344$	$2.300 \pm 0.0368$	$0.51793 \pm 0.0244$	0.5627±0.0307	71.25±0.5229	$71.30 \pm 0.4510$	$10.15 \pm 0.1237$	8.825±0.2138	$9.884 \pm 0.0560$	$10.30 \pm 0.1237$	$10.17 \pm 0.0498$	8.839±0.0860	9.898±0.0225
1237003343130837809	0.01616±0.00001	-21.20±0.0024	0.8060±0.0034	3.360±0.1321	3.304±0.1188	4.4/4±1.1978	3.995±0.9695	49.48±0.2253	48.93±0.2189	10.85±0.0115	10.36±0.0264	10.53±0.0257	10.83±0.0115	11.06±0.0037	10.77±0.0085	10.73±0.0083
1237003784191324949 1237672815077406655	0.02489±0.000001	- 20.85±0.0070	0.4296±0.0103	1.980±0.1884	2.055±0.3359	0.3660±0.0611	0.4064±0.1284	00.20±0.6040 81	01.38±0.3911 81	10.45±0.0991	10.38±0.0161	10.32±0.0199	10.38±0.0991	10.51±0.0368	10.40±0.0060	10.40±0.0075
1237669518514913516	-	-	-	-	-	-	-	60	60	-	-	-	-	-	-	-

Table A2. Dynamical masses of a subsample of 145 LTGs from	n
Catinella et al. (2005) with photometric and/or spectroscopic in	-
formation in the SDSS DR16.	

8					
AGC Name	Other Name	SDSS DR16 Name	$\alpha$	δ	$M_{Dyn}$
			J2000	J2000	$10^{11} \dot{\mathbf{M}_{solar}}$
144	450.044	1997059059447190545	00 15 00 0	10 14 05	0 61   0 17
144	456-044	1237053053447180545	$00\ 15\ 26.8$	10 14 05	$0.61 \pm 0.17$
400814	- N917	1237052029038873182	00 31 30.7	-10 15 08	$3.05 \pm 0.51$
400343	IN 21 (	1237652947456360495	00 41 33.7	-10 01 18	$0.31 \pm 1.00$
400373	M-203006	1237652947993624616	00 45 08.8	-09 37 53	$0.46 \pm 0.15$
400846	M-203014	1237652900753244294	00 47 25.2	-09 51 10	$0.27 \pm 0.07$
400390	M-203015	1237652900753244175	00 47 46.2	-09 50 05	$2.46 \pm 0.48$
400387	UA14	1237652900753244328	00 47 46.5	-09 53 54	$0.06 \pm 0.02$
400848	-	1237652947993952343	00 47 51.9	-09 38 46	$0.23 \pm 0.05$
410518	384-064	1237663782593822774	01 04 15.0	-01 06 51	$0.58 \pm 0.23$
410526	-	1237666338115027075	01 04 41.5	$00\ 57\ 24$	$0.29 \pm 0.05$
410530	-	1237663783130759334	01 04 51.7	$00 \ 38 \ 52$	$0.19 \pm 0.07$
410531	-	1237666338115092762	$01 \ 04 \ 58.0$	$00 \ 50 \ 59$	$2.34 \pm 0.69$
410534	-	1237663783130824820	$01 \ 05 \ 26.2$	$00 \ 48 \ 07$	$1.85 \pm 0.49$
410541	M + 004027	1237666338652618892	$01 \ 11 \ 15.8$	$00 \ 27 \ 21$	$0.15 \pm 0.04$
410770	A168-33	1237663784205680908	$01 \ 15 \ 51.2$	$00 \ 08 \ 48$	$1.84{\pm}0.70$
866	385-072	1237666339190472839	$01 \ 20 \ 06.6$	$00 \ 12 \ 20$	$0.08 {\pm} 0.03$
894	I1681	1237663784206270641	$01 \ 21 \ 21.2$	$00 \ 05 \ 24$	$0.10 {\pm} 0.03$
915	N497	1237666338116993064	$01 \ 22 \ 23.8$	$00 \ 52 \ 32$	$16.18 {\pm} 2.68$
931	385-094	1237663783132790881	$01 \ 23 \ 14.5$	$00 \ 42 \ 04$	$0.03 {\pm} 0.01$
410148	385-093	1237657189840584856	$01 \ 23 \ 17.0$	$00 \ 54 \ 22$	$0.70 {\pm} 0.17$
1116	386-007	1237663782597034125	$01 \ 33 \ 34.5$	$-01 \ 05 \ 27$	$0.39 {\pm} 0.12$
1120	386-010	1237663782597099527	$01 \ 34 \ 02.4$	-01 04 33	$1.21 \pm 0.23$
1123	386-011	1237657069546831898	$01 \ 34 \ 08.0$	$-01 \ 01 \ 58$	$1.16 {\pm} 0.26$
410955	-	1237678880495894618	01  50  54.7	-02 22 23	$0.91 {\pm} 0.31$
1428	I1755	1237653652921057594	$01 \ 57 \ 09.8$	$14 \ 32 \ 59$	$2.43 {\pm} 0.74$
410408	N747	1237652900223909957	$01 \ 57 \ 30.2$	$-09 \ 27 \ 45$	$0.79 {\pm} 0.16$
1901	N926	1237663783676477669	$02 \ 26 \ 06.6$	$00 \ 19 \ 55$	$6.52 \pm 1.57$
420405	-	1237657070628503722	$02 \ 47 \ 00.2$	00 09 20	$2.77 {\pm} 0.91$
420434	-	1237657584951034038	$02 \ 48 \ 34.2$	00 59 33	$0.88 {\pm} 0.17$
2291	I1856	1237663783142096968	$02 \ 48 \ 50.7$	$00 \ 46 \ 02$	$2.56 {\pm} 0.72$
420384	389-026	1237663783142228130	$02 \ 49 \ 35.2$	$00 \ 43 \ 25$	$0.52 {\pm} 0.15$
420428	-	1237663783142228165	$02 \ 49 \ 49.2$	$00 \ 47 \ 35$	$2.56 {\pm} 0.83$
2319	389-029	1237657584951230617	$02 \ 49 \ 53.5$	-01 00 13	$2.54{\pm}0.42$
420308	N1148	1237652900767268885	02 57 04.0	$-07 \ 41 \ 08$	$0.75 {\pm} 0.15$
2479	M + 008065	1237663784217149628	$03 \ 00 \ 40.2$	00 01 13	$0.47 \pm 0.15$
2628	390-041	1237666300018229273	03 16 31.7	00 28 07	$2.09\pm0.33$
430240	N1324	1237649964066406405	$03\ 25\ 01.6$	-05 44 42	$11.32 \pm 1.74$
3917	N2410	1237653588477411643	07 35 02.4	32 49 20	$6.87 \pm 1.09$
4257	118-069	1237660764834103400	08 10 11 1	24 53 32	$0.91 \pm 0.25$
4308	119-029	1237664837535858925	08 17 25 8	$21 \ 00 \ 02$ $21 \ 41 \ 07$	$0.84 \pm 0.23$
180814	-	1237667782809223472	08 18 24 8	11 37 08	$0.19 \pm 0.24$
180815	-	1937667789800993509	08 18 24.0	11 27 59	$1.82\pm0.07$
100010	-	1201001102003220002	00 10 21.1	11 01 02	1.0210.00

AGC Name	Other Name	SDSS DR16 Name	$\alpha$ J2000	$\delta$ J2000	${f M_{Dyn}}\ 10^{11} {f M_{solar}}$
180869	_	1237661086957568117	08 27 13.3	25 58 01	$3.80 {\pm} 0.91$
4501	N2620	1237664092898852896	$08 \ 37 \ 28.2$	24 56 47	$11.74 \pm 1.93$
4691	N2713	1237654601019686930	08  57  20.6	$02 \ 55 \ 14$	$19.48 {\pm} 3.57$
4698	150-053	1237664093438214204	08  58  32.5	$28 \ 15 \ 59$	$11.81 \pm 2.00$
4823	N2777	1237660412649865229	$09 \ 10 \ 41.7$	$07 \ 12 \ 23$	$0.14 {\pm} 0.05$
190864	-	1237671260664168763	$09\ 15\ 28.2$	11  50  05	$0.15 {\pm} 0.05$
4915	006-026	1237648720676061404	$09\ 17\ 29.0$	$00 \ 37 \ 14$	$0.95 {\pm} 0.25$
4923	I531	1237650795680235542	$09\ 17\ 50.5$	$00 \ 16 \ 44$	$1.22 \pm 0.30$
190809	-	1237660763768029308	$09 \ 18 \ 33.4$	$34 \ 20 \ 42$	$1.67 {\pm} 0.64$
490302	-	1237648720676585591	$09 \ 22 \ 09.6$	$00 \ 32 \ 22$	$05.02 \pm 1.33$
490303	-	1237648720676585778	$09 \ 22 \ 22.6$	$00 \ 29 \ 18$	$5.26 \pm 1.22$
5010	N2862	1237665097926115359	$09 \ 24 \ 55.2$	$26 \ 46 \ 29$	$5.14 \pm 1.25$
5064	I540	1237658493336879239	09 30 10.1	$07 \ 54 \ 07$	$0.22 {\pm} 0.07$
190788	092-049	1237668289080000630	$09 \ 46 \ 30.7$	15  53  09	$0.33 {\pm} 0.08$
5250	N2998	1237658205573808201	$09 \ 48 \ 43.5$	$44 \ 04 \ 50$	$3.46 {\pm} 0.81$
190867	-	1237671122692210971	$09 \ 49 \ 53.4$	12 54 35	$3.53 {\pm} 1.27$
191921	-	1237668289080983802	09  56  06.9	$16\ 17\ 22$	$0.32 {\pm} 0.09$
5341	123-008	1237667541753331904	09  56  35.9	$20 \ 38 \ 41$	$14.9 \pm 2.19$
5472	I594	1237651800161321169	$10 \ 08 \ 32.0$	$00 \ 40 \ 02$	$1.32 {\pm} 0.23$
201117	-	1237667292659384635	$10\ 21\ 34.5$	$23 \ 57 \ 34$	$0.51 {\pm} 0.12$
5813	184-004	1237664667363246202	$10 \ 41 \ 08.8$	$36 \ 22 \ 20$	$9.19 {\pm} 1.59$
201196	-	1237667323784527982	$10 \ 44 \ 05.6$	$26 \ 03 \ 41$	$0.27 {\pm} 0.09$
5985	I653	1237648720686415913	$10 \ 52 \ 06.8$	$00 \ 33 \ 39$	$2.85 {\pm} 0.53$
6340	011-059	1237648720152625168	$11 \ 19 \ 55.2$	$00 \ 52 \ 45$	$6.30{\pm}1.28$
510263	012-002	1237650760240005233	$11 \ 31 \ 38.0$	-03 38 51	$3.23 \pm 0.73$
6595	N3769	1237661358615035950	$11 \ 37 \ 44.0$	47 53 34	$0.15 {\pm} 0.04$
6608	012-046	1237674648852627562	$11 \ 38 \ 33.2$	-01 11 04	$1.91 {\pm} 0.36$
6667	268-071	1237657856071827493	$11 \ 42 \ 25.2$	$51 \ 35 \ 50$	$0.08 {\pm} 0.02$
6720	I728	1237671140406657069	$11 \ 44 \ 50.4$	$-01 \ 36 \ 05$	$2.10 \pm 0.34$
510217	012-079	1237650760778448980	$11 \ 46 \ 16.8$	$-03 \ 10 \ 50$	$0.64 {\pm} 0.15$
510383	-	1237650760778449122	$11 \ 46 \ 33.2$	$-03 \ 08 \ 25$	$0.08 {\pm} 0.03$
510381	-	1237650760241774845	$11 \ 48 \ 01.7$	-03 42 25	$1.01 {\pm} 0.21$
510373	-	1237650760241905743	$11 \ 49 \ 09.6$	-03 37 08	$2.44{\pm}0.53$
510377	-	1237650760241905753	$11 \ 49 \ 12.6$	-03 39 35	$0.10 {\pm} 0.03$
510161	012 - 097	1237650760241971341	$11 \ 49 \ 37.9$	-03 34 07	$2.76 {\pm} 0.53$
510306	012-100	1237650369407090853	$11 \ 49 \ 49.7$	$-03 \ 31 \ 03$	$1.41 {\pm} 0.24$
6973	I750	1237662195061686301	11  58  51.9	$42 \ 43 \ 20$	$0.22 {\pm} 0.04$
211853	-	1237658491205582919	11  59  50.9	$08 \ 47 \ 35$	$0.20 {\pm} 0.06$
7015	N4043	1237655124470661181	$12 \ 02 \ 23.0$	$04 \ 19 \ 47$	$0.23 {\pm} 0.07$
7196	098-095	1237664291001335947	$12 \ 11 \ 59.2$	$15 \ 24 \ 03$	$7.22 \pm 1.72$
221736	-	1237661950790992019	$12 \ 15 \ 49.2$	$13 \ 11 \ 48$	$1.25 {\pm} 0.37$
221829	-	1237664289391116484	$12 \ 16 \ 03.2$	14  00  46	$0.55 {\pm} 0.19$
221828	FGC1395	1237664289391182057	$12 \ 16 \ 11.6$	$13 \ 59 \ 34$	$1.15 \pm 0.42$

AGC Name	Other Name	SDSS DR16 Name	α 12000	δ	M <sub>Dyn</sub>
			J2000	J2000	10 <sup>11</sup> M <sub>solar</sub>
7297	N4226	1237661433771261955	$12 \ 16 \ 26.2$	$47 \ 01 \ 32$	$2.52 {\pm} 0.56$
7337	013-121	1237648702966988820	$12 \ 18 \ 08.6$	$-01 \ 03 \ 52$	$0.91 {\pm} 0.16$
221991	-	1237665441511964722	$12 \ 19 \ 44.0$	$29 \ 34 \ 49$	$1.85 {\pm} 0.48$
7478	N4357	1237661149765107752	$12 \ 23 \ 58.7$	$48 \ 46 \ 45$	$3.67 {\pm} 0.81$
221659	-	1237661971186188446	$12 \ 25 \ 41.7$	$07 \ 10 \ 01$	$0.28 {\pm} 0.09$
221928	-	1237667255627087966	$12 \ 26 \ 51.7$	$31 \ 05 \ 39$	$6.11 \pm 1.75$
222003	-	1237661970112577674	$12\ 27\ 06.5$	$06 \ 25 \ 32$	$0.56 {\pm} 0.15$
221950	-	1237651755087691887	$12 \ 32 \ 59.7$	$03 \ 23 \ 37$	$1.05 {\pm} 0.32$
7883	015-002	1237671764786020385	$12 \ 42 \ 57.2$	-01 13 46	$0.90 {\pm} 0.19$
520620	015-003	1237671764786020514	$12 \ 43 \ 02.9$	$-01 \ 16 \ 58$	$0.70 {\pm} 0.14$
520563	-	1237671764249477365	$12 \ 44 \ 52.0$	$00\ 25\ 48$	$6.52 \pm 1.55$
7931	N4668	1237648720698867721	$12 \ 45 \ 31.7$	$00 \ 32 \ 09$	$0.09 {\pm} 0.02$
7963	015-022	1237671763175473314	$12 \ 47 \ 52.7$	-01 11 10	$1.33 {\pm} 0.22$
222035	-	1237664289932640543	12 59 44.2	$14 \ 10 \ 54$	$1.67 {\pm} 0.50$
8238	016-013	1237648702972625038	$13 \ 09 \ 41.0$	$-01 \ 02 \ 53$	$1.99 {\pm} 0.36$
530631	-	1237650761862086739	$13 \ 16 \ 34.0$	$-02\ 17\ 22$	$0.08 {\pm} 0.03$
8348	I4218	1237650761862086708	$13\ 17\ 03.4$	$-02 \ 15 \ 40$	$2.15 \pm 0.40$
8475	N5174	1237671992947703853	$13 \ 29 \ 25.7$	$11 \ 00 \ 28$	$7.45 {\pm} 1.51$
8485	N5183	1237655499737661514	$13 \ 30 \ 06.1$	-01 43 13	$1.93 {\pm} 0.44$
8487	N5184	1237655499737727088	$13 \ 30 \ 11.5$	$-01 \ 39 \ 47$	$3.35 {\pm} 0.51$
8518	N5207	1237662529524531258	$13 \ 32 \ 14.0$	$13 \ 53 \ 31$	$7.46{\pm}1.36$
231092	045-042	1237662247667171600	$13 \ 36 \ 35.5$	$08 \ 11 \ 34$	$0.74 {\pm} 0.25$
231195	-	1237667783917174819	$13 \ 45 \ 36.9$	$22 \ 03 \ 16$	$0.32 {\pm} 0.08$
8766	I944	1237664291011887113	$13 \ 51 \ 30.8$	$14 \ 05 \ 30$	$10.12 \pm 2.05$
231174	-	1237662225686003729	$13 \ 52 \ 21.2$	$38 \ 11 \ 43$	$0.17 {\pm} 0.05$
8828	132-040	1237667783918026937	$13 \ 54 \ 26.7$	$21 \ 49 \ 45$	$3.27 {\pm} 1.04$
8831	N5356	1237654881271152801	$13 \ 54 \ 58.4$	$05 \ 20 \ 00$	$0.39 {\pm} 0.07$
8844	018-004	1237655495981990086	$13 \ 55 \ 59.4$	$-01 \ 15 \ 42$	$2.32 {\pm} 0.41$
8918	074-031	1237662237477241008	$14 \ 00 \ 14.5$	08  58  01	$0.33 {\pm} 0.07$
230925	074-035	1237662263240949953	$14 \ 00 \ 31.0$	$08 \ 39 \ 01$	$0.25 {\pm} 0.06$
8994	018-042	1237674601605103640	$14 \ 04 \ 52.5$	$00 \ 36 \ 39$	$1.02 {\pm} 0.23$
241267	M+631092	1237662224077815972	$14\ 17\ 11.6$	$35 \ 24 \ 30$	$2.87 {\pm} 0.64$
9201	N5584	1237648704054296626	$14 \ 22 \ 23.7$	$00\ 23\ 18$	$1.37 {\pm} 0.29$
241270	M + 632024	1237662662133416147	$14 \ 24 \ 12.0$	$35 \ 08 \ 45$	$0.6 {\pm} 0.13$
241336	-	1237662224615342283	$14 \ 24 \ 58.2$	$35 \ 21 \ 15$	$0.80 {\pm} 0.22$
540242	019-024	1237674655289966817	$14\ 25\ 49.7$	$-02 \ 20 \ 01$	$5.45 \pm 1.16$
9250	N5618	1237655498670211218	$14 \ 27 \ 11.8$	$-02 \ 15 \ 46$	$1.36 {\pm} 0.26$
9462	N5719	1237648704056328322	$14 \ 40 \ 56.0$	$00 \ 19 \ 04$	$0.72 {\pm} 0.10$
9483	I1048	1237654881276395557	$14 \ 42 \ 57.9$	$04 \ 53 \ 24$	$0.52 {\pm} 0.12$
9512	N5750	1237648704056918077	$14 \ 46 \ 11.1$	$00\ 13\ 22$	$0.73 {\pm} 0.13$
9537	193-001	1237662305118650412	$14 \ 48 \ 26.7$	34  59  50	$4.56 {\pm} 0.79$
9538	I1058	1237667781239636022	$14 \ 49 \ 12.3$	$17 \ 01 \ 13$	$2.82 {\pm} 0.73$
241306	-	1237668272980754643	$14 \ 51 \ 18.7$	$16 \ 41 \ 41$	$0.64 {\pm} 0.21$

AGC Name	Other Name	SDSS DR16 Name	lphaJ2000	$\delta$ J2000	$\mathbf{M_{Dyn}}$ $10^{11}\mathbf{M_{solar}}$
9645	N5806	1237651736313528355	15  00  00.3	$01 \ 53 \ 28$	$1.01 {\pm} 0.22$
9681	M + 731023	1237661211510833280	$15 \ 03 \ 39.7$	$42 \ 07 \ 33$	$0.32 {\pm} 0.07$
9888	I1125	1237655692481986636	$15 \ 33 \ 05.6$	$-01 \ 37 \ 42$	$0.22 {\pm} 0.05$
10306	023-031	1237655550742298700	$16 \ 16 \ 43.5$	$00 \ 14 \ 46$	$10.15 \pm 1.52$
10692	139-034	1237662302453039177	$17 \ 05 \ 28.0$	$23 \ 09 \ 11$	$4.76 {\pm} 0.73$
10706	197-035	1237654954281468455	$17 \ 06 \ 28.3$	$38\ 21\ 47$	$1.83 {\pm} 0.30$
600138	M-153012	1237652598487646631	$20 \ 49 \ 52.0$	$-07 \ 01 \ 17$	$4.41 {\pm} 0.75$
11649	374-028	1237656567038935144	20 55 27.6	-01 13 31	$1.44 {\pm} 0.34$
310030	426-015	1237652944768008329	$21 \ 12 \ 01.2$	$11 \ 29 \ 45$	$0.20 {\pm} 0.05$
610024	375-011	1237663457240089137	$21 \ 13 \ 12.8$	$00\ 21\ 58$	$0.86 {\pm} 0.15$
11712	N7047	1237663456703545733	$21 \ 16 \ 27.6$	$00 \ 49 \ 36$	$2.28 {\pm} 0.49$
610495	-	1237666210347614532	21  56  49.5	$-07 \ 45 \ 33$	$1.45 {\pm} 0.45$
610499	-	1237666210347745660	21  58  05.8	-07 50 43	$0.73 {\pm} 0.16$
12174	N7364	1237663543150837809	$22 \ 44 \ 24.2$	$00 \ 09 \ 44$	$2.58 {\pm} 0.39$
12363	379-034	1237663784191524949	$23 \ 06 \ 31.5$	$00 \ 10 \ 18$	$0.99 {\pm} 0.20$
35971	604G7	1237672815977496655	$23 \ 15 \ 17.2$	$-21 \ 21 \ 57$	$3.18 {\pm} 0.85$
12834	N7782	1237669518514913516	$23 \ 53 \ 54.0$	$07 \ 58 \ 14$	$9.73 {\pm} 1.59$

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