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# MgH<sub>2</sub> synthesis during reactive mechanical alloying studied by in-situ pressure monitoring

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#### ABSTRACT

The synthesis of MgH<sub>2</sub> by reactive mechanical milling has been studied by monitoring H<sub>2</sub> pressure changes inside a milling chamber. Mg and a Mg-10 wt.% C mixture were used as starting materials and milled under 0.5 MPa of H<sub>2</sub>. The addition of C doubles the MgH<sub>2</sub> synthesis efficiency due to C acting as a process control agent. MgH<sub>2</sub> formation has been observed throughout milling and during the rest periods between milling stages. Mg hydriding during the rest periods has been found to be controlled by hydrogen diffusion through MgH<sub>2</sub>. High-diffusivity paths along grain boundaries seem to be operative during the process. A lower bound for the diffusion coefficient of H in MgH<sub>2</sub> at room temperature of  $10^{-25}$  m<sup>2</sup> s<sup>-1</sup> has been estimated from the data.

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# 1. Introduction

In the last years Mg and its hydride have been extensively studied due to their potential application to store hydrogen [1-7]. MgH<sub>2</sub> main advantages are its low cost and high hydrogen content per mass (7.6 wt.%); its principal drawbacks are its high stability and the extremely slow hydrogen absorption and desorption rates near room temperature. To overcome these disadvantages mechanochemical methods have been successfully employed to obtain Mg-based materials with better hydrogen sorption properties [5,8–10].

Reactive mechanical alloying (RMA) is a mechanochemical technique that allows hydride synthesis by processing the materials under a reactive  $H_2$  atmosphere [11]. Interesting results have been observed when following the RMA process

by pressure measurements. Chen et al. were the first to show that  $MgH_2$  formation can be analyzed by monitoring the  $H_2$ pressure decrease inside a milling vial [12]. More recently, Doppiu *et al.* have used the same technique to determine the effect of different  $H_2$  pressures on Mg hydriding by RMA [13]. The synthesis of other hydrides has also been followed by pressure measurements: Chen *et al.* and Dunlap *et al.* have studied the hydriding behavior of Ti [12,14], Friedrichs *et al.* have analyzed the reaction of  $Mn_3Ti_2V$  and Ca with  $H_2$  during RMA [15], and likewise Zhang and coworkers have determined the reaction path leading to the formation of  $Mg_2TM$  (TM = Fe, Co, Ni) complex hydrides [16]. Interestingly, in a few cases it has been mentioned that the hydriding process not only occurs during milling, but also happens throughout the rest periods between milling stages [12,14]. However, these

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processes were not further studied, and their main characteristics remain unknown.

Mg can be hydrided by RMA at room temperature as a result of the generation of free-from-oxide fresh surface and the removal of surface hydride layers that impair further hydriding due to the sluggish H diffusion through MgH<sub>2</sub>. Hydrogen diffusion in MgH<sub>2</sub> has been moderately studied up to now [17–23], and the reported results have always been obtained above room temperature. Additionally, it is not yet clear if H diffusion through MgH<sub>2</sub> occurs via a high-diffusivity path along grain boundaries or not.

In this work, we present an analysis of  $MgH_2$  synthesis by RMA from Mg and a mixture of Mg and C. The study is based on hydriding data inferred from *in-situ* pressure measurements. Our results allow us to establish a connection between hydrogen diffusion in MgH<sub>2</sub> and the RMA process.

## 2. Experimental

Mg (Riedel de Häen, 99%, average size 100 μm) denoted as (Mg) and a mixture of Mg-10 wt.% C (Sigma-Aldrich, 99.9%, platelets, average diameter 200 µm, average thickness 50 µm) designated as (Mg + C) were ball-milled in a Uni-Ball-Mill II apparatus under 0.5 MPa of high-purity H<sub>2</sub>. The ball-topowder mass ratio was 44:1, and the rotational speed was 195 rpm. Constant pressure inside the milling vial was ensured by regularly refilling the chamber. The milling program consisted of milling stages of up to 10 h followed by rest periods of variable duration. In-situ pressure measurements were done via an Omega PX-181 pressure transducer. Data were stored in a HOBO H8 data logger attached to the milling chamber. A Bacharach Leakator 10 combustible gas detector was used to check for H2 leaks. SEM images were obtained with a Philips Electronic Instruments SEM 515. All handlings were done within a Glove box with a purified argon atmosphere with O<sub>2</sub> and H<sub>2</sub>O levels below 1 ppm.

### 3. Results and discussion

#### 3.1. Milling

 $H_2$  pressure inside the milling chamber decreased both throughout milling and during the rest periods (Fig. 1). Pressure decrease during milling is the consequence of  $H_2$ consumption to form MgH<sub>2</sub> in the closed milling vessel. The amount of MgH<sub>2</sub> formed can be deduced at the pressures involved here by applying the ideal gas law. Pressure changes during the rest periods, as will be discussed below, are also due to  $H_2$  consumption to form MgH<sub>2</sub>. These last processes were observed regularly, with the exception of the initial milling period of (Mg) and the final stages of (Mg) and (Mg + C) (Fig. 2). Similar observations have been reported in Ti [12,14] and  $Mn_3Ti_2V$  [15]. In both cases, pressure drops were attributed to hydride formation.

The reduction in  $H_2$  pressure during the rest periods can be a consequence of: a)  $H_2$  leaks, b) gas cooling and c) hydrogen consumption due to hydride formation. Gas leaks were discarded as the system was thoroughly examined with



Fig. 1 – Pressure changes inside the milling chamber during milling (open symbols) and resting periods (filled symbols). Error bars are of the order of symbols size.

a combustible gas detector and no leaks were detected. Besides, the observed saturation pressure (the final pressure at the end of the drop during the rest period) is well over ambient pressure (Fig. 1). Gas cooling would be the natural consequence of gas heating during mechanical processing. It has been reported that the temperature of milling chambers and balls can increase noticeably when milling is performed with intermediate or high-energy milling devices [13,16,24]. Several processes contribute to the heating of the milling media: mechanical energy converted into heat, MgH<sub>2</sub> formation reaction, Mg plastic deformation, etc. However, the temperature increase in the case of this low-energy miller is rather small. After a typical milling stage, the temperature of the external part of the chamber did not exceed room temperature by more than 3 °C. Additionally, the pressure drops are less pronounced after the later milling stages and even disappear for the last stages (Fig. 2), contradicting the possibility of the pressure drops being a consequence of gas cooling. The



Fig. 2 – Amount of MgH<sub>2</sub> formed during the mechanochemical treatment. The figure includes milling periods (open symbols) and resting intervals (filled symbols). Error bars are of the order of symbols size.

absence of a substantial increase in temperature (and posterior cooling) can be attributed to an efficient heat dissipation process resulting from the combination of a reduced milling energy, the high thermal conductivity of H<sub>2</sub>, and the large milling chamber volume ( $\sim$ 0.8 l) and mass ( $\sim$ 8 kg), the latter compared with the milled powder mass ( $\sim$ 7 g). This was quantitatively confirmed by an estimation of the timescale of the heat dissipation process, as we did not have the possibility to measure gas temperature inside the chamber. We have calculated a characteristic time associated with the cooling process of the hydrogen mass contained in the milling chamber of the order of minutes, taking into account the thermal properties of hydrogen at the milling pressure and the chamber dimensions. This value is considerably shorter than the timescale of 10–20 h observed in the pressure drops during the rest periods. The estimated timescale agrees well with the typical times experimentally observed in a different milling device, with a small chamber but a higher milling energy [16]. Therefore, having discarded gas leaks and gas cooling as causes of pressure drops, we attribute pressure changes to H<sub>2</sub> consumption by MgH<sub>2</sub> formation.

#### 3.2. Hydriding during milling period

Fig. 3 shows the amount of  $MgH_2$  formed in (Mg) and (Mg + C) without considering the pressure changes registered during the rest periods. Both curves have a sigmoidal shape. Similar shapes have been reported for Mg [12,13,25], Ti [14] and Ca [15]. The induction period is associated with the microstructural refinement necessary for hydriding to begin [13,14]. The final stage is related to magnesium exhaustion. Overall, we observe that (Mg + C) needs almost half the time required for (Mg) to be fully hydrided. To be able to extract more information from the curves, a simple model for the process is developed. The model considers three species: Mg, Mg\* ("activated" Mg) and MgH<sub>2</sub>. Mg represents the starting material, not yet modified by milling, Mg\* describes Mg "activated" by the mechanical process and MgH<sub>2</sub> denotes the hydride formed from the reaction of Mg\* with  $H_2$ . Mg<sup>\*</sup> has a microstructure modified by the milling process, and more importantly, a fresh surface, free from



Fig. 3 – MgH $_2$  amount in (Mg) and (Mg + C) formed during milling. Error bars are of the order of symbols size.

oxides and previously formed  $MgH_2$  layers. The hydriding process is modeled by a series reaction schematized as:

$$Mg \rightarrow Mg^*$$

 $Mg^* + H_2 \rightarrow MgH_2$ 

During these reactions, Mg<sup>\*</sup> acts as an intermediate species that is produced in a characteristic time  $\tau_{\rm m}$  by mechanically processing Mg, and is consumed by reacting with hydrogen to produce MgH<sub>2</sub> in a characteristic reaction time  $\tau_{\rm r}$ . The reaction rates of Mg, Mg<sup>\*</sup> and MgH<sub>2</sub> are given by:

$$\frac{dN_{Mg}}{dt} = -\frac{N_{Mg}}{\tau_{m}} \tag{1}$$

$$\frac{\mathrm{d}N_{\mathrm{Mg}^*}}{\mathrm{d}t} = \frac{N_{\mathrm{Mg}}}{\tau_{\mathrm{m}}} - \frac{N_{\mathrm{Mg}^*}}{\tau_{\mathrm{r}}} \tag{2}$$

$$\frac{\mathrm{d}N_{\mathrm{MgH}_2}}{\mathrm{d}t} = \frac{N_{\mathrm{Mg}^*}}{\tau_{\mathrm{r}}} \tag{3}$$

where  $N_{\rm Mg},\,N_{\rm Mg^*}$  and  $N_{\rm MgH2}$  represent the number of moles of Mg, Mg\* and MgH<sub>2</sub>, respectively. The characteristics of the general solution of this model are well-known [26]. In this particular case, the experimental data after the induction period can be very well fitted with the expression:

$$N_{MgH_2}(t) = N_F (1 - e^{-t/\tau})$$
(4)

that corresponds to the limiting cases of a milling controlled process ( $\tau_r << \tau_m$ ) or a hydriding reaction controlled process ( $\tau_m << \tau_r$ ). In Eq. (4) N<sub>F</sub> represents the final amount of MgH<sub>2</sub> and  $\tau$  is either  $\tau_r$  or  $\tau_m$ , depending on the specific rate controlling process. The hydriding rate from Eq (4) is

$$\frac{\mathrm{d}N_{\mathrm{MgH}_{2}}}{\mathrm{d}t} = \frac{N_{\mathrm{F}}}{\tau} e^{-t/\tau} \tag{5}$$

and in terms of the conversion fraction

$$\alpha = \frac{N_{\rm MgH_2}}{N_{\rm F}} = 1 - e^{-t/\tau}$$
(6)

it is given by

$$\frac{dN_{MgH_2}}{dt} = \frac{N_F}{\tau} (1 - \alpha)$$
(7)

Eq. (7) shows that the rate is proportional to the unreacted fraction  $(1 - \alpha)$ .

The fitted  $\tau$  values are 23 h for (Mg) and 10 h for (Mg + C). Taking into account that we are using a low-energy milling device and that MgH<sub>2</sub> formation by RMA can be completed in much less than 50 h [12,13,25], it seems that the hydriding process here is controlled by milling. Within this interpretation,  $\tau$  corresponds to  $\tau_m$ , and the shorter timescale observed for (Mg + C) can be attributed to C acting as a process control agent. This is achieved by the well-known C lubricating properties that limit cold-welding.

#### 3.3. Hydriding during the rest periods

Mg hydriding data during the rest periods present a different time-dependence (Fig. 4). Data was very well fitted with a function of the form (8)

# $N_{H_2} = N_0 + (Bt)^{\frac{1}{2}}$

where  $N_{H_2}$  is the hydrogen content of the material,  $N_0$  is the hydrogen initial amount and B is a coefficient whose physical meaning is discussed below (see Eq. (17)). The parabolic timedependence suggests a diffusion-limited process. A possible scenario is the following. During milling Mg hydriding is controlled by the milling rate, by means of the fresh surface creation rate. Once milling is stopped, and the rest period begins, the formation of fresh surface ends and only a fraction of Mg exposes a clean surface to H<sub>2</sub>. This fraction is the main part of the material that is going to be hydrided during the rest period. Hydriding starts on the surface and advances towards the interior forming a hydride layer that grows in depth. This process assumes that many nuclei are formed on the surface to ensure the establishment of a hydride layer. Within this picture, further hydriding can only occur by hydrogen diffusion through the hydride layer, which due to the well-known slowness of the process [17-23] will naturally control the whole hydriding process. An idealized diagram of the model is schematized in Fig. 5. A spherical particle of radius Ro is hydrided by being exposed to an external hydrogen pressure  $p_{\rm H2}$ . The particle has an external MgH<sub>2</sub> shell that extends from the surface down to r<sub>i</sub>, where the interface between MgH<sub>2</sub> and Mg is located. The internal region of the particle is composed of unhydrided Mg. As hydrogen diffuses through the hydride, the interface moves towards the interior of the particle and the surrounding hydride layer grows. Recalling that the amount of hydride that forms during the rest periods is a small fraction of the total amount of MgH<sub>2</sub> (Fig. 2), the depth of the hydride layer grown during the rest periods can be considered much smaller than the radius of the particle. This assumption allows us to model hydriding as a onedimensional process. By additionally assuming a steady state solution, the hydrogen diffusive flow through the hydride layer is given by:

$$J = Mc \frac{d\mu}{dx} \approx Mc_{MgH_2} \frac{\mu(R_0) - \mu(r_i)}{R_0 - r_i}$$
(9)



Fig. 4 – Hydrogen content in (Mg) and (Mg + C) during typical rest periods. The fits follow Eq. (8). The jumps in the experimental values are due to the data acquisition system discretization.



Fig. 5 - Scheme of the hydriding process model.

where  $\mu$  is the hydrogen chemical potential, M the hydrogen mobility and  $c_{MgH2}$  the hydrogen concentration in MgH<sub>2</sub>, assumed to be approximately the same in R<sub>0</sub> or in r<sub>i</sub> (there is no appreciable H<sub>2</sub> solubility in MgH<sub>2</sub> [27,28]). The amount of hydrogen in the particle, neglecting H solubility in Mg [27,28], can be given by

$$N_{H_2} = Ac_{MgH_2}(R_0 - r_i),$$
(10)

where A is the area of the particle of radius  $R_0$  (hydride layer thickness much smaller than the particle radius). The time derivative of Eq. (10) connects the hydriding rate with the interface velocity.

$$\frac{\mathrm{d}N_{\mathrm{H}_{2}}}{\mathrm{d}t} = -\mathrm{A}c_{\mathrm{MgH}_{2}}\frac{\mathrm{d}r_{\mathrm{i}}}{\mathrm{d}t}.$$
(11)

On the other hand, the hydriding rate is proportional to the hydrogen flow through the hydride layer.

$$\frac{\mathrm{d}N_{\mathrm{H}_2}}{\mathrm{d}t} = \mathrm{AJ}.$$
(12)

using the following expression for the chemical potential.

$$\mu(\mathbf{R}_0) - \mu(\mathbf{r}_i) = \frac{\mathbf{R}T}{2} \ln\left(\frac{p_{\mathrm{H}_2}}{\mathrm{Peq}}\right),\tag{13}$$

and combining Eqs. (9) and (11)–(13), the temporal evolution of  $r_i$  can be obtained as

$$r_{i}(t) = R_{0} - \left[D \ln \left(\frac{p_{H_{2}}}{peq}\right)t\right]^{\frac{1}{2}}, \tag{14}$$

where *D* denotes the tracer diffusion coefficient, equal to the product MRT. Replacing Eq. (14) in Eq. (10), the amount of hydrogen in the hydride is obtained as

$$N_{H_2}(t) = Ac_{MgH_2} \left[ D \ln \left( \frac{p_{H_2}}{peq} \right) t \right]^{\frac{1}{2}}.$$
 (15)

This expression has been derived for one particle. Its generalization to the whole sample can be made by replacing

A by  $A_{eff}$ , the area of Mg "activated" by milling corresponding to the whole sample. The "activated" fraction is taken into account by the factor  $\gamma$ , and the fraction of the total surface that corresponds to Mg by the hydriding degree  $\alpha$ . The effective total area is then given by:

$$A_{\rm eff} = \gamma A_0 (1 - \alpha), \tag{16}$$

where  $A_0$  is the total area of the sample. Replacing A by  $A_{eff}$  in Eq. (15), the expression for the amount of hydrogen in the material takes the form:

$$N_{H_2}(t) = \left[ D\gamma^2 A_0^2 (1-\alpha)^2 c_{MgH_2}^2 ln\left(\frac{p_{H_2}}{p_{eq}}\right) t \right]^{\frac{1}{2}}.$$
 (17)

By fitting our data with Eq. (17) we have calculated  $D\gamma^2 A_0^2$ (Fig. 6). We observe a good agreement between the values corresponding to different (Mg) samples, showing a very good repeatability. We also note that the (Mg + C) values are slightly higher than those of (Mg). Additionally, we see an increase in  $D\gamma^2 A_0^2$  as the conversion fraction approaches unity, more pronounced for (Mg) than for (Mg + C). The increase in  $D\gamma^2 A_0^2$ can be attributed to the increase in  $A_0$ , due to the size reduction consequence of milling.

To estimate the value of  $A_0$  we have considered two possible scenarios: a first one in which diffusion takes place in the Mg particles that compose the sample, and a second one in which hydrogen diffusion through grain boundaries is much faster than bulk diffusion, and the effective particles into which hydrogen is diffusing are the crystallites. Particle area for the first situation has been estimated from SEM images (Fig. 7), while grain boundary area for the second option has been calculated from grain size data estimated from XRD results [29]. In both cases, the following expression for the total surface of a sample of mass *m* and density  $\rho$ , composed of a great number of spherical particles of radius  $R_0$  has been used.

$$A_0 = \frac{3m}{\rho R_0} \tag{18}$$



Fig. 6 – Values of  $D\gamma^2 A_0^2$  obtained by fitting the hydriding data during rest periods. Circles correspond to (Mg + C) and squares to (Mg). Three different (Mg) samples have been measured; each sample is identified by distinct square symbols.



Fig. 7 – SEM images exemplifying particle-size changes with milling in (Mg). A: 12 h ( $\alpha$  = 0.07), B: 50 h ( $\alpha$  = 0.6) and C: 100 h ( $\alpha$  = 1).

The  $A_0$  values associated with each scenario are presented in Fig. 8. It can be seen that the square of crystallite area spans a range of almost one order of magnitude, whereas particle area extends over nearly four orders of magnitude. As the  $D\gamma^2 A_0^2$  values range over one order of magnitude, and there are no reasons to expect a decrease in D or a change in  $\gamma$  as the conversion fraction grows, a diffusion process in which the effective particles are the crystallites is assumed. Therefore,



Fig. 8 –  $A_0$  values corresponding to particle area (open symbols) and crystallite area (filled symbols) as a function of the conversion fraction. Square symbols correspond to (Mg) and circles to (Mg + C).

a lower bound for D, denoted as  $D_{LB}$ , can be estimated by setting  $\gamma$  equal to 1 (Fig. 9). The observed data dispersion is narrower than that of Fig. 6, suggesting that a rapid mobility along grain boundaries, together with the crystallites being the effective particles for diffusion could be the correct explanation. A similar idea has been proposed by [16,20-22,30,31]. A slight increasing trend in D<sub>LB</sub> values is observed for (Mg) as  $\alpha$  goes up to 0.6. At this value, (Mg) and (Mg + C) data roughly coincide. The increasing  $D_{LB}$  values for (Mg) can be linked with the microstructural evolution of the sample during milling. This trend is less evident for (Mg + C) as a consequence of the more efficient milling process. The relationship between microstructural refinement and diffusion is the defect mediated H diffusion process that takes place in MgH<sub>2</sub> [32]. For  $\alpha$  beyond 0.6, D<sub>LB</sub> values for both materials slightly decrease. We interpret this as our simplified



Fig. 9 – Lower bound value for the diffusion coefficient of H in MgH<sub>2</sub>. Circles correspond to (Mg + C) and squares to (Mg). Different (Mg) samples are identified by distinct square symbols.

model failing to represent the process when the material is almost fully hydrided. Taking all this into account, a value of  $10^{-25}$  m<sup>2</sup> s<sup>-1</sup> can be taken as a rough estimation of  $D_{LB}$ . To the best of our knowledge, there are no reports of D values measured at room temperature, but this lower bound for H diffusion in MgH<sub>2</sub> at room temperature can be compared with D values extrapolated from data measured at higher temperatures. We have found three different D data sources: 1) D values deduced from fitting macroscopic hydrogen absorption and desorption curves with kinetic models that consider diffusion as a rate controlling step [21-23], 2) D values obtained from nuclear magnetic resonance measurements of H hoping rate in MgH<sub>2</sub> [19,20] and 3) D values determined from first principles calculations [32]. With the exception of the calculated data, that cover a temperature range that includes room temperature, the extrapolated D values have been obtained by using an Arrhenius dependence with the corresponding parameters reported in each reference. In the case of the D values estimated from the H hoping rate, the diffusion coefficient has been calculated by us assuming the H diffusion pathway reported in [32].

As can be seen in Table 1, literature data span a range from  $10^{-35}$  to  $10^{-21}$  m<sup>2</sup> s<sup>-1</sup>. Our determination is well within the range of group 1) values, obtained from hydrogen absorption and desorption measurements. Moreover, the value from [21], the only one that corresponds to MgH<sub>2</sub> without additives, can be matched by setting  $\gamma$  equal to 0.01. This  $\gamma$  value implies that 1% of the surface is "activated" by milling in each milling event, a more realistic assumption than setting  $\gamma$  equal to 1. The NMR values corresponding to coarse grained MgH<sub>2</sub> are consistently below our lower bound for D, which is reasonable considering the microstructural differences between that material and our ball-milled powders. Additionally, our value could also be incremented by extrinsic defects due to impurities potentially present in the starting Mg [20]. For the same reasons mentioned above, D values obtained from first principles calculations performed on bulk MgH<sub>2</sub>, are also below our lower bound. Interestingly however, first principles calculations predict the coincidence of the D values obtained for (Mg) and (Mg + C). In [33] it is reported that graphite is incorporated as a neutral dopant in MgH<sub>2</sub>, and as such, it does not change the concentration of defects because it does not alter the charge neutrality in the material. Therefore, H diffusion should not change by the addition of C to MgH<sub>2</sub>, as is found here.

#### 3.4. Hydriding process, general description

We can now try to connect the diffusion-limited hydriding process taking place throughout the rest periods with the MgH<sub>2</sub> synthesis that occurs during milling. An extremely simplified model is considered. When the material is milled, several milling events such as ball-to-ball collisions and ballto-chamber impacts modify the material so as to create fresh surface, by separating the previously formed hydride layers from the external parts of the material. Between two milling events, it can be assumed that hydriding proceeds through a diffusion-limited process similar to the one observed during the rest periods. Each time a milling event occurs, a new diffusion process starts. This process continues

Table 1 $-$ Values of the hydrogen diffusion coefficient in MgH $_2$ estimated from literature data.				
D @ 294 K (m <sup>2</sup> s <sup>-1</sup> )	System	Method	Temperature range (K)	Ref
$\begin{array}{l} 1.4 \times 10^{-25} \\ 1.0 \times 10^{-28} \\ 1.3 \times 10^{-21} \\ 3 \times 10^{-35} \\ 6 \times 10^{-33} \\ 1 \dots 10^{-29} \end{array}$	Mg–V nanoblades Mg–FeTi–CNT's MgH <sub>2</sub> powder and foil coarse grained MgH <sub>2</sub> coarse grained MgH <sub>2</sub>	Absorption curves fitting Absorption curves fitting Desorption curves fitting NMR NMR	500–570 373–573 580–700 533–673 500–750	[23] [22] [21] [20] [19]

until the next milling event happens. Within this picture, hydriding during milling can be thought as the succession of many short-lived diffusion curves separated in time by  $\tau_{mill}$ , the characteristic time between two effective milling events (Fig. 10). In a  $\tau_{mill}$  time the amount of hydrogen incorporated by the sample is given by  $N_{H2}$  ( $\tau_{mill}$ ) (Eq. (17)). If  $\tau_{mill}$  is short enough, the hydriding rate during milling can be estimated as (Fig. 10):

$$\frac{\mathrm{d}N_{\mathrm{H}_{2}}}{\mathrm{d}t} \approx \frac{N_{\mathrm{H}_{2}}(\tau_{\mathrm{mill}})}{\tau_{\mathrm{mill}}} \tag{19}$$

in terms of the parameter  $\lambda$  defined as

$$\lambda = \left[ D\gamma^2 A_0^2 c_{MgH2}^2 ln\left(\frac{p_{H2}}{peq}\right) \right]^{\frac{1}{2}}$$
(20)

 $N_{H2}$  ( $\tau_{mill}$ ) can be written as

$$N_{H_2}(\tau_{mill}) = \lambda (1 - \alpha) \tau_{mill}^{1/2}$$
(21)

and the hydriding rate during milling is

$$\frac{\mathrm{d}N_{\mathrm{H2}}}{\mathrm{d}t} \approx \frac{\lambda}{\tau_{\mathrm{mill}}^{1/2}} (1-\alpha)$$
(22)

Considering the stoichiometric molar ratio between H<sub>2</sub> and MgH<sub>2</sub>, Eq. (22) can be compared with the macroscopic rate previously derived [Eq. (7)]. Both expressions present the same  $\alpha$  dependence, and the link between the phenomenological treatment of Eqs (1)–(3) and the diffusional approach can be made by equating the corresponding coefficients.

$$\frac{N_{\rm F}}{\tau_{\rm m}} = \frac{\lambda}{\tau_{\rm mill}^{1/2}} \tag{23}$$

By expressing  $N_F$  in terms of  $c_{MgH2}$ ,  $A_0$  and  $R_0$ , and recalling Eq. (18), the following relationship is obtained from Eq. (23):



Fig. 10 – Representation of the hydriding process during milling as a sequence of short diffusion-controlled hydriding processes separated by milling events.

$$\frac{D_{\rm m}^2}{D\gamma^2 A_0^2 \left(\frac{\rho}{m}\right)^2 \ln\left(\frac{p_{\rm H_2}}{p_{\rm eq}}\right)} \tag{24}$$

therefore, the macroscopic timescale  $\tau_{\rm m}$  is connected to material properties through D,  $p_{\rm eq}$   $\rho$  and  $A_0$ , to experimental properties through  $p_{\rm H_2}$  and m, and to milling parameters through  $\tau_{\rm mill}$ . Unfortunately, the characteristics of the milling apparatus employed in this study do not allow us to change the milling rate in order to check experimentally the relationship predicted by Eq. (24). The milling rate and the milling mode are strongly correlated in our device, and it is not possible to change  $\tau_{\rm mill}$  without affecting the milling mode, and hence altering the whole process. However, Eq. (24) allows us to estimate values of  $\tau_{\rm mill}$  using the  $D\gamma^2A_0^2$  values depicted in Fig. 6 and the  $\tau_{\rm m}$  values previously determined. The calculated  $\tau_{\rm mill}$  values are in the range of 0.5–1 min during the first milling stages and increase up to 4–6 min when  $\alpha$  is around 0.6.

As a final remark, we want to mention that we have tried to register hydrogen absorption in (Mg) and (Mg + C) at room temperature using a volumetric device, but no hydriding was observed. The experiments were conducted as follows. The samples were dehydrided in the volumetric apparatus under mechanical vacuum during heating to 325 °C at 5 °C/min, then they were cooled under dynamic vacuum down to 25 °C and finally exposed to 0.5 MPa H<sub>2</sub> for as long as 12 h. Despite this, no hydrogen absorption was registered. We attribute this to a much slower hydriding process consequence of the microstructural changes that occur during the initial desorption at high-temperature [10,30], as well as to a possible surface poisoning [34-36], regardless of manipulating the samples within a glove box at all times. Therefore, both the microstructural changes and the generation of fresh surface consequence of mechanical milling seem to play a crucial role to allow the observation of hydrogen diffusion in MgH2 at room temperature.

### 4. Conclusions

MgH<sub>2</sub> formation from Mg and H<sub>2</sub> during mechanical milling, with and without C as an additive, was characterized by *in-situ* pressure measurements. Hydriding has been observed during milling and throughout the rest periods between milling stages. From the analysis of hydrogen absorption during milling, it is concluded that hydriding is controlled by the mechanical process. Additionally it was established that C acts as a process control agent that effectively reduces the mechanical processing time to a half. From the analysis of hydrogen absorption during the rest periods, it is deduced that the process is controlled by H diffusion in MgH<sub>2</sub>. Throughout this process Mg crystallites acts as the effective particles were H diffusion takes place and grain boundaries behave as highdiffusivity paths. From the measured data a lower bound for the diffusion coefficient of H in MgH<sub>2</sub> at room temperature of  $10^{-25}$  m<sup>2</sup> s<sup>-1</sup> has been estimated.

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