This article was downloaded by: [BURTON, B.P.] On: 11 December 2008 Access details: Access Details: [subscription number 906617806] Publisher Taylor & Francis Informa Ltd Registered in England and Wales Registered Number: 1072954 Registered office: Mortimer House, 37-41 Mortimer Street, London W1T 3JH, UK



To cite this Article BURTON, B.P., TINTE, SILVIA, COCKAYNE, ERIC and WAGHMARE, U.V.(2008)'THE EFFECT OF NEAREST NEIGHBOR [PbO] DIVACANCY PAIRS ON THE FERROELECTRIC-RELAXOR TRANSITION IN NANO-ORDERED Pb(Sc_{1/2}Nb_{1/2})O₃',Integrated Ferroelectrics,101:1,37 — 43

To link to this Article: DOI: 10.1080/10584580802451439

URL: http://dx.doi.org/10.1080/10584580802451439

PLEASE SCROLL DOWN FOR ARTICLE

Full terms and conditions of use: http://www.informaworld.com/terms-and-conditions-of-access.pdf

This article may be used for research, teaching and private study purposes. Any substantial or systematic reproduction, re-distribution, re-selling, loan or sub-licensing, systematic supply or distribution in any form to anyone is expressly forbidden.

The publisher does not give any warranty express or implied or make any representation that the contents will be complete or accurate or up to date. The accuracy of any instructions, formulae and drug doses should be independently verified with primary sources. The publisher shall not be liable for any loss, actions, claims, proceedings, demand or costs or damages whatsoever or howsoever caused arising directly or indirectly in connection with or arising out of the use of this material.

Integrated Ferroelectrics, 101: 37–43, 2009 Copyright © Taylor & Francis Group, LLC ISSN 1058-4587 print / 1607-8489 online DOI: 10.1080/10584580802451439



The Effect of Nearest Neighbor [Pb–O] Divacancy Pairs on the Ferroelectric-Relaxor Transition in Nano-Ordered Pb(Sc_{1/2}Nb_{1/2})O₃

B. P. Burton,^{1,*} Silvia Tinte,¹ Eric Cockayne,¹ and U. V. Waghmare²

¹Ceramics Division, Materials Science and Engineering Laboratory, National Institute of Standards and Technology, Gaithersburg, MD 20899-8520, USA

²J. Nehru Theoretical Sciences Unit, JNCASR, Jakkur, Bangalore, 560 064, India

ABSTRACT

Molecular dynamics simulations were performed on a first-principles-based effective Hamiltonians for chemically short-range ordered Pb(Sc_{1/2}Nb_{1/2}) O₃ with nearest neighbor [Pb–O] divacancy pairs. The divacancy-concentration ($X_{[Pb-O]}$) vs. temperature phase diagram was calculated, and it is topologically equivalent to the hydrostatic pressure (P) vs. temperature diagram: a ferroelectric ground-state phase at low $X_{[Pb-O]}$ (P); that transforms to a relaxor paraelectric phase at moderate $X_{[Pb-O]}$ (P); followed by a crossover to a normal paraelectric phase at high $X_{[Pb-O]}$ (P).

Keywords: PSN, relaxor ferroelectric, lead vacancies, oxygen vacancies, phase transitions, random fields

INTRODUCTION

Chemically disordered Pb(Sc_{1/2}Nb_{1/2})O₃ (PSN) exhibits a relaxor ferroelectric (RFE [1, 2]) to normal ferroelectric (FE) transition; and Chu et al. [3] demonstrated that the addition of 1.7 atomic percent [Pb–O] divacancy pairs depresses the FE transition temperature (T_{FE}) of chemically disordered PSN from ~373 K to ~338 K. Chu et al. also reported similar and more complete results for isostructural Pb(Sc_{1/2}Ta_{1/2})O₃ (PST) [4–6]. These results suggest that a sufficient concentration of divacancy pairs, X_[Pb–O], will drive the system to a fully relaxor state, that has no FE ground-state phase. Introducing Pb-vacancies [7], or [Pb–O] divacancy pairs [8] (Fig. 1) increases the average

Received February 15, 2007; in final form May 12, 2007.

^{*}Corresponding author. E-mail: benjamin.burton@nist.gov



Figure 1. Representation of the $2 \times 2 \times 2$ perovskite supercell for chemically ordered Pb₈(Sc₄Nb₄)O₂₄ and the Pb₇(Sc₄Nb₄)O₂₃supercells with nearest- and next-nearest neighbor divacancy pairs. Atoms are only shown in 1/8 of the supercell. (See Color Plate V)

strength of local "random fields" $\langle h_i \rangle$, ($\langle \cdots \rangle$ indicates spatial statistical averaging) [9,10] that, at sufficient $X_{[Pb-O]}$ yield a fully relaxor state. Thus, $\langle h_i \rangle$ can be regarded as a *nonordering* field [11] that tunes the proportions of RFE and FE character in the system.

Increasing hydrostatic pressure (P, Fig. 2a) drives chemically disordered PSN into a fully relaxor state [12] and the results of previous simulations by Tinte et al. [9] convincingly explain this as follows: 1) P has a negligible effect on $\langle h_i \rangle$; 2) P smoothly and monotonically reduces FE well depths [13–15] and thus destabilizes the FE phase relative to the RFE state of the paraelectric (PE) phase; 3) Keeping $\langle h_i \rangle$ constant while reducing FE well depth corresponds to an *indirect relative increase* in $\langle h_i \rangle$. Because P *indirectly* increases $\langle h_i \rangle$, it will only induce a FE-RFE transition in a sample that has some RFE character even at P = 0 (e.g. chemically disordered PSN). In a sample without significant $\langle h_i \rangle$ (e.g. PSN with perfect chemical order) moderate pressure induces a FE-PE transition [16] without RFE character. Increasing $X_{\text{[Pb-O]}}$, *directly* increases $\langle h_i \rangle$, and drives the system towards a FE-RFE transition, even if $\langle h_i \rangle = 0$ initially (e.g. PSN with perfect chemical order has $\langle h_i \rangle = 0$).

COMPUTATIONAL METHODS

Simulations were performed using the first-principle effective Hamiltonian, H_{eff} , which is described in detail in [10]; H_{eff} is an expansion of the potential energy of PSN in a Taylor series about a high-symmetry perovksite reference



Figure 2. Predicted PSN phase diagrams: (a) pressure vs. reduced temperature [9]; (b) [Pb–O] divacancy concentration vs. reduced temperature. Dashed lines indicate ferroelectric-relaxor transitions. Dotted lines indicate Burns temperatures, T_B [23]. Triangles indicate upper- and lower-bounds, u- and l- respectively. The diagrams are topologically equivalent because both P and $X_{[Pb-O]}$ tune the delicate balance between FE well depth (increasing P reduces well depths) and the spatial average strength of the "random fields," $<h_i >$, that promote the relaxor state. (See Color Plate VI)

structure. It includes those degrees of freedom relevant to ferroelectric phase transitions:

$$\begin{split} H_{e\!f\!f} &= \mathrm{H}(\{ \raisebox{-1.5mm}{\boxtimes} I\}) + \mathrm{H}(e_{\mathfrak{SQ}}) + \operatorname{Psi}({\mathbb{S}}^{\mathfrak{SQ}}) \operatorname{PV} + H(\{ \raisebox{-1.5mm}{\boxtimes} I\}, \{\bullet_l\}, \{$$

where \mathbb{Z}_i represents Pb-site centered local polar distortion variables; $e_{\mathcal{D}\mathcal{A}}$ is the homogeneous strain term; $H(\{\mathbb{Z}_i\}, e_{\mathcal{D}\mathcal{A}}, \mathcal{D}\}$ is a strain coupling term; and *PV* the standard pressure-volume term. The first four terms are sufficient to model pressure-dependent phase transitions in a normal FE perovskite [17]. The fifth term, $H(\{\mathbb{Z}_i\}, \{^{t}_i\}, \{Pb-O\}\} \mathcal{D}$, represents coupling between polar variables and "random" local fields, $\langle \mathbf{h}_i \rangle = [10,18,19]$ from: 1) screened electric fields from the quenched distribution of Sc³⁺ and Nb⁵⁺ ions ($^{t}_i$; and 2) randomly distributed nearest neighbor (NN) Pb-O divacancy pairs, [Pb-O].

Further details of the simulations used to calculate Fig. 2 are given in: the review by Burton et al. [10]; the study of P-effects [9]; and the first-principles calculation of the dipole moment for a [Pb–O] NN divacancy pair in PbTiO₃ [8]. In Tinte et al. [9] the simulation supercell contained $40 \times 40 \times 40$ Pb-site local mode variables in a "nano-ordered" chemical configuration of 20 ordered 800-site clusters, in a percolating random matrix which (for accounting purposes only) was subdivided into 60 disordered clusters. The same simulation cell is used here, except that $(40^3)X_{[Pb-O]}$ randomly selected local mode variables are replaced by dipole moments corresponding to NN [Pb–O] divacancy pairs. This



Figure 3. Predicted cluster-cluster spin products for a nano-ordered system with (a) $X_{[Pb-O]} = 0.02$ and (b) $X_{[Pb-O]} = 0.03$. Vertical lines indicate T_{FE} and T_B , the ferroelectric transition temperature and the Burns temperature [20], respectively. Increasing $X_{[Pb-O]}$ increases the relaxor interval and, drives the ferroelectric-relaxor transition to lower temperature. (See Color Plate VII)

treatment is distinct from Bellaiche et al. [7] which considered [Pb]-vacancies without charge-compensating [O]-vacancies; presumably the real system has both [Pb]- and [O]-vacancies as reported by Chu et al. [3].

RESULTS AND DISCUSSION

The simulations predict a significantly steeper slope for the FE-RFE transition than is observed experimentally. A possible explanation is that the populations of second- and possibly farther- neighbor divacancy pairs are significant, and that a realistic representation would include local electric fields induced by [Pb]- and [O]-vacancies and by closely bound [Pb-O] divacancy pairs. In fact, Vienna abinitio simulation package with projector aumented wave potentials and a generalized gradient approximation for the exchange/correlation potential [20] calculations for NN and next-NN (NNN) [Pb–O] divacancy pairs in a $2 \times$ 2×2 supercell (40 atoms for PSN; 38 atoms with a divacancy) indicate that NNN divacancies are actually ~0.016 eV lower in energy than NN divacancies (Fig. 1; Table 1).

There are two plausible relations from which to estimate formation energies for the NN and NNN divacancy pairs:

1. $\P E_f = E(Pb_7Sc_4Nb_4O_{23}) + E(\mathfrak{O} - PbO) - E(Pb_8Sc_4Nb_4O_{24}).$

2. $\Re E_f = E(Pb_7Sc_4Nb_4O_{23}) - (7/8)E(Pb_8Sc_4Nb_4O_{24}) - (1/2)E(ScNbO_4)$ Initial structures for \mathfrak{D} -PbO and Wolframite-structure ScNbO₄ were taken from [21] and [22] respectively (the CdWO₄ structure in their Table II).

Table 1

Formation energies and formation volumes of nearest- and next-nearestneighbor [Pb-O] divacancy pairs in a chemically ordered $Pb_8Sc_4Nb_4O_{24}$ supercell.

| | Relation 1 | | Relation 2 | |
|---|---|------------------------------------|--|---|
| System NN [Pb-O] divacancy NNN [Pb-O] divacancy | $\begin{array}{c} \Delta \mathrm{E}_{f}(\mathrm{eV}) \\ 1.54 \\ 1.40 \end{array}$ | $\Delta V_f (A^3)$ 37.6 34.9 | $\begin{array}{c} \Delta \mathrm{E}_{f} \ \mathrm{(eV)} \\ 1.51 \\ 1.38 \end{array}$ | $\begin{array}{c} \Delta \mathrm{V}_{f} \ \mathrm{(A^{3})} \\ 43.6 \\ 40.8 \end{array}$ |

Munkhorst-Pack k-point meshes were used: $10 \times 10 \times 8 \ \mathfrak{S}$ -PbO; $6 \times 6 \times 6 \operatorname{ScNbO_4}$; $4 \times 4 \times 4$ for Pb₈Sc₄Nb₄O₂₄ and Pb₇Sc₄Nb₄O₂₃ supercells. All calculations were done with an energy cuttoff of 500 eV, and all were fully relaxed. The (very similar) results from both are listed in Table 1 with corresponding volumes of formation, $\mathfrak{P}V_f$.

The results presented in Table 1 indicate that our NN divacancy approximation is an oversimplification, because $\mathscr{P}E_f(NN) > \mathscr{P}E_f(NNN)$. Thus, a realistic treatment would at least include about equal concentrations of NN- and NNNdivacancies, and probably isolated [Pb] and [O] vacancies as well, with the precise distribution depending on temperature. That said, there is no obvious reason to believe that a more realistic model for the vacancy distribution would yield qualitatively different results.

Calculated P vs. T/T_{FE} and $X_{[Pb-O]}$ vs. T/T_{FE} diagrams are plotted in Figs. 2a and 2b, respectively. Dashed lines indicate FE-RFE transitions, and dotted lines indicate Burns temperatures, T_B [20]. Qualitatively, the only apparent (small) difference between Figures 2a and 2b is that the RFE-FE transition in Fig. 2a is approximately linear, while in Fig. 2b it exhibits slight negative curvature.

As in the P-dependent simulations, cluster-cluster spin products were calculated for 800-site clusters (Figs. 3): O–O are the products between average spins on two chemically ordered clusters; O–D are products between one chemically ordered and one chemically disordered cluster; and D–D the products between two chemically disordered clusters. These results are analogous to those from P-dependent simulations, in that they exhibit the same hierarchy of correlations: O–O > O–D > D–D. Also, as $X_{[Pb-O]}$, and therefore $\langle h_i \rangle$, is increased, the RFE-state region grows, mostly at the expense of the FE-phase.

CONCLUSIONS

Directly increasing local "random fields", $\langle h_i \rangle$, by increasing X_[Pb-O], enlarges the RFE-state region and ultimately drives the system into a fully relaxor

state. This progression mirrors the phenomenology of PSN under increasing hydrostatic pressure. The essential difference is that $X_{[Pb-O]}$ directly increases $\langle h_i \rangle$, whereas increasing pressure makes FE well depths shallower, which corresponds to an thus *indirect* increase in $\langle h_i \rangle$, relative to FE well depth.

REFERENCES

- G. A. Smolensky and A. I. Agranovskaya, Sov. Phys. Sol. State 1, 1429 (1959).
- 2. L. E. Cross, Ferroelectrics 76, 241 (1987).
- 3. F. Chu, I. M. Reaney, and N. Setter, J. Appl. Phys. 77[4], 1671 (1995).
- 4. F. Chu, N. Setter, and A. K. Tagantsev, J. Appl. Phys. 74[8], 5129 (1993).
- F. Chu, I. M. Reaney, and N. Setter, J. Amer. Ceram. Soc. 78[7], 1947 (1995).
- 6. F. Chu, G. Fox, and N. Setter, J. Amer. Ceram. Soc. 81(6) 1577 (1998).
- L. Bellaiche, J. Iniguez, E. Cockayne, and B. P. Burton, *Phys. Rev. B* 75, 014111 (2007).
- 8. E. Cockayne and B. P. Burton, Phys. Rev. B 69, 144116 (2004).
- S. Tinte, B. P. Burton, E. Cockayne, and U. V. Waghmare, *Phys. Rev. Lett.* 97, 137601 (2006).
- B. P. Burton, E. Cockayne, S. Tinte, and U. V. Waghmare, *Phase Trans.* 79, 91 (2006).
- 11. J. M. Kosterlitz, D. R. Nelson, and M. E. Fisher, *Phys. Rev. B*, **13**, 412 (1976). "A nonordering field [g] alters nonuniversal critical parameters, like critical-point energies specific heat, and spontaneous order amplitudes, but does *not* change the basic nature of the critical point so that, in particular, universal quantities such as critical exponents do not vary with g".
- E. L. Venturini, R. K. Grubbs, G. A. Samara, Y. Bing, and Z.-G. Ye, *Phys. Rev. B* 74, 064108 (2006).
- R. E. Cohen, Nature (London) 358, 137 (1992), Also, R. E. Cohen and H. Krakauer, *Ferroelectrics*. 136 no.1–4 65 (1992)
- G. Saghi-Szabo, R. E. Cohen, and H. Krakauer, *Phys. Rev. Lett.* 80, 4321 (1998).
- 15. M. Fornari and D. Singh, Phys. Rev. B 63, 092101 (2001).
- G. A. Samara, *Phys. Rev. Lett.* **77**, 314 (1996); *J. Appl. Phys.* **84**, 2538 (1998); in *Fundamental Physics of Ferroelectrics 2000*, edited by R. E. Cohen (American Institute of Physics, New York, 2000), p. 344; *J. Phys. Condens. Matter* **15**, R367 (2003).
- W. Zhong, D. Vanderbilt, and K. M. Rabe, *Phys. Rev. Lett.* **73**, 1861 (1994);
 K. M. Rabe and U. V. Waghmare, *Phys. Rev. B* **52**, 13236 (1995);
 U. V. Waghmare and K. M. Rabe, *Phys. Rev. B* **55**, 6161 (1997).

- U. V. Waghmare, E. Cockayne, and B. P. Burton, *Ferroelectrics* 291, 187 (2003).
- 19. B. P. Burton, U. V. Waghmare, and E. Cockayne, TMS Letters, 1, 29 (2004).
- G. Kresse and J. Hafner, *Phys. Rev. B* 47, RC558 (1993); G. Kresse, Thesis, Technische Universitat Wien, 1993; G. Kresse and J. Furthmuller, *Comput. Mat. Sci.* 6, 15 (1996); G. Kresse and J. Furthmuller, *Phys. Rev. B* 54, 11169 (1996).
- 21. G. W. Watson, S. C. Parker, and G. Kresse, Phys. Rev. B 59, 8481 (1999)
- Y. Abarham, N. A. W. Holzwarth, and R. T. Williams, *Phys. Rev. B* 62, 1733 (2000)
- 23. G. Burns and F. H. Dacol, Solid State Commun. 48, 853 (1983).