

in southeastern South America have interannual cycles (at about 3.5 and 6 yr), a near-decadal cycle with period of approximately 9 yr, as well as a nonlinear trend. Genta et al. (1998) demonstrate that the 30-yr running averaged streamflows increased after the mid-1960s at a rate that is approximately linear but not the same in all rivers. Also, the increased streamflow is consistent with a significant decrease in the amplitude of the seasonal cycle in all rivers.

Analyzing interannual variability Camilloni and Barros (2000), Berri et al. (2002), Camilloni and Barros (2003) indicate that this kind of variability is linked with El Niño – Southern Oscillation (ENSO). Berbery and Barros (2002) shown that the historical maxima of river discharge during the year following the onset of El Niño can triple the typical mean river discharge.

The aim of this paper is two-fold: on the one hand, to analyze the runoff series for Paraná and Uruguay rivers at several gauge stations, and to study the behavior of monthly negative as well as positive anomalies along with the frequency distribution of the annual frequency for this anomalies, their extreme values, and the spells of extreme values in order to establish the presence of transference functions both for rainfall and discharge. On the other hand, to estimate the homogeneity and representativeness of the measurements for a single river at different gauge stations and for both rivers jointly were studied. Also that allows to assess on the joint risks for extreme anomalies in runoff occurrence. A more general goal of this work is to diagnose extreme minimum and maximum runoff and their joint occurrence. An example of the potential relation between the functions of extreme runoff and precipitation can be found in Vargas and Bischoff (2000).

In this paper the compatibility of the models that adjust the properties of the monthly rainfall and monthly streamflows are analyzed. Section 2 presents the methods and data used for the study. Monthly runoff anomalies frequency and extreme anomalies are presented in Sect. 3. Section 4 shows the spatial behavior of the entropy and evaluates the joint risk of extreme anomalies. The temporal variability of the monthly runoff are anomalies are presented in Sect. 5. Finally, Sect. 6 summarizes the main

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conclusions.

2 Methodology and data management

Data used consist in mean monthly flows, collected at four gauge stations in the Paraná River and other four in the Uruguay River. Gauge station information is shown in Table 1. Data were provided by Water Resources Secretary (www.hidricosargentina.gov.ar). Besides, monthly precipitation data obtained by the National weather service of Argentina (SMN) was also used for the Paraná basin (see Table 2). Figure 1 shows the basins for both rivers and the position of the gauge stations.

Both for runoff and precipitation monthly anomalies were calculated. By this way the most part of the influence of the annual wave was eliminated. Monthly positive (negative) anomalies are defined as positive (negative) values regarding monthly mean value. Extreme monthly positive (or negative) anomalies are defined as those anomalies included within the seventh to tenth (first to third) deciles. The variable to study is the frequency of same sign anomalies for any year. The spell of monthly anomalies is defined by the monthly sequence of anomalies with the same sign.

3 Monthly runoff anomalies frequency per year

For each gauge station the number of positive and negative anomalies per year was calculated separately. Figure 2 show the frequency distributions for the negative (positive) anomalies for both rivers. As shown in Fig. 2 it can be stated that the selected gauge stations for each river possess similar statistical structures in terms of the occurrence of both, positive and negative anomalies. Perhaps the exception is the Paraná Túnel gauge station where the yearly anomalies are lesser than in the other gauge stations. For monthly positive as well as negative anomalies it can be seen that Uruguay River show a very distinctive main maximum and two secondary maxima. Negative

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This could be associated to different precipitation drainage processes for both rivers. In the case of the Paraná River this processes seems to be slower, even for intense rainfall associated to synoptic weather systems during several days within its basin, establishing differences in the number of monthly spells, in particular those associated to 1 and 2 months. This is not the case for the Uruguay River since the draining processes for this river are very sensitive to precipitation associated with synoptic-scale weather systems, or even with shorter timescales.

Major duration for positive spells can be found in the Paraná River with one event of 16 consecutive months and can be identified at all the gauge stations simultaneously. Particularly for the Uruguay River the maximum positive spell corresponds to 7 months, also identified at all the gauge stations. This entails an important difference regarding the behaviour of the two rivers. As to the negative spells, the long-lasting ones (those lasting at least 13 or 14 months) can be found at both rivers, although detected at isolated gauge stations. In summary, at least for both studied basin extreme positive spells affect the river basin as a whole, while the extreme negative spells are more regional and cannot be extended to the whole basin. Finally, frequency distributions for the spells of extreme monthly anomalies are similar to the frequency distributions for extreme monthly anomalies per year. This would indicate that the monthly extreme anomalies have a high probability of occurring in one month

20 4 Entropy and joint diagnosis

To analyse persistence and to assess on the difficulties to forecast these individual events with a model, the randomness features for the monthly flow were also investigated in this research. This was done with the aid of the concept of entropy (Shannon, 1948). Entropy for a set Z is defined as

$$25 \quad H(Z) = \sum_i P(A_i) \ln P(A_i) \quad (1)$$

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where A_i are disjoint events within the space of occurrence with probability

$$P(A_1, A_2, A_3, \dots, A_r) = 1 \quad (2)$$

$H(Z)$ measures randomness for the individual random events. From Eq. (1) it can be seen that the highest amount of uncertainty from an information source is realized when the output symbols of the source are equally probable. The entropy varies from 0 to $\log(m)$, so the entropy may be standardized such that it would range from 0 to 1 by dividing it by its maximum.

In this case, the individual events are the monthly flows. Table 4 show entropy for the gauge stations at both rivers. Greater entropy corresponds to CR, located northeast of Argentina, in the confluence of Paraná and Paraguay rivers. Comparing the results presented in Table 4 it can be seen that the Uruguay River presents higher values of entropy for all the gauge stations, indicating a greater variability in the monthly flows. This means that if an adjustment of a forecast model to the Uruguay River monthly flows is intended, it requires more information and a much more complex model.

15 4.1 Analysis of the partial spatial coherence

In order to complete the verification of the homogeneity of the anomalies structure for each river and to consider the spatial and temporal coherence, the correlations between the series of monthly anomalies of runoff were calculated. Tables 5 and 6 show cross-correlations for the time series of monthly anomalies between the gauge stations in the Uruguay and Paraná rivers.

Despite all the correlations are significant, these are greater for the Uruguay River. In other words, this imply a greater homogeneity for the monthly runoff anomalies in the Uruguay River, a fact that can be due to the greater number of tributaries Paraná River has, many of them affected by different regimes. Under the light of the results presented here the time series from any gauge station represents well the behavior of the anomalies for the whole river basin.

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Table 1. Gauge stations of Uruguay and Paraná rivers.

Code	Gauge station	Abbreviation	River	Period	Latitude	Longitude
1	Santo Tomé	ST	Uruguay	1908–1998	–28.50	–56.01
2	Monte Caseros	MC	Uruguay	1908–1989	–30.25	–57.63
3	Paso de los Libres	PL	Uruguay	1908–1988	–29.72	–57.07
4	Concordia	CO	Uruguay	1898–1998	–31.30	–58.01
5	Posadas	PO	Paraná	1901–1990	–27.37	–55.97
6	Itatí	IT	Paraná	1911–2000	–27.28	–58.24
7	Corrientes	CR	Paraná	1904–2000	–27.45	–58.82
8	Paraná Túnel	TU	Paraná	1904–1994	–31.70	–60.51

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Table 2. Posadas precipitation station.

Station	Abbreviation	start year	end year	Latitude	Longitude
Posadas	PO	1901	1991	-27.22	-55.58

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Table 3. Frequency and duration of extreme (a) Negative and (b) Positive monthly anomalies spells at the eight Paraná and Uruguay rivers gauge stations.

DURATION (MONTHS)	Extreme Positive Spells (1911–1989)								
	Túnel	Itati	Itacua	Corrientes	Posadas	S. Tomé	Paso	Concordia	Caseros
1	739	645	746	736	716	696	685	704	695
2	21	29	36	22	34	48	38	39	45
3	16	16	17	20	16	18	25	26	21
4	15	8	9	15	11	11	10	8	7
5	2	4	3	4	7	1	2	2	3
6	3	–	2	–	1	1	1	4	1
7	1	–	1	–	2	2	2	2	3
8	–	1	–	1	1	2	1	–	–
9	–	–	–	1	–	2	2	1	2
10	–	2	1	–	1	–	–	–	–
11	1	–	–	–	–	–	–	–	–
12	–	–	–	1	–	–	–	–	–
13	–	–	–	–	–	–	–	–	1
14	1	–	–	–	–	–	–	–	–
1	774	648	790	781	784	777	757	775	758
2	20	29	36	26	36	43	44	43	44
3	6	9	11	11	10	16	18	18	19
4	11	9	2	7	3	4	4	4	6
5	5	5	6	3	7	3	2	1	3
6	3	1	–	4	–	–	–	1	–
7	2	1	–	–	–	1	1	1	1
8	–	1	–	–	–	–	–	–	–
9	–	–	–	–	–	–	–	–	–
10	–	–	–	–	–	–	–	–	–
11	–	–	–	–	–	–	–	–	–
12	–	–	–	–	–	–	–	–	–
13	–	–	–	–	–	–	–	–	–
14	–	–	–	–	–	–	–	–	–
15	–	–	–	–	–	–	–	–	–
16	1	1	1	1	1	–	–	–	–

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Table 4. Entropy calculated according Eq. (1) at each of the gauge stations.

Paraná River				
IT	PO	IT	CR	TU
1.64	1.65	1.48	2.14	1.82
Uruguay River				
ST	MC	CO	PL	
2.18	2.78	2.76	2.67	

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Table 5. Cross-correlations for the time series of anomalies between the gauge stations of the Uruguay river. The colored values are significant at 5%.

	ST	MC	PL	CO
ST	1.00	0.91	0.95	0.89
MC	0.91	1.00	0.98	0.98
PL	0.95	0.98	1.00	0.97
CO	0.89	0.98	0.97	1.00

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Table 6. As in Table 4 but for the Paraná river. Colored values are significant at 5%.

	PO	IT	CR	TU
PO	1.00	0.83	0.93	0.75
IT	0.83	1.00	0.84	0.79
CR	0.93	0.84	1.00	0.89
TU	0.75	0.79	0.89	1.00

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Table 7. Joint frequency for Minimum runoff between stream water gauge stations in both rivers in percentage for 0 to 4. Grey cells indicate joint probabilities greater than 10%.

		Uruguay				
Gauge station		0	1	2	3	4
PARANÁ	0		9.7	3.0	4.0	12.0
	1	10.4	0.3	0.3	1.0	3.0
	2	9.0	0.7	0.7	1.3	1.0
	3	9.4	1.7	0.3	0.3	4.3
	4	15.4	1.3	1.0	1.0	8.7
						299 months

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Table 8. Joint frequency for Maximum runoff between stream water gauge stations in both rivers in percentage for 0 to 4. Grey cells indicates joint probabilities greater than 10%.

		Uruguay				
Gauge station		0	1	2	3	4
PARANÁ	0		6.9	4.0	8.4	12.9
	1	13.9	1.5	1.5	2.0	2.5
	2	6.4	0.0	0.5	1.0	4.5
	3	11.4	2.0	1.0	2.5	7.4
	4	5.9	1.0	0.0	1.0	2.0
						202 months

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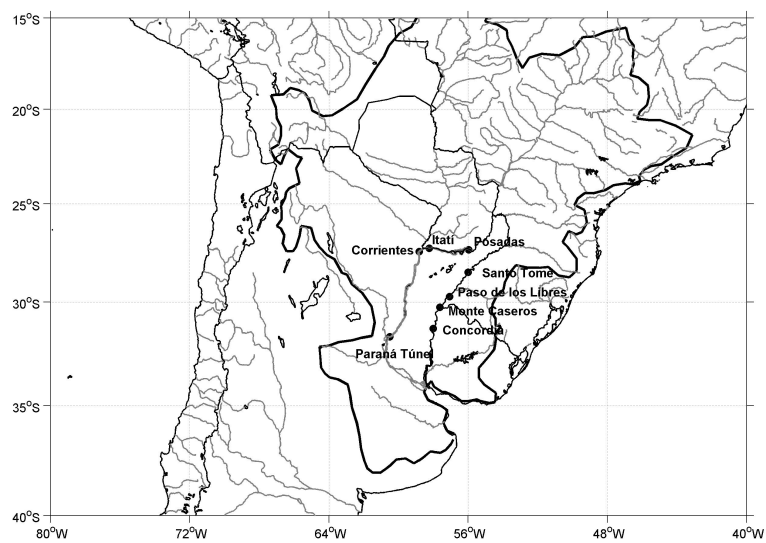


Fig. 1. La Plata Basin and the position of the gauge stations for both rivers according to code at Table 1.

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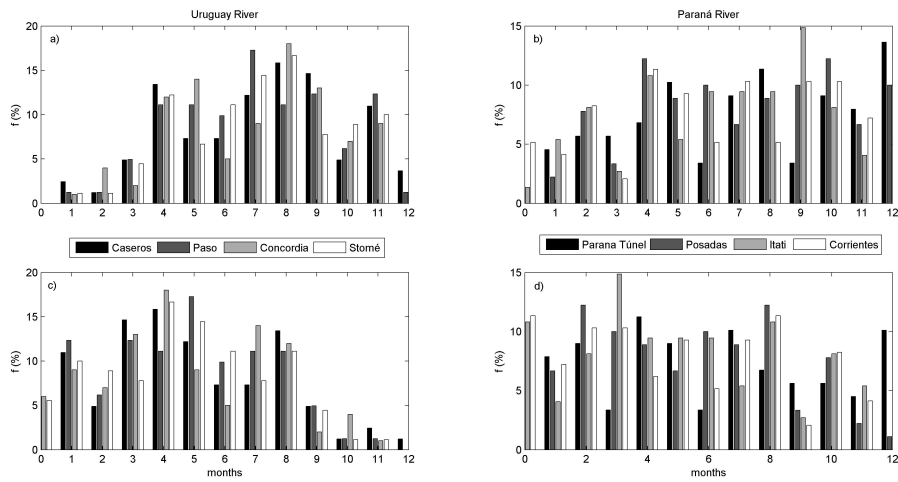


Fig. 2. Frequency percentage for the negative yearly anomalies (upper panel) and positive anomalies (lower panel) in Uruguay River (a), (c) and Paraná River (b), (d).

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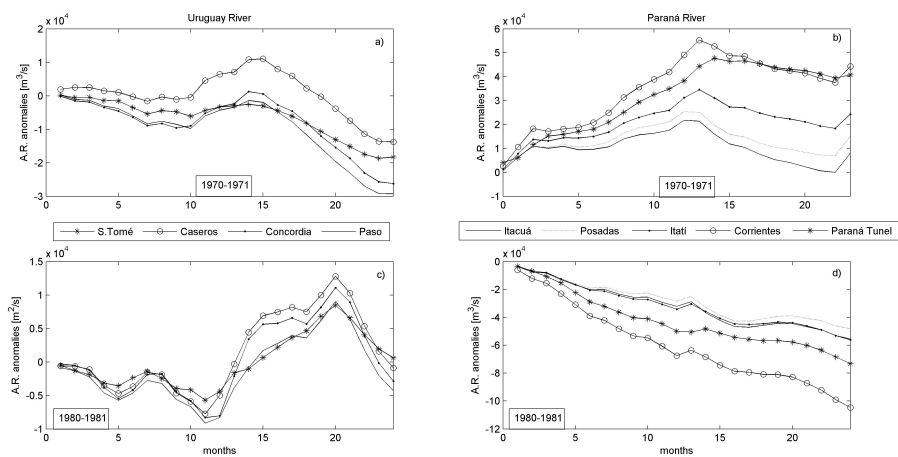


Fig. 3. Accumulated runoff monthly anomalies during 1970–1971 period (upper panel) and 1980–1981 period (lower panel) at Uruguay River (a), (c) and Paraná River (b), (d).

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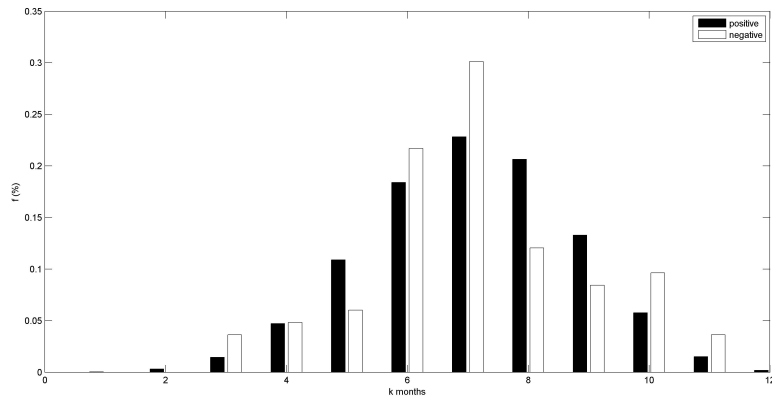


Fig. 4. Relative frequency distribution of positive (black) and negative (white) monthly anomaly precipitation at Posadas station, located in the Paraná River.

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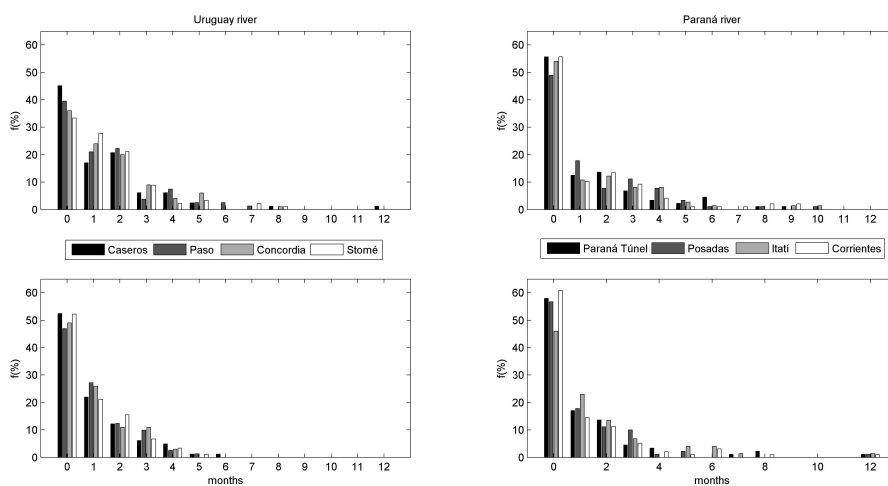


Fig. 5. Frequency in percentage of negative (upper panel) and positive (lower panel) extreme anomalies per year in the Uruguay River (left panel) and Paraná River (right panel).

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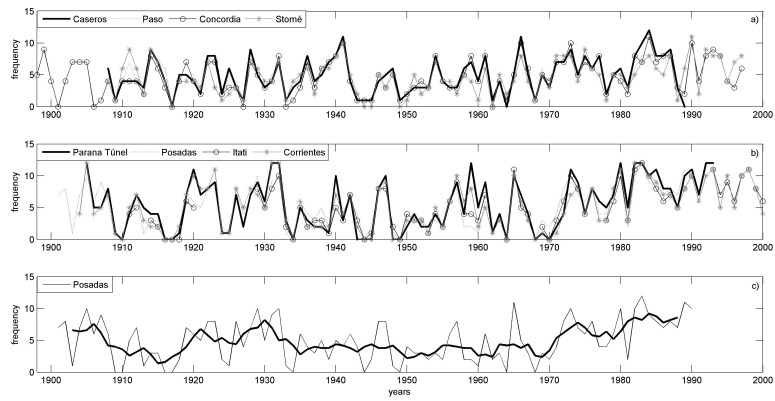


Fig. 6. Interannual variability of the positive anomalies frequency of runoff at Uruguay River **(a)**, Paraná River **(b)** and positive precipitation anomalies frequency and moving average at Posadas station **(c)**.