

The impact of Coulomb diffusion of ions on the pulsational properties of DA white dwarfs

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ABSTRACT

Context. Element diffusion is a key physical process that substantially impacts the superficial abundances, internal structure, pulsation properties, and evolution of white dwarfs.

Aims. We study the effect of Coulomb separation of ions in the cooling times of evolving white dwarfs, their chemical profiles, the Brunt-Väisälä (buoyancy) frequency, and the pulsational periods at the ZZ Ceti instability strip.

Methods. We follow the full evolution of white-dwarf models in the range $0.5 - 1.3 M_{\odot}$ derived from their progenitor history on the basis of a time-dependent element diffusion scheme that incorporates the effect of gravitational settling of ions due to Coulomb interactions at high densities. We compare the results for the evolution and pulsation periods of ZZ Ceti stars with the case where this effect is neglected.

Results. We find that Coulomb sedimentation profoundly alters the chemical profiles of ultra-massive ($M_{\star} \gtrsim 1M_{\odot}$) white dwarfs along their evolution, preventing helium from diffusing inward toward the core, and thus leading to much narrower chemical transition zones. As a result, significant changes in the g -mode pulsation periods as high as 15% are expected for ultra-massive ZZ Ceti stars. For less-massive white dwarfs, the impact of Coulomb separation is much less noticeable, inflicting period changes in ZZ Ceti stars that are below the period changes that result from uncertainties in progenitor evolution, albeit larger than typical uncertainties of observed periods.

Conclusions. Coulomb diffusion of ions profoundly affects the diffusion flux in ultra-massive white dwarfs, driving the gravitational settling of ions with the same A/Z (mass to charge number). We show that it strongly alters the period spectrum of such white dwarfs, which should be taken into account in detailed asteroseismological analyses of ultra-massive ZZ Ceti stars.

Key words. stars: evolution — stars: interiors — stars: white dwarfs — stars: oscillations (including pulsations)

1. Introduction

Element diffusion is a key physical process that may substantially modify the superficial abundances, internal chemical structure, pulsation properties, and evolution of a large variety of stars at different evolutionary stages, including our Sun (see Michaud et al. 2015). Because of their extremely large gravities, this is particularly true in the case of white-dwarf (WD) stars, for which diffusion driven by gravity is responsible for the purity of the outer layers that characterizes most of these stars (see Winget & Kepler 2008; Althaus et al. 2010; Córscico et al. 2019a, for reviews). Also, at the chemical interfaces of these stars, characterized by large composition gradients, chemical diffusion tends to dominate over diffusion driven by gravity, thus strongly smoothing out the chemical profiles during WD evolution, which have consequences for the predicted pulsational properties of these stars. Earlier studies by the La Plata Group demonstrated the necessity of a proper treatment of element diffusion for an assessment of the adiabatic oscillation properties of pulsating WDs and the mode-trapping features produced by the outer chemical transition regions (see Córscico et al. 2002; Althaus & Córscico 2004). Also, diffusion processes are at the root of the occurrence of diffusion-induced novae, i.e., WDs that under certain circumstances experience a thermonuclear flash induced by chemical diffusion that carries hydrogen (H) to deeper and hotter layers (Miller Bertolami et al. 2011). Finally, gravitational settling of

minor species such as ^{22}Ne in the carbon/oxygen (CO) core of WDs releases enough energy so as to impact substantially the cooling times of WDs (Deloye & Bildsten 2002; García-Berro et al. 2010).

Chang et al. (2010) and Beznogov & Yakovlev (2013) have studied the diffusion process in strongly-coupled Coulomb plasmas. In particular, Beznogov & Yakovlev (2013) have explored the diffusion currents for strongly-coupled Coulomb mixtures of ions in dense stellar matter typical of compact stars such as WDs and neutron stars. These authors extended the work of Chang et al. (2010) to the case of non-equilibrium mixtures, and showed that Coulomb separation affects the diffusion flux in WDs, driving the gravitational settling of ions with the same A/Z (mass to charge number). Indeed, in such mixtures, the contribution of gravity and induced electric field to sedimentation is negligible, and the effect of Coulomb separation becomes relevant. They find that ions with larger Z move to deeper layers, being this effect stronger for a larger difference of Z in the mixture and for larger gravities, i.e., massive WDs. In a more recent paper, Koester et al. (2020) have implemented the Coulomb corrections following Beznogov & Yakovlev (2013) to study the problem of carbon dredge-up in helium (He)-rich WDs.

Beznogov & Yakovlev (2013) suggest that the redistribution of ions due to Coulomb separation could affect the thermal evolution of WDs and their pulsational properties, thus impacting

the predictions of asteroseismology. Our paper is aimed at precisely studying the impact of Coulomb separation of ions on the evolution and pulsations of ZZ Ceti stars. These pulsating stars are H-rich (DA spectroscopic class) WDs with $10\,400\text{ K} \lesssim T_{\text{eff}} \lesssim 12\,400\text{ K}$ and $7.5 \lesssim \log g \lesssim 9.1$, characterized by multi-periodic luminosity variations due to g (gravity)-mode pulsations (see Córscico et al. 2019a, for a recent review). In particular, ultra-massive ZZ Ceti stars —where Coulomb separation of ions would be more relevant and the impact on their pulsation periods could be larger— have been reported (Kanaan et al. 2005; Castanheira et al. 2010, 2013; Hermes et al. 2013; Curd et al. 2017; Rowan et al. 2019). Specifically, we study here the evolution of WD models with masses in the range $0.5 - 1.3 M_{\odot}$ derived from their progenitor history. The WD mass values cover the range of relevant stellar masses expected for these stars. We consider a time-dependent element diffusion scheme that incorporates the gravitational settling term due to Coulomb interactions at high densities. We assess the impact of Coulomb separation on the cooling times of our WD models and on their chemical profiles, Brunt-Väisälä frequency, and pulsational periods. The paper is organized as follows. In Sect. 2 we describe the input physics of our stellar models, in particular the modification to our treatment of element diffusion to include the Coulomb interaction effect. In that section we also discuss the impact of Coulomb sedimentation on the evolving chemical profiles. In Sect. 3 we describe the impact of Coulomb diffusion on the pulsational properties of DA WDs. Finally, in Sect. 4 we summarize the main findings of the paper.

2. Input physics and white dwarf models

2.1. Numerical codes

The pulsational properties of the WD models presented in this work are based on the evolutionary models provided by the LPCODE stellar evolution code. This code has been amply used and tested in numerous stellar evolution contexts of low-mass and, particularly WD stars (see Althaus et al. 2003, 2005; Salaris et al. 2013; Althaus et al. 2015; Miller Bertolami 2016; Silva Aguirre et al. 2020; Christensen-Dalsgaard et al. 2020, for details). Specifically, LPCODE considers a full treatment of energy sources, including the energy contribution due to phase separation of core chemical species upon crystallization. The treatment of crystallization is based on the phase diagrams of Horowitz et al. (2010) for dense CO mixtures, and that of Medin & Cumming (2010) for ONe mixtures. Relevant for this work, LPCODE computes WD evolution in a self-consistent way with the changes in the internal chemical distribution that result from the mixing of all the core chemical components induced by the mean molecular weight inversion, element diffusion (see below), and phase separation of core chemical constituents upon crystallization (and the ensuing mixing in the layers above the crystallized core). Concerning this work, abundance changes during crystallization is a relevant issue in the case of pulsating ultra-massive ZZ Ceti stars that are expected to be mostly crystallized. In LPCODE, these abundance changes are assessed in a self-consistent way with WD evolution. Energy release resulting from ^{22}Ne sedimentation was not considered in this study.

For the pulsational analysis we use the LP-PUL pulsation code described in Córscico & Althaus (2006). This code employs the "hard-sphere" boundary conditions to account for the effects of crystallization on the pulsation spectrum of g modes. These conditions assume that the amplitude of the radial and horizontal eigenfunctions of g -modes is null below the solid/liquid inter-

face because of the non-shear modulus of the solid, as compared with the fluid region (see Montgomery & Winget 1999). The central boundary conditions are located at the mesh-point of the crystallization front (see Córscico et al. 2004, 2005; De Gerónimo et al. 2019; Córscico et al. 2019b). The Brunt-Väisälä frequency is computed as in Tassoul et al. (1990). The computation of the Ledoux term B includes the effects of having multiple chemical species that vary in abundance.

2.2. Diffusion treatment in a strongly coupled Coulomb plasma of ions

LPCODE considers a new full-implicit treatment of time-dependent element diffusion that includes thermal and chemical diffusion and gravitational settling (Althaus et al. 2020). In this work, we follow the diffusion for the isotopes ^1H , ^3He , ^4He , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , ^{17}O , ^{18}O , ^{19}F , ^{20}Ne , ^{22}Ne , ^{23}Na , and ^{24}Mg . Our treatment of diffusion is based on the formalism of Burgers (1969) that provides the diffusion velocities in a multi-component plasma under the influence of gravity, partial pressure, and induced electric fields. Here, diffusion velocities satisfy the set of $N - 1$ independent equations for ions¹:

$$\frac{dp_i}{dr} - \frac{\rho_i}{\rho} \frac{dP}{dr} - n_i Z_i e E = \sum_{j \neq i}^N K_{ij} (w_j - w_i), \quad (1)$$

where p_i , ρ_i , n_i , Z_i , and w_i denote, respectively, the ion partial pressure, mass density, number density, mean charge, and diffusion velocity for chemical species i . N is the number of ionic species plus electrons, e the charge unit and E the electric field. Resistance coefficients K_{ij} are from Paquette et al. (1986). This set of equations is solved together with the equations for no net mass flow $\sum_i A_i n_i w_i = 0$, with A_i being the atomic mass number, and no electrical current $\sum_i Z_i n_i w_i = 0$.

Using $dP/dr = -g\rho$ and $\rho_i = A_i n_i m_u$, Eq. (1) can be written as

$$\frac{1}{n_i} \sum_{j \neq i}^N K_{ij} (w_i - w_j) - Z_i e E = -A_i m_u g - \frac{1}{n_i} \frac{dp_i}{dr}, \quad (2)$$

where g is the gravitational acceleration and m_u the atomic mass. Diffusion velocities at each depth of the star are found as described in Althaus et al. (2020). To include the Coulomb interaction effect we proceed as in Koester et al. (2020) and Beznogov & Yakovlev (2013), and write

$$\frac{dp_i}{dr} = \frac{dp_i^{\text{ideal}}}{dr} + n_i \frac{d\mu_i^{\text{coul}}}{dr}, \quad (3)$$

where p_i^{ideal} and μ_i^{coul} are the ideal pressure and the chemical potential due to Coulomb interactions of ion i . μ_i^{coul} is given by Beznogov & Yakovlev (2013) as

$$\mu_i^{\text{coul}} = -0.9 \frac{Z_i^{5/3} e^2}{a_e}, \quad (4)$$

with $a_e = (4\pi n_e/3)^{-1/3}$ being the electron-sphere radius. Hence,

¹ For the sake of simplicity, we do not write here the equations that describe thermal diffusion.

$$\frac{dp_i}{dr} = \frac{dp_i^{\text{ideal}}}{dr} - n_i 0.3 \frac{Z_i^{5/3} e^2}{a_e} \frac{1}{n_e} \frac{dn_e}{dr}. \quad (5)$$

This treatment is justified in the regime of strong ion coupling. Coulomb sedimentation may be relevant in a mixture of ions with the same A/Z (such as ^4He , ^{12}C , and ^{16}O). We can illustrate this by simplifying the set of Eq. (2) to the case of two ion species ($i = 1, 2$). Assuming no temperature gradients and electron to have zero mass, the diffusion flux of ion 2 ($J_2 = \varrho_2 w_2$) can be expressed as the contributions from gravitational settling, Coulomb diffusion, and ordinary diffusion due to chemical gradients as

$$J_2 = J_2^{\text{grav}} + J_2^{\text{coul}} + J_2^{\text{diff}}, \quad (6)$$

where

$$J_2^{\text{grav}} = \varrho_2 \frac{\varrho_1 n Z_1 Z_2 D}{\varrho n_e K_B T} \left(\frac{A_1}{Z_1} - \frac{A_2}{Z_2} \right) m_u g, \quad (7)$$

$$J_2^{\text{coul}} = \varrho_2 \frac{\varrho_1 n D Z_1 Z_2}{n_e K_B T} g \left(Z_1^{2/3} - Z_2^{2/3} \right) \frac{0.3 e^2}{a_e P \gamma}, \quad (8)$$

and

$$J_2^{\text{diff}} = \frac{D m_1 m_2 n}{n_e \varrho} \left(n_2 Z_2 \frac{dn_1}{dr} - n_1 Z_1 \frac{dn_2}{dr} \right). \quad (9)$$

Here, D is the standard diffusion coefficient, $m_i = A_i m_u$, and $\gamma = \partial \ln P / \partial \ln \varrho^2$. Pressure has been assumed to be provided by strongly degenerate electrons. We note that Coulomb interaction contributes to the gravitational settling in such a way that ions with larger Z move to deeper layers. We note also that for plasmas made of a mixture of ^4He and ^{12}C , J_2^{grav} vanishes, and Coulomb separation should be important in driving gravitational settling of ions. This is particularly true in the case of more massive (and compact) WDs characterized by larger gravities (Beznogov & Yakovlev 2013). In fact, we will see that Coulomb sedimentation cannot be neglected in ultra-massive WDs. In the case of a WD envelope made of ^1H and ^4He , J_2^{grav} dominates and Coulomb separation constitutes a minor contribution to the settling of ions.

2.3. White dwarf models

To assess the impact of Coulomb diffusion, we have computed the WD evolution considering and disregarding the Coulomb interaction term in the diffusion equations. We consider four WD models extracted from the evolution of single progenitors with final stellar masses of 0.576, 0.833, 1.159 and 1.292 M_\odot . The starting 0.576 and 0.833 M_\odot WD configurations, characterized by CO cores, are H-burning post asymptotic giant branch (AGB) star models computed by Miller Bertolami (2016) from the full evolution of their progenitor stars with metallicity $Z=0.02$ and initial masses of 1.5 and 4.0 M_\odot , respectively. Such starting WD models are based on detailed and improved micro- and macro-physics processes involved in AGB and thermally-pulsing AGB

² Our expression for the diffusive flux is similar to that shown in Eqs.17-19 of Beznogov & Yakovlev (2013).

modeling, of relevance for the predicted internal composition of WDs. The starting 1.159 and 1.292 M_\odot ultra-massive WDs were taken from Camisassa et al. (2019). These WDs result from off-center carbon burning in the single-evolution scenario. Their progenitors experience a violent carbon-ignition phase followed by the development of an inward-propagating convective flame that transforms the CO core into a degenerate ONe one. Such WDs are composed of ^{16}O and ^{20}Ne —with traces of ^{23}Na and ^{24}Mg — (see Siess 2007, 2010). All of the WD models were evolved from the beginning of cooling track, where we performed the core mixing implied by the inversion of the mean molecular weight left by prior evolution, down to low effective temperatures, in a consistent way with abundances changes resulting from element diffusion, phase separation on crystallization, convective mixing and residual nuclear burning in the case of CO WD models.

The chemical profiles of our initial WD models are shown in Fig. 1 for some selected isotopes. The internal composition of WDs is a crucial aspect for the determination of the pulsational properties of these stars. The WD models shown in the figure correspond at the beginning of their cooling phase prior to the onset of element diffusion and after the core mixing due to the inversion of the mean molecular weight. Their core chemical structure reflects the nuclear burning and mixing history along progenitor evolution. We note that both the H and He contents of the WDs decrease with the stellar mass³. Also is noted the large abundance of ^{14}N in the He-rich buffer of the CO WD models, in particular for the 0.576 M_\odot WD model, reflecting the occurrence of appreciable third dredge-up. This model experiences a final thermal pulse at the very end of the thermally pulsing AGB phase that is responsible for larger surface carbon abundances (see Miller Bertolami 2016).

During WD cooling, element diffusion processes alter the chemical abundance distribution in the outer layers of all of the initial models. In the case of ultra-massive WDs, phase separation of the core chemical constituents upon crystallization modifies the shape of the ^{16}O and ^{22}Ne profiles. The resulting chemical profile by the time evolution reached the ZZ instability strip is shown in Fig. 2 at $T_{\text{eff}} = 11\,000$ K, which also illustrates the impact of Coulomb sedimentation on the chemical profiles. As discussed, Coulomb sedimentation is relevant for massive WDs and for mixtures of ions with equal A/Z . In this case, Coulomb separation drives gravitational settling (see Eqs. 6-9) and, thus, ions with larger Z move to deeper layers. We note that the H/He interface is not affected by Coulomb diffusion, since in this case the contribution due to gravity is dominant (Eq. 7), and Coulomb diffusion represents a minor contribution to the diffusion flux. We also note that for ultra-massive WDs, Coulomb sedimentation prevents the strong inward diffusion of He toward the core, leading to the formation of a pure-He buffer with the consequent appearance of two well separated chemical transition regions, one located at the base and the other at the top of that buffer. The neglect of Coulomb diffusion in ultra-massive WDs, on the contrary, causes chemical diffusion, which in this case is dominant (see Eq. 9), to virtually erode the initial pure He buffer, as illustrated by the figure. Consider, for example, the case of the 1.292 M_\odot model (upper panel of Fig. 2). When Coulomb diffusion is taken into account, there is the C/He interface located at $\log(1 - m_r/M_\star) \sim -5$, and the He/H interface, located at $\log(1 - m_r/M_\star) \sim -5.8$. On the contrary, for this model there is a single chemical transition region at $\log(1 - m_r/M_\star) \sim -5.8$

³ For the 1.292 M_\odot WD model, the H envelope was artificially imposed, without considering nuclear burning processes.

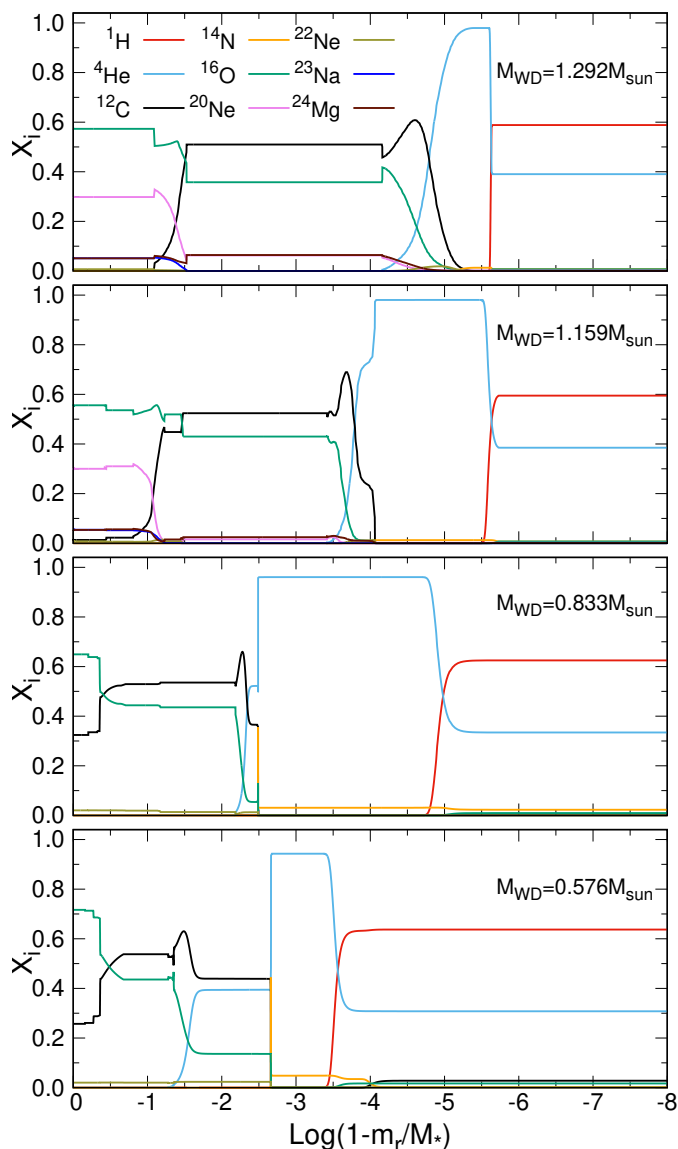


Fig. 1. Abundance by mass of ^1H , ^4He , ^{12}C , ^{14}N , ^{16}O , ^{20}Ne , ^{22}Ne , ^{23}Na , and ^{24}Mg versus the outer mass coordinate for our 0.576, 0.833, 1.159 and $1.292 M_{\odot}$ WD models at the beginning of the cooling track.

of ^{16}O , ^{12}C , ^4He and ^1H when Coulomb diffusion is neglected. Finally, we note that when we consider Coulomb diffusion, there is an internal chemical transition (located in the fluid part of the star, at $\log(1 - m_r/M_{\star}) \sim -3$) due to the variation of chemical abundances of ^{24}Mg , ^{20}Ne , ^{16}O , and ^{12}C . This chemical transition is virtually absent in the case in which Coulomb diffusion is neglected. As we shall see, all these differences impact the theoretical pulsational spectrum of these stars to some extent.

We also compare the resulting WD cooling times and find that the impact of Coulomb diffusion on the cooling times is minor, except for the $1.292 M_{\odot}$ WD sequence, which evolves about 6 % faster at low luminosities when Coulomb diffusion is considered. For the CO-core WD sequences, differences in the cooling times remain below 1 %.

3. Pulsation results

In this section, we assess the impact of Coulomb separation of ions on the predicted pulsation periods of our WD models. We

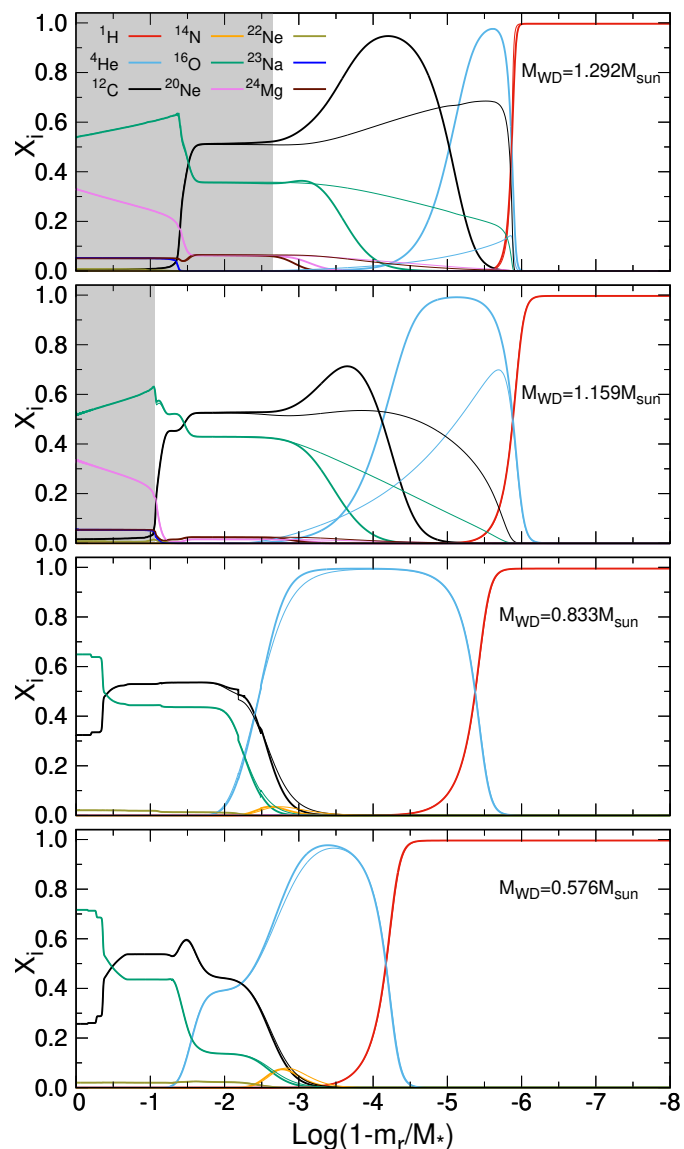


Fig. 2. Same as Fig. 1, but at an effective temperature of $T_{\text{eff}} = 11\,000$ K, corresponding to the domain of pulsating ZZ Ceti stars. Thick (thin) lines correspond to the case when Coulomb sedimentation of ions is considered (disregarded) in the diffusion equations. The gray area marks the domain of core crystallization.

begin by illustrating in Fig. 3 the changes in the run of the Brunt-Väisälä and Lamb frequencies induced by Coulomb sedimentation for all of our WD models at $T_{\text{eff}} = 11\,000$ K. In particular, the 1.16 and $1.29 M_{\odot}$ models start to crystallize before reaching the blue edge of the ZZ Ceti instability strip. In these cases, the gray area marks the domain of core crystallization. Any chemical interface located within the crystallized region has no relevance to the pulsation properties of the g modes, that is why we have hidden them under the gray area in the plots. The Brunt-Väisälä frequency reflects any change in chemical composition in the interior of the model. Indeed, there exist dominant bumps in the run of the Brunt-Väisälä frequency associated to the various chemical transition regions, particularly the H/He interface, which produces the most dominant feature in the Brunt-Väisälä frequency. We note that, in the case of the $1.292 M_{\odot}$ model computed with Coulomb diffusion, there exist two bumps, one of them due to the chemical transition region of C and He, and the

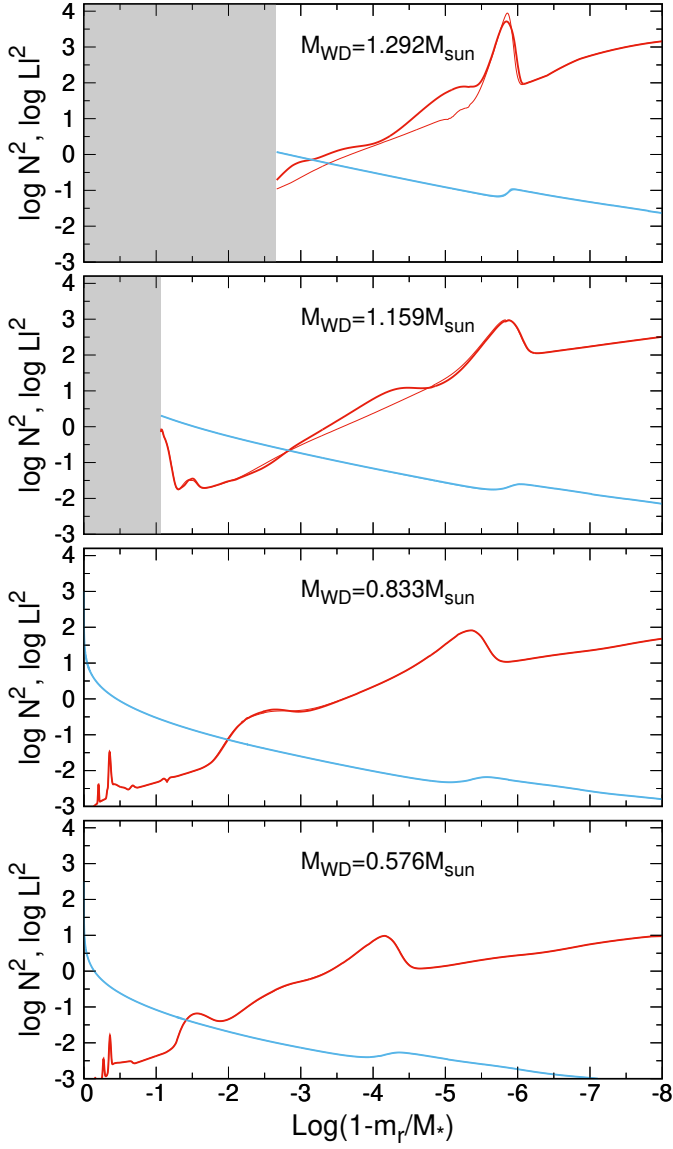


Fig. 3. Logarithm of the squared Brunt-Väisälä and Lamb frequencies (red and blue lines respectively) corresponding to the same models analyzed in Fig. 2 at $T_{\text{eff}} = 11\,000$ K. Thick (thin) lines correspond to the case when Coulomb sedimentation of ions is considered (disregarded) in the diffusion equations. The gray area marks the domain of core crystallization. The Lamb frequency corresponds to dipole ($\ell = 1$) modes.

other one associated to the He/H chemical interface (see Fig. 2). At variance with this, in the case in which Coulomb diffusion is neglected, there is a single bump in the Brunt-Väisälä frequency which is due to the chemical interface of O, C, He and H. On the other hand, there is an additional internal bump in the Brunt-Väisälä frequency at $\log(1 - m_r/M_*) \sim -3$ that is due to the multiple chemical transition region of ^{24}Mg , ^{20}Ne , ^{16}O , and ^{12}C (see also Fig. 2), which is absent in the case in which Coulomb diffusion is neglected. This bump is located in the fluid part of the star, that is, within the mode propagation zone, and therefore it has a non-zero impact on the mode trapping properties of g modes.

The shape of the Brunt-Väisälä frequency has a strong impact on the g -mode period spectrum and mode-trapping properties of pulsating WDs. In view of the above discussion about the Brunt-Väisälä frequency, we expect that Coulomb diffusion

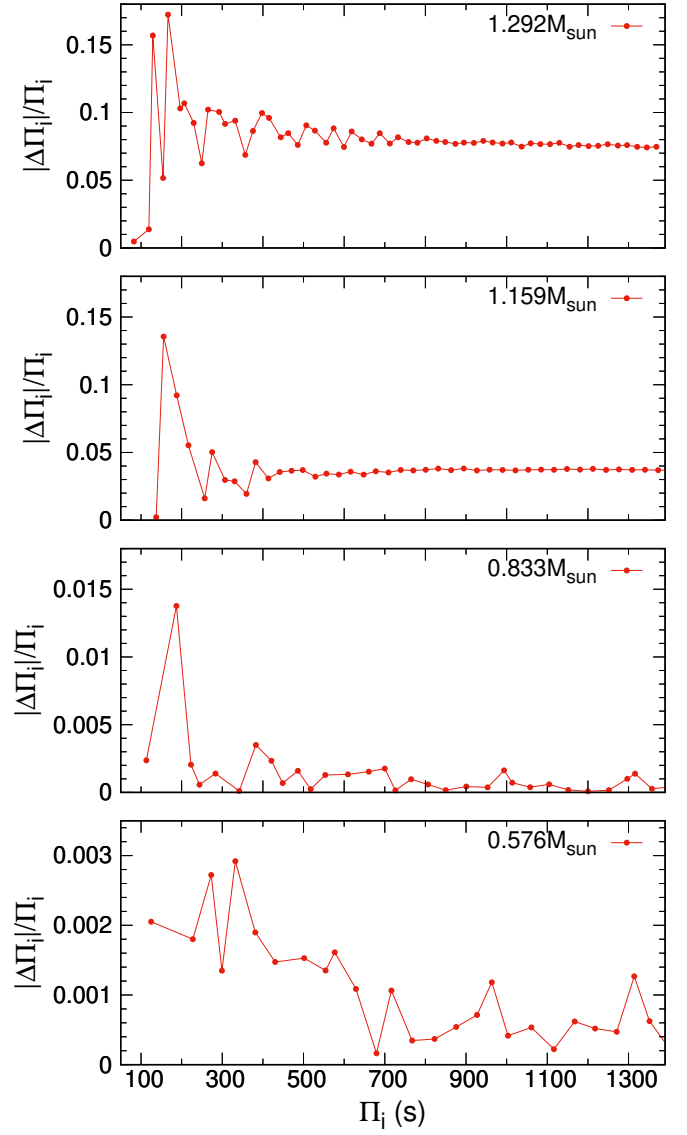


Fig. 4. Relative period differences in terms of the periods of $\ell = 1$ pulsation g modes resulting from including and disregarding Coulomb separation in the same models analyzed in Fig. 2 at $T_{\text{eff}} = 11\,000$ K.

of ions alters markedly the g -mode pulsation periods of massive ZZ Ceti stars. This is borne out by Fig. 4, that displays the relative period differences in terms of the periods of $\ell = 1$ pulsation g modes resulting from including and disregarding Coulomb separation in our WD models at $T_{\text{eff}} = 11\,000$ K. The differences are defined as the periods calculated with Coulomb diffusion minus the periods neglecting this effect, divided by the periods computed with Coulomb diffusion. This relative difference is plotted in terms of the periods calculated with Coulomb diffusion. We note that for the ultra-massive WDs ($M_* > 1.16M_\odot$), Coulomb diffusion yields significant changes in the g -mode pulsation periods by as much as $\sim 15\%$, which is given for the lowest radial-order modes ($\Pi \lesssim 600$ s). This is a relevant effect and should be taken into account in detailed asteroseismological analyses of these pulsating stars. On the other hand, the impact on less massive WDs is much less noticeable, with changes in the pulsation periods no larger than 0.3% . Such period changes remain still above the typical uncertainties of the observed periods ($\lesssim 0.01\%$) but well below the period changes that result from un-

certainties in convective boundary mixing and nuclear reactions during WD progenitor evolution (see De Gerónimo et al. 2017).

4. Summary and conclusions

Motivated by the result of Beznogov & Yakovlev (2013) who suggest that the redistribution of ions due to Coulomb separation could affect the thermal evolution of WDs and their pulsational properties, we have undertaken the present investigation to precisely assess the impact of such Coulomb separation on the WD evolution as well as on their chemical profiles, the Brunt-Väisälä frequency, and their pulsational periods at the ZZ Ceti instability strip. To this end, we have followed the full evolution of white dwarf models in the range $0.5\text{-}1.3 M_{\odot}$ derived from their progenitor history on the basis of a time-dependent element diffusion scheme that incorporates the effect of gravitational settling of ions due to Coulomb interactions at high densities.

We find that Coulomb sedimentation profoundly alters the chemical profiles of ultra-massive white dwarf along their evolution, preventing the strong inward diffusion of He toward the core, and thus leading to the formation of a pure-He buffer with two separate chemical interfaces, at variance with what happens when Coulomb diffusion is neglected. These changes in the inner chemical distribution barely affect the cooling properties of the WDs. However, the impact on the pulsation periods is quite different. In fact, large changes in the g -modes pulsation periods as high as 15% are expected for ultra-massive ZZ Ceti stars. For less massive ZZ Ceti stars, the impact of Coulomb separation is much less noticeable, inflicting period changes that are below the period changes that result from uncertainties in progenitor evolution, albeit larger than typical uncertainties of observed periods. The process of Coulomb diffusion of ions profoundly affects the diffusion flux in massive white dwarfs, driving the gravitational settling of ions with the same A/Z (mass to charge number). In this study, we have quantified the magnitude of the impact of such effect on the period spectrum of ZZ Ceti stars. The changes in the pulsational periods are sufficiently important that they should not be neglected in detailed asteroseismological analyses of massive ZZ Ceti stars.

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