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Improving the schedulability of soft real-time open dynamic systems: The inheritor is actually a debtor

Rodrigo Santos^{a,*}, Giuseppe Lipari^b, Jorge Santos^a

^a Dep. Ing. Eléctrica y Computadoras, Universidad Nacional del Sur, Avda. Alem 1253, 8000 Bahía Blanca, Argentina ^b RETIS Lab, Scuola Superiore Sant'Anna, Piazza Martiri della Liberà 33, 56127 Pisa, Italy

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9 Abstract

10 This paper presents the Clearing Fund Protocol, a three layered protocol designed to schedule soft real-time sets of precedence related 11 tasks with shared resources. These sets are processed in an open dynamic environment. Open because new applications may enter the system at any time and dynamic because the schedulability is tested on-line as tasks request admission. Top-down, the three layers 12 13 are the Clearing Fund, the Bandwidth Inheritance and two versions of the Constant Bandwidth Server algorithms. Bandwidth Inheri-14 tance applies a priority inheritance mechanism to the Constant Bandwidth Server. However, a serious drawback is its unfairness. In fact, a task executing in a server can potentially steal the bandwidth of another server without paying any penalty. The main idea of the Clear-15 ing Fund Algorithm is to keep track of processor-time debts contracted by lower priority tasks that block higher priority ones and are 16 executed in the higher priority servers by having inherited the higher priority. The proposed algorithm reduces the undesirable effects of 17 18 those priority inversions because the blocked task can finish its execution in its own server or in the server of the blocking task, whichever 19 has the nearest deadline. If demanded, debts are paid back in that way. Inheritors are therefore debtors. Moreover, at certain instants in time, all existing debts may be waived and the servers are reset making a clear restart of the system. The Clearing Fund Protocol showed 20 21 definite better performances when evaluated by simulations against Bandwidth Inheritance, the protocol it tries to improve. © 2007 Published by Elsevier Inc. 22

23 Keywords: Open systems; Soft real-time; Scheduling 24

1. Introduction 25

In the classical definition, Real-Time Systems are those 26 in which results must be not only correct from an arithme-27 tic-logical point of view but also produced before a certain 28 instant called *deadline*. Because of that it is said that the 29 system has time constraints. If no deadline can be missed, 30 the system is said to be hard real-time as opposed to soft 31 real-time, in which some deadlines may be missed. Schedul-32 ing theory addresses the problem of determining the neces-33 34 sary and sufficient conditions that a real-time system must

01 Corresponding author. Tel.: +54 291 4595181; fax: +54 291 4595154. E-mail addresses: ierms@criba.edu.ar (R. Santos), lipari@sssup.it (G. Lipari), iesantos@criba.edu.ar (J. Santos).

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meet in order that no deadline is missed (hard systems) or that as few as possible are missed (soft systems).

In some cases, tasks' parameters (execution and interarrival times, and deadlines) are not exactly known in advance. Because of this uncertainty, it may happen that a task exceeds its expected execution time or has a shorter interarrival time. In that case, interference with other tasks must be prevented. This can be done by the provision of 42 temporal isolation implemented by means of dedicated 43 constant bandwidth servers, each one serving only one 44 application (Deng and Liu, 1997; Lipari and Butazzo, 45 2000; Caccamo and Sha, 2001) (a server is an entity used 46 by the scheduler to reserve a fraction of processor-time to 47 a task Marzario et al., 2004). In that way, a task can use 48 only the time assigned to it and cannot use time assigned 49 to others tasks. When tasks do not share resources, they 50

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51 are said to be spatially isolated. If they are not spatially isolated, undue priority inversions may take place and it is 52 desirable not only to bound their duration but also to 53 reduce the undesirable effects suffered by the task which 54 55 execution was postponed in spite of having a higher priority. The Clearing Fund Protocol makes all this in the frame 56 57 of an Open Dynamic System, ODS. It is open because new applications may enter the system at any time and dynamic 58 because the acceptance test, even if the tasks' parameters 59 are not exactly known, is performed on-line. 60

The main load is composed of sets of periodic or quasi-61 periodic preemptible soft real-time tasks related by prece-62 dence (STRP). Each STRP can be executed independently 63 of the others by a series of linearly ordered computational 64 steps on the single processor; in this way, logical concur-65 rency is achieved. The tasks of one STRP may share 66 resources with tasks of the same or of different STRPs. 67 Hard real-time tasks and non-real-time tasks may, under 68 certain circumstances, be admitted. After this introduction, 69 related work is discussed in Section 2; in Section 3, the Sys-70 71 tem Model and in Section 4 the Clearing Fund Protocol are 72 respectively presented; Section 5 is devoted to the manage-73 ment of hard real-time STRPs sharing the processor with soft real-time STRPs; in Section 6, experimental results 74 are analysed. Finally, conclusions are drawn in Section 7. 75

76 2. Related work

The problem of scheduling real-time systems with 77 resource constraints is addressed, for instance, in Lipari 78 and Butazzo (2000). When resources are shared, a lower 79 priority task may block the execution of a higher priority 80 one. This is called the priority inversion problem. In Sha 81 et al. (1990), the authors proposed two protocols to deal 82 with it, the Priority Inheritance and the Priority Ceiling 83 protocols. Both work under Rate Monotonic Scheduling, 84 a fixed priority discipline in which tasks are ordered by 85 86 decreasing rates or, what is the same, by increasing periods. The Stack Resource Policy (Baker, 1990), is a concurrency 87 control protocol that bounds the priority inversion phe-88 nomenon in static as well as in dynamic priority systems, 89 expanding the previous results. However, it does not 90 91 address the problem of scheduling ODSs.

Many algorithms designed to deal with aperiodic and 92 sporadic tasks have been proposed. The Polling, Deferrable 93 94 (Strosnider et al., 1995), Priority Exchange (Sprunt et al., 1988) and Sporadic (Sprunt et al., 1989) servers, are some 95 examples. All these algorithms have in common that they 96 97 work with fixed priorities, in particular Rate Monotonic. They are used in hybrid systems where there are hard 98 real-time periodic tasks and non-real-time aperiodic ones. 99 The servers are meant to reduce the mean response time 100 of aperiodic tasks. In order to do it, the hard real-time sys-101 102 tem must be completely specified, in the sense that tasks' execution times, periods and deadlines must be known. 103 This restriction prevents their use in ODSs, in which tasks' 104 parameters are not exactly known. Some other algorithms, 105

Slack Stealing (Ramos-Thuel and Lehoczky, 1994) and kschedulability (Santos et al., 2004), have a better performance at a higher computational cost but, again, they cannot be applied to the ODSs case. 109

Other related works addressing the problem are Con-110 stant Bandwidth Servers with shared resources (Caccamo 111 and Sha, 2001), Resource Kernel (Rajkumar et al., 2000), 112 Cooperative Scheduling Server (Saewong and Rajkumar, 113 1999) and Constant Utilization and Total Bandwidth Serv-114 ers (Deng and Liu, 1997), but they require a complete 115 knowledge of the sistem's specification. This makes their 116 use impossible in applications in which the parameters 117 are not exactly known and resources are shared, which is 118 precisely the problem this paper addresses. 119

The Bandwidth Inheritance algorithm, BWI, proposed 120 in Lipari et al. (2004), extends the Constant Bandwidth 121 Server, CBS, algorithm (Abeni and Buttazzo, 1998) to 122 real-time tasks not spatially isolated, by using a technique 123 derived from the Priority Inheritance Protocol (Sha et al., 124 1990). However, BWI presents some drawbacks. One prob-125 lem is that a blocking task can capture most of the band-126 width of a blocked task, causing long priority inversions 127 without paying any penalty. Besides, the computation of 128 sets of precedence constrained tasks is not considered. In 129 Santos and Lipari (2003) an Extended BWI was presented 130 to deal with precedence constrained tasks and it corrected, 131 in some way, the bandwidth distribution by penalizing the 132 blocking server. This is not enough because the blocked 133 server never receives back the time it has spent servicing 134 inherited tasks and, consequently, it may miss deadlines 135 that could otherwise be met. 136

The scheduling of resource-sharing precedence-related tasks is addressed here by means of the three layered Clearing Fund Protocol, CFP. Top down, the three layers are the Clearing Fund, the BWI, and the CBS algorithms. Temporal isolation is provided between spatially isolated sets of tasks by separate constant bandwidth servers. However, priority inversions may take place between groups of sets sharing resources. Their effect, however, is reduced by the possibility of executing the blocked task either in its own server or in the server of the blocking task.

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The basic idea consists in the incorporation of a balanc-147 ing fund similar to the clearing realized by banks at the end 148 of the day. When a task of low priority blocks a task of 149 higher priority, it migrates to the server of the blocked task 150 and it is executed at the priority of the blocked task. Then 151 the blocking server contracts a processor-time debt with 152 the blocked server that, if the lender demands its payment, 153 will have to be paid. Moreover, the mechanism reduces the 154 postponements in the deadlines of the servers, which is a 155 characteristic of the CBS algorithm. The main advantage 156 is that the effects of priority inversions due to the lack of 157 spatial isolation are reduced because the blocked STRP 158 can finish its execution in its own server or in the server 159 of the blocking STRP. This gives the option of choosing 160 the one with the nearest deadline making possible to meet 161 deadlines that would otherwise be missed. Finally a pre-162

163 scription law for debts is incorporated: at certain instants in the evolution of the system, called singularities (Santos 164 et al., 2004), the last pending task released before the singu-165 larity has completed its execution. From the point of view 166 167 of pending executions, the system is as in the initial state. Servers may update their parameters (partially consumed 168 169 budgets and postponed deadlines) and a reinitialization of the system takes place. Consequently, debts may be for-170 given. Although in an ODS paradigm, hard schedulability 171 guarantees are not the main target, the CFP is also able to 172 provide them although at the expense of certain limitations 173 on the acceptance of soft applications. 174

The main ideas of this article have been presented at the 175 10th International Conference on Real-Time Computing 176 177 Q2 Systems and Applications (Göteborg and Sweden, 2004) (Santos et al., 2004). The presentations, however, were only 178 179 preprinted for the conference's attendants and are not commercially available nor can they be downloaded from the 180 conference's web page. Besides, this paper enhances the ori-181 ginal presentation by adding a second protocol using the 182 Constant Bandwidth Server Algorithm with Hard Reserva-183 184 tion as the first layer. This modified version of the CBS 185 Algorithm was designed to cope with some problems that 186 may arise when acyclic multimedia or interactive tasks are processed. 187

188 3. System model

189 The system model will now be described. The CFP is slated to schedule soft real-time STRP, defined as sets of peri-190 odic or quasi-periodic preemptible soft real-time tasks 191 related by precedence and sharing resources. Each set can 192 193 be executed independently of the others by a series of linearly ordered computational steps. However, a variant of 194 the protocol is proposed to handle also acyclic tasks, 195 understood as non periodic tasks, active during long inter-196 vals of time. In certain applications, and although non-197 198 real-time in a strict sense, they are better processed if the rate of execution does not vary much along time. Finally, 199 although not as efficiently as other methods, the CFP can 200 also handle hard real-time tasks. 201

Since tasks are periodic, they can be viewed as a stream 202 203 of jobs (or instances) requesting the execution of a computation on a shared processor. τ_{ip} shall denote the *p*th instan-204 tiation of τ_i . In the model, time is considered to be slotted 205 206 and the duration of one slot is taken as the indivisible unit of time. Slots are notated t and numbered 1, 2, ... The 207 expressions at the beginning of slot t and instant t mean 208 the same. The execution of a task can be interrupted by a 209 task of higher priority. This preemption is assumed to be 210 211 possible only at the beginning of slots. An *empty* slot is a slot in which there is no task ready to be executed; the pro-212 213 cessor, then, goes idle. A *singularity*, s, is a slot in which all 214 real-time tasks released in [1, (s-1)] have been executed (San-215 tos et al., 2004). Note that s-1 can be either an empty slot or a slot in which a last pending task completes its execution. s 216 is a singularity even if at t = s, other tasks are released. The 217

concept of singularity is similar to the end of a busy period as defined in Palencia and Gonzalez Harbour (1999).

When, in order to be executed, a task τ_j needs data produced by other task τ_i , a precedence relation, notated $\tau_i \prec \tau_j$, is established and determines a partial ordering of the tasks. If $\tau_i \prec \tau_j$ and there is no task τ_l such that $\tau_i \prec \tau_l \prec \tau_j$, τ_i and τ_j shall be called predecessor and successor, respectively.

A digraph G can be associated to the computation (Ramammritham, 1990). Each node of the graph represents a task and there is a directed arc from the node representing τ_i to the node representing τ_j only if they are predecessor and successor respectively.

As usual, a root is a task with no predecessor and a leaf is a task with no successor. The level of the task in the graph is its minimum distance to the root, measured in arcs. Although they may share resources, tasks of one STRP are not precedence-related to tasks of other STRPs. A STRP starts always at a root node and ends at a leaf node. Since the tasks that form a STRP are periodic, the STRP itself is periodic and will have successive instantiations. In what follows it will be assumed that all the tasks of a STRP have the same period which will also be the period of the STRP.

The STRP starting at node g shall be notated γ_g . The cardinality of the STRP, i.e., the number of tasks in the STRP, shall be notated γ_g . Single independent tasks have $\gamma_g = 1$ (unitary STRPs).

Example. The set of tasks $\{\tau_1, \tau_2, \dots, \tau_{10}\}$ in Fig. 1 are arranged in three STRPs

$$\begin{aligned} \gamma_1 &= \{\tau_1, \tau_2, \dots, \tau_6\} \quad \Upsilon_1 = 6 \\ \gamma_7 &= \{\tau_7, \tau_8, \tau_9\} \quad \Upsilon_7 = 3 \\ \gamma_{10} &= \{\tau_{10}\} \quad \Upsilon_{10} = 1 \end{aligned}$$

Tasks may share physical or logical resources, notated251 R_k . A shared resource may be, for instance, a section of252memory. If the contents of the shared section are not253



Fig. 1. $\gamma_1, \gamma_7, \gamma_{10}$, execute at servers S_1, S_7 and S_{10} , respectively. Nodes and arcs indicate tasks and precedence, respectively. Dashed lines indicate shared resources.

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modified by the accessing tasks (e.g., a read-only portion of 254 code), a mutual exclusion problem does not exist. How-255 ever, if the contents, for instance data, can be modified, 256 access must be serialized in order to maintain consistency. 257 258 The section is then called critical and its access is controlled by the use of mutual exclusion semaphores with wait and 259 260 signal operations, notated $P(R_k)$ and $V(R_k)$, respectively. When a task enters a critical zone, the semaphore is locked 261 and no other task can enter the zone. Successive accesses to 262 critical sections can be nested. In that case, it is assumed 263 that they are always properly nested, in the sense that it 264 is only possible to have sequences of the type 265 $P(R_a)\cdots P(R_b)\cdots V(R_b)\cdots V(R_a)$. The times of use of a crit-266 ical section may be different for different tasks. 267

268 **Example.** In Fig. 1, τ_1 and τ_8 share resource R_1 ; τ_3 and τ_6 269 share resource R_2 ; τ_3 and τ_9 share resource R_3 ; τ_9 and τ_{10} 270 share resource R_4 .

The relative deadlines (absolute deadline slot minus absolute release slot) of all the tasks of a STRP are assumed to be equal among them and equal to or greater than the period of the server.

Two STRPs that share a common resource are said to 275 have an interference relation. The interference relation is 276 reflexive, symmetric and transitive and it is therefore an 277 equivalence relation partitioning the set of STRPs in equiv-278 alence classes. A STRP belonging to a class must not inter-279 fere with STRPs of other classes. Therefore, temporal 280 isolation (in the CBS sense) must be guaranteed between 281 282 STRPs of different classes.

The priority discipline to be used is Earliest Deadline 283 First, EDF. It is a dynamic priority discipline in which 284 the task to be executed at each unit of time is the one nearer 285 its deadline. In Liu and Layland (1973) it has been formally 286 proved that EDF is optimal in the sense that if a real-time 287 system is not schedulable under EDF is not schedulable at 288 all. The schedulability test boils down to verify that the sis-289 tem's utilization factor is less than, or equal to, 1. Because 290 of its simplicity it may be performed on-line when deciding 291 if a task may be accepted or not. If, because the tasks' 292 parameters are not exactly known in the accepting process, 293 while executing, the task actually exceeds the processing 294 time alloted to it, its deadline may be missed but it certainly 295 will not affect the execution of other tasks, isolated by their 296 297 own servers.

298 4. The Clearing Fund Protocols

The Clearing Fund Algorithm, CFA, is the third layer of a three layered protocol. The second layer is the BWI algorithm. There are two versions of the first layer, the CBS algorithm: plain CBS and CBS with hard reservation, CBSHR. Consequently, there are two versions of the protocol, CFP and CFPHR. As illustrated in Fig. 2 the protocols run in an Open System Architecture.



Fig. 2. Open System Architecture.

4.1. Open system architecture

The Open System Architecture resembles the one proposed by Deng and Liu (1997), in which: 308

- Each CBS is considered to be a virtual processor and holds only one STRP.
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- (2) Each virtual processor has its own bandwidth, which is the product of its utilization factor times the bandwidth of the real processor, e.g., in Mflops.
- (3) There are two distinct schedulability architectural levels: STRPs must be scheduled in the virtual processors and virtual processors must be scheduled in the real processor.
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- (4) In case that a level in the STRP (its distance to the root) has more than one task, the tasks that do not share resources with other tasks outside the STRP are executed first; the others execute in reverse order of their declared execution time. The rationale behind this rule is that tasks imposing shorter delays to other tasks are taken out of the way first.
- (5) Tasks can share resources with tasks of the same or of different STRPs, i.e., executed in the same or in different virtual processors, respectively.
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4.2. How CFP improves BWI

A well known phenomenon of priority inversion may 331 take place in the case of tasks sharing a resource. It hap-332 pens when a lower priority task is executed instead of a 333 higher priority one because of the lower priority task hav-334 ing accessed first, and not being able to release, the shared 335 resource. Note that inversions may exist in a priority driven 336 system regardless of the scheduling discipline used. In 337 inheritance type protocols, the lower priority task inherits 338

339 the priority of the higher one which is then said to be blocked. Combined with a proper use of semaphores 340 guarding the entrance to the shared resources, the time that 341 a task can be blocked may be bounded, and that is pre-342 343 cisely what the BWI algorithm does. However, although BWI provides a bounding mechanism, it does not provide 344 345 a compensating one such that the lower priority task (inheritor) pays back to the higher priority one the time 346 spent in executing under a priority inversion. 347

CFP improves BWI by converting the inheritor into a 348 debtor; it does so by incorporating a new queue and a 349 dynamic variable to each server. The variable is incre-350 mented by one for each slot that the STRP is executed out-351 side the server contracting a debt, and decremented by one 352 for each slot used to pay back the debt. The blocked STRP 353 that has been postponed in its execution, is enqueued in the 354 high priority queue of the server of the blocking STRP. 355 Depending on which is the nearest deadline, it may be exe-356 cuted in its own server or in the server of the blocking 357 STRP until the debt is paid or prescribes in a singularity. 358 A singularity means that the last pending task released 359 360 before the singularity has completed its execution; collecting debts is no longer necessary for the lenders and debts 361 may therefore prescribe and be cleared. 362

In the CFA, each STRP is assigned to a dedicated periodic server. Each server, S_g , is specified by two parameters: Q_g and P_g , where Q_g is the budget, time available for execution, and P_g is the period. The server is allowed to execute at least during Q_g out of every P_g units of time. The period of the server is assumed to be shorter or equal to the period of the STRP it hosts.

The relation between Q_g and P_g is the utilization factor of the server. Since there is only one real processor in the system, the total utilization factor can not be greater than 1, that is $\forall i \quad \sum Q_i/P_i \leq 1$.

In the CFA, the servers have three dynamic variables: 374 q_g , δ_g and $v_{g,f}$. The first variable is the current available 375 376 budget and keeps track of the portion already consumed. The second variable, δ_g , is the server's absolute deadline, 377 that is the number of the slot or, what is the same, the 378 instant before which the task is expected to be processed. 379 The third variable, $v_{g,f}$, counts the borrowed budget and 380 keeps track of the debts contracted by the server S_g with 381 382 the server S_f of higher priority.

Each server has two STRP queues, each one with a dif-383 ferent priority. The higher priority one is for external 384 STRPs; it holds the blocked STRP after an inheritance 385 has taken place. The lower one is for the STRP allocated 386 to the server. Initially q_g is equal to Q_g and is decremented 387 by one for each unit of time the server executes. When it 388 reaches zero, the budget is recharged and the deadline is 389 postponed. 390

The CBS presents some drawbacks when serving acyclic tasks, understood as non-periodic non-real-time tasks that are active for long intervals of time, covering therefore many periods of the sever. This is particularly negative for multimedia or for interactive tasks since it may lead to a loss of quality of service and interactivity. The main cause is the fact that in CBS, servers, recharged immediately after being exhausted, can be used immediately within the same period if the server's deadline, although postponed, is still the earliest. This leads to a temporal over execution that may be followed by a starvation altering the rate of the multimedia or the interactive application.

IRIS (Marzario et al., 2004) was proposed to solve this problem. Besides the budget and the period parameters of the server, a recharging time, r_i , is set in such a way that under no circumstances the server that exhausts its budget may execute again until r_i . In IRIS, r_i is the beginning of the next period of the server and in the interval between exhausting its budget and been able to use it again, the server is said to be in the recharging state. The method is called hard reservation and the modified CBS algorithm is notated CBSHR.

In CBSHR, servers have three states: idle (no task is 414 demanding execution within the server), active (at least 415 one task is demanding execution) or recharging (there is 416 at least one task demanding execution but the server has 417 consumed his budget). It may happen, however, that being 418 no active servers in the system and some of them being in 419 the recharging state, deadlines are missed. To avoid this, 420 a simple rule to advance the activation instant is included. 421

Example. Suppose there is only one server in the system 422 with parameters (2, 6) and a task requires an execution time 423 of 4. Following CBS, the temporal evolution of the system 424 will be the one shown in Fig. 3a. Following CBSHR 425 instead, the evolution will be as shown in Fig. 3b. As can be 426 seen, CBS produces an over execution followed by a 427 starvation while CBSHR keeps processing the application 428 at a constant rate. 429

4.3. Rules

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The rules of the two versions of the Clearing Fund Pro-431tocol will now be presented.432



Fig. 3. CBS with and without Hard Reservation.

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433 *4.3.1. CFP (CFA/BWI/CBS)*

Rules A–C correspond to CBS, rules D and E correspond to BWI and rules F to I are CFA specific:

436 A. When at time a_{gh} the *h*th instantiation of γ_g arrives,

437 the server S_g checks the condition $q_g \leq Q_g(\delta_g - a_{gh})/P_g$. If it holds, the current pair (q_g, δ_g) stands, other-439 wise a new pair $q_g := Q_g$ and $\delta_g := a_{gh} + P_g$ is com-440 puted to be used.

- 441 B. If server S_g executes for Δt units of time, the budget is 442 decremented accordingly, that is $q_g := q_g - \Delta t$.
- 443 C. Server S_g is allowed to execute while $q_g > 0$. When the 444 budget is depleted, a new pair (q_g, δ_g) is computed: the 445 absolute deadline is postponed to $\delta_g = \delta_g + P_g$ and 446 the budget is recharged to $q_g := Q_g$. Since the sched-447 uling deadline has changed, the EDF queue of the 448 servers may have to be reordered and preemptions 449 may occur.
- D. If task $\tau_i \in \gamma_g$ is blocked when accessing a resource R_k 450 that is locked by task $\tau_j \in \gamma_l$, then τ_j is added to the 451 queue of the server S_g . If, in turn, τ_i is currently 452 453 blocked on some other resource, then the chain of blocked tasks is followed, and server S_g adds all the 454 tasks in the chain to its queue, until it finds a non 455 blocked task. In this way, each server can have tasks 456 belonging to more than one STRP, but only one of 457 these tasks is not blocked. 458
- 459 E. If there is more than one task blocked in R_k , one of 460 them is unblocked when the resource is released. All 461 the servers that added it to their list must discard it.
- 462 F. After each singularity *s*, when a new instance of γ_g 463 arrives, the server S_g updates its variables: $q_g := Q_g$ 464 and $\delta_g := a_{gh} + P_g$.
- 465 G. If $\tau_j \in \gamma_l$ allocated to server S_l executes inside server S_g 466 postponing the execution of STRP γ_g , then γ_g is incor-467 porated to the high priority queue of server S_l with a 468 priority higher than that of γ_l . γ_g is in the queue of both 469 servers S_l and S_g and executes in the one with the clos-470 est relative deadline. Until the debt is paid or forgotten, 471 each time it is released, Γ_g will remain on both queues.
- 472 H. For each unit of time that γ_g , allocated to server S_l , 473 executes inside server S_g postponing the execution 474 of STRP γ_g , the variable $v_{l,g}$ is incremented by one 475 unit. It keeps track of the debt contracted by debtor 476 S_l with lender S_g .
- 477 I. For each unit of time that γ_g , allocated to server S_g , is 478 executed inside server S_l after being blocked by γ_l , the 479 variable $v_{l,g}$ is decremented by one unit. The debt is 480 being paid and the execution can go on until $v_{l,g}$ 481 reaches value 0.

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The first three rules, corresponding to the CBS mechanism, provide the important properties of temporal isolation and hard schedulability guarantee. However, a
transient overload produced by an increment in the execution time of a task produces a postponement in its deadline.
While this mechanism guarantees that the overload does

not affect other tasks, it penalizes the server for the rest 489 of the life of the system by differentiating the deadline of 490 the STRP from the deadline of the server. The idea is to 491 establish a prescription to this penalization whenever a sin-492 gularity appears in the system. In this way, successive post-493 ponements in the deadlines of a CBS are forgotten and new 494 values for the dynamic variables can be computed as if an 495 initialization of the system is taking place; this is done by 496 means of rule F. Rules D and E implement the Bandwidth 497 Inheritance among servers when a STRP is blocked. The 498 other rules describe the balancing mechanism when a debt 499 is contracted and paid later. 500

The performance of CFP will generally improve the performance of BWI. To begin with, in order to complete its execution, a blocked task will never have less time, as proved in the following lemma:

Lemma 1. *A task blocked under CFP never has less* 505 *available time to complete its execution than under BWI.* 506

Proof. From rules D and E, under BWI a blocked task can 507 resume its execution only when its server has no more 508 blocking tasks in its ready queue and has the earliest dead-509 line among all active servers (giving it the highest priority). 510 Under CFP, instead, rules G-I guarantee that a blocked 511 task may execute on its own server or in the debtor server, 512 whichever has the higher priority. In this way, the time 513 available to complete its execution may be increased but 514 never reduced. 515

As a consequence, a schedule under CFP will not pro-516 duce more deadlines' misses than a schedule under BWI, 517 and it may produce less. This is because, with the exception 518 of the case in which rules H and I are not used because 519 debts are cancelled at singularities, the blocked task will 520 have its own time plus more time available to complete 521 its execution. Having more time available, the number of 522 deadlines' misses cannot be increased and, on the contrary, 523 it may be reduced. 524

Example. In order to illustrate the main characteristics of 525 the CFA, an example is given. In Figs. 4 and 5, the 526 evolution of a system operating under the BWI/CBS and 527 the CFA/BWI/CBS protocols in the interval [1,30] are 528 respectively depicted. The explanation about how the rules 529 are applied is restricted to the interval [1,6]. In Appendix, 530 however, the explanation is extended to the interval [1, 30]. 531 The system has three servers: S_1 (2,6), S_2 (6,18) and S_3 532 (8,24). Each one serves a task with period equal to the 533 server-period and worst case execution time equal to the 534 budget of the server. The first two servers share a critical 535 section on resource R, S_1 for the duration of its execution 536 time and S_2 for the first five slots of its execution time. 537

The rules of the BWI/CBS protocol as applied in the 538 interval [1,6] are: 539

-t = 1. τ_{21} and τ_{31} arrive. Since $\delta_2 = 19 < \delta_3 = 25$ holds, 540 the processor is assigned to S_2 (EDF policy). *R* is locked. 541

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Fig. 4. System evolution under BWI. \uparrow , task arrival; δ , new deadline. In the three axes the activity of each server is depicted.



Fig. 5. System evolution under CFA. \uparrow , task arrival; δ , new deadline. In the three axes the activity of each server is depicted.

542	$-t = 2$. τ_{11} arrives. It cannot access R. Since τ_{11} has the
543	earliest deadline, τ_{21} is transferred to S_1 (Rule D) and
544	executed there.

545 -t = 4. S_1 's budget is depleted and recharged to 2. Its 546 deadline is postponed to 14 (Rule C).

547 -t = 6. S_1 's budget is depleted and recharged to 2. Its 548 deadline is postponed to 20 (Rule C). τ_{21} frees *R* but 549 now, $\delta_2 = 19 < \delta_1 = 20$ holds. τ_{21} returns to S_2 (EDF 550 policy) and finishes its execution there.

552 The rules of the CFA/BWI/CBS protocol as applied in 553 the interval [1,6] are:

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554 -t = 1. τ_{21} and τ_{31} arrive. Since $\delta_2 = 19 < \delta_3 = 25$ holds, 555 the processor is assigned to S_2 (EDF policy). *R* is locked. 556 -t = 2. τ_{11} arrives. It cannot access *R*. Since S_1 has the 557 earliest deadline, τ_{21} is transferred to S_1 (Rule D) and 558 executed there. For every slot executed by τ_{21} in S_1 , 559 ν_{21} is incremented in one unit (Rule H). τ_{11} is incorpo-560 rated to the high priority queue of S_2 (Rule G).

561 -t = 4. S_1 's budget is depleted and recharged to 2. Its 562 deadline is postponed to 14 (Rule C). v_{21} is equal to 2 563 (Rule H).

564 -t = 6. S_1 's budget is depleted and recharged to 2. Its 565 deadline is postponed to 20 (Rule C). v_{21} is equal to 4 566 (Rule H). τ_{21} frees *R* but now, $\delta_2 = 19 < \delta_3 = 20$ holds. τ_{21} returns to S_2 . τ_{11} starts execution in S_2 (Rule G) and locks *R*. For each slot executed in S_2 , v_{21} is decremented in one unit (Rule I).

As can be seen, executing under BWI/CBS, in the interval [1, 30] τ_1 misses the deadlines in the first four instantiations. This does not happen if CFA/BWI/CBS is used.

4.3.2. CFPHR (CFA/BWI/CBSHR)

For the CFP to work under the hard reservation scheme, rule C has to be modified.

C. Server S_g is allowed to execute while $q_g > 0$. When the budget is depleted, a new pair (q_g, δ_g) is computed: the absolute deadline is postponed to $\delta_g = \delta_g + P_g$ and the server goes into a recharging state. At $r_g = P_g - \delta_g$ the budget is recharged to $q_g := Q_g$ and the server becomes active again. In case no server is active and there is at least one server in the recharging state, the activation time for the servers can be advanced by determining $advance = \min \{r_i - t\}$ for every server in the recharging state. Then update the activation time of the servers: $r_i = r_i - advance$.

This modification does not alter the basic properties explained in the previous section. It must be noticed, however, that under hard reservation a server may not postpone its deadline more than once per period. Moreover, the maximum debt that an inheritor server may contract in a period is bounded by the budget of the lender server, as proved in the following theorem.

Theorem 2. Under CBSHR the maximum debt a server S_i can contract with server S_g is limited to Q_g per period.

Proof. A server S_g executing a blocking task can execute up to Q_g units of time before suspending itself and passing to the recharging queue. Only at the reactivation time the server will be able to continue with the execution. Thus, server S_i can only contract a debt of Q_g units of time out of every P_g . \Box

The previous theorem does not bound the total debt a server may contract but the rate at which it does it. In fact, the critical section of the blocking task may be so large compared to the period of the blocked one that it may take several periods of the lender to execute it.

In Fig. 6, the temporal evolution of the previous example is shown and explained.

At t = 4, the budget of S_1 is depleted and there is a dead-611 line postponement. By the modified Rule C, S_1 will not be 612 active until t = 14. As S_2 is the server with the nearest dead-613 line, the scheduler dispatches it and continues with the exe-614 cution of the critical section. The debt contracted is $v_{ig} = 2$. 615 As soon as task 2 releases the semaphore at t = 6, τ_1 col-616 lects its debt by executing in S_2 . At t = 14, S_1 becomes 617 active again and has the higher priority so task 1 can be 618 executed in it. 619

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Fig. 6. System evolution under CFAHR. \uparrow , task arrival; δ , new deadline. In the three axes the activity of each server is depicted.

As can be seen, there are some differences between the 620 temporal evolutions under both protocols. The debt con-621 tracted by S_2 with S_1 in the first period is only of 2 units 622 of time instead of 4 and, as a consequence, at t = 8, server 623 S_1 resumes the execution of task 1. 624

In general, the hard reservation approach may cause the 625 loss of more deadlines than the simple one. This is because, 626 once their budgets have been depleted, the servers are 627 suspended until the next activation instant if other servers, 628 even of lower priority, are in the active state and may 629 execute. This is the price to pay for ensuring a more con-630 stant rate in multimedia applications. The designer may 631 632 chose the proper protocol having in mind the intended applications. 633

5. Catering for HRT STRPs 634

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As it was shown in the previous section, the Clearing 635 Fund Protocol is specially apt to manage an Open 636 Dynamic System of soft real-time STRPs. However, it 637 may be used to schedule hard real-time systems, although 638 with two caveats: 639

- (i) If it handles only hard tasks, its use is not as efficient 640 as for instance Rate Monotonic plus Priority Inheri-641 tance and Ceiling protocols. 642
 - (ii) If it handles a mix of hard and soft subsystems, the price to be paid is that a complete spatial isolation must exist between both subsystems.

If a soft application shares resources with a hard one, meeting hard deadlines cannot be guaranteed anymore. 648 If, on the contrary, spatial isolation is preserved, the hard 649 subsystem will meet all its time-constraints while the soft subsystem will receive the second best treatment.

Having that in mind, some definitions about blocking 652 chains must be given. Then some properties of the algo-653 rithm used in determining the HRT schedulability will be 654 proved. Based on them, the actual method to compute 655 656 the duration that an HRT STRP may suffer is given. With them, the schedulability of the HRT subsystem may be 657 tested. 658

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5.1. Blocking chains

A blocking chain, notated $H_i = \{\tau_I, R_I, \tau_{II}, R_{II}, \dots, \tau_k, \}$ 660 $R_k, \ldots, R_{z-1}, \tau_z$ is a set of tasks and shared resources 661 ordered according to the following rules: 662

$$-\tau_1 = \tau_i \tag{663}$$

$$-I_k \leqslant I_{k+1}$$

-
$$A_{ccesses}$$
 are of type 666

$$P(R_{k-1})\cdots P(R_k)\cdots V(R_k)\cdots V(R_{k-1}).$$
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$$\tau_k \in \gamma_g \Rightarrow \nexists \tau_{h \in 1, 2, \dots, z-k} \in \gamma_g$$

Therefore:

- (1) The subscript of the chain identifies its first task in the 670 graph as defined in Section 3. 671
- (2) Tasks are ordered by monotonically increasing periods.
- (3) Each pair of adjacent tasks share the resource in 674 between. 675
- (4) Accesses are properly nested (the higher subscript inside the lower one).
- (5) Only one task of each STRP belongs to a given blocking chain.

It must be noted that, according to the previous rules, τ_{II} will be the first task of a chain H_{II} , which is a subchain of H_I .

It is assumed that because of the precedence relation, a 684 successor cannot start its execution until its predecessor fin-685 ishes its execution. Therefore, although they can share a 686 resource, no blocking may take place between tasks 687 belonging to the same STRP. 688

Example. In the graph of Fig. 1, three blocking chains can 689 be identified: 690

$$H_{1} = \langle \tau_{1}, R_{1}, \tau_{8} \rangle$$

$$H_{3} = \langle \tau_{3}, R_{3}, \tau_{9}, R_{4}, \tau_{10} \rangle$$

$$H_{9} = \langle \tau_{9}, R_{4}, \tau_{10} \rangle$$

$$692$$

Note that H_9 is a subchain of H_3 . Also that, although 693 sharing R_2 , τ_6 can not block τ_3 and therefore there is not 694 H_2 . 695

Each task can have more than one blocking chain. The 696 *h*th blocking chain of task τ_i is notated H_i^h . 697

Example. In Fig. 7

$$\begin{split} H_{2}^{1} &= \langle \tau_{2}, R_{1}, \tau_{4}, R_{2}, \tau_{5} \rangle \\ H_{2}^{2} &= \langle \tau_{2}, R_{1}, \tau_{4}, R_{3}, \tau_{6} \rangle \\ H_{2}^{3} &= \langle \tau_{2}, R_{1}, \tau_{7} \rangle \\ H_{3}^{1} &= \langle \tau_{3}, R_{4}, \tau_{7} \rangle \\ H_{4}^{1} &= \langle \tau_{4}, R_{2}, \tau_{5} \rangle \\ H_{4}^{2} &= \langle \tau_{4}, R_{3}, \tau_{6} \rangle \end{split}$$

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Q3

Fig. 7,

701 Example. In Fig. 8

> $H_1^1 = \langle \tau_1, R_1, \tau_2 \rangle$ $H_1^2 = \langle \tau_1, R_1, \tau_3 \rangle$

 $H_2^1 = \langle \tau_2, R_1, \tau_3 \rangle$ 703

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704 Γ_i denotes the set of tasks of all the blocking chains or 705 subchains starting at τ_i but excluding it. $\Gamma(\gamma_g)$ denotes the union of all $\Gamma_i | \tau_i \in \gamma_g$ and represents, therefore, the set of 706 tasks that may interact with the STRP γ_g . 707

708 Example. In Fig. 7

$$\Gamma_{2} = \{ \tau_{4}, \tau_{5}, \tau_{6} \}$$

$$\Gamma_{3} = \{ \tau_{7} \}$$

$$\Gamma_{4} = \{ \tau_{5}, \tau_{6} \}$$

$$\Gamma(\gamma_{1}) = \Gamma_{2} \bigcup \Gamma_{3} = \{ \tau_{4}, \tau_{5}, \tau_{6}, \tau_{7} \}$$

$$\Gamma(\gamma_{4}) = \{ \tau_{5}, \tau_{6} \}$$

711 $\Gamma_{g,l}$ denotes the set of tasks belonging to Γ_g that may be blocked by γ_l such that the last task in the blocking chain 712 belongs to γ_l . 713

Example. In Fig. 1, $\Gamma_{1,7} = \{\tau_1, \tau_3\}, \Gamma_{1,10} = \{\tau_3\}$. In Fig. 7, 714 $\Gamma_{1,4} = \{\tau_2\}, \quad \Gamma_{1,5} = \{\tau_2\}, \quad \Gamma_{1,7} = \{\tau_2, \tau_3\}.$ In Fig. 715 8, 716 $\Gamma_{1,2} = \{\tau_1\}, \ \Gamma_{1,3} = \{\tau_1\}.$

5.2. Properties 717

718 Only properties that modify, or are added to, the properties of the CBS and the BWI algorithms presented in 719 Abeni and Buttazzo (1998) and Lipari et al. (2004) shall 720 be proved. 721

Lemma 3. Only one task of γ_l can block γ_g in each instance. 722

Proof. Assume that γ_g , in the present instance, is blocked a 723 724 first time by a task belonging to γ_l . After that blocking



ceases, γ_g will execute, either in S_g or in S_l , with higher pri-725 ority than γ_l and therefore cannot be blocked again by γ_l in 726 the present instance. 727

Lemma 4. A STRP can be blocked on the same resource more than once.

Proof. Although, according to Lemma 1, only one task of each STRP can block another STRP, nothing precludes that two tasks of different STRPs block another STRP on the same resource.

The interference time of STRP γ_g , notated I_g , is defined as the total blocking time that γ_g may suffer in the worst case. It will be the sum of the longest blocking times that each of its tasks may suffer. Because of the precedence relations, tasks of one STRP cannot block tasks of the same STRP or, in other words, a STRP cannot block itself.

Lemma 5. Each STRP containing tasks belonging to $\Gamma(\gamma_g)$ can contribute to I_g for at most the longest execution among the critical sections shared by both STRPs.

Proof. Immediate from Lemma 3

However, a STRP may be successively blocked by several other STRPs. Obviously, only tasks belonging to $\Gamma(\gamma_g)$, as defined in Subsection 5.1, can interfere and I_g results to be the maximum time that those tasks can execute inside S_g for each instantiation of γ_g .

 $B_k(R_{k-1})$ shall denote the longest time that task τ_k can 749 spend in the critical section of resource R_{k-1} , blocking 750 therefore tasks $\tau_I, \tau_{II}, \ldots, \tau_{k-1}$. $B(H_i^h) = \sum_k B_k(R_{k-1})$ is the sum of the longest times that each task of the chain H_i^h can block task τ_i . Of all the H_i^h chains, the one producing 753 the maximum $B(H_i^h)$ shall be chosen. I_{σ} will be the sum of the maximums for each task of the STRP.

5.3. Computation of the interference time

An algorithm to compute the interference time is pre-757 sented in pseudo code. It is based on the previous defini-758 tions and lemmas. The computation is made for each 759 STRP. Two sets are passed as parameters to the algorithm: 760 $\mathbf{G} = \{ \Gamma_{gl}, \ l \neq g \} \text{ and } \Psi = \{ \Psi_{gi}^{\hat{l}}, \forall i, l \}$ 761

The algorithm presented in pseudo code computes I_g , the interference time for STRP γ_g , exploring all the possible blocking chains. They are grouped according to the STRP of the last task. In this way all the blocking chains that end in γ_l are considered together (lines 6–9). In order to do this, for each task $\tau_i \in \gamma_g$ that can be blocked directly or indirectly by a task in γ_l , it computes the maximum blocking time.

Since γ_l can block γ_g only once, the longest blocking chain is considered (line 8). When all the tasks τ_i that can be blocked by γ_l have been considered, the maximum blocking time computed in line 8 is added to I_g (line 10) and a new blocking STRP is considered (lines 3-11). When

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all the STRPs have been considered I_g has the interference time that γ_g may suffer.

777 6. Experimental results

A comparative performance evaluation of the CFA/
BWI/CBS and the CFA/BWI/ CBSHR protocols against
BWI was carried out. Since BWI was taken as benchmark
and it cannot handle STRPs of precedence related tasks,
the evaluation was performed on sets of unitary STRPs.

783 Algorithm 1. Interference Time Computation Interfer-784 ence_Computation (G, Ψ)

785	1 {	
786	2 I _g	= 0;
787	3 for	r each ${{arGamma}_{ heta extsf{l}}} \in extsf{G}$
788	4 {	
789	5	<pre>block = 0;</pre>
790	6	for each $ au_{ extsf{i}} \in arGamma_{ extsf{gl}}$
791	7	{
792	8	$block = max(max_h(B(H_i^h) H_i^h \in \Psi_{gi}^1), block);$
793	9	}
794	10	$I_g = I_g + block;$
795	11 }	
796		

797 6.1. Setting the simulations

About one hundred thousand sets composed of 10 uni-798 tary STRPs each were run. The STRPs' periods were ran-799 domly generated with uniform distribution in the sample 800 space [10, 20, 30, ..., 100]. The set utilization factor was 801 forced to take values in the range $[0.54, 0.55, \ldots, 0.99]$. Nine 802 of the ten STRPs (each one already with its defined period) 803 were selected at random. Each one was assigned an execu-804 tion time to produce a STRP utilization factor randomly 805 806 selected in the interval [0.03, 0.10] of the set of STRPs' utilization factor. The execution time of the tenth STRP was 807 adjusted to produce the final sought set utilization factor. 808 Also, for each set, the following parameters were randomly 809 generated: (1) The number of shared resources (none, 1, 2 810 or 3). (2) Which STRPs access a shared resource. (3) For 811 how long each sharing STRP uses the resource and at what 812 instant it access it. 813

For each STRP in the system a CBS server with budget 814 and period equal to the worst case execution time and per-815 iod of the STRP, respectively, were assigned. Each set was 816 run for about ten thousand slots, a run time long enough to 817 produce a good variety of inheritances and preemptions 818 among the servers holding the STRPs. Each generated set 819 820 of ten STRPs was run under the three protocols. Whenever a task missed a deadline, a counter was incremented; when 821 822 the run of the system was finished, this counter was stored together with the utilization factor of the system. Finally, a 823 factor of demerit was computed. It is the Average Missed 824 Deadline Ratio (AMDR), defined as the ratio between 825

the sum of all the missed deadlines associated to a certain826utilization factor and the number of systems run with that827utilization factor. A metric for the QoS of the methods828could be the reciprocal of the AMDR.829

6.2. Results obtained 830

Results (AMDR vs. UF), plotted in a semilogarithmic graph, are presented in Fig. 9.

BWI, CFAHR and CFA, in that order, start losing deadlines at utilization factors of approximately 0.53, 0.57 and 0.73, respectively. As could be expected, the miss-ratio increases with utilization factors. For UF = 0.99, the miss-ratios differ roughly by one and two orders of magnitude.

As the difference between BWI and the other two protocols is of one and two orders of magnitude, the results are plotted in a semilogarithmic graph. 841

6.3. Results explained

The results obtained sustain the conclusions drawn from 843 the examples. The BWI has the higher AMDR because the 844 inheritance procedure has no compensating mechanism for 845 the lender server; since, according to the CBS rules, the 846 servers recharge their budget and postpone their deadline 847 everytime the budget is depleted, the deadline of the server 848 is soon very different (much later) than the deadline of the 849 STRP, producing a degradation of the servers's priority. 850 For the CFA/BWI/CBSHR case, things improve consider-851 ably. There is a compensating mechanism but the restric-852 tion on the activation of the server prevents sometimes 853 the immediate restitution of the bandwidth consumed. 854 Finally, the CFA/BWI/CBS has the best performance of 855 the three protocols. This is due to the fact that there is 856 no restriction for the servers to execute if there are ready 857 tasks in their queues. 858



Fig. 9. Simulation Results, o - BWI, + - CFAHR, * - CFA. Zero values have no representation on logarithmic scale.

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The AMDR for the BWI/CBS protocol at the higher uti-859 lization factor is approximately 0.1, which is quite good 860 considering that it is a simple straightforward protocol. In 861 the CFA/BWI/CBS case, things are much better because 862 863 the ratio of missed deadlines is only slightly bigger than 0.001, certainly a good result specially for applications in 864 865 which although some deadlines may be missed, it is better to lose as few as possible. CFA/BWI/CBSHR has a general 866 performance in between the other two protocols and it 867 would be useful in cases in which more uniform rates of exe-868 cution of STRPs with long total execution times, necessarily 869 partitioned in successive smaller budgets, are convenient. 870

871 7. Conclusions

In this paper, the Clearing Fund Protocol was pre-872 sented. It is a three layered protocol, based on the CBS 873 and the BWI algorithms, to schedule soft real-time STRPs 874 875 in an open and dynamic environment. In the context of this paper, they are defined as sets of precedence-related shar-876 ing-resources tasks, each one executed in its own constant 877 878 bandwidth server. A STRP may consist of only one task 879 (unitary STRPs). The main idea behind the protocol is 880 the facility of executing a blocked STRP either in its own server or in the server of the blocking STRP, whichever 881 has the nearest deadline. For accounting purposes, a coun-882 ter in the blocking server keeps tab of the time its STRP 883 spent in the higher priority server. This acquired debt must 884 be paid on demand but it can also be cleared at singulari-885 ties, defined as instants in the evolution of the system in 886 which the last pending task is executed. At that time, bud-887 gets and deadlines are restored to their original values, 888 reinitializing the whole system with a clear start. 889

Extensive simulations were performed to obtain a com-890 parative evaluation of the proposed protocols against BWI. 891 The metric used is a factor of demerit, the Average Missed 892 Deadlines Ratio, defined as the ratio between the number 893 894 of deadlines that were missed while running different sets of STRPs with the same utilization factor, and the number 895 of jobs generated in those sets. The results favour the two 896 variants of the Clearing Fund Protocol, CFP and CFPHR, 897 898 by two and one order of magnitude, respectively.

899 Acknowledgements

The authors express their sincere appreciation to the anonymous referees for all their comments and suggestions, which have substantially improved the paper.

903 Appendix

The example presented in Fig. 4 is now described completely. The rules of the BWI algorithm as applied in the interval [1, 30] are:

907 -t = 1. τ_{21} and τ_{31} arrive. Since $\delta_2 = 19 < \delta_3 = 25$ holds, 908 the processor is assigned to S_2 (EDF policy). *R* is locked.

- -t = 2. τ_{11} arrives. It cannot access *R*. Since τ_{11} has the earliest deadline, τ_{21} is transferred to S_1 (Rule D) and executed there.
- -t = 4. S_1 's budget is depleted and recharged to 2. Its deadline is postponed to 14 (Rule C).
- t = 6. S_1 's budget is depleted and recharged to 2. Its deadline is postponed to 20 (Rule C). τ_{21} frees R but now, $\delta_2 = 19 < \delta_1 = 20$ holds. τ_{21} returns to S_2 (EDF policy) and finishes its execution there.
- -t = 7. τ_{11} starts execution in S_1 (EDF policy). *R* is locked.
- t = 8. τ_{12} arrives. τ_{11} keeps executing in S_1 but it misses its deadline.
- t = 9. S_1 's budget is depleted and recharged to 2. R is unlocked. Its deadline is postponed to 26 (Rule C). τ_{31} starts executing in S_3 because $\delta_3 = 25 < \delta_1 = 26$ holds (EDF policy).
- t = 14. τ_{13} arrives, and τ_{12} misses its deadline. Rule A is applied and S_1 keeps its parameters unchanged.
- -t = 16. τ_{31} finishes and S_3 's budget is recharged to 8 and its deadline postponed to 49 (Rule C).
- $-t = 17. S_1$ is the only active server so it begins to execute τ_{12} .
- t = 19. S_1 's budget is depleted and recharged to 2. Its deadline is postponed to 32 (Rule C). τ_{13} misses its deadline. τ_{14} arrives and τ_{13} begins its execution. *R* is locked. τ_{22} arrives, S_2 's parameters are updated (Rule A), budget recharged to 6 and deadline postponed to 37.
- t = 21. S₁'s budget is depleted and recharged to 2. *R* is unlocked. Its deadline is postponed to 38 (Rule C). $\delta_2 = 36 < \delta_1 = 38$ so S₂ has the earliest deadline and begins to execute τ₂₂. *R* is locked.
- t = 25. τ_{32} arrives, S_3 's parameters are kept unchanged (Rule A). *R* is unlocked.
- t = 26. τ_{22} finishes its execution, S_2 's budget is depleted and recharged to 6 and its deadline postponed to 55. τ_{14} misses its deadline. τ_{15} arrives. Rule A is applied and S_1 keeps its parameters unchanged. $\delta_1 = 38 < \delta_3 =$ 49, by EDF, the processor is granted to S_1 and τ_{14} executes. *R* is locked.
- -t = 28. S_1 's budget is depleted and recharged to 2 and its deadline postponed to 44. R is unlocked. $\delta_1 = 44 < \delta_3 = 49$ and S1 is granted the processor by EDF and τ_{15} executes. R is locked.
- $-t = 30.S_1$'s budget is depleted and recharged to 2 and its deadline postponed to 50. τ_1 meets its fifth deadline after loosing the first four. *R* is unlocked.

In Fig. 5 the evolution of the same example is presented for the case of the CFA. The rules applied in the interval [1, 30] are:

 $- t = 1, \tau_{21} \text{ and } \tau_{31} \text{ arrive. Since } \delta_2 = 19 < \delta_3 = 25 \text{ holds,} \qquad 960$ the processor is assigned to S_2 (EDF policy). *R* is locked. 961 $- t = 2, \tau_{11} \text{ arrives. It cannot access } R. \text{ Since } S_1 \text{ has the} \qquad 962$ earliest deadline, τ_{21} is transferred to S_1 (Rule D) and 963 executed there. For every slot executed by τ_{21} in S_1 , 964

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- 965 v_{21} is incremented in one unit (Rule H). τ_{11} is incorpo-966 rated to the high priority queue of S_2 (Rule G).
- 967 -t = 4. S_1 's budget is depleted and recharged to 2. Its 968 deadline is postponed to 14 (Rule C). v_{21} is equal to 2 969 (Rule H).
- 970 $-t = 6. S_1$'s budget is depleted and recharged to 2. Its
deadline is postponed to 20 (Rule C). v_{21} is equal to 4971(Rule H). τ_{21} frees R but now, $\delta_2 = 19 < \delta_3 = 20$ holds.
 τ_{21} returns to S_2 . τ_{11} starts execution in S_2 (Rule G)
and locks R. For each slot executed in S_2 , v_{21} is decre-
mented in one unit (Rule I).
- 976 -t = 8. τ_{11} finishes on time, *R* is unlocked. v_{21} is equal to 2 977 (Rule I). τ_{12} arrives and begins its execution in S_2 (Rules 978 G–I). *R* is locked. S_1 's parameters are kept unchanged 979 (Rule A).
- 980 -t = 10. τ_{12} meets its deadline. v_{21} is equal to 0, τ_1 is 981 removed from S_2 high priority queue. τ_{21} continues its 982 execution in S_2 (Rules G–I).
- 983 -t = 11. S_2 's budget is depleted and recharged to 6. Its 984 deadline is postponed to 37. (Rule C). S_3 is the only 985 active server so τ_{31} begins its execution.
- 986 -t = 14. τ_{13} arrives and S_1 's parameters are kept 987 unchanged (Rule A). $\delta_1 = 19 < \delta_3 = 25$ so S_1 is granted 988 the processor (EDF policy) and τ_{13} begins its execution. 989 *R* is locked.
- 990 -t = 16. τ_{13} finishes and S_1 's budget is recharged to 2 and 991 its deadline postponed to 26 (Rule C). *R* is unlocked. S_3 992 is the only active server and continues with the execution 993 of τ_{31} .
- 994 -t = 19. τ_{21} arrives, S_2 's parameters are kept unchanged. 995 $\delta_3 = 25 < \delta_2 = 37$ so S_3 is granted the processor (EDF 996 policy) and τ_{31} continues executing.
- 997 -t = 20. τ_{14} arrives, S_1 's parameters are kept unchanged. 998 $\delta_3 = 25 < \delta_1 = 26$ so S3 is granted the processor (EDF 999 policy) and τ_{31} continues executing.
- 1000 -t = 21. S_3 's budget is depleted and recharged to 8, its 1001 deadline is postponed to 49 (Rule C). 1002 $\delta_1 = 26 < \delta_2 = 37$ so S_1 is granted the processor (EDF 1003 policy) and τ_{14} begins its execution. *R* is locked.
- 1004 -t = 23. τ_{14} finishes, S_1 's budget is depleted and recharged 1005 to 2 and its deadline postponed to 31 (Rule C). S_2 is the 1006 only active server so τ_{22} begins its execution.
- 1007 -t = 25. τ_{32} arrives, S_3 's parameters are kept unchanged 1008 (Rule A).
- -t = 26. τ_{15} arrives. Rule A is applied and S_1 keeps its 1009 parameters unchanged. $\delta_1 = 31 < \delta_2 = 37 < \delta_3 = 49$, 1010 by EDF, the processor is granted to S_1 and τ_{15} tries to 1011 lock R. It cannot access R. τ_{22} is transferred to S_1 (Rule 1012 E) and executed there. For every slot executed by τ_{22} in 1013 S_1 , v_{21} is incremented in one unit (Rule H). τ_1 is incorpo-1014 rated to the high priority queue of S_2 (Rule G). v_{21} is 1015 equal to 0. 1016
- 1017 -t = 28. S_1 's budget is depleted and recharged to 2 and its 1018 deadline postponed to 37. R is unlocked. $\delta_1 = 37 < \delta_2 = 37$ and S_2 is granted the processor by EDF and 1020 τ_{15} executes in S_2 . R is locked. v_{21} is decremented in 1021 one for each slot τ_1 executes in S_2 (Rules H, I).

- $-t = 31. \tau_{15}$ finishes, v_{21} is equal to $0. \tau_{22}$ completes its execution, S_2 's budget is depleted and recharged to 6 and its deadline postponed to 55.
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