

Predictive QSAR study of chalcone derivatives cytotoxicity activity against HT-29 human colon adenocarcinoma cell lines

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ABSTRACT

Chalcones and their derivatives exhibit a wide range of important pharmacological activities; among the most relevant ones is their anticancer activity. For this reason we performed a predictive Quantitative Structure–Activity Relationships (QSAR) analysis of the anticancer activity against HT-29 human colon adenocarcinoma cell lines by chalcones. The best linear model constructed from 136 molecular structures incorporated seven molecular descriptors, selected from more than a thousand geometrical, topological, quantum-mechanical and electronic types of descriptors, showed good predictive ability. The model analysis showed that the descriptors with highest importance on the activity are the number of 10-member rings and a BCUT descriptor weighted by the van der Waals volume.

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1. Introduction

Constantly increasing number of cancer cases around the world is one of the main causes of death in both economically developed and developing countries [1]. In view of the unlimited ability of tumor cells to the proliferation, avoiding of apoptosis, degree of the invasion and presence of metastases, cancer is considered to be the biggest challenge of present medicine [2]. In spite of progress in chemotherapy, there are no clinically effective substances acting selectively on tumor cells [3].

One of the pharmacologically relevant group of substances that possess an interesting range of biological activities are chalcones and their derivatives, exhibiting a wide range of pharmacological activities, as anticancer [3,4], anti-inflammatory [5,6], antimalarial [6–8], etc.

Chalcones are 1,3-diphenyl-2-propene-1-one consisting of two aromatic rings linked by a three carbon α , β -unsaturated carbonyl system and are fundamental intermediate compounds in flavonoid and isoflavonoid biosynthesis in plants. Synthetic and naturally occurring chalcones are regarded to be pharmacologically important compounds [9]. Numerous substances of this group have been approved to affect with each level of carcinogenesis and to exhibit activity against cancer cells. This suggests that chalcones may be considered as a group of potential anticancer agents [10]. Changes in their structure have offered a high level of variation that may be useful for the development of new therapeutic agents having improved potency and lower toxicity [11].

A great deal of chalcones derivatives were previously obtained and assessed for their cytotoxic and anticancer activity against series of cancer cell lines. In this paper we have taken into consideration the HT-29 human colon adenocarcinoma cell line. These cells exhibit the ability to form three-dimensional structures called multicellular spheroids showing a great similarity to natural tissue [12].

Within the currently ongoing search for effective anticancer drugs candidates in the present study we have carried out and established a reliable quantitative structure–activity relationship (QSAR) analysis based on 155 chalcones derivatives.

2. Methods

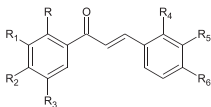
2.1. Data sets

In our QSAR study, a total of 162 chalcone molecules were gathered from the literature [3,13–22], to our knowledge this set of molecules was not employed in a predictive (QSAR) study before. The log IC₅₀ value, concentration of the compound (μ M) exhibiting 50% inhibition of cell growth [21], for human colorectal cancer cell line, HT-29, was employed as the dependent variable (Table 1). The data-set was divided into a training set of 136 compounds and a test set of 19 compounds (7 compounds were identified as outliers).

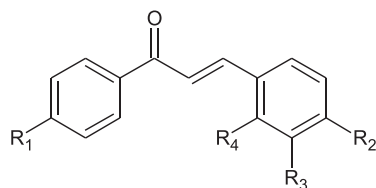
All the compounds were evaluated for their cytotoxic activity by the 3-(4,5-dimethylthiazol-2-yl)-2,5-diphenyltetrazolium bromide (MTT) assay based on mitochondrial reduction of yellow MTT tetrazolium dye to a highly colored blue formazan product [23].

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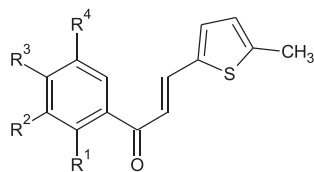
Table 1

Structure of compounds, experimental log IC₅₀, predicted log IC₅₀ by Eq. (4), and residuals. Superscript “t” indicates test set substances.


Compound	R	R ₁	R ₂	R ₃	R ₄	R ₅	R ₆	log IC ₅₀ exp. [13]	log IC ₅₀ pred.	Res.
1	H	H	NH ₂	H	Cl	H	Cl	1.602	1.497	0.105
2	H	H	OCH ₃	H	Cl	H	Cl	1.276	1.316	−0.040
3	OH	H	H	H	Cl	H	Cl	1.627	1.355	0.272
4	H	H	NH ₂	H	Cl	H	H	1.469	1.665	−0.196
5	H	H	H	H	H	H	OCH ₃	1.384	1.720	−0.336
6	H	H	NH ₂	H	H	H	OCH ₃	1.746	1.759	−0.014
7	H	NH ₂	H	H	H	H	OCH ₃	1.631	1.754	−0.123
8	H	H	OCH ₃	H	H	H	OCH ₃	1.691	1.585	0.106
9	OH	H	H	H	H	H	OCH ₃	1.775	1.641	0.134
10	H	F	H	F	H	H	OCH ₃	2.005	1.595	0.409
11	H	H	NH ₂	H	F	H	H	1.680	1.799	−0.119
12	H	H	OCH ₃	H	F	H	H	1.276	1.625	−0.349
13	H	H	H	H	H	H	OH	1.391	1.763	−0.372
14	H	H	OCH ₃	H	H	H	OH	1.269	1.614	−0.345
15	H	H	H	H	OCH ₃	H	OCH ₃	2.116	1.595	0.521
16	H	H	F	F	H	OCH ₃	H	1.726	1.608	0.118
17	H	H	NH ₂	H	OCH ₃	OCH ₃	H	1.843	1.698	0.145
18	H	NH ₂	H	H	OCH ₃	OCH ₃	H	1.641	1.635	0.006
19	H	H	OCH ₃	H	OCH ₃	OCH ₃	H	1.621	1.563	0.058
20 ^t	H	H	H	H	CF ₃	H	H	1.632	1.672	−0.040
21 ^t	H	H	OCH ₃	H	CF ₃	H	H	1.562	1.527	0.035
22 ^t	H	H	NH ₂	H	Br	H	H	1.549	1.498	0.051
23	H	H	OCH ₃	H	Br	H	H	1.411	1.320	0.091
24	H	H	OCH ₃	H	F	H	F	1.047	1.487	−0.440
25	H	OCH ₃	OCH ₃	H	Cl	H	Cl	1.272	1.201	0.071
26	H	OCH ₃	OCH ₃	H	H	H	N(CH ₃) ₂	1.698	1.796	−0.098
27	H	OCH ₃	OCH ₃	H	Cl	H	H	1.189	1.394	−0.205
28	H	OCH ₃	OCH ₃	H	H	H	OCH ₃	1.737	1.620	0.118
29	H	OCH ₃	OCH ₃	H	OCH ₃	H	OCH ₃	1.816	1.384	0.433
30	H	OCH ₃	OCH ₃	H	OCH ₃	OCH ₃	H	1.555	1.480	0.075
31	H	OCH ₃	OCH ₃	H	Br	H	H	1.145	1.210	−0.065



Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [3]	log IC ₅₀ pred.	Res.
32	H	H	H	H	1.686	1.899	−0.212
33	CH ₃	H	H	H	1.935	1.995	−0.060
34	OCH ₃	H	H	H	2.195	1.807	0.388
35	H	H	H	Cl	1.738	1.641	0.097
36	OH	H	H	Cl	1.779	1.550	0.230
37	H	H	CH ₃	H	1.932	2.010	−0.079
38	OH	H	CH ₃	H	1.706	1.986	−0.280
39	CH ₃	H	CH ₃	H	1.839	2.058	−0.219
40	OCH ₃	H	CH ₃	H	1.796	1.917	−0.120
41	CH ₃	OCH ₃	H	H	2.069	1.847	0.222
42	H	N(CH ₃) ₂	H	H	2.408	1.903	0.505
43	CH ₃	N(CH ₃) ₂	H	H	2.419	2.004	0.415
44	H	H	H	OH	1.947	1.822	0.126
45	CH ₃	H	H	OH	1.737	1.899	−0.162
46	OCH ₃	H	H	OH	1.653	1.665	−0.011
47	H	H	Cl	H	1.507	1.694	−0.188

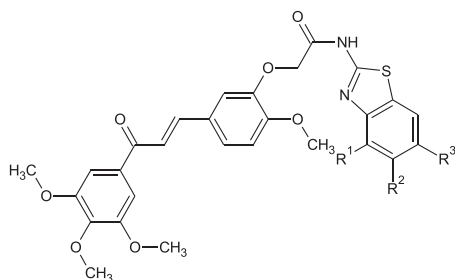


Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [14]	log IC ₅₀ pred.	Res.
48	OH	H	H	OC ₂ H ₅	1.638	1.793	−0.156

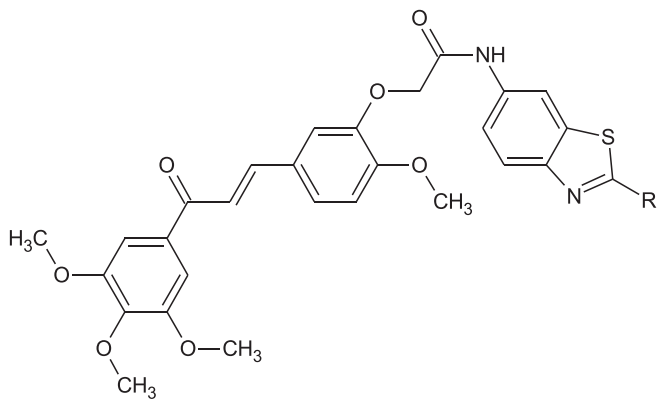
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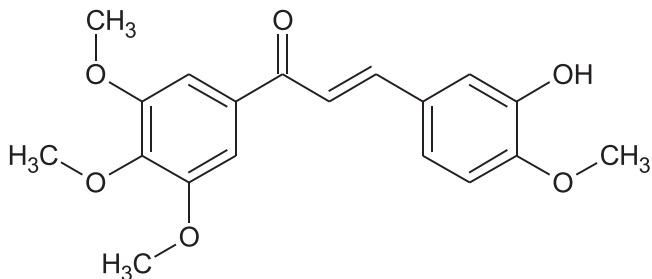
49	OC ₂ H ₅	H	H	OC ₂ H ₅	0.505	–	–
Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [14]	log IC ₅₀ pred.	Res.
50	OH	H	H	OC ₃ H ₇	2.099	1.815	0.284
51	OH	H	H	OCH(CH ₃) ₂	1.480	1.749	–0.269
52	OH	H	H	OC ₄ H ₉	1.854	1.753	0.101
53	OH	H	H	OCH ₂ CH(CH ₃) ₂	1.487	1.911	–0.424
54	OH	H	H	OC ₅ H ₁₁	1.939	1.638	0.301
55	OH	H	H	OCH ₃	1.854	1.708	0.146
56	OC ₂ H ₅	H	H	OCH ₃	–1.000	–	–
57	OC ₃ H ₇	H	H	OCH ₃	1.938	1.788	0.149
58	OC ₄ H ₉	H	H	OCH ₃	1.786	1.732	0.054
59	OH	OH	OCH ₃	H	1.728	1.599	0.129
60	OH	OH	OH	H	1.555	1.595	–0.040



Compound	R ₁	R ₂	R ₃	log IC ₅₀ exp. [15]	log IC ₅₀ pred.	Res.
61	H	H	H	0.185	0.669	–0.484
62	H	H	F	1.076	0.657	0.419
63	H	H	Cl	0.785	0.587	0.198
64	H	H	NO	0.940	0.725	0.214
65	H	H	OCH ₃	0.532	0.542	–0.010
66	H	H	OCF ₃	0.041	0.349	–0.307
67 ^t	H	H	CF ₃	0.568	0.514	0.054
68	H	H	CH ₃	0.322	0.618	–0.296
69	H	H	OC ₂ H ₅	0.380	0.556	–0.176
70	CH ₃	H	H	0.785	0.578	0.207
71	H	CH ₃	CH ₃	0.771	0.681	0.090

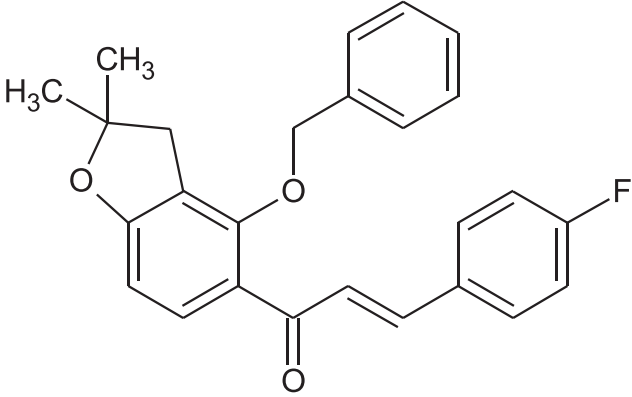
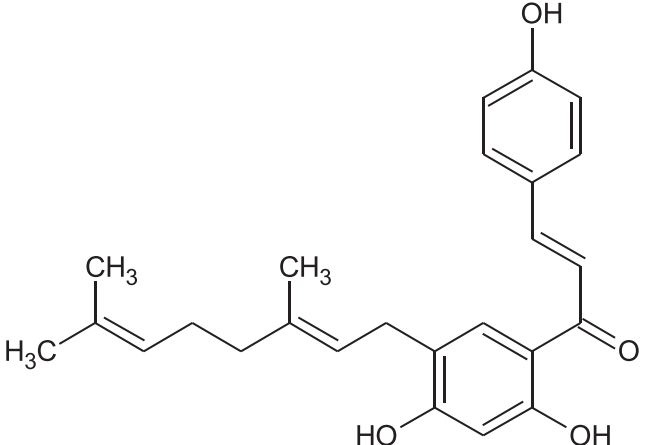
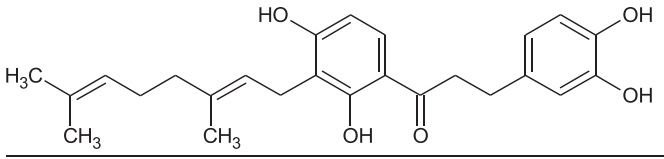


Compound	R	log IC ₅₀ exp. [15]	log IC ₅₀ pred.	Res.
72	H	0.924	0.806	0.118
73	CH ₃	0.978	1.348	–0.371



Compound	log IC ₅₀ exp. [16]	log IC ₅₀ pred.	Res.
74	0.279	–	–

Table 1 (continued)

			
Compound	log IC ₅₀ exp. [16]	log IC ₅₀ pred.	Res.
75	1.362	1.130	0.231
			
Compound	log IC ₅₀ exp. [17]	log IC ₅₀ pred.	Res.
76	1.041	0.696	0.346
			
Compound	log IC ₅₀ exp. [17]	log IC ₅₀ pred.	Res.
77	1.065	1.092	−0.028
			
Compound	log IC ₅₀ exp. [17]	log IC ₅₀ pred.	Res.
78	1.295	1.419	−0.125

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Table 1 (continued)

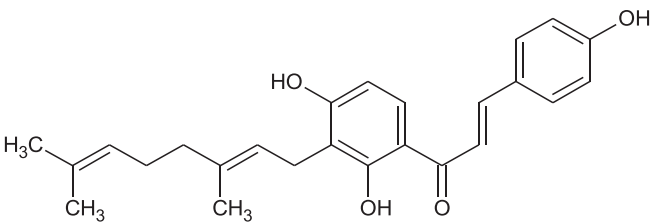
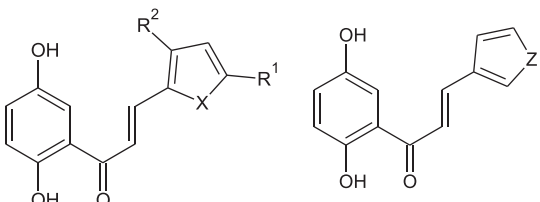
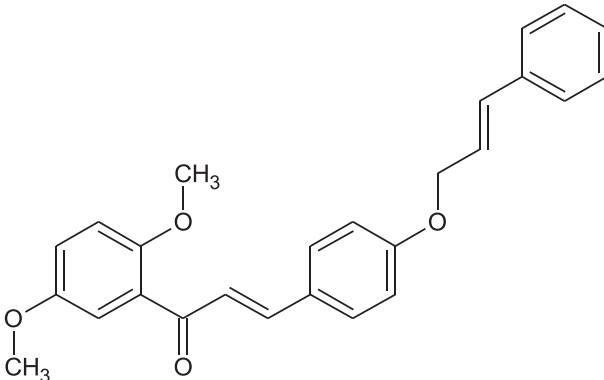
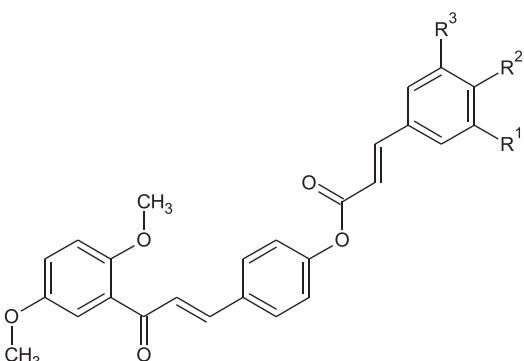
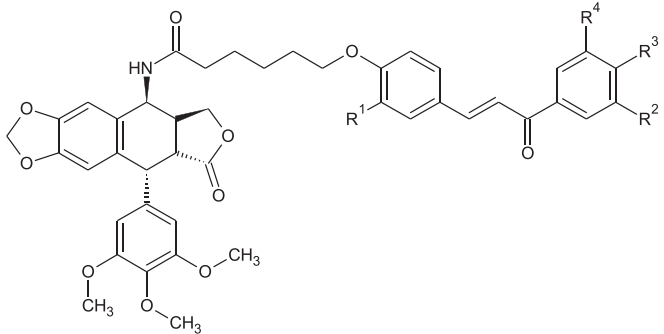
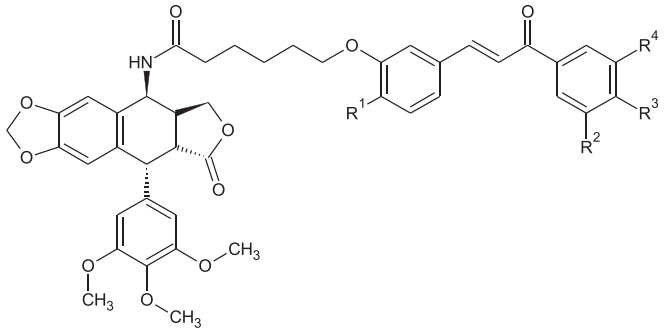
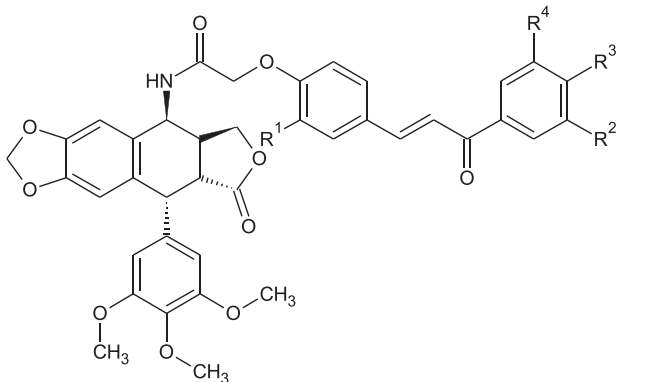
							
Compound	log IC ₅₀ exp. [17]				log IC ₅₀ pred.		Res.
79	1.212				1.250		−0.037
							
Compound	R ₁	R ₂	X	Z	log IC ₅₀ exp. [18]	log IC ₅₀ pred.	Res.
80 ^t	H	H	O		1.395	1.384	0.010
81				O	1.328	1.397	−0.069
82 ^t	H	H	S		1.124	1.193	−0.069
83				S	0.724	1.321	−0.596
84	CH ₃	H	O		1.634	1.943	−0.309
85	CH ₃	H	S		0.255	–	–
86	H	CH ₃	S		1.288	1.190	0.098
87	Br	H	O		1.182	1.153	0.029
							
Compound	log IC ₅₀ exp.[18]				log IC ₅₀ pred.		Res.
88	1.420				1.346		0.074
							
Compound	R ₁	R ₂	R ₃		log IC ₅₀ exp. [18]	log IC ₅₀ pred.	Res.
89 ^t	H	CH ₃	H		1.215	1.614	−0.399
90	H	OCH ₃	H		1.362	1.326	0.036
91	OCH ₃	OCH ₃	OCH ₃		1.377	1.344	0.033

Table 1 (continued)

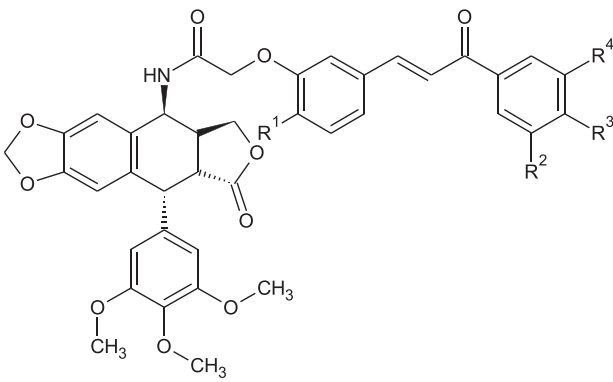
							
Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
92	H	OCH ₃	OCH ₃	OCH ₃	1.185	1.085	0.099
93	OCH ₃	OCH ₃	H	H	1.076	1.093	−0.018
94^t	OCH ₃	H	OCH ₃	H	1.207	1.157	0.050
95	OCH ₃	NO	H	H	0.942	1.183	−0.241
96	OCH ₃	OCH ₃	OCH ₃	OCH ₃	1.083	1.112	−0.030
97	OCH ₃	H	F	H	1.068	1.205	−0.137

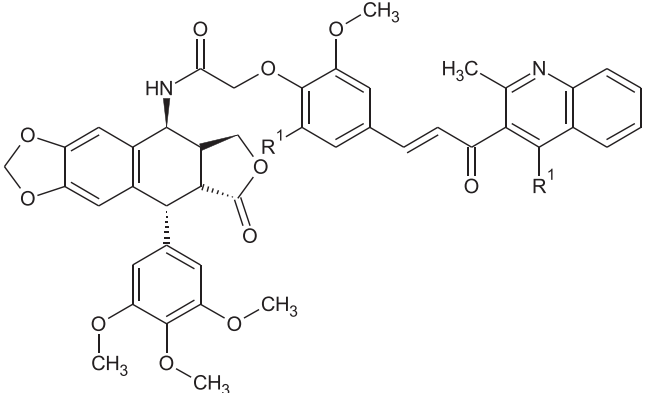
							
Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
98	H	OCH ₃	OCH ₃	OCH ₃	1.324	1.138	0.186
99^t	OCH ₃	OCH ₃	OCH ₃	OCH ₃	0.811	0.926	−0.115

							
Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
100	H	OCH ₃	OCH ₃	OCH ₃	1.093	0.969	0.125
101	OCH ₃	OCH ₃	H	H	0.909	0.785	0.123
102^t	OCH ₃	H	OCH ₃	H	1.228	0.992	0.236
103	OCH ₃	NO	H	H	0.925	1.077	−0.152
104	OCH ₃	OCH ₃	OCH ₃	OCH ₃	0.980	0.883	0.096
105^t	OCH ₃	H	F	H	1.335	1.062	0.273

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Table 1 (continued)

							
Compound	R ₁	R ₂	R ₃	R ₄	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
106	H	OCH ₃	OCH ₃	OCH ₃	1.193	0.938	0.255
107	OCH ₃	OCH ₃	OCH ₃	OCH ₃	0.777	0.965	−0.189

				
Compound	R ₁	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
108	CH ₃	1.090	0.922	0.168
109^t	Ph	0.889	0.709	0.181

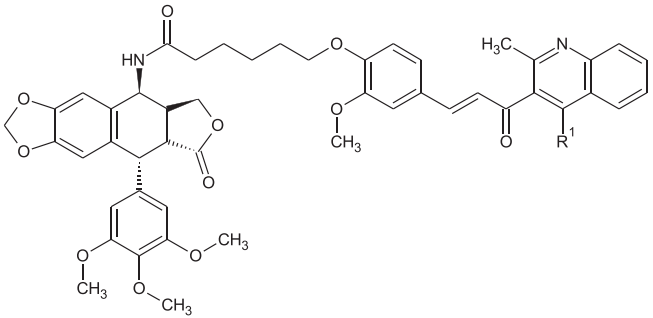
				
Compound	R ₁	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
110	CH ₃	1.072	1.046	0.026
111	Ph	0.949	0.949	0.000

Table 1 (continued)

Compound	R ₁	R ₂	R ₃	log IC ₅₀ exp. [19]	log IC ₅₀ pred.	Res.
112	H	H	H	0.373	–	–
113^t	H	F	H	0.851	1.227	–0.376
114	H	Cl	H	1.057	1.211	–0.154
115	H	Br	H	1.283	1.147	0.136
116^t	H	OCH ₃	H	1.246	1.179	0.067
117	H	OCF ₃	H	–0.432	–	–
118	H	NO	H	1.258	1.259	–0.001
119	Cl	Cl	H	1.322	1.164	0.158
120	OCH ₃	OCH ₃	OCH ₃	0.921	1.212	–0.290

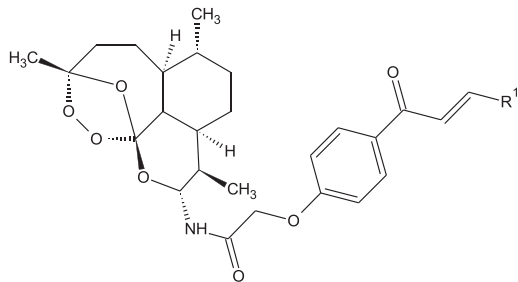
Compound	R ₁	log IC ₅₀ exp. [20]	log IC ₅₀ pred.	Res.
121^t	4-(Dimethylamino)phenyl	0.272	0.858	–0.586
122	Naphthalen-2-yl	0.651	0.906	–0.254
123	4-(Diethylamino)phenyl	–0.260	–	–
124	4-(Pyrrolidin-1-yl)phenyl	0.922	0.763	0.159
125^t	4-(1H-Imidazol-1-yl)phenyl	0.820	0.886	–0.066
126	Quinolin-2-yl	0.579	0.453	0.126
127	4-Nitrophenyl	0.572	0.786	–0.215
128	3-Nitrophenyl	0.629	0.835	–0.206
129	3-(Trifluoromethyl)phenyl	0.957	0.687	0.270
130	Pyridin-2-yl	0.326	0.832	–0.506
131	3,4-Dichlorophenyl	0.880	0.625	0.255
132	2-(4-Chloro)phenol	0.696	0.632	0.064

Compound	R ₁	log IC ₅₀ exp. [21]	log IC ₅₀ pred.	Res.
133	2,4-Difluorophenyl	–0.032	–0.018	–0.013
134	3,4,5-Trimethoxyphenyl	–0.620	–0.242	–0.378
135	4-Trifluoromethoxyphenyl	–0.444	–0.405	–0.039
136	3-Trifluoromethylphenyl	–0.585	–0.322	–0.263
137	4-Fluorophenyl	–0.155	–0.173	0.018
138	4-Chlorophenyl	–0.301	–0.261	–0.040

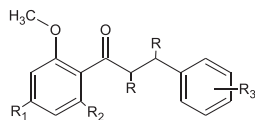
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Table 1 (continued)

Compound	R ¹	log IC ₅₀ exp. [21]	log IC ₅₀ pred.	Res.
139	2,6-dichlorophenyl	−0.854	−0.285	−0.569
140^t	3-Methoxyphenyl	−0.143	−0.178	0.035
141	Phenyl	−0.187	−0.137	−0.050
142	2-Furyl	0.362	0.211	0.150
143	2-Thienyl	0.204	0.080	0.124
144	1,3-Benzodioxo-5-yl	0.079	−0.089	0.168



Compound	R ₁	log IC ₅₀ exp. [21]	log IC ₅₀ pred.	Res.
145	2,4-Difluorophenyl	0.415	−0.022	0.437
146	3,4,5-Trimethoxyphenyl	−0.155	−0.203	0.048
147	4-Trifluoromethoxyphenyl	−0.409	−0.339	−0.070
148	3-Trifluoromethylphenyl	−0.620	−0.315	−0.305
149	4-Fluorophenyl	−0.119	−0.177	0.057
150^t	4-Chlorophenyl	−0.174	−0.246	0.073
151	2,6-Dichlorophenyl	−0.301	−0.271	−0.030
152	3-Methoxyphenyl	−0.174	−0.173	−0.001
153	Phenyl	−0.125	−0.131	0.006
154	2-Furyl	0.146	0.152	−0.006
155	2-Thienyl	0.322	0.017	0.306
156	1,3-Benzodioxo-5-yl	0.230	−0.088	0.318



Compound	R	R ₁	R ₂	R ₃	log IC ₅₀ exp. [22]	log IC ₅₀ pred.	Res.
157	H	OCH ₃	OH	3,4 OCH ₂ O	2.161	1.688	0.472
158	Double bond	OCH ₃	OH	3 OCH ₃	1.656	1.535	0.121
159	Double bond	OH	OH	3 OCH ₃	1.335	1.600	−0.265
160	Double bond	OH	OH	3,4 OCH ₂ O	1.316	1.459	−0.143
161	Double bond	OCH ₂ CH=CH ₂	OCH ₂ CH=CH ₂	3 OCH ₃	1.453	1.389	0.065
162	Double bond	OCH ₂ CH=CH ₂	OCH ₂ CH=CH ₂	3,4 OCH ₂ O	1.382	1.300	0.082

Preliminary tests indicated that molecules **49**, **56**, **74**, **85**, **112**, **117** and **123** presented excessively high errors indicating that they were outliers. The tests were performed comparing the results of approximately 1000 different calibrations, where the outliers presented errors that greatly exceeded the limit of 2.5σ; for these calculations the complete set of molecules was used. Since the prediction from any QSAR model cannot be intrinsically better than the experimental data employed to develop it, and the quality of the input data greatly influences the performance of QSAR models [24], these outliers were preventively left aside and not used in further calculations.

2.2. Molecular descriptors

The structures of the compounds were firstly pre-optimized with the Molecular Mechanics Force Field (MM+) procedure included in the Hyperchem 6.03 package [25], and the resulting geometries were further refined by means of the semi-empirical method AM1 (Austin Method 1) using the Polak–Ribière algorithm and a gradient norm limit of 0.01 kcal·Å^{−1}. The molecular descriptors were computed using the software Parameter Client, Virtual Computational Chemistry Laboratory [26,27] which calculates parameters of all types such as Constitutional, Topological, Geometrical, Charge, GETAWAY (Geometry, Topology and Atoms-Weighted Assembly), WHIM (Weighted Holistic

Invariant Molecular descriptors), 3D-Morse (3D-Molecular Representation of Structure based on Electron diffraction), Molecular Walk Counts, BCUT descriptors, 2D-Autocorrelations, Aromaticity Indices, Randic Molecular Profiles, Radial Distribution Functions, Functional Groups, Atom-Centered Fragments [28], electrotopological state molecular indices (ETState) and two sets of fragment descriptors (GSFRAG and GSFRAG-L) [27]. Parameter Client requires MOL2 (Sybyl) input format; in order to translate the structures to this format the software Open Babel was employed [29]. The initial descriptor matrix from Parameter Client contained 1932 descriptors. Nevertheless, some molecules did not permit the calculation of a number of descriptors; after removing these descriptors and linear dependant ones, the resulting total pool consisted of $D = 1433$ descriptors.

2.3. Model search

It is our purpose to search the set **D**, containing D descriptors, for an optimal subset **d**, with $d \ll D$, and with minimal standard deviation S ,

$$S = \sqrt{\frac{1}{(N-d-1)} \sum_{i=1}^N res_i^2} \quad (1)$$

by means of the Multivariate Linear Regression (MLR) technique. In this equation N is the number of molecules in the training set, and res_i , the residual for molecule i , is the difference between the experimental property (p) and predicted property (p_{pred}). More precisely, we want to obtain the global minimum of $S(d)$ where d is a point in a space of size $D!/[(d!)(D-d)!]$. A full search (FS) of optimal variables is impractical because it requires $D!/[(d!)(D-d)!]$ linear regressions. Therefore, an alternative method is necessary. We selected the optimum set of descriptors using a new advanced version of the Enhanced Replacement Method (ERM) [30,31] as a search algorithm that produces linear regression QSAR models with results similar to the FS, but with much less computational work. This technique approaches the minimum of S by judiciously taking into account the relative errors of the coefficients of the least-squares model given by a set of d descriptors $d = \{X_1, X_2, \dots, X_d\}$. The ERM [32] gives models with better statistical parameters than the Forward Stepwise Regression procedure [33], and the more elaborated Genetic Algorithms [34].

Among several other approaches to address this problem, the principle component regression (PCR) and partial least squares (PLS) analyses provide highly predictive QSAR, however they are difficult to understand and interpret for being abstract. A combination of GA and MLR has shown to produce simple, less sophisticated models with better performance on external testing set predictions than PLS [35]. In addition, on an extensive contrast work ERM has shown to further improve the performance of the obtained models when compared to GA [34]. Since ERM provides the same type of models in terms of simplicity compared to GA, ERM was selected for this work.

For the theoretical validation of all models, we chose the well-known Leave-One-Out (loo) and the Leave-More-Out Cross-Validation procedures ($l - n\% - o$) [36], where $n\%$ accounts for the number of molecules removed from the training set. We generated 1,000,000 cases of random data removal for 20 molecules in the case of Leave-More-Out. In our calculations we used the computational environment Matlab 5.0 (MathWorks, Natick, Massachusetts, U.S.A.). The predictive ability of the model was further evaluated by $(r^2 - r^2_o) / r^2$, $(r^2 - r^2_o) / r^2$, k and k' [37,38].

The applicability domain (AD) for the QSAR models was explored in order to obtain a reliable prediction for external samples. The AD is a theoretical region in the chemical space, defined by the model descriptors and modeled response, and thus by the nature of the chemicals in the training set, as represented in each model by specific molecular descriptors [39]. The AD can be characterized in various ways such as the leverage approach [40], which allows verifying whether a new

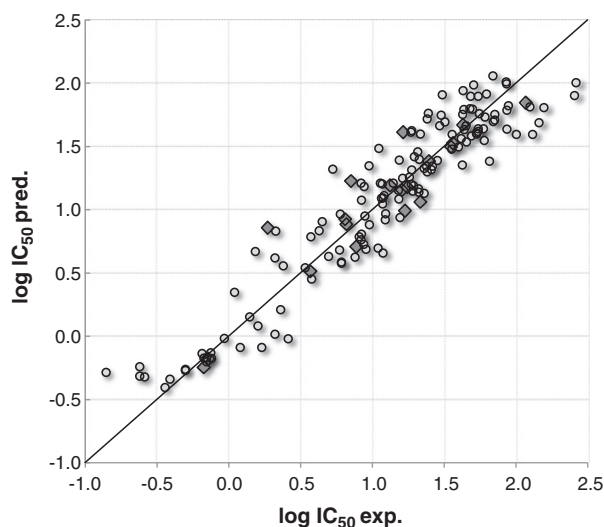


Fig. 1. Predicted (Eq. (4)) vs experimental $\log IC_{50}$ for the training (circles) and test (rhombus) sets.

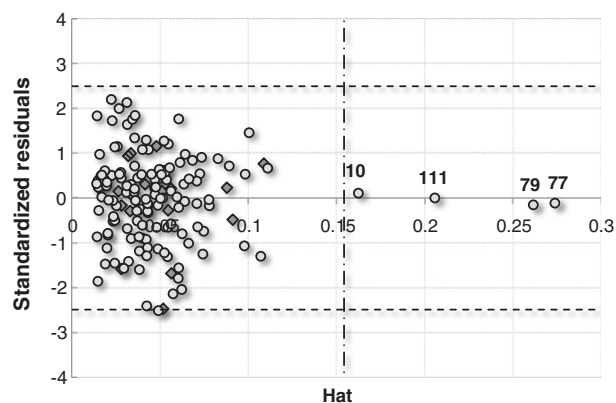


Fig. 2. Williams plot of the Eq. (4) showing the Application Domain. The vertical dashed line indicates the limiting leverage h^* .

chemical can be considered as interpolated and with reduced uncertainty or extrapolated outside the domain. If it is outside the model domain, a warning must be given. The leverage (h) is defined as [40]:

$$h_i = x_i (X^T X)^{-1} x_i^T \quad (i = 1, \dots, M) \quad (2)$$

where x_i is the $1 \times d$ descriptor row-vector of compound i , M is the number of compounds in the dataset, and X is the $N \times d$ matrix of the training set (d is the number of model descriptors, and N is the number of training set samples). The leverage is suitable for evaluating the degree of extrapolation, its limit of normal values is set as $h^* = 3(N + 1) / M = 3(\sum h_i + 1) / M$, and a leverage greater than h^* for the training set means that the chemical is highly influential in determining the model, while for the test set, it means that the prediction is the result of substantial extrapolation of the model and may not be reliable.

The standardized residual (σ) for molecule i is defined as:

$$\sigma_i = \frac{res_i}{S_{tr}} \quad (3)$$

where res_i is the residual of molecule i and S_{tr} is the standard deviation of the training set.

In order to visualize the AD of a QSAR model a Williams plot of standardized residuals (σ) vs leverage values (h) can be used to obtain an immediate and simple graphical detection of both the response outliers (Y outliers) and the structurally influential chemicals (X outliers) of a model.

Table 2
Symbols for molecular descriptors involved in the model.

Molecular descriptor	Type	Description
<i>nR10</i>	Constitutional	Number of 10-membered rings
<i>Mor32p</i>	3D-MorSE	3D-MorSE — signal 32/weighted by atomic polarizabilities
<i>SEigm</i>	Topological	Eigenvalue sum from mass weighted distance matrix
<i>BELm1</i>	BCUT	Lowest eigenvalue n. 1 of Burden matrix/weighted by atomic masses
<i>BEHv1</i>	BCUT	Highest eigenvalue n. 1 of Burden matrix/weighted by atomic van der Waals volumes
<i>H-051</i>	Constitutional	H attached to alpha-C
<i>SdssC</i>	E-state	Sum of all ($=C-$) E-state values

Table 3
Correlation matrix for descriptors of Eq. (4) ($N = 136$).

	<i>nR10</i>	<i>Mor32p</i>	<i>SEigm</i>	<i>BELm1</i>	<i>BEHv1</i>	<i>H-051</i>	<i>SdssC</i>
<i>nR10</i>	1	0.3696	0.5333	0.8191	0.3942	0.0712	0.3512
<i>Mor32p</i>		1	0.4048	0.3795	0.2597	0.2015	0.3377
<i>SEigm</i>			1	0.5126	0.7260	0.2795	0.6549
<i>BELm1</i>				1	0.6615	0.1117	0.3299
<i>BEHv1</i>					1	0.3844	0.4739
<i>H-051</i>						1	0.1587
<i>SdssC</i>							1

3. Results and discussion

Using the ERM we searched the total pool of $D = 1433$ descriptors and obtained an optimal model with $d = 7$ parameters (Table 2) linking the molecular structure of the compounds with their activity. The optimal QSAR model according to ERM was:

$$\begin{aligned} \log IC_{50} = & -7.4149(\pm 2) - 0.9949(\pm 0.05)nR10 + 1.0716(\pm 0.2)Mor32p \\ & - 0.2291(\pm 0.04)SEigm + 1.8729(\pm 1)BELm1 - 3.6116(\pm 0.8)BEHv1 \\ & + 0.1777(\pm 0.02)H-051 - 0.278(\pm 0.05)SdssC \end{aligned} \quad (4)$$

$$\begin{aligned} N = 136, R = 0.9468, S = 0.2360, FIT = 5.993, p < 10^{-4} \\ R_{loo} = 0.9405, S_{loo} = 0.2492, R_{l-20\%-o} = 0.9237, S_{l-20\%-o} = 0.2823 \\ R_{TS} = 0.9250, S_{TS} = 0.2236 \end{aligned}$$

here, the standard errors of the regression coefficients are given in parentheses; p is the significance of the model, FIT the Kubinyi function, loo and $l - 20\% - o$ stand for the Leave-One-Out and Leave-More-Out Cross Validation techniques respectively and TS stands for Test Set.

To demonstrate that Eq. (4) is not the result of happenstance, we resorted to a widely used approach to establish the model robustness: the so-called y -randomization [41]. It consists of scrambling the experimental p property, so that activities do not correspond to the respective compounds. After analyzing 1,000,000 cases of y -randomization, the smallest S value obtained in this way was 0.6256, which is larger than the one coming from the true calibration (0.2360). These results suggest that the model is robust, that its calibration is not a fortuitous correlation, and that we have derived a reliable structure–activity relationship.

The plot of values predicted by Eq. (4) vs. experimental $\log IC_{50}$ shown in Fig. 1 suggests that the 136 compounds from the training set and 19 from the test set follow a straight line. The predicted activity given by Eq. (4) for the training and test sets are shown in Table 1. The Williams plot of the standardized residual in terms of the leverages illustrated in Fig. 2 shows that most compounds lie within the AD of Eq. (4) and were calculated correctly. Compounds **10**, **111**, **77** and **79** are X outliers of the training set reinforcing the model [40]; there are no compounds with a standardized residual higher than the limit (2.5σ) that can be considered outliers.

The correlation matrix shown in Table 3 reveals that the descriptors *nR10* and *BEHv1* show a relevant degree of inter-correlation, however the calibration and validation results indicate that they are important for the prediction of the activity.

The predictive power of the linear model is satisfactory as revealed by its stability upon the inclusion and/or exclusion of compounds, measured by the statistical parameters $R_{loo} = 0.9405$ ($R_{loo}^2 = 0.8845$) and $R_{l-20\%-o} = 0.9237$ ($R_{l-20\%-o}^2 = 0.8532$). As general rule $R_{l-n\%-o}(Q)$ should be higher than 0.71 ($Q^2 > 0.5$) to have a validated model [38,42].

The model was further validated by the following conditions [37,38]: $R_{TS}^2 = 0.8556 > 0.6$; $k = 0.9781$; $k' = 0.9875$ ($0.85 < k$ or $k' < 1.15$); $(r^2 - r_0^2) / r^2 = -0.1662 < 0.1$; $(r^2 - r_0'^2) / r^2 = -0.1681 < 0.1$.

The molecular descriptors appearing in the linear Eq. (4) combine two- and three-dimensional aspects of the molecular structure. The standardization of their regression coefficients of Eq. (4) allows

assigning greater importance to the molecular descriptors that exhibit the largest absolute standardized coefficients [33]. In this case we have,

$$nR10(1.1191) > BELm1(0.7532) > SEigm(0.3197) > H-051(0.3184) > BEHv1(0.2820) > Mor32p(0.2209) > SdssC(0.1909). \quad (5)$$

By looking at this order we can see that the most significant descriptor is the constitutional descriptor *nR10*, followed by the BCUT descriptor *BELm1*. The Parameter Client [27] provides e-Dragon, ETState, GSFRAG and GSFRAG-L descriptors; however the only descriptor from Eq. (4) that was not calculated using e-Dragon was the ETState descriptor *SdssC*, having the lowest importance in the model. This suggests that e-Dragon descriptors are superior to the rest for calculating the studied activity.

Constitutional descriptors are 0D-descriptors, independent from molecular connectivity and conformations [28]. The descriptor *nR10* is determined by counting the number of 10-member rings present in a molecule, this descriptor has a positive contribution to the cytotoxicity activity since as it increases the $\log IC_{50}$ decreases, please refer to Eq. (4). The descriptor *H-051* is determined by counting the number hydrogen linked to an α -carbon, this descriptor has a negative contribution to the activity.

BCUT descriptors are the eigenvalues of a modified connectivity matrix, the Burden matrix (**B**) [43,44]. The matrix is an H depleted molecular graph, defined as follows: diagonal elements are atomic numbers of the elements (Z_i); off diagonal elements (B_{ij}), representing bonded atoms i and j are equal to $\pi^* \cdot 10^{-1}$ where π^* is the conventional bond order (i.e. 1, 2, 3, 1.5 for single, double, triple and aromatic bonds respectively); off diagonal elements corresponding to terminal bonds are increased by 0.01 and all other matrix elements are set to 0.001. The ordered sequence of the n smallest eigenvalues of **B** was proposed as a molecular descriptor based on the assumption that the lowest eigenvalues contain contributions from all the atoms and thus reflects topology of the molecule. The BCUT descriptors are an extension of the Burden eigenvalues and consider 3 classes of matrices, whose diagonal elements account for atomic charge related values, atomic polarizability related values and atomic H bond abilities. A variety of definitions have been used for the off diagonal terms and both 2D and 3D approaches are considered. The highest and lowest eigenvalues of these matrices have been shown to be discriminating descriptors. *BELm1* is the lowest eigenvalue of **B** involving atomic masses as weighting scheme (presenting a negative contribution to the cytotoxicity activity), and *BEHv1* is the highest eigenvalue of **B** involving atomic van der Waals volumes as weighting scheme (showing a positive contribution to the activity).

Topological descriptors are derived from hydrogen-depleted molecular graphs, in which the atoms are represented by vertices and the bonds by edges. The connections between the atoms can be described by various types of topological matrices, which can be mathematically manipulated so as to derive a single number, usually known as graph invariant. *SEigm* is calculated as the eigenvalue sum from the mass weighted distance matrix [28], and this descriptor has a positive contribution to the activity.

The 3D-MoRSE (3D Molecule Representation of Structure based on Electron diffraction) descriptors provide 3D information from the three-dimensional structure of a molecule using a molecular transform derived from an equation used in electron diffraction studies. Several atomic properties can be taken into account, thus giving high flexibility to this representation of a molecule. The simplified form of the transform is:

$$\begin{aligned} I(s) = \sum_{i=2}^N \sum_{j=1}^{i-1} A_i A_j \frac{\sin sr_{ij}}{sr_{ij}} \\ s = 0, \dots, 31.0 \text{ \AA}^{-1} \end{aligned} \quad (6)$$

where N is the number of atoms; r_{ij} is the distance between atoms i and j ; A_i can be any atomic property of atom i such as atomic number, mass,

