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# Libor at crossroads: Stochastic switching detection using information theory quantifiers



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#### ABSTRACT

This paper studies the 28 time series of Libor rates, classified in seven maturities and four currencies, during the last 14 years. The analysis was performed using a novel technique in financial economics: the Complexity–Entropy Causality Plane. This planar representation allows the discrimination of different stochastic and chaotic regimes. Using a temporal analysis based on moving windows, this paper unveils an abnormal movement of Libor time series around the period of the 2007 financial crisis. This alteration in the stochastic dynamics of Libor is contemporary of what press called "Libor scandal", i.e. the manipulation of interest rates carried out by several prime banks. We argue that our methodology is suitable as a market watch mechanism, as it makes visible the temporal redution in informational efficiency of the market.

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#### 1. Introduction

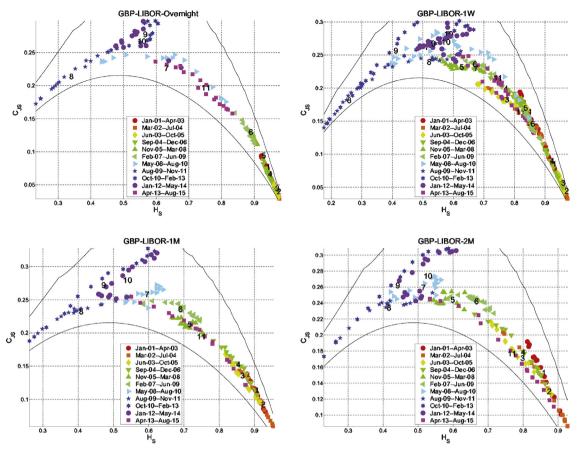
Interest rates no only reflect the time value of money, but also show the tension in the financial market. From the investors' point of view they provide a basic information for making decisions. From the government's point of view they are key elements for effective monetary policy

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transmission. Consequently fair market conditions in the money market arise as an important issue in political economy.

Libor stands for London Interbank Offered Rate and was created in 1986 by the British Banking Association (BBA). It is one of the most important economic benchmarks, followed closely by those who make financial decisions. According to BBA definition, Libor is "...the rate at which an individual Contributor Panel bank could borrow funds, were it to do so by asking for and then accepting inter-bank offers in reasonable market size, just prior to 11:00 a.m. London time". In fact, Libor rate does not necessarily reflect the cost or price of actual transactions. It is

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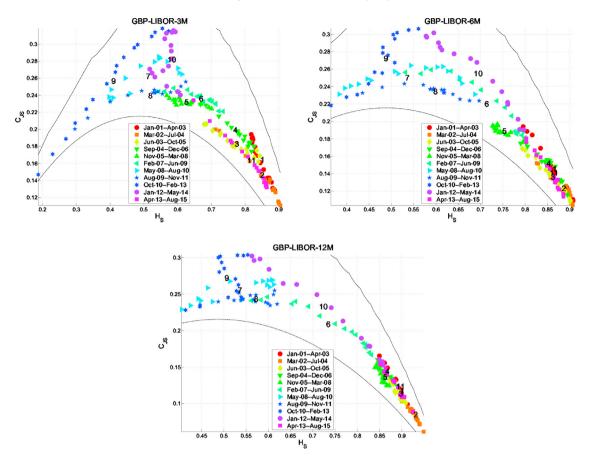
**Fig. 1.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of GBP Libor for different maturities: overnight (O/N), one week (1W), one month (1M), two months (2M). Numbers  $\{1...11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

a daily survey conducted by BBA among 16 prime banks, about their fair perception on their own borrowing costs. Every London business day, each bank in the Contributor Panel (selected banks from BBA) makes a blind submission such that each banker does not know the quotes of the other bankers. A compiler, Thomson Reuters, then averages the second and third quartiles. This average is published and represents the Libor rate on a given day. In other words, Libor is a trimmed average of the expected borrowing rates of leading banks. Libor rates has been published for ten currencies and fifteen maturities. As it is defined, Libor is expected to be the best self estimate of leading banks borrowing cost at different maturities. It is calculated for several currencies and maturities, and the panel composition is not the same for all currencies.

Until 2008, Libor was an uncontested benchmark. However, this situation changed due to a journal publication. Mollenkamp and Whitehouse [1] published a disruptive article in the Wall Street suggesting that the Libor rate did not reflect what it was expected, *i.e.* the cost of funding of prime banks. This, and other publications (e.g. [2,3]) triggered investigations conducted by the US Department of Justice, UK Financial Services Authority, EU European Commission and the Swiss Concurrence Commission. In June

2012 Barclays Bank pleaded guilty and accepted a fine of about \$480 millions. Other banks were also fined by improper financial conduct. For a full review of the Libor case from a regulator' point of view, please see Hou and Skeie [4].

Only a few papers deal with this topic in academic journals. Most of them uses basic econometric techniques aiming to detect varying differences between the Libor rate and another rate, supposedly not subject to manipulation. Among these papers we find Taylor and Williams [5], who documented the detachment of the Libor rate from other market rates such as Overnight Interest Swap (OIS), Effective Federal Fund (EFF), Certificate of Deposits (CDs), Credit Default Swaps (CDS), and Repo rates. Snider and Youle [6] studied individual quotes in the Libor bank panel and found that Libor quotes in the US were not strongly related to other bank borrowing cost proxies. Abrantes-Metz et al. [7] analyzed the distribution of the Second Digits (SDs) of daily Libor rates between 1987 and 2008 and, compared it with uniform and Benford's distributions. If we take into account the whole period, the null hypothesis that the empirical distribution follows either the uniform or Benford's distribution cannot be rejected. However, if we take into account only the period after the subprime crisis, the null hypothesis is rejected. This result calls into question



**Fig. 2.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of GBP Libor for different maturities (continuation): three months (3M), six months (6M) and twelve months (12M). Numbers  $\{1, ..., 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

the "aseptic" setting of Libor. Monticini and Thornton [8] found evidence of Libor under-reporting after analyzing the spread between 1-month and 3-month Libor and the rate of Certificate of Deposits using the Bai and Perron [9] test for multiple structural breaks.

Bariviera et al. [10] unveil strange movements in the stochasticity of the 3-month UK Libor, using the Complexity Entropy Causality Plane (CECP). More recently Bariviera et al. [11] studied the Libor scandal using the Shannon-Fisher plane, giving a new perspective under the lens of local-global information quantifies.

Our approach greatly expands [10], studying the behavior of the Libor for seven maturities and four currencies using the Complexity Entropy Causality Plane. This study highlights that Libor manipulation was more extensive as originally thought and was more subtle for some maturities.

The relevance for studying Libor manipulation is that, as stated in the independent study conducted by HM Treasury [12], more than \$300 trillion valued contracts uses Libor as benchmark. This means that the value of syndicated loans, floating rate notes and interest rate swaps were affected. Even more, many mortgages have their interests linked to Libor evolution. As a consequence borrow-

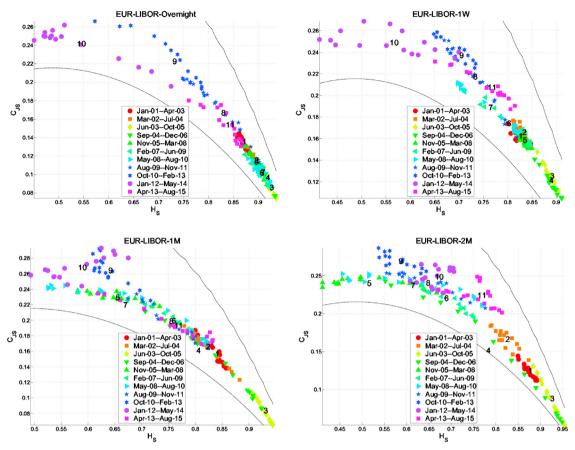
ers (mostly families) were directly affected by this unfair behavior.

The rest of the paper is structured as follows. Section 2 describes the methodology. Section 3 details the data under analysis. Section 4 comments the main findings of our study and, finally Section 5 concludes.

#### 2. Information theory quantifiers

Many economic data are recorded as a sequence of measurements equally spaced in time. This kind of data, commonly referred as time series, are usually the starting point for economic analysis. When the data are abundant, the number of adequate quantitative techniques increases. In particular, econophysics methods, as the one applied in this article, are innovative and appropriate to shed light on economic phenomena. In many cases, econophysics complement the limitations of traditional econometric techniques.

In this line, information-theory-derived quantifiers can help to extract relevant information from financial time series. The use of information quantifiers in economics is not new, but infrequent. The origins can be traced back to Theil and Leenders [13], who use entropy to predict short-term



**Fig. 3.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of EUR Libor for different maturities: overnight (O/N), one week (1W), one month (1M), two months (2M). Numbers  $\{1, \ldots, 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

price fluctuations in the Amsterdam Stock Exchange, Fama [14] and Dryden [15] replicate the same technique for the New York Stock Exchange and the London Stock Exchange respectively. [16] analyzes the proportion of securities with positive, negative and null returns on the American Stock Exchange using information theory methods and conclude that this proportions are dependent on the previous day and is not significantly influenced by the proportion of untraded securities. Philippatos and Wilson [17] proposes the average mutual information or shared entropy as a proxy of systematic risk. This technique was remained unused until recent years. For example, Risso [18] uses entropy and symbolic time series analysis in order to relate informational efficiency and the probability of having an economic crash. Later, Risso [19] uses Shannon entropy to rank the informational efficiency of several stock markets around the world. Ortiz-Cruz et al. [20] uses multiscale entropy analysis to analyze the evolution of the informational efficiency of crude oil prices.

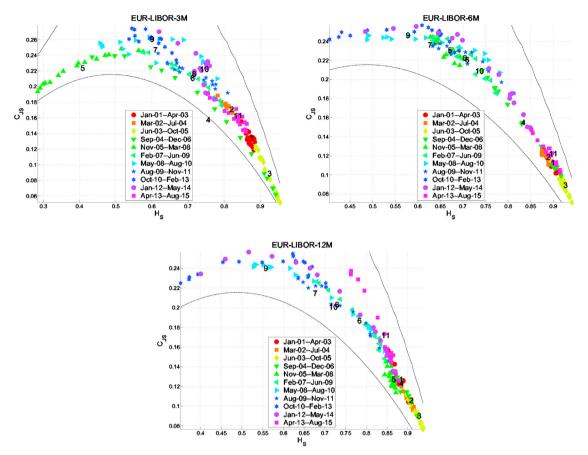
#### 2.1. Shannon entropy

When studying dynamical systems, the discrimination of the presence of correlations in time series, emerges as

one key task. Given a time series, one of the most natural measures of disorder, and thus absence of correlation, is Shannon entropy [21]. Given a discrete probability distribution  $P = \{p_i : i = 1, ...M\}$ , Shannon entropy is defined as:

$$S[P] = -\sum_{i=1}^{M} p_i \log(p_i)$$
(1)

This formula measures the information embedded into the physical process described by P. It is a bounded function in the interval  $[0, \log(M)]$ . S[P] = 0 means that one of the states  $p_{i^*} = 1$  and the remaining  $p_i = 0$  for  $i \neq i^*$ ,  $\forall i \in M$ . In other words, null entropy means full certainty about the system's outcome. On the other extreme, if  $S[P] = \log(M)$ , our knowledge about the system is minimal, meaning that all states are equally probable. Even though entropy can describe globally the level of order/disorder of a process, the analysis of time series using solely Shannon entropy could be incomplete [22]. The reason is that an entropy measure does not quantify the degree of structure or patterns present in a process. Consequently, a measure of statistical complexity is necessary in order to characterize the system.



**Fig. 4.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of EUR Libor for different maturities (continuation): three months (3M), six months (6M) and twelve months (12M). Numbers  $\{1, ..., 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

#### 2.2. Statistical complexity

Although Shannon entropy is a good measure of the order of a physical system, it has limitations. An additional measure in order to measure the hidden structure of the process is needed in order to fully characterize dynamical systems: an statistical complexity measure. A family of statistical complexity measures, based on the functional form developed by López-Ruiz et al. [23], is defined in [24,25]

$$C_{IS} = Q_I[P, P_e] \cdot \mathcal{H}[P] \tag{2}$$

where  $\mathcal{H}[P] = S[P]/S_{\text{max}}$  is the normalized Shannon entropy, P is the discrete probability distribution of the time series under analysis,  $P_e$  is the uniform distribution and  $\mathcal{Q}_J[P,P_e]$  is the so-called disequilibrium. This disequilibrium is defined in terms of the Jensen–Shannon divergence, which quantifies the difference between two probability distributions. Martín et al. [26] demonstrates the existence of upper and lower bounds for generalized statistical complexity measures such as  $\mathcal{C}_{JS}$ . Additionally, as highlighted in [27], the permutation complexity is not a trivial function of the permutation entropy because they are based on two probability distributions. A complete

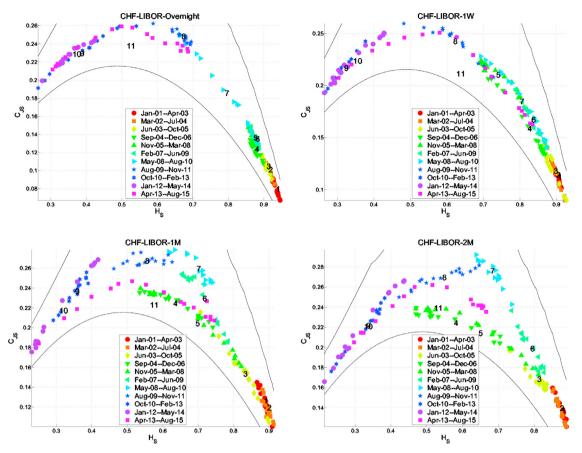
discussion about this measures and details about their calculation is in [28].

#### 2.3. Bandt-Pompe symbolization method

In order to evaluate this quantifiers, a symbolic technique should be selected in order to obtain the appropriate probability distribution function. Following [28–31], we use the Bandt and Pompe [32] permutation method, because it is the single symbolization technique that considers time causality. This methodology requires only weak stationarity assumptions.

The appropriate symbol sequence arises naturally from the time series. "Partitions" are devised by comparing the order of neighboring relative values rather than by apportioning amplitudes according to different levels. No model assumption is needed because Bandt and Pompe method makes partitions of the time series and orders values within each partition. Given a time series  $S(t) = \{x_t; t = 1, \ldots, N\}$ , an embedding dimension  $D > 1, D \in \mathbb{N}$ , and an embedding delay  $\tau, \tau \in \mathbb{N}$ , the BP-pattern of order D generated by

$$s \mapsto \left( \chi_{s-(D-1)\tau}, \chi_{s-(D-2)\tau}, \cdots, \chi_{s-\tau}, \chi_s \right) \tag{3}$$



**Fig. 5.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of CHF Libor for different maturities: overnight (O/N), one week (1W), one month (1M), two months (2M). Numbers  $\{1, ..., 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

is the one to be considered. To each time s, BP assign a D-dimensional vector that results from the evaluation of the time series at times  $s - (D-1)\tau$ ,  $s - (D-2)\tau$ ,  $\cdots$ ,  $s - \tau$ , s. Clearly, the higher the value of D, the more information about "the past" is incorporated into the ensuing vectors. By the ordinal pattern of order D related to the time s, BP mean the permutation  $\pi = (r_0, r_1, \cdots, r_{D-1})$  of  $(0, 1, \cdots, D-1)$  defined by

$$X_{S-r_{D-1}\tau} \le X_{S-r_{D-2}\tau} \le \dots \le X_{S-r_{1}\tau} \le X_{S-r_{0}\tau}.$$
 (4)

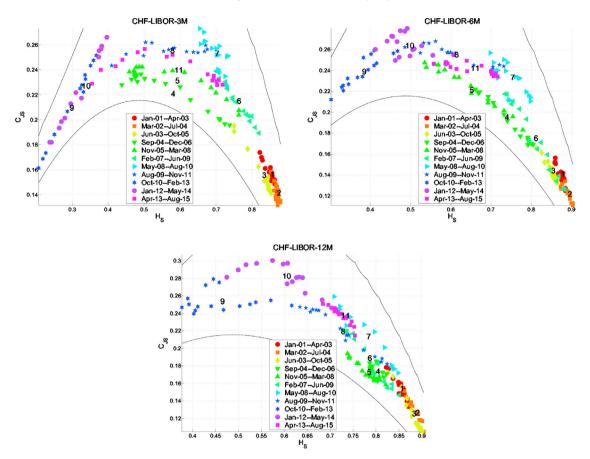
In this way the vector defined by Eq. (3) is converted into a definite symbol  $\pi$ . So as to get a unique result BP consider that  $r_i < r_{i-1}$  if  $x_{s-r_i\tau} = x_{s-r_{i-1}\tau}$ . This is justified if the values of  $x_t$  have a continuous distribution so that equal values are very unusual.

For all the D! possible orderings (permutations)  $\pi_i$  when embedding dimension is D, their associated relative frequencies can be naturally computed according to the number of times this particular order sequence is found in the time series, divided by the total number of sequences,

$$p(\pi_i) = \frac{\sharp \{s | s \le N - (D-1)\tau; (s) \text{ has type } \pi_i\}}{N - (D-1)\tau}$$
 (5)

In the last expression the symbol  $\sharp$  stands for "number". Thus, an ordinal pattern probability distribution  $P = \{p(\pi_i), i = 1, \dots, D!\}$  is obtained from the time series.

As we mention previously, the ordinal-pattern's associated PDF is invariant with respect to nonlinear monotonous transformations. Accordingly, nonlinear drifts or scalings artificially introduced by a measurement device will not modify the quantifiers' estimation, a nice property if one deals with experimental data (see i.e. [33]). These advantages make the BP approach more convenient than conventional methods based on range partitioning. Additional advantages of the method reside in (i) its simplicity (we need few parameters: the pattern length/embedding dimension D and the embedding delay  $\tau$ ) and (ii) the extremely fast nature of the pertinent calculation-process [34]. The BP methodology can be applied not only to time series representative of low dimensional dynamical systems but also to any type of time series (regular, chaotic, noisy, or reality based). In fact, the existence of an attractor in the *D*-dimensional phase space in not assumed. The only condition for the applicability of the BP method is a very weak stationary assumption (that is, for k = D, the probability for  $x_t < x_{t+k}$  should not depend on t [32]). The selected pattern length should fulfill  $N \gg D!$ , in order to obtain reliable quantifiers.



**Fig. 6.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of CHF Libor for different maturities (continuation): three months (3M), six months (6M) and twelve months (12M). Numbers  $\{1, ..., 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

# 2.4. The complexity entropy causality plane

When the Shannon entropy and the statistical complexity measures defined before are computed using the [32] symbolization technique, the quantifiers are named permutation entropy and permutation statistical complexity. Both quantifiers can be represented in a Cartesian plane, forming the Complexity Entropy Causality Plane (CECP). This planar representation was introduced in efficiency analysis in [28] and was successfully used to rank efficiency in stock markets [29], commodity markets [30], and to link informational efficiency with sovereign bond ratings [35]. Given the power of the CECP for the discrimination of random and chaotic signals, its application goes across disciplines. For example, Serinaldi et al. [36] studies the daily stream flow of United States rivers, and [37] reviews the main biomedical and econphysical applications of this methodology.

## 3. Data

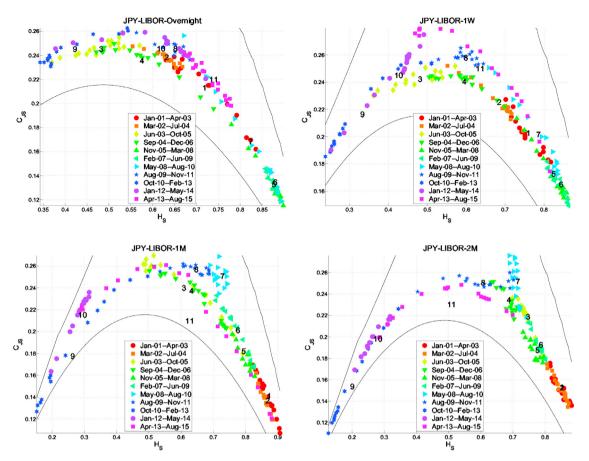
We analize the Libor rates in British Pounds (GBP), Euro (EUR), Swiss Franc (CHF) and Japanese Yen (JPY), for the following seven maturities: overnight (O/N), one week

(1W), one month (1M), two months (2M), three months (3M), six months (6M) and twelve months (12M). The data coverage is from 02/01/2001 until 06/10/2015, for a total of 3851 datapoints. All data were retrieved from Datastream.

We computed the permutation entropy and permutation statistical complexity for D=4, using daily values  $(\tau=1)$ . In order to assess the changes in the dynamical process that generates Libor time series, we used sliding windows. The sliding window approach works as follows: we compute the information quantifiers for the first 300 datapoints, then we move forward 20 datapoints ( $\delta=20$ ) and compute again the quantifiers for the next 300 datapoints. We continue in this way until the end of the data. Using this procedure, we obtained 177 windows, each one spanning slightly more than a year ( $\approx$ 13 months)

#### 4. Results

The results of the permutation entropy and statistical complexity are displayed in Cartesian planes called Complexity Entropy Causality Planes. This graphical representation allows the discrimination of stochastic and chaotic dynamics, as described in [31]. According to the classical



**Fig. 7.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of JPY Libor for different maturities: overnight (O/N), one week (1W), one month (1M), two months (2M). Numbers  $\{1, \ldots, 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

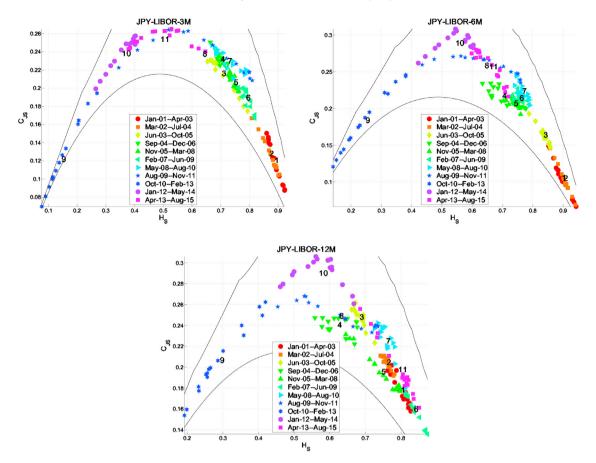
financial literature, prices in a competitive market should follow a memoryless stochastic process [38]. Thus, if Libor is freely set, without exogenous altering forces, it should approximately follow a random walk. In this situation, permutation entropy is maximized and permutation statistical complexity is minimized. We can safely say that, the closer the quantifiers to the point (1, 0), the more informational efficient the market is.

A simple observation of Figs. 1–8 shows that we are facing a changing dynamic. The process governing interest rates does not seem to be stable over time. The reflection of this is that the position of the estimators changes radically in different temporal windows. However, this change is not random, but rather seems to follow a directed path. To make a more visual presentation, we have grouped the windows in 11 periods of 16 windows each (17 windows in the last period). So we can differentiate each period with a color and a different marker. Additionally, we have put a number to each period and we have located in the average values of entropy and complexity of that period. As a general rule, we can see that GBP, EUR and CHF Libor behaves very efficiently during the first three periods (years 2001-2005). Indeed, entropy is greater than 0.8 and less than 0.2 complexity. Period 4 appears to be a certain transition. Entropy decreases and complexity increases. This trend is deepened in subsequent periods, with periods 6, 7 and 8 being the most inefficient (years 2007–2012). Periods 9, 10 and 11 (years 2012–2015) show a return to the area of greatest informational efficiency.

A more detailed analysis by currency allows us to discover that not all maturities followed the same pattern. Indeed, the most affected are the maturities of 1, 2 and 3 months. At the other extreme, the least affected were maturities of overnight and 12 months. Further analysis should JPY Libor. The behavior is similar to other currencies, but all maturities have also been affected in the rate rigging.

Probably one of the reasons for the distinct behavior of JPY and the rest of the currencies is that Libor JPY is less used as a benchmark for pricing other financial instruments. On the other hand, the distinct behavior in the different maturities can be also explained by their use as a reference rate<sup>1</sup>.

<sup>&</sup>lt;sup>1</sup> see the use of the different Libor rate maturities and currencies as a reference rate for interest rate swaps and floating rate notes in Table C.2 in [12].



**Fig. 8.** Complexity Entropy Causality Plane, with D = 4,  $\tau = 1$ ,  $\delta = 20$  of JPY Libor for different maturities (continuation): three months (3M), six months (6M) and twelve months (12M). Numbers  $\{1, \ldots, 11\}$  are the central points of each of the clusters. The solid lines represent the upper and lower bounds of the quantifiers as computed by Martín et al. [26].

We cannot discard that the financial crisis itself produced a disruption in the Libor market, making it less efficient. Its influence seems to depend on the nature of the financial assets under study. For example, [39] report an asymmetric impact of the crisis in the long memory of corporate and sovereign bonds. However, it is at least a remarkable coincidence that the changes in informational efficiency is contemporary with the alleged manipulation, specially in some maturities. Additionally, the informational efficiency recovery begins when banks were fined by improper conduct. Moreover, our results agree with the finding in [40], that between 2007 and 2009 the Libor time series was more predictable than either before or after those years.

In order to observe more clearly the temporal changes in informational efficiency, we compute the metric introduced in [41]:

Inefficiency = 
$$+\sqrt{(\mathcal{H}_S - 1)^2 + (\mathcal{C}_{JS})^2}$$
. (6)

This measure represents the Euclidean distance to the point  $\mathcal{H}_S=1$  and  $\mathcal{C}_{JS}=0$ , i.e. the maximal efficiency point. The results can be observed in Fig. 9.

#### 5. Conclusions

This paper studies the 28 time series of Libor rates during the last 14 years. The information theory based symbolic analysis is known as Complexity-Entropy Causality Plane, a novel approach in financial economics. The use of the CECP allows the discrimination of different stochastic and chaotic regimes. We used moving windows in order to introduce temporal dimension into our analysis. According to our results an abnormal movement of Libor time series around the period of the 2007 financial crisis is detected. This alteration in the stochastic dynamics of Libor is contemporary of what press called "Libor scandal", i.e. the manipulation of interest rates carried out by several prime banks. We argue that our methodology is suitable as a market watch mechanism, as it makes visible the temporal reduction in informational efficiency of the market. Our results could be useful for regulatory authorities, since the procedure detailed in this paper could act as an early warning mechanism to detect unusual dynamics in the Libor market.

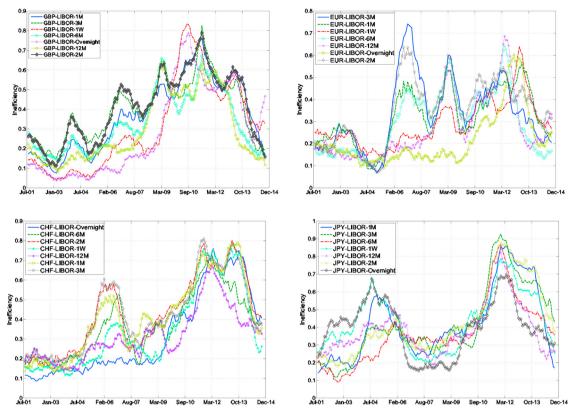


Fig. 9. Inefficiency evolution for each currency and maturity of Libor rates, according to Eq. (6).

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#### References

- [1] Mollenkamp C, Whitehouse M. Study casts doubt on key rate: WSJ analysis suggests banks may have reported flawed interest data for libor. Wall Street J Thursday, 29 May 2008:1.
- [2] Reuters. New york federal reserve knew about Libor rate-fixing issues as far back as 2007 and proposed changes but were ignored. Daily Mail July 10 2012.
- [3] Saigol L. Libor: The email trail, The Financial Times, 2013. http://www.ft.com/cms/s/0/cefd67a0-25df-11e3-aee8-00144feab7de. html#axzz3FNK2XAFe (accessed 10.11.15).
- [4] Hou D, Skeie DR. Libor: Origins, economics, crisis, scandal, and reform. report No. 667. Federal Reserve Bank of New York Staff; 2014.
- [5] Taylor JB, Williams JC. A black swan in the money market. Am Econ J Macroecon 2009(1):58–83.
- [6] Snider CA, Youle T. Does the libor reflect banks borrowing costs?2010. Available at SSRN: http://ssrn.com/abstract=1569603 (accessed 20.07.15).
- [7] Abrantes-Metz RM, Villas-Boas SB, Judge G. Tracking the libor rate. Appl Econ Lett 2011;18:893–9.
- [8] Monticini A, Thornton DL. The effect of underreporting on LIBOR rates. | Macroecon 2013;37:345-8.
- [9] Bai J, Perron P. Estimating and testing linear models with multiple structural changes. Econometrica 1998;66:47–78.
- [10] Bariviera AF, Guercio M, Martinez L, Rosso O. The (in)visible hand in the libor market: An information theory approach. Eur Phys J B 2015;88:208.

- [11] Bariviera AF, Guercio M, Martinez L, Rosso O. A permutation information theory tour through different interest rate maturities: the Libor case. Philos Trans R Soc Lond A Math Phys Eng Sci 2015;373:20150119.
- [12] Wheatley M. The wheatley review of LIBOR: Final report. independent report. H.M. Treasury; 2012.
- [13] Theil H, Leenders CT. Tomorrow on the amsterdam stock exchange. J Bus 1965;38:277–84.
- [14] Fama EF. Tomorrow on the new york stock exchange. J Bus 1965;38:285–99.
- [15] Dryden MM. Short-term forecasting of share prices: An information theory approach. Scott J Political Econ 1968;15:227–49.
- [16] Philippatos GC, Nawrocki DN. The behavior of stock market aggregates: Evidence of dependence on the American stock exchange. J Bus Res 1973;1:101–14.
- [17] Philippatos GC, Wilson CJ. Information theory and risk in capital markets. Omega 1974;2:523–32.
- [18] Risso WA. The informational efficiency and the financial crashes. Res Int Bus Financ. 2008;22:396–408.
- [19] Risso WA. The informational efficiency: The emerging markets versus the developed markets. Appl Econ Lett 2009;16:485–7.
- [20] Ortiz-Cruz A, Rodriguez E, Ibarra-Valdez C, Alvarez-Ramirez J. Efficiency of crude oil markets: Evidences from informational entropy analysis. Energy Policy 2012;41:365–73.
- [21] Shannon CE, Weaver W. The mathematical theory of communication. Champaign, IL: University of Illinois Press; 1949.
- [22] Feldman DP, Crutchfield JP. Measures of statistical complexity: Why? Phys Lett A 1998;238:244–52.
- [23] López-Ruiz R, Mancini HL, Calbet X. A statistical measure of complexity, physics. Letters A 1995;209:321–6.
- [24] Martín M, Plastino A, Rosso O. Statistical complexity and disequilibrium. Phys Lett A 2003;311:126–32.
- [25] Lamberti PW, Martín MT, Plastino A, Rosso OA. Intensive entropic non-triviality measure. Physica A 2004;334:119–31.
- [26] Martín MT, Plastino A, Rosso OA. Generalized statistical complexity measures: Geometrical and analytical properties. Physica A 2006;369:439–62.

- [27] Soriano MC, Zunino L, Rosso OA, Fischer I, Mirasso CR. Time scales of a chaotic semiconductor laser with optical feedback under the lens of a permutation information analysis. IEEE J Quantum Electron 2011;47:252–61.
- [28] Zunino L, Soriano MC, Fischer I, Rosso OA, Mirasso CR. Permutation-information-theory approach to unveil delay dynamics from time-series analysis. Phys Rev E 2010;82:046212.
- [29] Zunino L, Zanin M, Tabak BM, Pérez DG, Rosso OA. Complexity-entropy causality plane: A useful approach to quantify the stock market inefficiency. Phys A Stat Mech Appl 2010;389:1891–1901.
- [30] Zunino L, Tabak BM, Serinaldi F, Zanin M, Pérez DG, Rosso OA. Commodity predictability analysis with a permutation information theory approach. Phys A Stat Mech Appl 2011;390:876–90.
- [31] Rosso OA, Larrondo HA, Martín MT, Plastino A, Fuentes MA. Distinguishing noise from chaos. Phys Rev Lett 2007;99:154102.
- [32] Bandt C, Pompe B. Permutation entropy: A natural complexity measure for time series. Phys Rev Lett 2002;88:174102.
- [33] Saco PM, Carpi LC, Figliola A, Serrano E, Rosso OA. Entropy analysis of the dynamics of el niño southern oscillation during the holocene. Phys A Stat Mech Appl 2010;389:5022–7.

- [34] Keller K, Sinn M. Ordinal analysis of time series. Phys A Stat Mech Appl 2005;356:114–20.
- [35] Zunino L, Bariviera AF, Guercio MB, Martinez LB, Rosso OA. On the efficiency of sovereign bond markets. Physica A 2012;391:4342–9.
- [36] Serinaldi F, Zunino L, Rosso OA. Complexity-entropy analysis of daily stream flow time series in the continental united states. Stoch Environ Res Risk Assess 2014;28:1685–708.
- [37] Zanin M, Zunino L, Rosso OA, Papo D. Permutation entropy and its main biomedical and econophysics applications: A review. Entropy 2012;14:1553-77.
- [38] Samuelson PA. Proof that properly anticipated prices fluctuate randomly. Ind Manag Rev 1965;6:41–9.
- [39] Bariviera AF, Guercio MB, Martinez LB. A comparative analysis of the informational efficiency of the fixed income market in seven European countries. Econ Lett 2012;116:426–8.
- [40] Bariviera AF, Martíin MT, Plastino A, Vampa V. LIBOR troubles: Anomalous movements detection based on maximum entropy. Phys A Stat Mech Appl 2016;449:401–7.
- [41] Bariviera AF, Zunino L, Guercio MB, Martinez LB, Rosso OA. Revisiting the European sovereign bonds with a permutation informationtheory approach. Eur Phys J B 2013;86:509.