# DFT calculation of the chromyl nitrate, $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ The molecular force field 

S.A. Brandán, M.L. Roldán, C. Socolsky, A. Ben Altabef *,1<br>Cátedra de Fisicoquímica I, Instituto de Química Física, Facultad de Bioquímica, Química y Farmacia, Universidad Nacional de Tucumán, San Lorenzo 456, T4000CAN Tucumán, Argentina

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#### Abstract

We have carried out a structural and vibrational theoretical study for chromyl nitrate. The density functional theory has been used to study its structure and vibrational properties. The geometries were fully optimised at the B3LYP/Lan12DZ, B3LYP/6-31G* and B3LYP/6-311++G levels of theory and the harmonic vibrational frequencies were evaluated at the same levels. The calculated harmonic vibrational frequencies for chromyl nitrate are consistent with the experimental IR and Raman spectra in the solid and liquid phases. These calculations gave us a precise knowledge of the normal modes of vibration taking into account the type of coordination adopted by nitrate groups of this compound as monodentate and bidentate. We have also made the assignment of all the observed bands in the vibrational spectra for chromyl nitrate. The nature of the $\mathrm{Cr}-\mathrm{O}$ and $\mathrm{Cr} \leftarrow \mathrm{O}$ bonds in the compound were quantitatively investigated by means of Natural Bond Order (NBO) analysis. The topological properties of electronic charge density are analysed employing Bader's Atoms in Molecules theory (AIM). © 2007 Elsevier B.V. All rights reserved.


Keywords: $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$; Coordination monodentate; Coordination bidentate; DFT; Vibrational spectra; Theoretical study; Molecular geometry; Force field

## 1. Introduction

The study of compounds that contains transition metals, such as V and Cr [1-6] is of great interest in our laboratory. The compounds with the nitrate group as ligand are particularly interesting because this group is a versatile ligand and can act as monodentate or bidentate ligand [7]. The mode of coordination adopted by nitrate groups and the stereochemistry of this compound are important in relation to the vibrational properties and chemical reactivity [8-10]. The chromyl nitrate, $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$, compound presents vibrational properties imperfectly described and only the main characteristics of the infrared spectrum were published in liquid phase [11] and in previous studies we have assigned some bands observed in the vibrational spectra of the chromyl nitrate [1]. Marsden et al. have studied the gas-phase molecular structure of chromyl nitrate, $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$, by electron diffraction at a temperature of $50^{\circ} \mathrm{C}$ and by ab initio methods

[^0]at the HF level [12]. In this case the diffraction data are consistent with $C_{2}$ symmetry for the molecule. The Cr coordination is best described as derived from a severely distorted octahedron, since the nitrate group's act as bidentate ligands which are asymmetrically bonded to Cr .

This dark red liquid compound, can be obtained by several methods $[11-16]$ and it is very reactive at room temperature but less unstable than other compounds with the chromyl group [17,18]. The aim of this work is to carry out an experimental and theoretical study on this compound with the methods of quantum chemistry in order to have a better understanding of its vibrational properties. A precise knowledge of the normal modes of vibration is expected to provide a foundation for understanding the conformation-sensitive bands in vibrational spectra of this molecule. In this case the normal mode calculations were accomplished using a generalized valence force field (GVFF) and considering the nitrate group as monodentate and bidentate ligand. In the present work we have performed an experimental and theoretical study of chromyl nitrate, $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$, in order to study the coordination mode of nitrate groups and carry out its complete assignment. For that purpose, the optimised geometry and frequencies for the normal modes of vibration were calculated. In this case, there are no publications about experimental
or high-level theoretical studies on the geometries and force field of chromyl nitrate. Hence, obtaining reliable parameters by theoretical methods is an appealing alternative. The parameters obtained may be used to gain chemical and vibrational insights into related compounds. The election of the method and the basis sets are very important to evaluate not only the best level of theory but also the best basis set to be used to reproduce the experimental geometry and the vibrational frequencies. In previous studies of compounds that contain metal transition such as $\mathrm{VO}_{2} \mathrm{X}_{2}{ }^{-}(\mathrm{X}=\mathrm{F}, \mathrm{Cl})$ anions [3] the HF and MP2 methodologies are much less satisfactory than the DFT techniques specially for the $\mathrm{V}-\mathrm{Cl}$ distance. In this case the basis set that best reproduces the experimental geometrical parameters for the chloro compound is B3PW91/6-311G* while the inclusion of polarization functions is important to have a better agreement. In the $\mathrm{VOX}_{3}(\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}, \mathrm{I})$ series the optimised geometry which better reproduces the experimental parameters was obtained with the B3PW91/6-311G calculation while the B3LYP method produces the best results for the vibrational frequencies [4]. In a recent paper about oxotetrachlorochromate (V) anion [6] it was found that the inclusion of polarization functions in the basis sets significantly improved the theoretical geometry results and the lowest deviation with reference to the experimental data was obtained for the 6-31G* and 6-311G* basis sets and the B3PW91 functional [6]. In this case the lower difference between theoretical and experimental frequencies, measured by the root mean standard deviation (RMSD) was obtained with the combination B3LYP/6-31+G. We obtained similar results in the study of the [ $\mathrm{VOCl}_{4}$ ] ${ }^{-}$anion [5]. In the study of the structures and vibrational spectra of chromium oxo anions and oxyhalide compounds, Bell and Dines [19] have found that B3LYP/Lan12DZ combination gives the best fit for the geometries and observed vibrational spectra.

In this case, we used DFT calculations to study the structure and the vibrational properties of the compound. The normal mode calculations were accomplished by use of a GVFF. Here, we demonstrate that a molecular force field for the chromyl nitrate, considering the nitrate group as well as monodentate and bidentate ligand calculated using the DFT/Lanl2DZ, $6-31 \mathrm{G}^{*}$ and 6-311+G combinations is well represented. We obtained the force field scaling factors which produce satisfactory agreement between the calculated and experimental vibrational frequencies of chromyl nitrate. DFT normal mode assignments, in terms of the potential energy distribution (P.E.D.), are in general accord with those obtained from the normal coordinate analysis. Also, the nature of the two types of $\mathrm{Cr}-\mathrm{O}$ and $\mathrm{Cr} \leftarrow \mathrm{O}$ bonds in chromyl nitrate was systematically and quantitatively investigated by the NBO analysis [20-22]. In addition, the topological properties of electronic charge density are analysed employing Bader's Atoms in Molecules theory (AIM) [23].

## 2. Experimental

The infrared and Raman spectra of chromyl nitrate, $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$, were taken from a previous study where the compound was obtained as reported in Ref. [16] and from our measurements [1].

## 3. Computational details

All the calculations were made using the GAUSSIAN 03 [24] set of programs running on a PC Pentium III working under Windows operative system. Geometry calculations were performed using standard gradient techniques and the default convergence criteria as implemented in GAUSSIAN. The starting point for the geometry optimisation was modelled with the GAUSSIAN View program [25]. Calculations were made with hybrid density functional methods (DFT). In that last technique, Becke's three-parameter functional and the non-local correlation provided by Lee-Yang-Parr's (B3LYP) [26,27] expressions were used, as implemented in the GAUSSIAN programs. The Lanl2DZ, STO-3G, 3-21G*, 6-31G, 6-31G*, 6-31+G, 6-31+G*, $6-311 \mathrm{G}, 6-311 \mathrm{G}^{*}, 6-311+\mathrm{G}$ and $6-311+\mathrm{G}^{*}$ basis sets were used. For the compound we realized the normal mode analysis using Lanl2DZ, 6-31G* and 6-311+G basis sets.

The harmonic force field in Cartesian coordinates for chromyl nitrate which resulted from the calculations were transformed to "natural" internal coordinates [28] by the MOLVIB program [29,30]. The natural coordinates for monodentate and bidentate chromyl nitrate are shown in Tables 1 and 2, respectively, and have been defined as proposed by Fogarasi and Pulay [31]. Also, the analysis as bidentate ligand was performed with the three basis sets considering the nitrate groups as two rings of four members where the deformations and torsion coordinates of these groups have been defined as proposed by Fogarasi and Pulay [31] and are observed in Table 3. The numbering of the atoms for monodentate and bidentate chromyl nitrate is described in Figs. 1 and 2.

The force field was scaled and refined using, the MOLVIB program [29,30], in which the force constants are multiplied by scale factors until reproducing the experimental frequencies as


Fig. 1. The molecular structure of chromyl nitrate considering the nitrate group as monodentate ligand.

Table 1
Definition of natural internal coordinates for chromyl nitrate with monodentate coordination adopted by nitrate groups
Symmetry A

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    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(5-6)+\mathrm{s}(9-11)+\mathrm{s}(9-10)\)
    \(S_{2}=s(5-7)+s(9-11)-s(5-6)-s(9-10)\)
    \(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
    \(S_{4}=2 \beta(6-5-7)+2 \beta(10-9-11)-\beta(4-5-6)-\beta(4-5-7)-\beta(8-9-10)-\beta(8-9-11)\)
    \(S_{5}=\gamma(11-9-10)-\gamma(7-5-4-6)\)
    \(S_{6}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
    \(\mathrm{S}_{7}=\mathrm{s}(5-4)+\mathrm{s}(9-8)\)
    \(\mathrm{S}_{8}=\mathrm{r}(1-4)-\mathrm{r}(1-8)\)
    \(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-8)\)
    \(\mathrm{S}_{10}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{11}=\alpha(5-4-1)+\alpha(9-8-1)\)
    \(\mathrm{S}_{12}=\tau(3-1-4-5)+\tau(2-1-8-9)\)
    \(\mathrm{S}_{13}=\psi(2-1-8)+\psi(3-1-4)-\psi(2-1-4)-\psi(3-1-8)\)
    \(\mathrm{S}_{14}=\phi(4-1-8)\)
Symmetry B
    \(\mathrm{S}_{15}=\mathrm{s}(5-7)+\mathrm{s}(5-6)-\mathrm{s}(9-11)-\mathrm{s}(9-10)\)
    \(S_{16}=s(5-7)+s(9-10)-s(5-6)-s(9-11)\)
    \(\mathrm{S}_{17}=\mathrm{q}(1-2)-\mathrm{q}(1-3)\)
    \(\mathrm{S}_{18}=2 \beta(6-5-7)-2 \beta(10-9-11)-\beta(4-5-6)-\beta(4-5-7)+\beta(8-9-10)+\beta(8-9-11)\)
    \(\mathrm{S}_{19}=\gamma(11-9-8-10)+\gamma(7-5-4-6)\)
    \(S_{20}=2 \beta(4-5-6)-2 \beta(8-9-10)+\beta(8-9-10)+\beta(10-9-11)-\beta(4-5-7)-\beta(6-5-7)\)
    \(\mathrm{S}_{21}=\mathrm{s}(5-4)-\mathrm{s}(9-8)\)
    \(\mathrm{S}_{22}=\theta(2-1-3)\)
    \(\mathrm{S}_{23}=\psi(2-1-4)+\psi(3-1-4)-\psi(2-1-8)-\psi(3-1-8)\)
    \(\mathrm{S}_{24}=\alpha(5-4-1)-\alpha(9-8-1)\)
    \(\mathrm{S}_{25}=\tau(3-1-4-5)-\tau(2-1-8-9)\)
    \(\mathrm{S}_{26}=\tau(10-9-8-1)+\tau(11-9-8-1)-\tau(7-5-4-1)-\tau(6-5-4-1)\)
    \(\mathrm{S}_{27}=\psi(3-1-4)+\psi(3-1-8)-\psi(2-1-4)-\psi(2-1-8)\)
\(\nu s\left(\mathrm{NO}_{2}\right)\) ip
\(\nu \mathrm{a}\left(\mathrm{NO}_{2}\right)\) ip
    \(\nu \mathrm{s}(\mathrm{Cr}=\mathrm{O})\)
\(\delta\left(\mathrm{NO}_{2}\right)\) ip
\(\gamma \mathrm{N}=\mathrm{O}\) ор
\(\delta(\mathrm{O}=\mathrm{N}-\mathrm{O})\) ip
\(\nu \mathrm{s}(\mathrm{N}-\mathrm{O})\)
\(\nu \mathrm{L}(\mathrm{N}-\mathrm{O})\)
\(\nu \mathrm{Cr}-\mathrm{O})\)
\(\nu \mathrm{s}(\mathrm{Cr}-\mathrm{O})\)
\(\tau\left(\mathrm{NO}_{2}\right)\) ip
\(\delta(\mathrm{N}-\mathrm{O}-\mathrm{Cr})\) ip
\(\rho\left(\mathrm{NO}_{2}\right)\) ip
\(\rho\left(\mathrm{CrO}_{2}\right)\)
\(\delta(\mathrm{O}-\mathrm{Cr}-\mathrm{O})\)
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(
$\mathrm{q}=\mathrm{Cr}=\mathrm{O}$ bond distance; $\mathrm{r}=\mathrm{Cr}-\mathrm{O}$ bond distance; $\mathrm{s}=\mathrm{N}-\mathrm{O}$ bond distance; $\theta=\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ bond angle; $\phi=\mathrm{O}-\mathrm{Cr}-\mathrm{O}$ bond angle; $\psi=\mathrm{O}=\mathrm{Cr}-\mathrm{O}$ bond angles; $\alpha=\mathrm{Cr}-\mathrm{O}-\mathrm{N}$ bond angle; $\beta=\mathrm{O}-\mathrm{N}-\mathrm{O}$ bond angle. Abbreviations: $\nu$, stretching; $\delta$, deformation; $\rho$, in the plane bending or rocking; $\gamma$, out of plane bending or wagging; $\tau \mathrm{w}$, twisting; a, antisymmetric, s, symmetric; ip, in phase; op, out of phase.


Fig. 2. The molecular structure of chromyl nitrate considering the nitrate group as bidentate ligand.
well as possible. The potential energy distribution components larger than or equal to $10 \%$ are subsequently calculated with the resulting scaled quantum mechanics (SQM) force field.

An NBO analysis was then performed using the same basis sets with the NBO 3.1 program [32] included in GAUSSIAN 03 package programs [24]. The topological properties of the charge density in all systems studied were computed with the AIM2000 software [33].

## 4. Results and discussion

### 4.1. Geometry calculations

The B3LYP structures obtained for chromyl nitrate with the different basis sets have $C_{2}$ symmetries like to the experimental structure obtained by diffraction data and HF method by Marsden et al. [12]. Table 4 shows the comparison of the total energies and dipole moments values for chromyl nitrate with the B3LYP method using different basis sets. In all cases, the more stable structure is obtained using B3LYP/6-311+G* method combined with a diffuse function basis set while the structure with higher energy is obtained by B3LYP/Lan12DZ calculation. The higher dipole moment value agrees with the one obtained with the $6-311+G^{*}$ basis set and this indicates that the largest dipole moment value stabilizes the molecule.

Table 2
Definition of natural internal coordinates for chromyl nitrate with bidentate coordination adopted by nitrate groups

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Symmetry A
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    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
    \(\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
\(\mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
\(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3)\)
\(\mathrm{S}_{4}=2 \beta(4-5-6)+2 \beta(8-9-10)-\beta(4-5-7)-\beta(6-5-7)-\beta(8-9-11)-\beta(10-9-11)\)
\(\mathrm{S}_{5}=\gamma(11-9-8-10)-\gamma(7-5-4-6-)\)
\(\mathrm{S}_{6}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
\(\mathrm{S}_{7}=2 \beta(5-6-7)-2 \beta(9-10-11)+\beta(8-9-10)+\beta(8-9-11)-\beta(4-5-6)-\beta(4-5-7)\)
\(\mathrm{S}_{8}=\theta(2-1-3)\)
\(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
\(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
\(\mathrm{S}_{11}=\mathrm{r}(1-4)+\mathrm{r}(1-8)-\mathrm{r}(1-6)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{12}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
\(\mathrm{S}_{13}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
\(\mathrm{S}_{14}=\tau(10-9-8-1)+\tau(11-9-8-1)+\tau(7-5-4-1)+\tau(6-5-4-1)\)
Symmetry B
    \(\mathrm{S}_{15}=\mathrm{s}(5-7)+\mathrm{s}(9-11)\)
    \(\mathrm{S}_{16}=\mathrm{s}(4-5)+\mathrm{s}(8-9)-\mathrm{s}(5-6)-\mathrm{s}(9-10)\)
    \(\mathrm{S}_{17}=\mathrm{q}(1-2)-\mathrm{q}(1-3)\)
    \(S_{18}=2 \beta(4-5-6)-2 \beta(8-9-10)+\beta(8-9-10)+\beta(10-9-11)-\beta(4-5-7)-\beta(6-5-7)\)
    \(\mathrm{S}_{19}=\gamma(11-9-8-10)+\gamma(7-5-4-6)\)
    \(\mathrm{S}_{20}=\mathrm{s}(4-5)+\mathrm{s}(5-6)+\mathrm{s}(8-9)+\mathrm{s}(9-10)\)
    \(S_{21}=2 \beta(5-6-7)+2 \beta(9-10-11)-\beta(4-5-6)-\beta(4-5-7)-\beta(8-9-10)-\beta(8-9-11)\)
    \(\mathrm{S}_{22}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
    \(\mathrm{S}_{23}=\tau(10-9-8-1)+\tau(11-9-8-1)-\tau(7-5-4-1)-\tau(6-5-4-1)\)
    \(S_{24}=\psi(2-1-6)+\psi(3-1-4)+\psi(2-1-4)+\psi(3-1-6)-\psi(2-1-8)-\psi(3-1-10)-\psi(2-1-10)-\psi(3-1-8)\)
    \(\mathrm{S}_{25}=\phi(8-1-4)+\phi(10-1-6)\)
    \(\mathrm{S}_{26}=\phi(8-1-4)-\phi(10-1-6)\)
    \(\mathrm{S}_{27}=\tau(3-1-4-5)+\tau(3-1-10-9)-\tau(2-1-8-9)-\tau(2-1-6-5)\)
    \(\nu(\mathrm{N}=\mathrm{O})\) ip
\(\nu \mathrm{a}\left(\mathrm{NO}_{2}\right)\) op
\(\nu \mathrm{s}(\mathrm{Cr}=\mathrm{O})\)
    \(\delta\left(\mathrm{NO}_{2}\right)\) ip
    \(\gamma \mathrm{N}=\mathrm{O}\) op
    \(\mathrm{vs}\left(\mathrm{NO}_{2}\right)\) op
    \(\delta(\mathrm{O}=\mathrm{N}-\mathrm{O})\) op
    \(\delta\left(\mathrm{CrO}_{2}\right)\)
    \(\nu s(\mathrm{Cr}-\mathrm{O})\)
    \(\rho\left(\mathrm{CrO}_{2}\right)\)
    \(\mathrm{va}(\mathrm{Cr}-\mathrm{O})\)
    \(\tau \mathrm{w}\left(\mathrm{CrO}_{2}\right)\)
    \(\tau \mathrm{w}\left(\mathrm{CrO}_{2}\right)\)
\(\nu(\mathrm{Cr} \leftarrow \mathrm{O})\)
\(\tau\left(\mathrm{NO}_{2}\right)\) ip
    \(\nu(\mathrm{N}=\mathrm{O})\) op
    \(\mathrm{va}\left(\mathrm{NO}_{2}\right)\) ip
    \(\nu \mathrm{a}(\mathrm{Cr}=\mathrm{O})\)
    \(\delta\left(\mathrm{NO}_{2}\right)\) op
    \(\gamma \mathrm{N}=\mathrm{O}\) ip
    \(\nu s\left(\mathrm{NO}_{2}\right)\) ip
\(\delta(\mathrm{O}=\mathrm{N}-\mathrm{O})\) ip
\(\mathrm{va}(\mathrm{Cr} \leftarrow \mathrm{O})\)
\(\tau\left(\mathrm{NO}_{2}\right)\) op
\(\operatorname{wag}\left(\mathrm{CrO}_{2}\right)\)
\(\delta \mathrm{s}(\mathrm{O}-\mathrm{Cr}-\mathrm{O})\)
\(\mathrm{\delta a}(\mathrm{O}-\mathrm{Cr}-\mathrm{O})\)
\(\tau(\mathrm{N}=\mathrm{O})\)
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$\mathrm{q}=\mathrm{Cr}=\mathrm{O}$ bond distance; $\mathrm{r}=\mathrm{Cr}-\mathrm{O}$ bond distance; $\mathrm{s}=\mathrm{N}-\mathrm{O}$ bond distance; $\theta=\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ bond angle; $\phi=\mathrm{O}-\mathrm{Cr}-\mathrm{O}$ bond angle; $\psi=\mathrm{O}=\mathrm{Cr}-\mathrm{O}$ bond angles; $\beta=\mathrm{O}-\mathrm{N}-\mathrm{O}$ bond angle. Abbreviations: $\nu$, stretching; $\delta$, deformation; $\rho$, in the plane bending or rocking; $\gamma$, out of plane bending or wagging; $\tau w$, twisting; a, antisymmetric, s, symmetric; ip, in phase; op, out of phase.

Although the calculated structure with the Lanl2DZ basis set is unstable, the dipole moment value is comparable to the corresponding values obtained with the $6-31 \mathrm{G}^{*}$ and $6-31+\mathrm{G}$ basis sets.

The results of the calculations with all basis sets used can be appreciated in Table 5. According to these results, the method and basis set that best reproduces the experimental geometrical parameters for the chromyl nitrate compound is B3LYP/6$31+G^{*}$ where the mean difference for bond lengths is $0.019 \AA$, while with B3LYP/6-311G* it is $4.11^{\circ}$ for angles. The inclusion of polarization functions, however, is important to have a better agreement with the experimental geometry: mean differences degrade to $0.020 \AA$ and $4.24^{\circ}$ for the $6-311+G^{*}$ basis set. The B3LYP functional gives somewhat less satisfactory agreement using the Lanl2DZ ( $0.399 \AA$ and $7.90^{\circ}$ ) and STO-3G ( $0.107 \AA$ and 5.42) basis sets, contrary to what was observed by Bell and Dines [19] in chromium oxo anions and oxyhalides compounds. In our case, similarly to the experimental structure [12], also with B3LYP calculations, we can represent the coordination around Cr as derived from a severely distorted octahedron where the nitrate groups act as bidentate ligands and are asymmetrically bonded to Cr. The bond orders, expressed by Wiberg's indexes for chromyl nitrate are given in Tables S1 and S2 of the Supporting Material. We can see that the chromium atom forms six bonds, two $\mathrm{Cr}=\mathrm{O}$ bonds (bond order 1.9721 using 6-311+G basis set), two Cr-O (bond order 0.5374 using $6-311+G$ basis
set) and two $\mathrm{Cr} \leftarrow \mathrm{O}$ (bond order 0.1821 using $6-311+\mathrm{G}$ basis set). The bond order value of this last bond was estimated by Marsden et al. [12] between 0.19 and 0.29 . Experimentally the $\mathrm{Cr}-\mathrm{O}-\mathrm{NO}_{2}$ group is slightly non-planar with the dihedral angle of the planes $\mathrm{Cr}-\mathrm{O}-\mathrm{N}$ and $\mathrm{NO}_{2}$ equal to $16^{\circ}$ while in our B3LYP calculations the $\mathrm{Cr}-\mathrm{O}-\mathrm{N}-\mathrm{O}$ angle values are between 0.9 and $2.0^{\circ}$, as can be seen in Table 5. In this case the two $\mathrm{NO}_{2}$ groups are practically planar with the Cr atom and there is a slightly torsional motion around either of the $\mathrm{Cr}-\mathrm{O}$ bonds as was observed by the diffraction method. However, the bond orders obtained for chromyl nitrate with the three basis sets agree with the 0.4 values reported in symmetrically bidentate nitrate groups [7].

Other very important observations in these B3LYP calculations carried out precisely by Marsden et al. [12] with ab initio method are those that predict that the $\mathrm{O} 2=\mathrm{Cr} 1=\mathrm{O} 3$ bond angle in chromyl nitrate is smaller than the $\mathrm{O} 4-\mathrm{Cr} 1-\mathrm{O} 8$ angle, in contradiction with the valence-shell electron-pair (VSEPR) theory [34,35]. In fact, that theory predicts a larger angle between the bonds of the central atom with the two oxygen atoms in these pseudo-tetrahedral species as a consequence of the larger space in the coordination sphere requested by the pair of double bonds. In this case a possible explanation for the inverse angle relationship is due to the octahedral coordination for the Cr atom in the compound. A possible explanation for the inverse relationship obtained for chromyl nitrate can be given in terms of the

Table 3
Definition of natural internal coordinates for chromyl nitrate with bidentate coordination adopted for nitrate groups (as two rings of four members)

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Symmetry A
    \(\begin{array}{ll}\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11) & \nu(\mathrm{N}=\mathrm{O}) \text { ip } \\ \mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(8-9)-\mathrm{s}(5-6)-\mathrm{s}(9-10) & \nu a\left(\mathrm{NO}_{2}\right) \text { ip }\end{array}\)
    \(\begin{array}{ll}\mathrm{S}_{1}=\mathrm{s}(5-7)+\mathrm{s}(9-11) & \nu(\mathrm{N}=\mathrm{O}) \text { ip } \\ \mathrm{S}_{2}=\mathrm{s}(4-5)+\mathrm{s}(8-9)-\mathrm{s}(5-6)-\mathrm{s}(9-10) & \nu \mathrm{a}\left(\mathrm{NO}_{2}\right) \mathrm{ip}\end{array}\)
    \(\mathrm{S}_{3}=\mathrm{q}(1-2)+\mathrm{q}(1-3) \quad \mathrm{vs}(\mathrm{Cr}=\mathrm{O})\)
    \(\mathrm{S}_{4}=\mathrm{s}(4-5)+\mathrm{s}(5-6)+\mathrm{s}(8-9)+\mathrm{s}(9-10)\)
    \(S_{5}=\beta(6-5-4)+\beta(4-1-6)+\beta(8-9-10)+\beta(10-1-8)-\beta(5-4-1)-\beta(1-6-5)-\beta(9-10-1)-\beta(1-8-9)\)
    \(\mathrm{S}_{6}=\gamma(11-9-8-10)+\gamma(7-5-4-6)\)
    \(\mathrm{S}_{7}=\beta(4-5-7)+\beta(8-9-11)-\beta(5-6-7)-\beta(10-9-11)\)
    \(\mathrm{S}_{8}=\theta(2-1-3)\)
    \(\mathrm{S}_{9}=\mathrm{r}(1-4)+\mathrm{r}(1-6)+\mathrm{r}(1-8)+\mathrm{r}(1-10)\)
    \(\mathrm{S}_{10}=\psi(2-1-6)+\psi(2-1-4)+\psi(3-1-8)+\psi(3-1-10)-\psi(3-1-6)-\psi(3-1-4)-\psi(2-1-8)-\psi(2-1-10)\)
    \(S_{11}=r(1-4)+r(1-8)-r(1-6)-r(1-10)\)
    \(\mathrm{S}_{12}=\phi(8-1-4)-\phi(10-1-6)\)
    \(\mathrm{S}_{13}=\tau(6-1-4-5)+\tau(4-5-6-1)+\tau(8-1-10-9)+\tau(10-9-8-1)-\tau(1-4-5-6)+\tau(5-6-1-4)+\tau(1-10-9-8)-\tau(9-8-1-10)\)
\(\mathrm{S}_{14}=\tau(6-1-4-5)+\tau(4-5-6-1)+\tau(1-10-9-8)+\tau(9-8-1-10)-\tau(1-4-5-6)-\tau(5-6-1-4)-\tau(8-1-10-9)-\tau(10-9-8-1)\)
    \(\mathrm{S}_{13}=\tau(6-1-4-5)+\tau(4-5-6-1)+\tau(8-1-10-9)+\tau(10-9-8-1)-\tau(1-4-5-6)+\tau(5-6-1-4)+\tau(1-10-9-8)-\tau(9-8-1-10)\)
\(\mathrm{S}_{14}=\tau(6-1-4-5)+\tau(4-5-6-1)+\tau(1-10-9-8)+\tau(9-8-1-10)-\tau(1-4-5-6)-\tau(5-6-1-4)-\tau(8-1-10-9)-\tau(10-9-8-1)\)
Symmetry B
    \(\mathrm{S}_{15}=\mathrm{s}(5-7)-\mathrm{s}(9-11)\)
    \(\mathrm{S}_{16}=\mathrm{s}(4-5)+\mathrm{s}(9-10)-\mathrm{s}(5-6)-\mathrm{s}(8-9)\)
    \(\mathrm{S}_{17}=\mathrm{q}(1-2)-\mathrm{q}(1-3)\)
    \(\mathrm{S}_{18}=\mathrm{s}(4-5)+\mathrm{s}(5-6)-\mathrm{s}(8-9)-\mathrm{s}(9-10)\)
    \(\mathrm{S}_{19}=\beta(6-5-4)+\beta(4-1-6)+\beta(9-10-1)+\beta(1-8-9)-\beta(5-4-1)-\beta(1-6-5)-\beta(8-9-10)-\beta(10-1-8)\)
    \(\mathrm{S}_{20}=\gamma(11-9-8-10)-\gamma(7-8-4-6)\)
    \(S_{21}=\beta(4-5-7)+\beta(10-9-11)-\beta(5-6-7)-\beta(8-9-11)\)
    \(\mathrm{S}_{22}=\mathrm{r}(1-4)+\mathrm{r}(1-6)-\mathrm{r}(1-8)-\mathrm{r}(1-10)\)
    \(\mathrm{S}_{23}=\psi(2-1-6)+\psi(3-1-4)+\psi(2-1-4)+\psi(3-1-6)-\psi(2-1-8)-\psi(3-1-10)-\psi(2-1-10)-\psi(3-1-8)\)
    \(\mathrm{S}_{24}=\psi(2-1-6)+\psi(3-1-6)+\psi(2-1-8)+\psi(3-1-8)-\psi(2-1-4)-\psi(3-1-4)-\psi(2-1-10)-\psi(3-1-10)\)
    \(\mathrm{S}_{25}=\tau(2-1-4-5)+\tau(3-1-4-5)+\tau(2-1-8-9)+\tau(3-1-8-9)+\tau(2-1-10-9)+\tau(3-1-10-9)+\tau(2-1-4-5)+\tau(3-1-4-5)\)
    \(\mathrm{S}_{26}=\phi(8-1-4)+\phi(10-1-6)\)
    \(\mathrm{S}_{27}=\mathrm{r}(1-6)+\mathrm{r}(1-8)-\mathrm{r}(1-4)-\mathrm{r}(1-10)\)
    \(\nu s(\mathrm{Cr}=\mathrm{O})\)
\(\nu s\left(\mathrm{NO}_{2}\right)\) ip
\(\mathrm{vs}\left(\mathrm{NO}_{2}\right)\) ip
\(\delta\left(\mathrm{NO}_{2}\right)\) ip
\(\gamma \mathrm{N}=\mathrm{O}\) ip
\(\delta(\mathrm{O}=\mathrm{N}-\mathrm{O})\) ip
\(\delta\left(\mathrm{CrO}_{2}\right)\)
\(\nu s(\mathrm{Cr}-\mathrm{O})\)
\(\rho\left(\mathrm{CrO}_{2}\right)\)
\(\nu \mathrm{p}(\mathrm{Cr}-\mathrm{O})\)
\(\mathrm{va}(\mathrm{Cr}-\mathrm{O})\)
\(\delta \mathrm{a}(\mathrm{O}-\mathrm{Cr}-\mathrm{O})\)
\(\tau\left(\mathrm{NO}_{2}\right)\) ip
\(\tau\left(\mathrm{NO}_{2}\right)\) op
\(\nu(\mathrm{N}=\mathrm{O})\) op
\(\nu \mathrm{a}\left(\mathrm{NO}_{2}\right)\) op
\(\nu \mathrm{a}(\mathrm{Cr}=\mathrm{O})\)
\(\nu s\left(\mathrm{NO}_{2}\right)\) op
\(\delta\left(\mathrm{NO}_{2}\right)\) op
\(\gamma \mathrm{N}=\mathrm{O}\) op
\(\delta(\mathrm{O}=\mathrm{N}-\mathrm{O})\) op
\(\nu s(\mathrm{Cr} \leftarrow \mathrm{O})\)
wag \(\left(\mathrm{CrO}_{2}\right)\)
\(\tau \mathrm{w}\left(\mathrm{CrO}_{2}\right)\)
\(\tau(\mathrm{N}=\mathrm{O})\)
\(\mathrm{s}(\mathrm{O}-\mathrm{Cr}-\mathrm{O})\)
```

$\mathrm{q}=\mathrm{Cr}=\mathrm{O}$ bond distance; $\mathrm{r}=\mathrm{Cr}-\mathrm{O}$ bond distance; $\mathrm{s}=\mathrm{N}-\mathrm{O}$ bond distance; $\theta=\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ bond angle; $\phi=\mathrm{O}-\mathrm{Cr}-\mathrm{O}$ bond angle; $\psi=\mathrm{O}=\mathrm{Cr}-\mathrm{O}$ bond angles; $\beta=\mathrm{O}-\mathrm{N}-\mathrm{O}$ bond angle. Abbreviations: $\nu$, stretching; $\delta$, deformation; $\rho$, in the plane bending or rocking; $\gamma$, out of plane bending or wagging; $\tau w$, twisting; a, antisymmetric, s , symmetric; ip, in phase; op, out of phase.
calculated Mulliken atomic charges. Such charges, taken from the DFT calculations (see Table S2 using 6-31G* and 6-311+G basis sets), have the following values: $\mathrm{Cr} 1.364, \mathrm{O} 2-0.317$, $\mathrm{O} 3-0.317$ and $\mathrm{O} 4-0.438$, O8 -0.438 . These numbers show (using $6-31 \mathrm{G}^{*}$ basis set) that the remarkably higher negative charge on the oxygen atoms of chromyl nitrate could result in a relatively larger $\mathrm{O} \cdots \mathrm{O}$ repulsion and consequently in a larger $\mathrm{O} 4-\mathrm{Cr} 1-\mathrm{O} 8$ angle $\left(141.6^{\circ}\right)$, which for such compound exceeds the $\mathrm{O} 2-\mathrm{Cr} 1-\mathrm{O} 3$ angle $\left(107.9^{\circ}\right)$. It is interesting to observe that these values of Mulliken atomic charges are very different from those attained at B3LYP/Lan12DZ and B3LYP/6-311+G* lev-

Table 4
Total energy and dipole moment for chromyl nitrate at B3LYP method

| Basis set | ET (Hartree) | $\mu(\mathrm{D})$ |
| :--- | :--- | :--- |
| Lan12DZ | -797.26788972 | 0.54 |
| STO-3G | -1735.04954605 | 0.14 |
| 3-21G* | -1746.64837014 | 0.28 |
| 6-31G | -1755.21237919 | 0.43 |
| 6-31G* | -1755.48635040 | 0.50 |
| 6-311G | -1755.49143234 | 0.67 |
| 6-31+G | -1755.25752525 | 0.59 |
| 6-31+G* | -1755.51881813 | 0.71 |
| 6-311G* | -1755.73534229 | 0.70 |
| 6-311+G | -1755.52645780 | 0.63 |
| 6-311+G* | -1755.76567840 | 0.73 |

els, only as regards the numerical values but not the relative order within them. The inclusion of diffuse functions makes the charge on the oxygen bounded to the Cr atom to be lower $(\mathrm{O}=\mathrm{Cr}=\mathrm{O})$ than that located on the other O atoms $(\mathrm{O}-\mathrm{Cr}-\mathrm{O})$ in this case these values are positive as shown in Table S2. This leads to the conclusion that any analysis based on the Mulliken atomic charges must be made with care as it is apparent that a satisfactory explanation based on electronegativity criteria is not affordable [3]. A somewhat different but related explanation might be tried on the basis of the delocalised and/or bonding characters of the relevant molecular orbitals (MO), as observed in the series of the $\mathrm{VO}_{2} \mathrm{X}_{2}^{-}$anions [3]. After a careful inspection of the atomic orbital coefficients (AO) appearing in the different MO it is possible to note that as a general pattern, the highest occupied MO's show a rather localised character on the oxygen atoms being mainly described as p-type orbitals. The atomic orbital coefficients (AO) for Cr atom of chromyl nitrate (d-type orbitals) using Lan12DZ, 6-31G* and 6-311+G basis sets are observed in Table S3 of the Supporting Material. For the chromyl nitrate the strongest bonding MO's involving Cr d-type orbitals that seem to be sensitive to the geometry can be considered, in increasing energy, those numbered as 13 (HOMO-31); 13 (HOMO-36) and 14 (HOMO-32) calculated with Lan12DZ basis set; 20 (HOMO-36), 21 (HOMO-36) and 22 (HOMO-37) calculated with $6-31 \mathrm{G}^{*}$ basis set while those numbered as 25 (HOMO-36), 26 (HOMO-37) and 31 (HOMO-37) calculated

Table 5
Comparison of experimental and calculated geometrical parameters at different levels of theory for chromyl nitrate

| Atoms | B3LYP method ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Lan12DZ | STO-3G | 3-21G | 6-31G | 6-31+G | 6-31+G* | 6-31G* | 6-311G | 6-311G* | 6-311+G | 6-311+G* | Exp. ${ }^{\text {b }}$ | $a b$ initio $^{\text {b }}$ |
| Bond length (Á) |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1,2 | 1.568 | 1.484 | 1.561 | 1.573 | 1.577 | 1.554 | 1.548 | 1.569 | 1.546 | 1.574 | 1.550 | 1.586 | 1.522 |
| 1,3 | 1.568 | 1.484 | 1.561 | 1.573 | 1.577 | 1.554 | 1.548 | 1.569 | 1.546 | 1.574 | 1.550 | 1.586 | 1.522 |
| 1,4 | 1.914 | 1.864 | 1.888 | 1.933. | 1.935 | 1.923 | 1.920 | 1.933 | 1.916 | 1.941 | 1.924 | 1.957 | 1.958 |
| 1,8 | 1.914 | 1.864 | 1.888 | 1.933 | 1.935 | 1.923 | 1.920 | 1.933 | 1.916 | 1.941 | 1.924 | 1.957 | 1.958 |
| 1,6 | 1.409 | 2.155 | 2.205 | 2.275 | 2.287 | 2.243 | 2.229 | 2.283 | 2.253 | 2.284 | 2.263 | 2.254 | 2.191 |
| 1,10 | 1.310 | 2.155 | 2.205 | 2.275 | 2.287 | 2.243 | 2.229 | 2.283 | 2.253 | 2.284 | 2.263 | 2.254 | 2.191 |
| 4,5 | 1.231 | 1.436 | 1.432 | 1.397 | 1.396 | 1.340 | 1.340 | 1.394 | 1.342 | 1.393 | 1.342 | 1.341 | 1.342 |
| 5,6 | 1.409 | 1.372 | 1.325 | 1.296 | 1.296 | 1.261 | 1.261 | 1.298 | 1.255 | 1.298 | 1.254 | 1.254 | 1.342 |
| 5,7 | 1.310 | 1.294 | 1.222 | 1.216 | 1.218 | 1.195 | 1.194 | 1.219 | 1.185 | 1.220 | 1.186 | 1.193 | 1.205 |
| 8,9 | 1.231 | 1.436 | 1.432 | 1.397 | 1.396 | 1.340 | 1.340 | 1.394 | 1.342 | 1.393 | 1.342 | 1.341 | 1.342 |
| 9,10 | 1.568 | 1.372 | 1.325 | 1.296 | 1.296 | 1.261 | 1.261 | 1.298 | 1.257 | 1.298 | 1.254 | 1.254 | 1.342 |
| 9,11 | 1.568 | 1.294 | 1.222 | 1.216 | 1.218 | 1.195 | 1.194 | 1.219 | 1.185 | 1.220 | 1.186 | 1.193 | 1.205 |
| RMSD (Á) | 0.399 | 0.107 | 0.060 | 0.033 | 0.034 | 0.019 | 0.024 | 0.034 | 0.024 | 0.033 | 0.020 |  |  |
| Bond angle ( ${ }^{\circ}$ ) |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2,1,3 | 108.2 | 107.5 | 107.1 | 107.8 | 107.9 | 108.0 | 107.9 | 108.0 | 108.0 | 107.9 | 108.1 | 112.6 | 105.0 |
| 2,1,4 | 105.2 | 103.2 | 104.6 | 104.9 | 105.1 | 105.5 | 105.2 | 104.8 | 104.8 | 105.2 | 105.4 | 97.2 | 105.5 |
| 2,1,8 | 97.3 | 96.2 | 96.9 | 97.3 | 97.3 | 97.0 | 97.1 | 96.9 | 97.5 | 97.1 | 97.5 | 104.5 | 105.5 |
| 3,1,4 | 97.3 | 96.2 | 96.9 | 97.3 | 97.3 | 97.0 | 97.1 | 96.9 | 97.5 | 97.1 | 97.5 | 104.5 | 105.5 |
| 3,1,8 | 105.2 | 103.2 | 104.6 | 104.9 | 105.1 | 105.5 | 105.2 | 104.8 | 104.8 | 105.2 | 105.4 | 97.2 | 105.5 |
| 4,1,8 | 141.2 | 146.9 | 143.4 | 141.9 | 141.6 | 141.3 | 141.6 | 142.6 | 141.6 | 141.6 | 140.6 | 140.4 | 146.9 |
| 6,1,10 | 101.0 | 72.6 | 73.2 | 73.5 | 73.9 | 75.0 | 74.5 | 74.3 | 74.6 | 73.8 | 74.5 | 82.8 |  |
| 1,4,5 | 110.0 | 96.7 | 97.9 | 99.5 | 99.9 | 99.6 | 99.2 | 99.9 | 100.1 | 99.7 | 100.2 | 97.5 | 99.0 |
| 4,5,6 | 121.2 | 108.2 | 108.7 | 110.3 | 110.5 | 111.5 | 111.4 | 110.3 | 111.4 | 110.5 | 111.6 | 112.2 |  |
| 4,5,7 | 128.7 | 123.3 | 122.1 | 121.3 | 121.2 | 120.9 | 120.9 | 121.3 | 120.8 | 121.3 | 120.7 | 119.7 |  |
| 6,5,7 | 101.0 | 128.4 | 129.2 | 128.4 | 128.3 | 127.6 | 127.6 | 128.4 | 127.8 | 128.2 | 127.7 | 128.1 |  |
| 1,8,9 | 110.0 | 96.7 | 97.9 | 99.5 | 99.9 | 99.6 | 99.2 | 99.9 | 100.1 | 99.7 | 100.2 | 97.5 | 99.0 |
| 8,9,10 | 121.2 | 108.2 | 108.7 | 110.3 | 110.5 | 111.5 | 111.4 | 110.3 | 111.4 | 110.5 | 111.6 | 112.2 |  |
| 8,9,11 | 128.7 | 123.3 | 122.1 | 121.4 | 121.2 | 120.9 | 120.9 | 121.3 | 120.8 | 121.3 | 120.7 | 119.7 |  |
| 10,9,11 | 108.23 | 128.4 | 129.2 | 128.4 | 128.3 | 127.6 | 127.6 | 128.4 | 127.8 | 128.2 | 127.7 | 128.1 |  |
| RMSD ( ${ }^{\circ}$ ) | 7.90 | 5.42 | 4.49 | 4.23 | 4.27 | 4.36 | 5.00 | 4.33 | 4.11 | 4.33 | 4.24 |  |  |
| Bond dihedral angle (degrees) |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2,1,4,5 | -82.6 | -84.9 | -84.2 | -83.8 | -83.2 | -82.5 | -83.0 | -83.6 | -83.1 | -83.5 | $-82.8$ |  |  |
| 3,1,4,5 | 166.2 | 165.4 | 166.0 | 165.4 | 165.9 | 166.4 | 166.1 | 165.6 | 165.9 | 165.6 | 165.9 |  |  |
| 8,1,4,5 | 40.6 | 39.4 | 39.8 | 39.7 | 40.2 | 40.7 | 40.3 | 39.9 | 40.4 | 39.9 | 40.4 |  |  |
| 2,1,8,9 | 166.2 | 165.4 | 166.0 | 165.4 | 165.9 | 166.4 | 166.1 | 165.6 | 165.9 | 165.6 | 165.9 |  |  |
| 3,1,8,9 | -82.6 | -84.9 | -84.2 | -83.8 | -83.2 | -82.5 | -83.0 | -83.6 | -83.1 | -83.5 | -82.8 |  |  |
| 4,1,8,9 | 40.6 | 39.4 | 39.8 | 39.7 | 40.2 | 40.7 | 40.3 | 39.9 | 40.4 | 39.9 | 40.4 |  |  |
| 1,4,5,6 | -1.3 | -1.957 | -1.6 | -0.9 | -1.3 | -1.2 | -1.1 | -0.8 | -1.1 | -0.9 | -0.9 | 16 |  |
| 1,4,5,7 | 179.1 | 179.4 | 178.9 | 179.6 | 178.9 | 179.0 | 179.2 | 179.0 | 179.2 | 179.4 | 179.3 |  |  |
| 1,8,9,10 | -1.3 | -195.7 | -156.3 | -0.9 | -1.3 | -1.2 | -11.2 | -0.8 | -11.3 | -0.9 | -0.9 |  |  |
| 1,8,9,11 | 179.1 | 179.4 | 178.9 | 179.6 | 178.9 | 179.0 | 179.2 | 179.7 | 179.2 | 179.4 | 179.3 |  |  |

${ }^{\text {a }}$ This work.
${ }^{\mathrm{b}}$ Ref. [12].
with $6-311+\mathrm{G}$ basis set tend to widen the $\mathrm{O} 4-\mathrm{Cr} 1-\mathrm{O} 8$ angle ( $125.3^{\circ}$ using $6-31 G^{*}$ basis set) on a maximum overlapping basis.

For chromyl nitrate the intermolecular interactions have been analysed by using Bader's topological analysis of the charge electron density, $\rho(r)$ by means of the AIM program [33]. It is necessary to clarify that in this study, the Lanl2DZ, 6-31G* and $6-311+G$ basis sets have been considered because there are numerous references where the quality of the basis set has no influence on the topological results $[36,37]$ but, in this case there is a significative difference among them as can be seen in Table S4 of the Supporting Material.

The localisation of the critical points in the $\rho(r)$ and the values of the Laplacian at these points are important for the characterization of molecular electronic structure in terms of interactions nature and magnitude. The details of the molecular models for the compound studied showing the geometry of all their critical points is observed in Fig. 3. The analyses of the $\mathrm{Cr} \leftarrow \mathrm{O}$ bonds critical points in the compound studied are reported with the two basis sets in Table S4. In this case two important observations can be seen for the three basis sets. In one case, the $\mathrm{Cr} 1 \leftarrow \mathrm{O} 6$ and $\mathrm{Cr} 1 \leftarrow \mathrm{O} 10$ bonds critical points have the typical properties of the closed-shell interaction. That is, the value of $\rho(r)$ are relatively low ( 0.05 and 0.3 a.u.), the


Fig. 3. The critical points of the charge density for chromyl nitrate.
relationship, $|\lambda 1| / \lambda 3$ are $<1$ and the Laplacian of the electron density, $\nabla^{2} \rho(r)(0.04$ and 0.2 a.u.), are positive indicating that the interaction is dominated by the contraction of charge away from the interatomic surface toward each nucleus [36-43]. The $\rho(r)$ and $\nabla^{2} \rho(r)$ at the critical points related to $\mathrm{Cr} 1 \leftarrow \mathrm{O} 10$ bonds, which compare well with the respective 0.395 and 1.164 a.u. values reported for the $\mathrm{Cr}-\mathrm{O}$ bond critical point in the $\mathrm{CrOF}_{4}$ compound [35]. The other important observation, is related to the topological properties of the $\mathrm{Cr} 1 \leftarrow \mathrm{O} 6$ and $\mathrm{Cr} 1 \leftarrow \mathrm{O} 10$ bonds critical points as shown in Table S4. In these cases, the electron densities values are between 0.4 and 0.5 a.u. while the negative values of the Laplacian of the electron density for the $\mathrm{Cr} \leftarrow \mathrm{O}$ bonds ( -0.2 and -0.8 a.u.), observed in Table S 4 , indicate that the $\mathrm{Cr} 1 \leftarrow \mathrm{O} 6$ and $\mathrm{Cr} 1 \leftarrow \mathrm{O} 10$ bonds critical points are not found in a region of charge depletion. The interaction $\mathrm{Cr} 1 \leftarrow \mathrm{O} 10$ bond is the same as the $\mathrm{Cr} 1 \leftarrow \mathrm{O} 6$ bond, which has the characteristic of the shared interaction, i.e. the value of electron density at the bond critical point is relatively high and the Laplacian of the charge density is negative indicating that the electronic charge is concentrated in the internuclear region. These values of the Laplacian of the charge density compare well with the -1.096 a.u. values reported for the $\mathrm{C}-\mathrm{H}$ bond critical point in the $\mathrm{VMe}_{5}$ compound [35]. Moreover, the $(3,+1)$ critical point as shown in Table S 4 in the chromyl nitrate would confirm the two $\mathrm{Cr} \leftarrow \mathrm{O}$ bond in the respective structure. The 12 critical points and the 2 ring points of the electron density obtained by AIM analysis reveals that the mode of coordination adopted for the nitrate groups in chromyl nitrate is bidentate, as shown in Fig. 3. Those above B3LYP level results analysed for chromyl nitrate are in agreement with the structure observed by electron-diffraction experiments in gas phase and strongly support the conclusions reported previously about the nature of the coordination of the Cr atom for this compound [12].

### 4.2. Vibrational frequencies

The structure for the compound has $C_{2}$ symmetry and 27 vibrational normal modes. All vibrational modes are infrared and


Fig. 4. Theoretical Infrared spectrum of $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ at different levels of theory.

Raman active. As it is impossible to make a difference between monodentate and bidentate nitrate groups on the grounds of infrared and Raman spectra alone $[7,9]$ we have performed this study taking into account both possibilities. The observed frequencies and the assignment for chromyl nitrate considering the coordination adopted by nitrate groups as monodentate and bidentate are given in Table 6 . Vibrational assignments were made on the basis of the potential energy distributions in terms of symmetry coordinates and by comparison with molecules that contain similar groups [1,44-52].

Table S5 of the Supporting Material shows the calculated harmonic frequencies for chromyl nitrate using B3LYP method with different basis sets. Note that the lowest theoretical frequency was not observed in the vibrational spectrum and for this reason we took these frequencies as experimental values. In all cases the theoretical values were compared with the respective experimental values by means of the RMSD values. It can be seen that the best results are obtained with a B3LYP/6-311+G calculation and that the introduction of diffuse functions (but not of polarization functions!) is essential to have a good approximation to the experimental values, especially in the case of the $\mathrm{Cr}=\mathrm{O}$ and $\mathrm{Cr}-\mathrm{O}$ stretchings. We will refer to the results obtained at B3LYP level with $6-31 \mathrm{G}^{*}$ basis set because after scaling this method a satisfactory agreement is obtained between the calculated and the experimental vibrational frequencies of chromyl nitrate. In general, the theoretical infrared and Raman spectra of the chromyl nitrate demonstrate good agreement with the experimental spectrum (especially in the higher intensity of the $\mathrm{Cr}=\mathrm{O}$ stretching bands (see Figs. 4 and 5). It is possible to observe that in all calculations some vibration modes of different symmetries are mixed among them because the frequencies are approximately the same.

Bellow we discuss the assignment of the most important groups for the compounds studied considering the two coordination kinds (see Tables 7-9 and Tables S6-S11 of the Supporting Material).

Table 6
Experimental frequencies $\left(\mathrm{cm}^{-1}\right)$ for chromyl nitrate


Abbreviations: $v$, stretching; $\delta$, deformation; $\rho$, rocking; wag, $(\gamma)$ wagging; $\tau \mathrm{w}$, torsion, a, antisymmetric, s, symmetric op, out of phase; ip, in phase
${ }^{\text {a }}$ Ref. [1].
${ }^{\mathrm{b}}$ This work.
${ }^{c}$ Considering the nitrate group as ring of four members.

### 4.2.1. Coordination monodentate of the nitrate groups

The infrared and Raman frequencies, their respective intensities and the potential energy distribution obtained by DFT/B3LYP/6-31G*, B3LYP/Lan12DZ and B3LYP/6-311+G calculations considering monodentate coordination of the nitrate


Fig. 5. Theoretical Raman spectrum of $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ at different levels of theory.
groups appear in Tables 7, S6 and S7, respectively. In all cases the theoretical values were compared with the experimental values by means of the RMSD values. The calculated harmonic force field for chromyl nitrate can be obtained upon request. The frequencies calculated using the $6-311+G$ basis set for the compound are lower than those obtained using the Lanl2DZ and 6-31G* basis sets. The RMSD initial value using B3LYP/Lanl2DZ and B3LYP/6-31G* calculations are 62.2 and $73.5 \mathrm{~cm}^{-1}$ while with the $6-311+\mathrm{G}$ basis set is $53.1 \mathrm{~cm}^{-1}$. It can be seen that the best results for chromyl nitrate are obtained using B3LYP/6-31G* calculation with a RMSD final equal at $19.8 \mathrm{~cm}^{-1}$ although the introduction of the polarization function does not have a good approximation to the experimental values. In this case the covalent bonding of the nitrate group is easily recognized from its infrared spectrum because the symmetry group changes from the point group $D_{3 h}$ of the free ion to $C_{2 v}$ of the compound [7].
4.2.1.1. Nitrate groups. The strong bands observed in the infrared spectrum reported in previous paper [1] of $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$

Table 7
Experimental and calculated frequencies $\left(\mathrm{cm}^{-1}\right)$, potential energy distribution and assignment for monodentate chromyl nitrate

| Mode | Observed ${ }^{\text {a }}$ | Calculated ${ }^{\text {b }}$ | SQM ${ }^{\text {c }}$ | IR int. ${ }^{\text {d }}$ | Raman act. ${ }^{\text {e }}$ | P.E.D. $(\geq 10 \%)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Symmetry A |  |  |  |  |  |  |
| 1 | 1642 | 1743 | 1631 | 227.9 | 37.2 | $65 S_{1}+14 S_{2}+10 S_{6}$ |
| 2 | 1232 | 1289 | 1237 | 151.3 | 20.9 | $58 \mathrm{~S}_{2}+23 \mathrm{~S}_{1}$ |
| 3 | 959 | 1115 | 952 | 93.6 | 33.1 | $94 \mathrm{~S}_{3}$ |
| 4 | 835 | 991 | 846 | 96.5 | 8.3 | $45 \mathrm{~S}_{4}+36 \mathrm{~S}_{21}$ |
| 5 | 781 | 785 | 782 | 37.2 | 2.5 | $77 \mathrm{~S}_{5}+15 \mathrm{~S}_{12}$ |
| 6 | 774 | 778 | 765 | 1.8 | 0.5 | $52 \mathrm{~S}_{6}+17 \mathrm{~S}_{9}+15 \mathrm{~S}_{11}$ |
| 7 | 686 | 684 | 632 | 0.3 | 4.8 | $50 \mathrm{~S}_{7}+21 \mathrm{~S}_{18}+11 \mathrm{~S}_{9}$ |
| 8 | 460 | 475 | 464 | 4.1 | 14.6 | $71 \mathrm{~S}_{8}+11 \mathrm{~S}_{4}$ |
| 9 | 349 | 356 | 359 | 4.9 | 11.4 | $40 S_{22}+39 S_{9}+12 S_{12}$ |
| 10 | 242 | 274 | 262 | 0.0 | 1.4 | $44 \mathrm{~S}_{10}+17 \mathrm{~S}_{13}+14 \mathrm{~S}_{12}+10 \mathrm{~S}_{14}$ |
| 11 | 206 | 236 | 223 | 2.2 | 1.4 | $50 \mathrm{~S}_{11}+12 \mathrm{~S}_{12}+10 \mathrm{~S}_{9}$ |
| 12 | 206 | 207 | 192 | 0.6 | 2.7 | $55 \mathrm{~S}_{12}+21 \mathrm{~S}_{13}+15 \mathrm{~S}_{11}$ |
| 13 | 152 | 149 | 137 | 0.0 | 2.4 | $35 \mathrm{~S}_{13}+29 \mathrm{~S}_{10}+19 \mathrm{~S}_{14}+10 \mathrm{~S}_{12}$ |
| 14 | 76 | 76 | 75 | 0.2 | 5.7 | $48 \mathrm{~S}_{10}+40 \mathrm{~S}_{12}+11 \mathrm{~S}_{14}$ |
| Symmetry B |  |  |  |  |  |  |
| 15 | 1614 | 1724 | 1622 | 815.7 | 14.6 | $67 \mathrm{~S}_{15}+14 \mathrm{~S}_{16}$ |
| 16 | 1216 | 1285 | 1226 | 187.9 | 3.7 | $59 S_{16}+22 S_{15}$ |
| 17 | 945 | 1111 | 951 | 155.5 | 18.8 | $91 S_{17}$ |
| 18 | 800 | 986 | 840 | 45.6 | 1.0 | $47 \mathrm{~S}_{18}+37 \mathrm{~S}_{7}$ |
| 19 | 781 | 783 | 781 | 13.3 | 0.4 | $91 \mathrm{~S}_{19}$ |
| 20 | 774 | 777 | 762 | 88.0 | 1.5 | $52 \mathrm{~S}_{20}+17 \mathrm{~S}_{8}+15 \mathrm{~S}_{4}+11 \mathrm{~S}_{27}$ |
| 21 | 686 | 684 | 627 | 4.2 | 0.9 | $56 S_{21}+18 S_{47}+11 S_{8}$ |
| 22 | 446 | 453 | 450 | 78.0 | 5.7 | $63 S_{22}+16 S_{12}$ |
| 23 | 273 | 287 | 265 | 7.8 | 1.9 | $41 \mathrm{~S}_{23}+26 \mathrm{~S}_{27}+22 \mathrm{~S}_{26}$ |
| 24 | 223 | 247 | 237 | 3.8 | 0.4 | $45 \mathrm{~S}_{24}+29 \mathrm{~S}_{23}$ |
| 25 | 152 | 191 | 166 | 2.9 | 1.3 | $21 \mathrm{~S}_{25}+21 \mathrm{~S}_{27}+17 \mathrm{~S}_{23}+17 \mathrm{~S}_{26}+13 \mathrm{~S}_{24}$ |
| 26 | 100 | 112 | 100 | 12.6 | 0.3 | $60 \mathrm{~S}_{26}+35 \mathrm{~S}_{27}$ |
| 27 | 100 | 105 | 89 | 1.1 | 1.6 | $27 \mathrm{~S}_{25}+26 \mathrm{~S}_{27}$ |
| $\operatorname{RMSD}\left(\mathrm{cm}^{-1}\right)$ |  | 73.5 | 19.8 |  |  |  |

${ }^{\text {a }}$ This work.
${ }^{\mathrm{b}}$ DFT B3LYP/6-31G*.
${ }^{\text {c }}$ From scaled quantum mechanics force field.
${ }^{\mathrm{d}}$ Units are $\mathrm{km} \mathrm{mol}^{-1}$.
${ }^{\mathrm{e}}$ Raman activities in $\AA^{4}(\mathrm{amu})^{-1}$.
liquid at 1613 and $1215 \mathrm{~cm}^{-1}$, were assigned to $\mathrm{N}=\mathrm{O}$ antisymmetric and symmetric stretchings, respectively. In this work, the $\mathrm{N}=\mathrm{O}$ in phase and out of phase symmetric stretching modes are calculated by the B3LYP/6-31G* method at 1743 and $1724 \mathrm{~cm}^{-1}$, respectively. The B3LYP/Lanl2DZ and B3LYP/6$311+\mathrm{G}$ methods underestimate the $\mathrm{N}=\mathrm{O}$ stretching frequencies as compared to the experimental values. The frequencies predicted for these vibrational modes show that the two symmetric stretching modes are split by about $19 \mathrm{~cm}^{-1}$ with the $6-31 \mathrm{G}^{*}$ basis set (using Lan12DZ and 6-311+G basis sets the splitting is $18 \mathrm{~cm}^{-1}$ ). These modes are calculated slightly coupled with antisymmetric stretching modes but they are only mixed with the $\mathrm{O}=\mathrm{N}-\mathrm{O}$ in phase deformation mode using $6-31 \mathrm{G}^{*}$ and 6 $311+\mathrm{G}$ basis sets. Normally, the $\mathrm{N}=\mathrm{O}$ stretching frequencies of the nitrate ion and nitrate group are observed between 1531 and $1481 \mathrm{~cm}^{-1}[44,49,50]$ while in nitrogen oxides they are observed at 1758 and $1660 \mathrm{~cm}^{-1}$ [9]. In $\left[\mathrm{Zr}\left(\mathrm{NO}_{3}\right)_{6} 1^{2-}\right.$ complex [45] the $\mathrm{N}=\mathrm{O}$ stretching is observed at $1570 \mathrm{~cm}^{-1}$, in $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{5}(\mathrm{ONO})\right] \mathrm{Cl}_{2}$ complex at $1460 \mathrm{~cm}^{-1}$ [49] while this vibration mode in $\mathrm{HNO}_{3}$ [45] is observed at $1672 \mathrm{~cm}^{-1}$. In the $\mathrm{UO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ and $\mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}$ anhydrous salts, the $\mathrm{N}=\mathrm{O}$ stretch-
ing frequencies are observed at 1560 and $1585 \mathrm{~cm}^{-1}$ [47,48]. For these observations, the shoulder at $1640 \mathrm{~cm}^{-1}$ in the liquid spectrum and the very strong band at $1613 \mathrm{~cm}^{-1}$, with a difference among them of $27 \mathrm{~cm}^{-1}$ are assigned to these modes.

The $\mathrm{NO}_{2}$ in phase and out of phase antisymmetric modes are calculated with B3LYP/6-31G* method at 1289 and $1285 \mathrm{~cm}^{-1}$, respectively. In the three calculations these modes appear coupled with the stretching modes. Generally, in nitro complexes the $\mathrm{NO}_{2}$ antisymmetric stretching modes are observed between 1488 and $1343 \mathrm{~cm}^{-1}$ and in nitrate ion is observed at $1388 \mathrm{~cm}^{-1}$ [9,49] while the symmetric mode is observed between 1364 and $1315 \mathrm{~cm}^{-1}$ [49]. In the $\mathrm{UO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ and $\mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}$ anhydrous salts the $\mathrm{NO}_{2}$ stretching antisymmetric modes are observed in the $1300 \mathrm{~cm}^{-1}$ region while the $\mathrm{NO}_{2}$ stretching symmetric modes appear approximately at $1000 \mathrm{~cm}^{-1}$ [47,48]. In our previous paper [1] only the shoulder in the Raman spectrum at $945 \mathrm{~cm}^{-1}$ is assigned to one of these modes. Now, the shoulder in the infrared spectrum of the liquid phase at $1234 \mathrm{~cm}^{-1}$ and the strong band in the same spectrum at $1215 \mathrm{~cm}^{-1}$ are assigned to $\mathrm{NO}_{2}$ in phase and out of phase antisymmetric stretching modes, respectively.

Table 8
Experimental and calculated frequencies $\left(\mathrm{cm}^{-1}\right)$, potential energy distribution and assignment for bidentate chromyl nitrate

| Mode | Observed $^{\text {a }}$ | Calculated ${ }^{\text {b }}$ | SQM $^{\text {c }}$ | IR int. $^{\text {d }}$ | Raman act. $^{\text {e }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |

${ }^{\mathrm{a}}$ This work.
${ }^{\mathrm{b}}$ DFT B3LYP/6-31G*.
${ }^{\text {c }}$ From scaled quantum mechanics force field.
${ }^{\mathrm{d}}$ Units are $\mathrm{km} \mathrm{mol}^{-1}$.
e Raman activities in $\AA^{4}(\mathrm{amu})^{-1}$.

The $\mathrm{NO}_{2}$ out of phase and in phase deformation modes are perfectly characterized by the three calculations and are observed coupled with $\mathrm{N}-\mathrm{O}$ vibration modes. The bands observed in the infrared spectrum at low temperature at 835 and $800 \mathrm{~cm}^{-1}$ are assigned to $\mathrm{NO}_{2}$ in phase and out of phase deformation, respectively. These bands are predicted in the Raman spectrum with all basis sets with low intensity and experimentally are not observed.

Others modes well characterized by the three calculations are the $\mathrm{N}=\mathrm{O}$ out of plane in phase and out of phase deformation. The P.E.D. values indicate that the $\mathrm{O}=\mathrm{N}-\mathrm{O}$ in phase and out of phase deformation modes are strongly coupled with vibrations of the $\mathrm{CrO}_{2}$ and $\mathrm{NO}_{2}$ groups. In nitro complexes these modes are observed among 657 and $433 \mathrm{~cm}^{-1}$ [49] while in nitrate ion is observed at $831 \mathrm{~cm}^{-1}$ [9,49]. In this case, the band in the IR low temperature at $781 \mathrm{~cm}^{-1}$ is assigned to these vibration modes. The band in the IR low temperature observed at $774 \mathrm{~cm}^{-1}$ in the previous paper is assigned to these vibration modes [1]. In this case the calculations confirm such assignment.

The $\mathrm{N}-\mathrm{O}$ antisymmetric and symmetric stretching modes are calculated also coupled with vibrations of nitrate groups as
shown in Tables 6-8. In nitrate ion, these modes are observed at $831 \mathrm{~cm}^{-1}[9,49]$ while in $\mathrm{UO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ they appear at $800 \mathrm{~cm}^{-1}$ [47]. The weak band in the Raman spectrum at $686 \mathrm{~cm}^{-1}$, previously assigned to nitrate rocking mode [1], is assigned in this case to these vibration modes.

In the region of lower frequencies the vibration modes normally expected for the nitrate groups are the $\mathrm{N}-\mathrm{O}-\mathrm{Cr}$ bending, rocking, wagging and twisting modes as observed in covalent nitrates [45]. All modes, as shown in Tables 7, S6 and S7, appear coupled among them and with other modes of the chromyl group while the P.E.D. values are different in the calculations with all the basis sets.

Experimentally, in the nitro complexes the $\mathrm{NO}_{2}$ rocking and twisting modes are observed in the low frequencies region between 600 and $400 \mathrm{~cm}^{-1}$ and 300 and $240 \mathrm{~cm}^{-1}$, respectively [ $46,49,50]$. In a previous paper we assigned the $\mathrm{NO}_{2}$ rocking mode at $686 \mathrm{~cm}^{-1}$, the $\mathrm{NO}_{2}$ torsion at $152 \mathrm{~cm}^{-1}$ while the $\mathrm{CrO}_{2}$ twisting mode was not assigned [1]. In chromyl nitrate the $\mathrm{NO}_{2}$ in phase and out of phase torsion modes are calculated using the three basis sets which appear strongly mixed and with different P.E.D. Previously, we assigned only one of these modes

Table 9
Experimental and calculated frequencies $\left(\mathrm{cm}^{-1}\right)$, potential energy distribution and assignment for bidentate coordination adopted for nitrate groups (as two rings of four members)

| Mode | Observed ${ }^{\text {a }}$ | Calculated ${ }^{\text {b }}$ | SQM ${ }^{\text {c }}$ | IR int. ${ }^{\text {d }}$ | Raman act. ${ }^{\text {e }}$ | P.E.D. ( $\geq 10 \%$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Symmetry A |  |  |  |  |  |  |
| 1 | 1642 | 1743 | 1638 | 227.9 | 37.2 | $80 \mathrm{~S}_{1}+11 \mathrm{~S}_{4}$ |
| 2 | 1232 | 1289 | 1182 | 151.3 | 20.9 | $57 \mathrm{~S}_{2}+29 \mathrm{~S}_{7}$ |
| 3 | 959 | 1115 | 955 | 93.6 | 33.1 | $95 \mathrm{~S}_{3}$ |
| 4 | 835 | 991 | 872 | 96.5 | 8.3 | $64 \mathrm{~S}_{4}+23 \mathrm{~S}_{7}+11 \mathrm{~S}_{2}$ |
| 5 | 781 | 785 | 789 | 37.2 | 2.5 | $64 S_{5}+22 S_{9}$ |
| 6 | 774 | 778 | 776 | 1.8 | 0.5 | $47 \mathrm{~S}_{6}+33 \mathrm{~S}_{20}$ |
| 7 | 686 | 684 | 653 | 0.3 | 4.8 | $42 S_{2}+27 S_{7}+18 S_{4}$ |
| 8 | 460 | 475 | 455 | 4.1 | 14.6 | $67 \mathrm{~S}_{8}+19 \mathrm{~S}_{9}$ |
| 9 | 349 | 356 | 350 | 4.9 | 11.4 | $32 \mathrm{~S}_{8}+29 \mathrm{~S}_{9}+14 \mathrm{~S}_{5}+12 \mathrm{~S}_{25}$ |
| 10 | 242 | 274 | 260 | 0.0 | 1.4 | $39 \mathrm{~S}_{10}+19 \mathrm{~S}_{26}+19 \mathrm{~S}_{14}$ |
| 11 | 206 | 236 | 223 | 2.2 | 1.4 | $50 \mathrm{~S}_{11}+30 \mathrm{~S}_{9}$ |
| 12 | 152 | 191 | 172 | 2.9 | 1.3 | $23 \mathrm{~S}_{27}+22 \mathrm{~S}_{23}+14 \mathrm{~S}_{16}+12 \mathrm{~S}_{12}+12 \mathrm{~S}_{24}$ |
| 13 | 100 | 112 | 97 | 12.6 | 0.3 | $50 \mathrm{~S}_{13}+24 \mathrm{~S}_{25}+20 \mathrm{~S}_{12}$ |
| 14 | 76 | 76 | 70 | 0.2 | 5.7 | $48 \mathrm{~S}_{14}+26 \mathrm{~S}_{25}+25 \mathrm{~S}_{26}$ |
| Symmetry B |  |  |  |  |  |  |
| 15 | 1614 | 1724 | 1620 | 815.7 | 14.6 | $81 \mathrm{~S}_{15}+10 \mathrm{~S}_{18}$ |
| 16 | 1216 | 1285 | 1180 | 187.9 | 3.7 | $56 \mathrm{~S}_{16}+29 \mathrm{~S}_{21}$ |
| 17 | 945 | 1111 | 952 | 155.5 | 18.8 | $92 \mathrm{~S}_{17}$ |
| 18 | 800 | 986 | 870 | 45.6 | 1.0 | $61 \mathrm{~S}_{18}+25 \mathrm{~S}_{21}+10 \mathrm{~S}_{16}$ |
| 19 | 781 | 783 | 786 | 13.3 | 0.4 | $65 \mathrm{~S}_{19}+20 \mathrm{~S}_{22}$ |
| 20 | 774 | 777 | 773 | 88.0 | 1.5 | $47 \mathrm{~S}_{20}+31 \mathrm{~S}_{6}$ |
| 21 | 686 | 684 | 646 | 4.2 | 0.9 | $45 \mathrm{~S}_{16}+23 \mathrm{~S}_{21}+20 \mathrm{~S}_{18}$ |
| 22 | 446 | 453 | 444 | 78.0 | 5.7 | $33 \mathrm{~S}_{22}+17 \mathrm{~S}_{19}+14 \mathrm{~S}_{23}+13 \mathrm{~S}_{21}+13 \mathrm{~S}_{27}$ |
| 23 | 273 | 287 | 276 | 7.8 | 1.9 | $58 \mathrm{~S}_{23}+12 \mathrm{~S}_{13}+12 \mathrm{~S}_{12}$ |
| 24 | 223 | 247 | 235 | 3.8 | 0.4 | $37 \mathrm{~S}_{24}+20 \mathrm{~S}_{27}+19 \mathrm{~S}_{22}+12 \mathrm{~S}_{23}$ |
| 25 | 206 | 207 | 193 | 0.6 | 2.7 | $48 \mathrm{~S}_{25}+25 \mathrm{~S}_{11}+13 \mathrm{~S}_{9}$ |
| 26 | 152 | 149 | 139 | 0.0 | 2.4 | $42 \mathrm{~S}_{10}+31 \mathrm{~S}_{26}+16 \mathrm{~S}_{14}$ |
| 27 | 100 | 105 | 77 | 1.1 | 1.6 | $38 S_{27}+24 S_{24}+18 S_{22}+10 S_{16}$ |
| RMSD ( $\mathrm{cm}^{-1}$ ) |  | 73.5 | 23.6 |  |  |  |

a This work.
${ }^{\mathrm{b}}$ DFT B3LYP/6-31G*.
${ }^{\text {c }}$ From scaled quantum mechanics force field.
${ }^{\mathrm{d}}$ Units are $\mathrm{km} \mathrm{mol}^{-1}$.
${ }^{\mathrm{e}}$ Raman activities in $\AA^{4}(\mathrm{amu})^{-1}$.
at $152 \mathrm{~cm}^{-1}$ [1]. In this work, with the aid of the calculations the very weak band in the Raman spectrum at $242 \mathrm{~cm}^{-1}$ is assigned to $\mathrm{NO}_{2}$ in phase torsion mode while the band in the same spectrum at $100 \mathrm{~cm}^{-1}$ is assigned to $\mathrm{NO}_{2}$ out of phase torsion mode.

The assignment of the $\mathrm{N}-\mathrm{O}-\mathrm{Cr}$ in phase and out of phase bending modes is very difficult because these modes are calculated by three methods used at different frequencies and P.E.D. values. With the B3LYP/6-31G* calculation these modes appear more defined than with the other methods hence the shoulder observed in the IR spectrum of the liquid compound at $223 \mathrm{~cm}^{-1}$ and the weak Raman band at $206 \mathrm{~cm}^{-1}$ are assigned to $\mathrm{N}-\mathrm{O}-\mathrm{Cr}$ out of phase and in phase modes bending modes, respectively. In our assignment previously realized for this molecule only one of these modes was assigned at $247 \mathrm{~cm}^{-1}$ [1].

The $\mathrm{NO}_{2}$ in phase rocking mode is calculated clearly at $207 \mathrm{~cm}^{-1}$ with the B3LYP/6-31G* calculation and with higher P.E.D. value ( $55 \%$ ) than with the B3LYP/6-311+G calculation $(42 \%)$ but, in this last case it is calculated at $201 \mathrm{~cm}^{-1}$. The $\mathrm{NO}_{2}$ out of phase rocking mode appears mixed, in the three methods used, with different modes such as $\mathrm{NO}_{2}$ torsion and $\mathrm{CrO}_{2}$ twist-
ing. This mode, with the B3LYP/6-31G* method is calculated clearly at $112 \mathrm{~cm}^{-1}$ coupled with higher P.E.D. value ( $27 \%$ ) with the $\mathrm{CrO}_{2}$ twisting mode while with the B3LYP/6-311+G method it is calculated at $81 \mathrm{~cm}^{-1}$ with higher contribution ( $27 \%$ ) and, it is also calculated at $173 \mathrm{~cm}^{-1}$ but, with lower contribution ( $21 \%$ ). Experimentally, in nitro complexes the $\mathrm{NO}_{2}$ rocking mode is observed in the low frequencies region, between 600 and $400 \mathrm{~cm}^{-1}$ [49]. In a previous paper we assigned the $\mathrm{NO}_{2}$ rocking mode at $686 \mathrm{~cm}^{-1}$ [1]. In this case the theoretical calculations show clearly the $\mathrm{NO}_{2}$ in phase rocking mode and, for this reason the band at $206 \mathrm{~cm}^{-1}$ is also assigned to this vibration mode and to the $\mathrm{N}-\mathrm{O}-\mathrm{Cr}$ in phase bending mode. The band in the Raman spectrum at $100 \mathrm{~cm}^{-1}$ is assigned to the $\mathrm{NO}_{2}$ out of phase rocking mode.
4.2.1.2. Chromyl group. The frequencies predicted for the vibrational modes of chromyl nitrate show that the antisymmetric and symmetric $\mathrm{Cr}=\mathrm{O}$ stretchings are split by more than $4 \mathrm{~cm}^{-1}$, indicating a little contribution of the central Cr atom in these vibrations. The antisymmetric and symmetric $\mathrm{Cr}=\mathrm{O}$ stretchings modes were observed in the spectrum of the solid
sample at 968 and $962 \mathrm{~cm}^{-1}$, respectively, while the more intense band at $959 \mathrm{~cm}^{-1}$ in the Raman spectrum is assigned to the symmetric $\mathrm{Cr}=\mathrm{O}$ stretching. Tables 7, S 6 and S 7 for chromyl nitrate show that the unscaled DFT frequencies for the symmetric $\mathrm{Cr}=\mathrm{O}$ stretchings mode, are higher than the frequencies of the antisymmetric $\mathrm{Cr}=\mathrm{O}$ stretchings, an observation also reported by us [1]. In this compound these modes are uncoupled with other modes. In other chromyl compounds these modes appear in $1050-900 \mathrm{~cm}^{-1}$ region, i.e. in $\mathrm{CrO}_{2}\left(\mathrm{ClO}_{4}\right)_{2}$ they appear at 990 and $980 \mathrm{~cm}^{-1}$ [51], in $\mathrm{CrO}_{2}\left(\mathrm{SO}_{3} \mathrm{~F}\right)_{2}$ appear at 1061 and $1020 \mathrm{~cm}^{-1}$ [15] and in $\mathrm{CrO}_{2} \mathrm{~F}_{2}$ and $\mathrm{CrO}_{2} \mathrm{Cl}_{2}$ they are observed for the first compound at 1016 and $1006 \mathrm{~cm}^{-1}$ while for the second one at 1002 and $995 \mathrm{~cm}^{-1}$, respectively [45,49]. In this case the intense band in the Raman spectrum at $959 \mathrm{~cm}^{-1}$ is assigned to $\mathrm{Cr}=\mathrm{O}$ symmetric stretching mode while the shoulder observed in the same spectrum at $945 \mathrm{~cm}^{-1}$ is assigned to the corresponding antisymmetric stretching.

Also, the antisymmetric and symmetric $\mathrm{Cr}-\mathrm{O}$ stretchings are split by more than $26 \mathrm{~cm}^{-1}$, indicating a slight contribution of the central Cr atom in these vibrations. These stretchings in $\mathrm{CrO}_{2}\left(\mathrm{ClO}_{4}\right)_{2}$ they are observed, respectively, at 380 and $355 \mathrm{~cm}^{-1}$ [51] and in $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ were assigned previously by us at 460 and $446 \mathrm{~cm}^{-1}$, respectively [1]. In this case the theoretical calculation predicts these modes with greater P.E.D. value for the antisymmetric mode in reference to the symmetric mode. The intensities of these bands using all basis sets are not predicted correctly because the more intense band is related to the antisymmetric mode. Here, we confirm the assignment previously carried out by us for the antisymmetric mode at $460 \mathrm{~cm}^{-1}$ [1] while the band at $350 \mathrm{~cm}^{-1}$ of the higher intensity in the Raman spectrum is assigned to $\mathrm{Cr}-\mathrm{O}$ symmetric stretchings mode.

The $\mathrm{CrO}_{2}$ bending mode is observed in $\mathrm{CrO}_{2} \mathrm{~F}_{2}$ at $364 \mathrm{~cm}^{-1}$ while in $\mathrm{CrO}_{2} \mathrm{Cl}_{2}$ it is at $356 \mathrm{~cm}^{-1}[45,49]$. The band observed in the Raman spectrum at $350 \mathrm{~cm}^{-1}$ is assigned to the $\mathrm{CrO}_{2}$ bending $(\mathrm{O}=\mathrm{Cr}=\mathrm{O})$ of chromyl nitrate [1] while the other $\mathrm{CrO}_{2}$ bending $(\mathrm{O}-\mathrm{Cr}-\mathrm{O})$ was not assigned. In this work, the B3LYP/6$31 \mathrm{G}^{*}$ method calculates the $\mathrm{CrO}_{2}$ bending at $453 \mathrm{~cm}^{-1}$ with $63 \%$ of contribution P.E.D. and at $437 \mathrm{~cm}^{-1}$ with $56 \%$ of contribution P.E.D. With the other basis set this mode appears also coupled. In this case we assigned the intense band in the Raman spectrum at $446 \mathrm{~cm}^{-1}$ to $\mathrm{CrO}_{2}$ bending. The other $\mathrm{O}-\mathrm{Cr}-\mathrm{O}$ bending mode is calculated (at $149 \mathrm{~cm}^{-1}$ with $6-31 \mathrm{G}^{*}$ basis set and at $141 \mathrm{~cm}^{-1}$ with $6-311+\mathrm{G}$ basis set) strongly coupled with other modes. The very weak band observed in the Raman spectrum at $152 \mathrm{~cm}^{-1}$ is assigned to $\mathrm{O}-\mathrm{Cr}-\mathrm{O}$ bending. Previously this mode was not assigned by us [1].

The wagging, rocking and twisting modes of the $\mathrm{CrO}_{2}$ group are not assigned in a previous paper [1]. In this case the calculations predict these modes in the low frequencies region and it is coupled with other modes of the nitrate groups. The wagging $\mathrm{CrO}_{2}$ mode is calculated using all basis sets at higher frequency and with lower contribution of the P.E.D. than the rocking mode. For these observations, the weak band in the spectrum of the liquid at $273 \mathrm{~cm}^{-1}$ is assigned to the wagging mode while the Raman band at $152 \mathrm{~cm}^{-1}$ is assigned to the rocking mode.

The $\mathrm{CrO}_{2}$ twisting mode was not assigned previously. The P.E.D. values indicate that this mode is strongly coupled with
vibrations of the same group and the $\mathrm{NO}_{2}$ group as shown in Tables 7, S6 and S7. It is noticeable how the contribution of the P.E.D. value changes with the method used and it is possible to observe with all basis sets that this mode is strongly mixed at different frequencies (between 273 and $100 \mathrm{~cm}^{-1}$ ). In this case this mode could be assigned at $100 \mathrm{~cm}^{-1}$ because it appears with a higher P.E.D. value.

### 4.2.2. Coordination bidentate of the nitrate groups

4.2.2.1. Group nitrate without ring. The frequencies, infrared and Raman intensities and potential energy distribution obtained by B3LYP/6-31G*, B3LYP/Lan12DZ and B3LYP/6-311+G calculations considering the mode of coordination adopted by nitrate groups as bidentate appear in Tables 8, S8 and S9. In the three cases the comparison of the theoretical values with the respective experimental values (RMSD) is observed in the respective tables. The calculated harmonic force field for chromyl nitrate can be obtained upon request. It can be seen that the best results for bidentate coordination of chromyl nitrate are newly obtained with B3LYP/6-31G* calculation with a final RMSD of $10.6 \mathrm{~cm}^{-1}$ while with the Lan12DZ and 6-311+G basis sets the final RMSD were 18.7 and $16.5 \mathrm{~cm}^{-1}$, respectively.
4.2.2.1.1. Nitrate group. The theoretical results show slight changes in the P.E.D. values and in the coupling of the modes. In this case using the two basis sets the $\mathrm{N}=\mathrm{O}$ stretchings in phase mode appear coupled with the $\mathrm{NO}_{2}$ deformation in phase mode and, on the other hand, the corresponding out of phase modes are also coupled among them. This way, the shoulder in the spectrum of liquid phase at $1640 \mathrm{~cm}^{-1}$ and the very strong band in the same spectrum at $1613 \mathrm{~cm}^{-1}$ are assigned to these modes. Both bands in the Raman spectrum are observed at 1642 and $1614 \mathrm{~cm}^{-1}$.

The $\mathrm{NO}_{2}$ antisymmetric out of phase and in phase frequencies also appear coupled with the corresponding $\mathrm{O}=\mathrm{N}-\mathrm{O}$ out of phase and in phase deformation modes, respectively, but with greater contribution (in the two modes) when the $6-31 \mathrm{G}^{*}$ basis set is used. The assignment of these bands is similar to the monodentate type, where the shoulder at $1234 \mathrm{~cm}^{-1}$ and the strong band at $1215 \mathrm{~cm}^{-1}$ in the infrared spectrum of the liquid phase are assigned to $\mathrm{NO}_{2}$ antisymmetric in phase and out of phase modes, respectively.

The $\mathrm{NO}_{2}$ in phase and out of phase deformation modes are also coupled with vibrations of the nitrate groups as shown in Tables 8, S 8 and S 9 . In this case the $\mathrm{NO}_{2}$ in phase mode is calculated with $6-31 \mathrm{G}^{*}$ basis set at $991 \mathrm{~cm}^{-1}$ and the corresponding out of phase mode at $986 \mathrm{~cm}^{-1}$ while with $6-311+\mathrm{G}$ basis set they are calculated strongly coupled and with a higher contribution of P.E.D. at 863 and $858 \mathrm{~cm}^{-1}$, respectively. The bands in the IR low temperature spectrum are observed at 835 and $800 \mathrm{~cm}^{-1}$ are assigned to these vibration modes.

The two $\mathrm{N}=\mathrm{O}$ out of plane deformation modes (out of phase and in phase) appear strongly coupled when the $6-311+\mathrm{G}$ basis set is used (at 728 and $727 \mathrm{~cm}^{-1}$, respectively). The $\mathrm{N}=\mathrm{O}$ in phase deformation mode appears uncoupled (6-31G* basis set) at $783 \mathrm{~cm}^{-1}$ and with a percentage of $83 \%$ in the P.E.D. values while the corresponding out of phase deformation mode is calculated at $785 \mathrm{~cm}^{-1}$ (with $61 \%$ P.E.D.) slightly coupled with the
$\mathrm{N}=\mathrm{O}$ torsion mode. In both cases the scaled frequencies are 781 and $780 \mathrm{~cm}^{-1}$, respectively, with $6-31 \mathrm{G}^{*}$ basis set and 783 and 777 , respectively, with $6-311+G$ basis. Hence the band in the IR low temperature at 781 and at $782 \mathrm{~cm}^{-1}$ in the Raman spectrum is assigned to these vibration modes like in the monodentate type. The two calculations confirm such an assignment.

An important observation in this case is the great difference in frequency that appears between the corresponding $\mathrm{NO}_{2}$ symmetric out of phase and in phase modes. Particularly, the out of phase mode is strongly coupled with the $\mathrm{NO}_{2}$ out of phase deformation mode and has lower contribution but, only for the B3LYP/6-31G* calculation. For this last basis set the calculated frequencies are 785 and $777 \mathrm{~cm}^{-1}$, respectively. On the contrary, the $\mathrm{NO}_{2}$ symmetric out of phase and in phase modes are calculated with $6-311+\mathrm{G}$ basis set with higher percentage P.E.D. than the other basis set and both modes are calculated at the same frequency ( $714 \mathrm{~cm}^{-1}$ ). The shoulder in the Raman spectrum of the liquid phase at $774 \mathrm{~cm}^{-1}$ is assigned to these vibration modes.

The $\mathrm{O}=\mathrm{N}-\mathrm{O}$ out of phase and in phase deformation modes are also coupled and they are calculated at 618 and $617 \mathrm{~cm}^{-1}$ with Lan12DZ basis set while they appear at 624 and $621 \mathrm{~cm}^{-1}$, with $6-31 G^{*}$ and $6-311+G$ basis sets, respectively. For this observation, the weak band in the Raman spectrum at $686 \mathrm{~cm}^{-1}$ is assigned to these vibration modes. In the monodentate type these modes are assigned at $774 \mathrm{~cm}^{-1}$.

In the low frequencies region the vibration modes of the nitrate group appear strongly coupled with other modes of the chromyl group as shown in Tables $8, \mathrm{~S} 8$ and S 9 . When the nitrate groups present bidentate coordination other vibration modes, besides the $\mathrm{N}=\mathrm{O}$ torsion mode, as $\mathrm{NO}_{2}$ out of phase and in phase torsion modes are observed in this region.

The two calculations characterize perfectly the $\mathrm{NO}_{2}$ in phase torsion mode with a $54 \%$ of contribution P.E.D. $\left(6-31 \mathrm{G}^{*}\right.$ basis set). The corresponding out of phase mode is observed very mixed with different vibration modes but, the higher contribution to P.E.D. is at $287 \mathrm{~cm}^{-1}\left(6-31 \mathrm{G}^{*}\right.$ basis set). Both torsion modes are observed coupled with the vibration modes of the chromyl group at 76 and $273 \mathrm{~cm}^{-1}$, respectively. Similarly for the monodentate type, the very weak band in the Raman spectrum at $271 \mathrm{~cm}^{-1}$ is assigned to the $\mathrm{NO}_{2}$ torsion out of phase mode while the $\mathrm{NO}_{2}$ torsion in phase mode could not be assigned because the lower frequency is not observed in the vibrational spectra for the compound or probably is overlapped with the other bands.

The $\mathrm{N}=\mathrm{O}$ torsion mode is calculated with higher contribution at $105 \mathrm{~cm}^{-1}\left(6-31 \mathrm{G}^{*}\right.$ basis set) and $81 \mathrm{~cm}^{-1}$ when the size basis set increases. Thus, the observation of a weak band in the Raman spectrum of the liquid compound at $100 \mathrm{~cm}^{-1}$ could also be assigned to this mode as observed in Table 6.
4.2.2.1.2. Chromyl group. For chromyl nitrate it is possible to observe two $\mathrm{Cr}=\mathrm{O}$ stretching modes and four $\mathrm{Cr}-\mathrm{O}$ stretching modes due to bidentate coordination of the nitrate groups. The scaled DFT frequencies for the $\mathrm{Cr}=\mathrm{O}$ antisymmetric and symmetric stretching frequencies are in good agreement with the experimental frequencies and normal coordinate calculations. The $\mathrm{Cr}=\mathrm{O}$ antisymmetric and symmetric stretching modes are easily assigned by comparison with the calculations because in
the three cases studied they appear with a higher contribution to P.E.D. and without coupling as shown in Tables 8, S8 and S9. Moreover, in chromyl compounds these modes are observed in $1050-900 \mathrm{~cm}^{-1}$ region [44,45,49,51]. The assignment of these modes is similar to the monodentate type as shown in Table 6.

One important observation is that the $\mathrm{CrO}_{2}$ bending $(\mathrm{O}=\mathrm{Cr}=\mathrm{O})$ mode appears at higher frequencies than the monodentate type due to four $\mathrm{Cr}-\mathrm{O}$ bonds: two $\mathrm{Cr}-\mathrm{O}$ bonds and two $\mathrm{Cr} \leftarrow \mathrm{O}$ bonds (Fig. 5). Hence, it is possible to observe this mode at $475 \mathrm{~cm}^{-1}$ with a contribution to P.E.D. of $72 \%$ using $6-31 G^{*}$ basis set. In all calculations this mode appears slightly coupled with the $\mathrm{Cr}-\mathrm{O}$ symmetric stretching. Hence, the shoulder observed in the Raman spectrum at $460 \mathrm{~cm}^{-1}$ is assigned to $\mathrm{CrO}_{2}$ bending ( $\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ ).

The theoretical calculations predict approximately the $\mathrm{Cr}-\mathrm{O}$ symmetric stretching mode with the same percentage P.E.D. value ( $38 \%$ ) coupled with the $\mathrm{CrO}_{2}$ deformation and $\mathrm{Cr}-\mathrm{O}$ antisymmetric stretching modes. The antisymmetric mode is calculated at lower frequencies and both modes with approximately the same contribution (44\%). The symmetric mode calculated with higher intensity Raman was assigned to the intense band observed in the Raman spectrum at $446 \mathrm{~cm}^{-1}$ while the corresponding antisymmetric stretching was assigned to the weak band observed in the infrared spectrum of the liquid compound at $349 \mathrm{~cm}^{-1}$.

The antisymmetric and symmetric $\mathrm{Cr} \leftarrow \mathrm{O}$ stretchings are obviously calculated at lower frequencies because bond lengths are greater than the $\mathrm{Cr}-\mathrm{O}$ bonds (see Table 5). It is possible to observe the symmetric mode with higher contribution to P.E.D. at $112 \mathrm{~cm}^{-1}(26 \%)$ with $6-31 \mathrm{G}^{*}$ basis set. The antisymmetric stretchings are observed with lower contribution (25\%) mixed with other vibration modes at higher frequencies ( $453 \mathrm{~cm}^{-1}$ ) with $6-31 \mathrm{G}^{*}$ basis set. We assigned these modes in accordance to a higher contribution; i.e. at 206 and $100 \mathrm{~cm}^{-1}$ the higher frequency correspond to the antisymmetric stretchings.

In all calculations it is possible to observe the wagging, rocking and twisting modes of the $\mathrm{CrO}_{2}$ group strongly mixed with other modes. Differently from the monodentate type, the $\mathrm{CrO}_{2}$ wagging mode is calculated, using $6-31 \mathrm{G}^{*}$ basis set, at a lower frequency but, with higher contribution to P.E.D. $\left(247 \mathrm{~cm}^{-1}\right.$, $42 \%$ P.E.D.), while the opposite occurs for the $\mathrm{CrO}_{2}$ rocking mode (calculated at $274 \mathrm{~cm}^{-1}$ ( $34 \%$ ) with $6-31 \mathrm{G}^{*}$ basis set). In this case, the shoulders observed at 247 and $223 \mathrm{~cm}^{-1}$ in the infrared spectrum of the liquid chromyl nitrate are assigned to $\mathrm{CrO}_{2}$ rocking and wagging modes, respectively.

The P.E.D. values indicate that the $\mathrm{CrO}_{2}$ twisting mode are strongly coupled with vibrations of the same $\mathrm{CrO}_{2}$ group and $\mathrm{NO}_{2}$ groups with the 6-31G* basis set. In our case this mode is assigned to $152 \mathrm{~cm}^{-1}$.
4.2.2.2. Nitrate groups as rings of four members. Also, in the bidentate type the calculations were performed with the three basis sets considering the two nitrate groups as a ring of four members where the deformations and torsion coordinates of these groups have been defined as proposed by Fogarasi and Pulay [31] and are observed in Table 3. The frequencies, infrared intensities, Raman activities and potential energy
distribution obtained by B3LYP/6-31G*, B3LYP/Lan12DZ and B3LYP/6-311+G calculations, appear in Tables 9, S10 and S11, respectively. In all cases the comparison of the theoretical values with the respective experimental values are observed in the respective tables. The calculated harmonic force field for chromyl nitrate can be obtained upon request. Although the best results are obtained with a B3LYP/Lanl2DZ calculation with a RMSD final equal at $12.5 \mathrm{~cm}^{-1}$, the assignment was performed with B3LYP/6-31G* method because the vibration modes appear more defined. In this case a notable change in the assignment, in relation to the above bidentate considerations, is observed.
4.2.2.2.1. Nitrate group. As shown in Table 6, the assignment of the two $\mathrm{N}=\mathrm{O}$ and $\mathrm{NO}_{2}$ antisymmetric stretchings not change in reference to the above bidentate type. It is possible to observe some differences only in the frequencies of the two $\mathrm{NO}_{2}$ symmetric modes. In this case, these modes appear at higher frequencies than the $\mathrm{NO}_{2}$ deformation modes and the two $\mathrm{N}=\mathrm{O}$ out of plane deformation modes are observed at lower frequencies. These last modes are assigned to the same frequencies as in the above case while the $\mathrm{N}=\mathrm{O}$ torsion and two $\mathrm{NO}_{2}$ torsion modes (out of phase and in phase) are observed in the lower frequencies region, as shown in Table 6.
4.2.2.2.2. Chromyl group. For this group the calculations predict the two $\mathrm{Cr}=\mathrm{O}$ stretchings, the $\mathrm{CrO}_{2}$ bending and the four $\mathrm{Cr}-\mathrm{O}$ stretching modes at the same frequencies as the above bidentate coordination The only change is calculated for the wagging, rocking and twisting modes. In the lower region the A modes are calculated with the two basis sets strongly mixed while in the two bidentate coordinations of the $B$ modes are calculated coupled between them.

For this analysis we think that the two bidentate coordinations are possible but, not the monodentate type because the $\mathrm{Cr}-\mathrm{O}$ symmetric stretching modes should be observed with higher
intensity than the $\mathrm{CrO}_{2}$ bending mode. Moreover, as we will observe next, the force constants of the $\mathrm{Cr}-\mathrm{O}$ stretchings cannot be bigger than the corresponding to $\mathrm{Cr}=\mathrm{O}$ stretchings.

## 5. Force field

Having a secure assignment for the experimentally studied chromyl nitrate, the corresponding force constants were estimated using the scaling procedure of Pulay et al. [28], as mentioned before. The harmonic force fields in Cartesian coordinates were transformed to the local symmetry or "natural" coordinates proposed by Fogarasi and Pulay [31], as defined in Tables 1-3 (see Figs. 4 and 5) considering in the first case the mode of coordination adopted by nitrate groups as monodentate and in the two following cases as bidentate. The scaling factors affecting the main force constants were subsequently calculated by an iterative procedure $[29,30]$ to have the best possible fit between observed and theoretical frequencies. The resulting numbers for the three cases considered are collected in Table 10. These values are quite satisfactory, considering that the experimental frequencies were not corrected for anharmonicity. The frequencies, infrared intensities, Raman activities and potential energy distribution obtained for chromyl nitrate appear together with the values reached for the corresponding RMSD values in Tables 7-9 and Tables S6-S11 of the Supporting Material, for the three basis sets and for the three coordination modes considered for the nitrate groups in the compound. The force constants appearing in Table 11 expressed in terms of simple valence internal coordinates were calculated from the corresponding scaled force fields by using the expression: $F_{\mathrm{i}}=U^{\mathrm{t}} F_{\mathrm{s}} U$, where $F_{\mathrm{i}}$ is the force constants matrix in terms of simple valence internal coordinates, $F_{\mathrm{S}}$ the force constant matrix in terms of natural coordinates, $U$ the orthogonal matrix relating the natural coordinates to the simple valence

Table 10
Scale factors for the force field of chromyl nitrate

| Coordinates | Chromyl nitrate ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Monodentate |  |  | Bidentate |  |  | Bidentate ${ }^{\text {b }}$ |  |  |
|  | Lan12DZ | 6-31G* | $6-311++\mathrm{G}$ | Lan12DZ | 6-31G* | 6-311++G | Lan12DZ | 6-31G* | 6-311++G |
| $v(\mathrm{~N}=\mathrm{O})$ | 1.702 | 0.641 | 0.825 | 1.147 | 0.899 | 1.137 | 1.128 | 0.913 | 1.075 |
| $\nu(\mathrm{N}-\mathrm{O})$ | 0.798 | 0.641 | 0.825 | 1.147 | 0.899 | 1.137 | 1.128 | 0.771 | 0.956 |
| $\nu(\mathrm{Cr}=\mathrm{O})$ | 0.774 | 0.730 | 0.815 | 0.774 | 0.728 | 0.816 | 0.774 | 0.733 | 0.815 |
| $\nu(\mathrm{Cr}-\mathrm{O})$ | 1.406 | 1.029 | 1.426 | 1.118 | 0.908 | 1.061 | 1.116 | 0.950 | 0.979 |
| $\delta(\mathrm{O}=\mathrm{N}=\mathrm{O})$ | 1.090 | 0.968 | 1.055 |  |  |  | - | - | - |
| $\delta(\mathrm{O}-\mathrm{N}-\mathrm{O})$ |  |  |  | 1.255 | 1.041 | 1.248 | 1.363 | 1.050 | 1.397 |
| $\delta(\mathrm{O}=\mathrm{N}-\mathrm{O})$ | 1.090 | 0.968 | 1.055 | 1.255 | 1.041 | 1.248 | 1.363 | 1.050 | 1.397 |
| $\delta(\mathrm{O}=\mathrm{Cr}=\mathrm{O})$ | 1.117 | 0.917 | 0.942 | 1.063 | 0.941 | 1.083 | 0.962 | 0.906 | 1.002 |
| $\delta(\mathrm{O}-\mathrm{Cr}-\mathrm{O})$ | 1.117 | 0.917 | 0.942 | 1.063 | 0.941 | 1.083 | 1.029 | 0.941 | 1.083 |
| $\delta(\mathrm{O}-\mathrm{N}-\mathrm{Cr})$ | 1.117 | 0.917 | 0.942 |  |  |  | - | - | - |
| $\tau(\mathrm{O}-\mathrm{N}-\mathrm{O})$ | 1.034 | 1.006 | 1.054 | 0.984 | 0.988 | 0.999 | 0.946 | 0.941 | 1.083 |
| $\gamma(\mathrm{N}=\mathrm{O})$ | 1.302 | 1.002 | 1.185 | 1.254 | 0.999 | 1.159 | 1.316 | 1.008 | 1.158 |
| $\rho(\mathrm{O}-\mathrm{Cr}-\mathrm{O})$ | 0.861 | 0.791 | 0.913 | 0.785 | 0.854 | 0.825 | 0.946 | 0.941 | 1.083 |
| wagg (O-Cr-O) | 0.861 | 0.791 | 0.913 | 0.785 | 0.854 | 0.825 | 0.946 | 0.941 | 1.083 |
| $\tau \mathrm{w}(\mathrm{O}-\mathrm{Cr}-\mathrm{O})$ | 0.861 | 0.791 | 0.913 | 0.785 | 0.988 | 0.999 | 0.946 | 0.941 | 1.083 |

[^1]Table 11
Comparison of scaled internal force constants for chromyl nitrate

| Coordinates | Chromyl nitrate ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Monodentate |  |  | Bidentate |  |  | Bidentate ${ }^{\text {b }}$ |  |  |
|  | Lan12DZ | 6-31G* | 6-311++G | Lan12DZ | 6-31G* | 6-311++G | Lanl2DZ | 6-31G* | 6-311++G |
| $f(\mathrm{~N}=\mathrm{O})$ | 16.18 | 16.25 | 15.83 | 11.74 | 11.44 | 11.71 | 11.55 | 11.62 | 11.07 |
| $f(\mathrm{~N}-\mathrm{O})$ | 3.19 | 3.38 | 3.22 | 4.62 | 4.96 | 4.62 | 4.96 | 4.96 | 4.62 |
| $f(\mathrm{Cr}=\mathrm{O})$ | 6.55 | 6.55 | 6.56 | 6.55 | 6.53 | 6.57 | 6.55 | 6.57 | 6.56 |
| $f(\mathrm{Cr}-\mathrm{O})$ | 7.82 | 6.09 | 7.34 | 1.64 | 1.44 | 1.51 | 1.34 | 1.38 | 1.27 |
| $f(\mathrm{O}=\mathrm{N}=\mathrm{O})$ | 1.57 | 1.62 | 1.58 | - | - | - | - | - | - |
| $f(\mathrm{O}=\mathrm{N}-\mathrm{O})$ | 2.05 | 2.24 | 2.09 | 1.83 | 1.74 | 1.87 | 1.49 | 1.32 | 1.57 |
| $f(\mathrm{O}=\mathrm{Cr}=\mathrm{O})$ | 2.31 | 2.53 | 2.26 | 1.73 | 1.66 | 1.74 | 1.58 | 1.62 | 1.63 |
| $f(\mathrm{O}-\mathrm{Cr}-\mathrm{O})$ | 0.86 | 0.80 | 0.74 | 0.91 | 0.93 | 0.93 | 0.75 | 0.65 | 0.66 |
| $f(\mathrm{O}-\mathrm{N}-\mathrm{Cr})$ | 1.96 | 2.41 | 1.96 | - | - | - | - | - | - |
| $f(\mathrm{~N}=\mathrm{O}) /(\mathrm{N}-\mathrm{O})$ | 1.74 | 1.81 | 1.71 | 1.33 | 1.29 | 1.25 | 1.66 | 1.95 | 1.60 |
| $f(\mathrm{~N}=\mathrm{O}) /(\mathrm{Cr}-\mathrm{O})$ | 1.16 | 1.16 | 1.16 | -0.12 | -0.07 | -0.11 | -0.27 | -0.47 | -0.39 |
| $f(\mathrm{~N}-\mathrm{O}) /(\mathrm{N}-\mathrm{O})$ | 2.00 | 2.06 | 2.09 | -1.30 | -1.29 | -1.29 | -1.35 | -1.61 | -1.36 |

Units are mdyn $\AA^{-1}$ for stretching and stretching/stretching interaction and mdyn $\AA \mathrm{Aad}^{-2}$ for angle deformations.
${ }^{\text {a }}$ This work.
${ }^{\mathrm{b}}$ Considering the nitrate groups as ring of four members.
internal coordinates, and $U^{\mathrm{t}}$ is the transposed matrix of the $U$ matrix.

It is interesting to compare the principal force constants calculated at the B3LYP/Lanl2DZ, B3LYP/6-31G* and B3LYP/6-311++G levels for the common vibrations, which were collected in Table 11. In general, the calculated force constants values for the two bidentate coordinations considered here, with the B3LYP/Lan12DZ method are approximately the same as the calculated by B3LYP/6-311++G calculation. Obviously, some force constants values vary when the coordination mode of the nitrate group changes. As expected, the force constants of the $\mathrm{N}=\mathrm{O}$ and $\mathrm{Cr}-\mathrm{O}$ stretching change with the coordination mode of the nitrate group, being greater in the monodentate coordination than in the bidentate coordination. The force constants of $\mathrm{Cr}=\mathrm{O}$ and $\mathrm{O}-\mathrm{Cr}-\mathrm{O}$ deformation modes are practically the same in the two cases, while other modes change as the coordination modes of the nitrate groups change. In $\mathrm{CrO}_{2} \mathrm{~F}_{2}$ and $\mathrm{CrO}_{2} \mathrm{Cl}_{2}$, the scaled GVFF force constants (B3LYP/Lanl2DZ method) for the $\mathrm{Cr}=\mathrm{O}$ stretchings are 7.443 and 7.122 mdyn $\AA^{-1}$, respectively, while the corresponding force constants for the $\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ deformations are 1.110 and 0.938 mdyn $\AA \mathrm{rad}^{-2}$ [19]. This difference in the force constant values in reference to chromyl nitrate cannot be attributed to geometrical parameters because they are practically the same in the three compounds. The corresponding values are lower in $\mathrm{CrO}_{2} \mathrm{~F}_{2}$ and $\mathrm{CrO}_{2} \mathrm{Cl}_{2}$ because the scaled $\mathrm{Cr}=\mathrm{O}$ frequencies ( 1015 and $990 \mathrm{~cm}^{-1}$ ) are higher than the values for $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ as shown in Tables 7-9. The lower values of the force constants of $\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ deformations in $\mathrm{CrO}_{2} \mathrm{~F}_{2}$ and $\mathrm{CrO}_{2} \mathrm{Cl}_{2}$ in comparison with the corresponding to $\mathrm{CrO}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ can also be attributed to the scaled $\mathrm{O}=\mathrm{Cr}=\mathrm{O}$ frequencies that are higher in this last compound.

The force constants of $\mathrm{Cr}-\mathrm{O}$ stretchings considering bidentate nitrate groups are near the expected value reported by Hester and Grossman [53] for an M-O frequency ( $321 \mathrm{~cm}^{-1}$ in bidentate nitrate; $2.0 \mathrm{mdyn} \AA^{-1}$ ). The greater value for this force
constant (about $7.82 \mathrm{mdyn}^{\AA^{-1}}$ ) in the monodentate type suggests that the monodentate coordination for the nitrate groups in chromyl nitrate is impossible; therefore, this compound would have multiple coordination.

When the nitrate coordination is monodentate the force constants of $\mathrm{N}=\mathrm{O}$ stretchings are higher than other coordination modes while in the bidentate type the force constants of the $\mathrm{N}-\mathrm{O}$ stretchings are higher than the monodentate type. Moreover, our values for the force constants $\mathrm{N}=\mathrm{O}$ stretching are agree with that the reported value of $11.83 \mathrm{mdyn}^{\AA^{-1}}$ for $\mathrm{N}_{2} \mathrm{O}$ compound [9] while it is different from the $14.51 \mathrm{mdyn} \AA^{-1}$ value reported for the $\mathrm{N}_{2} \mathrm{O}_{2}$ compound [9]. The structures of both compounds are different from chromyl nitrate, being $\mathrm{N}_{2} \mathrm{O}$ linear and $\mathrm{N}_{2} \mathrm{O}_{2}$ angular with a $90^{\circ} \mathrm{O}-\mathrm{N}-\mathrm{N}$ angle. The force constant values reported for $\mathrm{KNO}_{3}$ by Beattie et al. [52] were: $9.26 \mathrm{mdyn}^{\AA^{-1}}$ for $\mathrm{N}=\mathrm{O}$ stretching; $6.72 \mathrm{mdyn}^{\AA^{-1}}$ for $\mathrm{N}-\mathrm{O}$ stretching; 1.54 mdyn $\AA \mathrm{rad}^{-2}$ for $\mathrm{O}-\mathrm{N}-\mathrm{O}$ deformation and 1.54 mdyn $\AA \mathrm{rad}^{-2}$ for $\mathrm{O}=\mathrm{N}-\mathrm{O}$ deformation. The force constant values reported by Brintzinger and Hester [54] for the free anion ( 6.35 mdyn $\AA^{-1}$ for $\mathrm{N}-\mathrm{O}$ stretching; $2.05 \mathrm{mdyn} \AA^{-1}$ for $\mathrm{N}-\mathrm{O} / \mathrm{N}-\mathrm{O}$ stretching and 0.54 mdyn $\AA \mathrm{rad}^{-2}$ for $\mathrm{O}-\mathrm{N}-\mathrm{O}$ deformation) are near the cited values by Topping for $\mathrm{D}_{3 \mathrm{~h}}$ nitrate ion ( $6.5 \mathrm{mdyn}^{\AA^{-1}}$ for $\mathrm{N}-\mathrm{O}$ stretching; $2.05 \mathrm{mdyn} \AA^{-1}$ for $\mathrm{N}-\mathrm{O} / \mathrm{N}-\mathrm{O}$ stretching and $0.54 \mathrm{mdyn}_{\mathrm{A}} \mathrm{rad}^{-2}$ for $\mathrm{O}-\mathrm{N}-\mathrm{O}$ deformation) [55]. For chromyl nitrate, those force constant values for the bidentate type are near to monodentate coordination as can be seen in Table 11. The observed differences in the force constants for $\mathrm{KNO}_{3}$ can be attributed to the calculations because in that compound they were carried out using three observed $\mathrm{N}-\mathrm{O}$ stretching frequencies (1460, 1293 and $1031 \mathrm{~cm}^{-1}$ ) and the $\mathrm{C}_{2 \mathrm{v}}$ bidentate model. The interaction force constants $\mathrm{N}=\mathrm{O} / \mathrm{N}-\mathrm{O}$ for the monodentate type in chromyl nitrate are slightly higher than the 1.11 mdyn $\AA^{-1}$ value reported for bidentate $\mathrm{KNO}_{3}$ [53] but close to the obtained values considering the nitrate groups in chromyl nitrate as bidentate.

The analysis of the force constants suggest that the coordination that better represents the group nitrate in chromyl nitrate is the bidentate because the obtained values for this case agree with the one reported by literature values for this coordination mode.

## 6. Conclusions

In the present paper an approximate normal coordinate analysis, considering the mode of coordination adopted by nitrate groups as monodentate and bidentate, was proposed for chromyl nitrate.

The assignments previously made [1] was corrected and completed in accordance with the present theoretical results. The assignments of the 27 normal modes of vibration corresponding to chromyl nitrate are reported.

The method that best reproduces the experimental vibrational frequencies, considering the two coordination types of the nitrate groups for chromyl nitrate, it is the B3LYP/6-31G*.

The NBO and AIM analysis confirm the hexacoordination of the Cr atom in chromyl nitrate.

We have employed the Lanl2DZ, 6-31G* and 6-311+G basis sets at the B3LYP level to obtain a molecular force field and vibrational frequencies.

An SQM force field was obtained for chromyl nitrate after adjusting the theoretically obtained force constants in order to minimize the difference between observed and calculated frequencies.

We demonstrate that a DFT molecular force field for the chromyl nitrate with the coordination mode adopted by nitrate groups as bidentate, computed using Lan12DZ, 6-31G* and 6$311+\mathrm{G}$ basis sets are well represented.

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## Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.saa.2007.06.020.

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[^0]:    * Corresponding author. Tel.: +54 3814311044 ; fax: +54 3814248169.

    E-mail address: altabef@fbqf.unt.edu.ar (A. Ben Altabef).
    ${ }^{1}$ A. Ben Altabef is member of the Research Career of CONICET (National Research Council of R. Argentina).

[^1]:    $\nu$, stretching; $\delta$, deformation; $\rho$, rocking; wag, $(\gamma)$ wagging; $\tau \mathrm{w}$, torsion.
    ${ }^{\text {a }}$ This work.
    ${ }^{\mathrm{b}}$ Considering the nitrate group as ring of four members.

