

5
6 The non-permutation flow-shop scheduling problem: a
7 literature review

8 *Rossit, Daniel Alejandro*^{*1,2}, *Tohmé, Fernando*^{2,3}, *Frutos, Mariano*^{1,4}

9 ¹*Department of Engineering, Universidad Nacional del Sur, Av. Alem 1253, Bahía Blanca (8000), Argentina.*

10 ²*INMABB-UNS-CONICET, Av. Alem 1253, Bahía Blanca (8000), Argentina.*

11 ³*Department of Economics, Universidad Nacional del Sur, San San Andrés 800, Bahía Blanca (8000), Argentina.*

12 ⁴*IIESS UNS CONICET, San Andrés 800, Bahía Blanca (8000), Argentina.*

13 **corresponding author*

14 Abstract

15 The Non-Permutation Flow-Shop scheduling problem (NPFS) is a generalization of the
16 traditional Permutation Flow-Shop scheduling problem (PFS) that allows changes in the job order on
17 different machines. The flexibility that NPFS provides in models for industrial applications justifies
18 its use despite its combinatorial complexity. The literature on this problem has expanded largely in
19 the last decade, indicating that the topic is an active research area. This review is a contribution
20 towards the rationalization of the developments in the field, organizing them in terms of the objective
21 functions in the different variants of the problem. A schematic presentation of both theoretical and
22 experimental results summarizes many of the main advances in the study of NPFS. Finally, we
23 include a bibliometric analysis, showing the most promising lines of future development.

24 Keywords: Non-permutation Flow-shop; Scheduling; Flow-Shop; Review

25 Highlights

- 26
- An exhaustive review of the Non-Permutation Flow-Shop Scheduling problem.
 - A comprehensive classification in terms of objective functions and the solution methods employed in the literature.
 - A compilation of problems that, modeled as PFS, do not ensure optimality.
 - A revision of the main experimental results.
- 27
28
29
30

- A detailed description of future research lines and literature gaps.

32

33 1. Introduction

34 Scheduling problems of production systems have been extensively analyzed and worked out
35 under different approaches (Błazewicz, et al (1996, [8]); Allahverdi et al (1999, [3]); Kis (2003, [37]);
36 Allahverdi et al (2008, [4]); Kis and Kovacs (2012, [39]) and Allahverdi (2015) [5]). The results in
37 this field have contributed to the improvement of manufacturing systems (Błazewicz, et al (2007,
38 [11])).

39 Flow-shop configurations are commonplace in manufacturing settings where a set of jobs N
40 $= \{1, 2, \dots, n\}$ are processed by a set of machines $M = \{1, 2, \dots, m\}$. Each job goes through the
41 machines in the same technological order, i.e. it starts at machine 1, then goes to machine 2, ... up to
42 machine m . The decision to make is to choose the order on which the different jobs will pass through
43 the machines. If the job sequence is the same for all the machines, the schedule is called a *permutation*
44 and the problem of choosing the best one is known as the Permutation Flow-Shop problem (PFS). If
45 instead the processing sequence can change from one machine to the next, the permutation condition
46 is relaxed and the problem is known as Non-Permutation Flow-Shop (NPFS). The standard
47 description of the NPFS problem considers the following specifications:

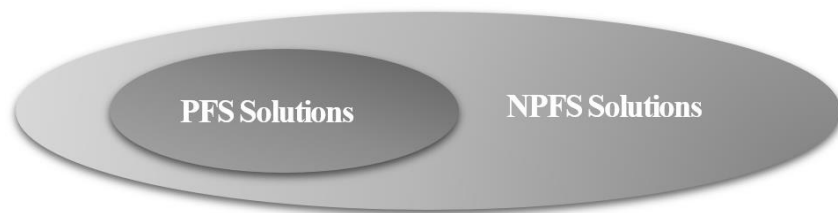
- 48 1. Each machine can process only one job at a time.
- 49 2. Each job j has a processing time p_{ij} on machine $i = 1, 2, \dots, m$.
- 50 3. The capacity of intermediate buffers must be large enough to allow the reordering of the job
51 sequence.

52 The standard settings of NPFS and PFS are very similar, being the third item the most relevant
53 potential difference between them. In some cases, PFS problems assume also intermediate buffers
54 with unlimited capacity, being so perfectly compatible with NPFS. On the other hand, in the absence
55 of intermediate buffers, the NPFS approach is not applicable to obtain a feasible scheduling scheme
56 (the same happens with the “no-wait” flow-shop case [48]). Besides the aforementioned three main
57 specifications in the standard NPFS form, there are other requirements: all the jobs and machines
58 must be available from the beginning; preemption is not allowed; machines can be idle during the
59 planning horizon; each job can be processed by only one machine at a time; and the problem data is
60 deterministic and known in advance. This description does not encompass the entire realm of NPFS

61 problems, but serves as a template for them. With minor changes (such as adding or removing
62 constraints), all the different NPFS variants can be obtained.

63 In the last decade, the researchers in the scheduling community have shown a growing
64 interest in the analysis NPFS problems. Among the important issues that have since been considered,
65 one is the detection of the manufacturing conditions for which NPFS is more promising than PFS,
66 since the solutions that are obtained under the latter approach can be inferior to those of NPFS
67 problems. This approach has been extensively analyzed in the literature on flow shop systems,
68 yielding new views on the schedule of production activities. This is in particular the case of
69 environments in which the optimizing criterion is related to due-dates. Liao et al (2006, [43]) indicates
70 that solving flow shop problems minimizing total tardiness under the PFS approach leads to
71 efficiency losses of around a 10% of the objective in comparison to the solutions obtained under
72 NPFS. Moreover, Lin et al (2009, [46]) shows that in flow shop systems organized in manufacturing
73 cells with due-date related objectives the gains in efficiency obtained with NPFS schedules are, for
74 some cases, of 30%, while in average of around 10%. In the case of completion time-related objective
75 functions the gains are of 5% to 6%. Some of these results were extended by Ying et al (2010, [97]),
76 showing empirically that if set up and processing times have larger dispersion the improvements are
77 even larger. For instance, if the range of set up times increases, the average improvement of NPFS
78 schedules over PFS ones for completion time objectives, when the range of set up times increases,
79 grows from 0,5% to 1,5%, reaching in some cases up to 13%. For objective functions related to
80 delivery dates, the average improvements grow from 0.5% under PFS to 7% with NPFS, with many
81 instances above 30% reaching even 40%.

82 This is extremely relevant since flow-shop settings are very common in actual industrial
83 plants, representing nearly a quarter of manufacturing systems, assembly lines and information
84 service facilities (Pan et al., 2011, [59]). Therefore, the possibility of improving the performance of
85 manufacturing systems by means of a better scheduling approach can have a huge impact on a number
86 of industry and organizations.



87

88

Figure 1. Solution spaces of NPFS and PFS

89 The main reason for the late concern with NPFS problems is their hardness: while the PFS
90 approach searches its optimal solution among $n!$ feasible schedules, being n the number of jobs, the
91 NPFS approach has to consider $n!^m$ possibilities. The increase of hardware computational power in
92 the last decade has nevertheless fueled the interest in finding efficient algorithms for NPFS problems.
93 In fact, more than the 65% of the papers reviewed for this paper, have been published after 2006. This
94 shows that NPFS is currently a fashionable topic in the flow-shop scheduling literature. Furthermore,
95 the results obtained indicate that this approach has large potential benefits superseding those of the
96 classic PFS one. Moreover, as shown in Figure 1, since the class of solutions of PFS is a subset of
97 those of NPFS.

98 We conceive our survey as a contribution to the systematization of the literature on NPFS
99 problem, highlighting important results and outlining future research lines. This review gathers, to
100 the best of our knowledge, all the NPFS literature, describing the NPFS problems discussed there,
101 classifying them in terms of the objective functions and commenting on the solution methods applied.
102 The organization of the paper is as follows. Section 2 presents the classification and notation used in
103 the paper. Once laid out the basis for the review, section 3 presents a description of the literature,
104 classified according to the objective functions considered there. In Section 4, we present a statistical
105 analysis of the problems and solutions methods developed in the literature, obtaining interesting
106 bibliometric data and results. Finally, section 5, presents the conclusions of this work and an outline
107 of promising future lines of research.

108 2. Non-Permutation Flow-Shop problems: classification, notation 109 and other considerations

110 To represent the different NPFS variants we have to consider some modifications of the
111 standard form presented in the previous section, namely removing or adding assumptions and
112 constraints. To denote them we adopt the classification and nomenclature proposed by Graham et al.
113 (1979, [29]) and implemented by Pinedo (2012, [62]). The resulting NPFS variants are characterized
114 as a triplet $\alpha | \beta | \gamma$. The first field, α , describes the machine environment or shop configuration and
115 contains only one entry. The β field provides details of the processing characteristics and constraints
116 and may contain no entry at all, a single entry, or multiple entries. The γ field describes the objective
117 function, usually in a single entry (more than one entry indicates a multi-objective case).

118 With regard to the α field, the possible entries could be either F (for pure flow-shop settings
119 with m stages and only one machine or processor per stage), or J (for job-shop with m stages). Despite
120 this potential variety, in this paper we consider only the pure flow-shop settings. The reason of this is
121 that the other settings have been already described in the literature. For instance, the hybrid flow-shop

122 has been reviewed by Linn et al. (1999, [49]); Ruiz et al. (2010, [81]); Ribas et al. (2010, [74]) and
123 Li et al. (2015, [42]). Thus, for us, the only possible entry in the α field is F .

124 With respect to the β field, multiple entries are possible, enumerating the constraints and
125 assumptions considered for the specific cases. The appearance of an entry implies that the
126 corresponding condition applies. The possible entries are:

- 127 • r_j : indicates that jobs cannot start their processing before their release date. If r_j is not present
128 in the β field, jobs can start their processing at any time. In contrast to release dates, due dates
129 are not specified in this field. The objective function gives sufficient indication whether or
130 not there are due dates.
- 131 • $Prmp$: means that preemption is allowed, while its absence indicates that they are not allowed.
- 132 • s_{jk} : denotes the sequence-dependent setup time of job k after finishing job j . If this setup time
133 depends on the machine, the machine subscript i is included, i.e., s_{ijk} . If no s_{jk} appears in the
134 β field, all setup times are supposed to be sequence independent (included in the processing
135 times) or 0.
- 136 • $prmu$: indicates that the job ordering is the same order for every machine.
- 137 • $block$: implies that buffer capacities between machines are limited. Jobs must wait in the
138 previous stage until sufficient space is free. This condition is not enough to prevent NPFS
139 schedules, since the buffer capacity may be enough to reorder at least one job. This topic will
140 be thoroughly discussed in the next section.
- 141 • $unavail$: states that machines are not available at some times.

142 In the case of stochastic parametrizations, we will indicate it with the same notation but in
143 capital letters. For instance, if the release date of job j is an uncertain parameter, the entry at the β
144 field will be denoted R_j , while the regular non-stochastic entry is r_j . This notation is adopted from
145 Pinedo (2012, [63]). Other possible entries for β exist, but do not apply in our study, as for instance
146 no-wait (it does not work for NPFS) and precedence (it is redundant for flow-shop settings).
147 Nevertheless, if some other entry appears in our review, its denotation will be self-explanatory.

148 Let C_{ij} represent the completion time of the operation of job j on machine i , and C_{mj} the
149 completion time on the last machine (that is, when j exits the system). The flowtime of job j is denoted
150 by F_j , and indicates the time spent by the job in the system, which can be calculated as: $F_j = C_{mj} - r_j$.
151 The lateness of job j is defined as L_j , and is $L_j = C_{mj} - d_j$. So expressed, L_j can be negative. The
152 tardiness of job j is $T_j = \max\{C_{mj} - d_j, 0\}$ and the earliness $E_j = \max\{d_j - C_{mj}, 0\}$. Both of them are
153 nonnegative by definition. If there exists a penalty for each tardy job, then the unit penalty is used,

154 U_j , which is 1 if $C_{mj} > d_j$ and 0 otherwise. Many objective functions associate a weight to each job,
155 w_j . These weights gauge the importance of each job respect to the others, representing different costs,
156 volume, priorities or other special features consider relevant by the decision-maker.

157 To illustrate how this notation is used, let us consider the standard version of NPFS presented
158 in the introduction of the paper, which will be denoted as $F \mid \mid C_{max}$ (notice that the β field is empty).
159 This means that the production setting is a flow-shop system of m machines and the optimization
160 criterion is captured by makespan. For another example, suppose that the number of machines is
161 limited to 10, the jobs have release dates, the setups are sequence dependent for each machine, and
162 the optimality criterion is maximal tardiness. This problem is represented as $F \mid r_j, s_{ijk} \mid T_{max}$.

163 2.1. How buffers influence policies

164 As already mentioned, a NPFS treatment requires the existence of intermediate buffers that
165 smooth out the production system. There exist various kinds of intermediate buffers, depending on
166 their capacity. The most common in the literature satisfies the condition of *unlimited intermediate*
167 *storage* (UIS). On the other extreme of the range of possibilities, we find the case in which no
168 intermediate buffers exist, corresponding to the *no intermediate storage* (NIS) condition. Between
169 them, we have the cases of finite *intermediate storage* (FIS). We have also the case in which products
170 must go immediately from a workstation to another, the *zero wait* (ZW) case. Finally, the *mixed*
171 *intermediate storage* (MIS) case obtains as a combination of two or more of the previous cases.

172 The UIS condition covers the cases in which the buffering capacity is at least $n - 1$, where n
173 is the number of jobs. This ensures the absence of deadlocks in the production system, since each
174 machine has a buffer that allows it to store all the intermediate products except the one that is being
175 processed. Rossi and Lanzetta (2013, [75]) reduce the storing capacity of the buffer, in this case, to n
176 $- 2$ since the previous machine can keep on hold the result of the last processing job without
177 interrupting the flow of the rest of jobs. However, the usual minimal bound for the capacity of UIS
178 buffers in the literature is, as said, $n - 1$.

179 The opposite is the case of the NIS condition. When a job finishes its process on machine i ,
180 if machine $i + 1$ is busy processing another job, the former must stay on machine i generation a
181 deadlock in the flow of the system, since there is no buffering facility that could be used to store it.
182 This kind of production system does not lend itself to a NPFS treatment and admits only PFS
183 solutions. The FIS condition, in turn, allows for the use buffers able to store $|b_i|$ units¹ after machine
184 i has finished its operation, with $|b_i|$ less than $n - 1$ units. This implies that if job j finishes on machine

¹ By a slight abuse of language, we denote with $|b_i|$ the capacity of buffer b_i .

185 i , and b_i situated between i and $i + 1$, is full while machine $i + 1$ is processing job k , the result of job
 186 j must wait until it finds a place in b_i obstructing machine i . b_i will be able to free space once machine
 187 $i + 1$ finishes job k and transfers the result to $i + 2$ or to buffer b_{i+1} between $i + 1$ and $i + 2$, $i = 1, 2,$
 188 $\dots, m - 2$.

189 The complexity of the problem with intermediate buffers with limited capacity is analyzed in
 190 Papadimitriou and Kanellakis (1980, [61]), showing that even with only two machines is NP-hard. If
 191 only schedules that do not generate deadlocks are considered feasible, the number of NPFS feasible
 192 schedules depends on the capacity of each b_i . To see this, consider on one hand the case in which
 193 each b_i has capacity 0, not allowing NPFS solutions, being the number of feasible schedules $n!$
 194 (corresponding to PFS solutions), where n is the number of jobs. On the other hand, if each b_i has at
 195 least a capacity of $n - 1$, no deadlock can arise and thus each NPFS schedule is a feasible solution,
 196 implying that the number of feasible solutions is $n!^m$. In turn, if the capacity of each b_i strictly larger
 197 than 0 but also less than $n - 1$, not all NPFS schedules will be feasible since some of them will
 198 generate deadlocks. Brucker et al (2003, [16]) analyzed this case, showing that the cardinality of the
 199 set of feasible schedule Ω grows with the capacity of each buffer b_i according to the following
 200 expression:

$$201 \quad \Omega = n! \prod_{i=1}^{m-1} |b_i|! (|b_i| + 1)^{n-|b_i|}$$

202 The ZW case focuses on jobs that, after finishing on a machine i have to transfer immediately its
 203 output to machine $i + 1$. It is immediate that this condition can be only satisfied by PFS schedules
 204 and thus it does not allow NPFS feasible schedules. Finally, the MIS case mixes UIS and FIS buffers
 205 with instances of NIS or ZW. Thus, NPFS feasible schedules can only exist for some parts of the
 206 system where the storing policies satisfy UIS or FIS.

207

208 3. The Literature on NPFS

209 The notation presented above will be applied to characterize 72 papers. The resulting
 210 information is presented in Table 1 (at the end of Section 3.5), which indicates in its first column the
 211 year of the publication, in the second the reference and in the third the characterization of the problem
 212 addressed in that publication. The last column includes some comments about the publications, such
 213 as the approach used and other aspects of the paper. This table follows a similar format to the one
 214 presented in Ruiz and Vázquez-Rodríguez (2010, [81]). We encourage the reader to examine the

215 different solution methods that have been proposed for flow shop systems: in the case of exact
216 solutions see Kis and Pesch (2005, [38]), for the late work criterion Błażewicz, et al (2005, [10]) and
217 for meta-heuristics with sequence-dependent setups Ruiz, et al (2005, [80]).

218 In order to organize the review, we will divide the papers according to the type of objective
219 used in each work. Among the objectives we will consider are completion-time, cost and due-date.
220 On the other hand, we devote a particular interest to makespan (by far the most popular completion-
221 time objective) as a category in itself. Finally, we have two special “portmanteau” cases, one of the
222 papers that consider multi-objective problems and the other covering those concerned with all other
223 single-objective cases.

224 3.1. Completion-time based objective

225 3.1.1. Makespan

226 Makespan is the most frequently considered objective function. In fact, around 55% of the
227 papers under review consider makespan as a single objective. Thus, we separate this objective from
228 the rest of the completion-time ones. The first work dealing with a makespan NPFS problem was
229 Janiak (1988, [36]). In that paper, the duration of each operation depends linearly on the fraction of a
230 limited resource allotted to each machine (for instance fuel), and the decision is twofold, involving
231 the choice of the job sequence and the allocation of the resource to the different machines. To solve
232 the problem, a Branch & Bound procedure is applied. Potts et al. (1991, [64]) quantified for the first
233 time the impact of enforcing permutation schedules. They found a set of instances for which the worst
234 case of PFS makespan is $1/2\sqrt{m}$ times the NPFS makespan. Tandon et al. (1991, [90]) compared
235 empirically PFS against NPFS schedules. For small instances, they adopted an enumerative procedure
236 while for bigger ones they used simulated annealing. They showed that, for wider ranges of
237 processing times and bigger instances, NPFS becomes more advantageous than PFS. Strusevich and
238 Zwaneveld (1994, [86]) addressed two-machine cases, considering separately the setup, processing
239 and removal times. In this case, PFS cannot ensure optimality, and in the worst case the makespan of
240 PFS is $3/2$ of the NPFS makespan. They also analyzed the two-machine case with finite buffer
241 capacity, to show again that PFS does not ensure optimality. Both cases analyzed by Strusevich and
242 Zwaneveld are NP-hard. Deal, et al (1994, [21]) analyze problems of petrochemical plants for which
243 NPFS schedules are feasible, using FIS buffering. To solve the problem these authors use a heuristic
244 method identifying critical jobs, balancing the job load among processing stations and avoiding
245 bottlenecks. Grau et al (1996, [31]) study the scheduling of multipurpose batch plants with a finite
246 wait inter-stage policy (after finishing the processing a job in a machine, the time that the next job
247 can wait is restricted). To face this NPFS problem they implemented recursive procedures. Koulamas

248 (1998, [40]) presented a heuristic (HFC) capable of generating non-permutation schedules when it
249 deems appropriate. This heuristic has a similar performance as the NEH heuristic (Nawaz et al 1989,
250 [57]), with the advantage of yielding NPFS solutions while the NEH algorithm does not. Schwindt &
251 Trautmann (2000, [84]) analyze scheduling in batch production systems seen as an instance of
252 resource-constrained project scheduling by incorporating sequence-dependent facility setup times
253 and finite intermediate storage constraints. They also take into consideration possible production
254 shutdowns and time-varying work force. Jain and Meeran (2002, [35]) propose a multi-level hybrid
255 meta-heuristic enabling an efficient interaction between strategies of intensification and
256 diversification, based on scatter search and path relinking techniques. Liu and Ong (2002, [50])
257 propose three meta-heuristics for PFS and NPFS problems based on the neighborhood structure of
258 insertions. The meta-heuristic for NPFS problems has a critical-path neighborhood structure. Méndez
259 & Cerdá (2003, [53]) formulates a mathematical model of operational strategies changing the
260 precedences in the production line, also assuming that decisions can be made on the use of
261 intermediary buffers shared by several stages of the process. Pugazhendhi et al. (2003, [65]) consider
262 the NPFS problem assuming skipping or missing operations. A heuristic procedure (called NPS) that
263 inserts a job in the sequence whenever it improves the makespan. Brucker et al. (2003, [16]) handle
264 the NPFS problem with limited buffer capacity, which can eventually lead to blockings (when the
265 buffer is complete, the job must wait occupying the machine after its processing has finished). To
266 solve the problem, they implement a Tabu Search algorithm. Aggoune (2004, [66]) addresses the
267 NPFS problem considering availability constraints due to maintenance activities. Two types of
268 maintenance activities are considered separately, one of a fixed type, and the other of a time-window
269 kind. In the fixed case, the tasks must be carried out according to a fixed timetable, while in the time-
270 window case, there exists a time interval to perform the maintenance tasks. The solution is obtained
271 using a combination of a genetic algorithm and Tabu Search. Pugazhendhi et al. (2004, [66]) tackle
272 the NPFS problem with missing operations and sequence-dependent setup times. The optimizing
273 procedure consists in a new recursive formulation that gives a good permutation solution, followed
274 by the NPS heuristic ([65]) improving the solution by yielding non-permutation schedules. This
275 paper, also, deals with the objective function of minimizing the total weighted flow time. Rebaine
276 (2005, [73]) studies the worst-case performance ratio between the solutions of NPFS and PFS
277 problems with time delays. For the two-machine case, the solution of the PFS version does not ensure
278 optimality yielding a worst-case makespan ratio of 2. But if the operation times are just of one unit
279 of execution time, the makespan ratio is reduced to $(2-(3/n+2))$. For the m -machine case, the
280 makespan ratio is bounded by m . Haq et al. (2007, [32]) address the NPFS problem with a Scatter
281 Search algorithm. The algorithm is based on joining solutions and exploiting the adaptive memory to

282 avoid generating or incorporating duplicate solutions at various stages of the problem. Ying and Lin
283 (2007, [96]) present a Multi-Heuristic Desirability Ant Colony system (MHD-ACS) for NPFS
284 problems. They show the benefits of ant colony optimization for the solution of NPFS problems. Ying
285 (2008, [97]) proposed an iterated greedy heuristic for NPFS problems. This heuristic is compared to
286 other simple constructive heuristics and state-of-the-art meta-heuristics. As a conclusion, the author
287 indicates that iterated greedy methods are promising for NPFS problems. Rayward-Smith and
288 Rebaine (2008, [72]) present two heuristics for the two-machine unit execution time operations with
289 time delays. The heuristics are based on ordering jobs in terms of a non-increasing time delays order.
290 Sadjadi et al. (2008, [82]) analyze three NPFS problems, two of them with makespan as the objective
291 function and the other one with total weighted tardiness. In the makespan cases different features are
292 considered, one of them involves including time lags while another assumes sequence-dependent
293 setup times. Both of these cases consider missing operations. Mixed-Integer linear programming
294 formulations are presented for both cases. Sadjadi et al. (2008, [83]) consider two NPFS problems
295 with different objectives: one with makespan and the other with total flow time as goals. To solve
296 this problem, they implement a two-step procedure. Initially, an Ant Colony optimization algorithm
297 is used to obtain a good permutation solution. Then, this solution is improved by means of a local
298 search procedure that yields a non-permutation solution. Lin and Ying (2009, [46]) present a hybrid
299 Simulated Annealing and Tabu Search algorithm for the NPFS problem also yielding a non-
300 permutation solution. Nagarajan and Sviridenko (2009, [58]) present a bound for the PFS and the
301 NPFS solutions to the general case, showing that the makespan of the PFS optimal solution can be at
302 most $2\sqrt{\min\{m, n\}}$ times the makespan of the NPFS optimal solution.

303 Zheng and Yamashiro (2010, [100]) propose a quantum differential evolutionary algorithm
304 (QDEA) for the NPFS problem. The algorithm is based on running differential operations and local
305 search over a so-called Q-bit representation. Färber et al. (2010, [26]) address a scheduling problem
306 in which resequencing is permitted when workstations have access to intermediate or centralized
307 resequencing buffers, although this access is restricted by the number of available buffer places and
308 the physical size of the products. To solve this problem, the authors apply a hybrid approach, based
309 on constraint logic programming (CLP). Brucker and Shakhlevich (2011, [17]) study the inverse
310 scheduling version of the flow-shop problem, i.e. one in which, firstly, a job sequence is given, and
311 then, to make it optimal, processing times are restricted as to satisfy certain boundaries. They deduce
312 necessary and sufficient conditions for both PFS and NPFS problems. Ramezani et al. (2011, [70])
313 study the NPFS problem with missing operations, solving it with a genetic algorithm and Tabu
314 Search. Rudek (2011, [79]) prove that in the two-machine case with learning effects, PFS does not
315 ensure optimality, and both approaches (PFS and NPFS) are NP-hard, even if the learning effect is

316 assumed for only one of the machines (in a form of steep learning curve). Cheng et al. (2012, [18])
317 analyze the process of tearing-down and reconstructing buildings as a two-machine flow-shop with
318 resource-constrained problem. The authors provide MIP problem formulations and discuss their
319 complexity, developing polynomial algorithms for special cases. Rossi and Lanzetta (2013, [75])
320 address the NPFS problem with an ACO algorithm, establishing that the minimum buffer capacity to
321 avoid blockings is $(n-2)$. Rossi and Lanzetta (2013, [76]) deal with the same problem. A particular
322 feature of the ACO algorithm is that from the beginning it explores non-permutation solutions. In
323 [76] the authors tested the ACO algorithm on Taillard's (1993, [89]) benchmarks, but in Rossi and
324 Lanzetta (2014, [77]) they use the benchmarks of Demirkol et al. (1998, [22]) benchmarks. For these
325 instances, their ACO algorithm outperforms other variants also used to solve NPFS problems. Shen
326 et al. (2014, [85]) tackle the NPFS batching problem with sequence-dependent family setup time.
327 These authors develop a Tabu Search algorithm, including double tabu lists and multilevel
328 diversification. The group technology assumption is relaxed, allowing the family of jobs to be split.
329 Gharbi et al. (2014, [27]) present lower and upper bounds for several single-machine adjustment
330 procedures. Moukrim et al. (2014, [56]) introduce a Branch & Bound algorithm for the problem
331 described in Rebaine (2005, [73]). They present both new bounding procedures for this B&B
332 algorithm as well as new dominance rules. Benavides et al. (2014, [13]) deal with heterogeneous
333 NPFS problems for which two simultaneous issues need to be addressed: the assignment of workers
334 to workstations and the scheduling problem itself. The motivation comes from cases in which workers
335 are disabled people, and thus, their skills are not homogeneous. To solve this optimizing problem, a
336 Scatter Search and a Path Relinking algorithm are proposed. In Nikjo and Zarook (2014, [59]) the
337 problem analyzed is a NPFS in the context of a manufacturing cell with agreeable release dates and
338 setup times dependent on the sequence of parts of related products. Genetic algorithms and Tabu
339 Search yield the solutions. Zhang et al. (2014, [99]) approach the NPFS problem with periodical
340 maintenance activities. The method used for its solution is a hybrid genetic algorithm and a heuristic
341 based on NEH theory. Rossit et al. (2016, [78]) deals with NPFS problem under lot streaming
342 considerations. Benavides and Ritt (2016, [15]) propose a constructive iterated local search heuristic
343 for the NPFS problem. The algorithm is based on the observation that permutation and non-
344 permutation schedules are similar enough as to facilitate finding a non-permutation solution after
345 obtaining a good permutation one. Cui et al. (2016, [20]) deal with NPFs problems with availability
346 constraints. The availability of machines depends on two kinds of extra-production tasks, one
347 involves fixed tasks while the other refers to tasks with flexible time intervals with the continuous
348 working time assigned to machines cannot surpass a maximum allowed time. The optimization is

349 carried out running a hybrid incremental genetic algorithm combining local refinements and a
350 population diversity supervision scheme.

351 3.1.2. Other completion-time based objectives

352 We will review here the literature on NPFS problems with other completion-time based
353 objectives. In particular, we will focus on the following objective functions: total completion time,
354 total weighted completion time, total flow time and total weighted flow time.

355 Rajendran and Ziegler (2001, [69]) study the NPFS problem with missing operations when
356 the objective function is the minimization of total flow time. The authors solve it using dispatching
357 rules combined with a heuristic rule. Pugazhendhi et al. (2004, [67]) deal with two NPFS problems
358 with missing operations, the first one minimizing the total flow time, and the second, minimizing the
359 total weighted flow time. They present a heuristic (NPS-set), which works by improving a
360 permutation schedule. Färber and Coves Moreno (2006, [24]) propose a genetic algorithm for NPFS
361 problems when intermediate buffers are not available for every station or machine, each of which is
362 assumed to be capacitated. Färber et al. (2007, [25]) tackle a NPFS problem in which the demand is
363 semi-dynamic and the resequencing is restricted (similarly to [24]). The objective function is total
364 weighted completion time. The authors solve the problem by applying two approaches: the first a
365 Constraint Logic Programming analysis and the second a genetic algorithm. Li et al. (2010, [41])
366 address a two-machine robotic NPFS problem with total weighted completion as the performance
367 criterion. Robots take care of loading, unloading and translating jobs from a station to another. These
368 robots can handle only one job at a time. Optimal solutions arise from the application of a genetic
369 algorithm. Vahedi-Nouri et al. (2013, [91]) address the NPFS problem with learning effects and
370 machine availability constraints under the minimization of total flow time. The authors present a MIP
371 formulation and propose an improvement heuristic. Isenberg and Scholz-Reiter (2013, [34]) deal with
372 a batching NPFS problem, where batches are built at each stage. This results in a stage-interdependent
373 batching and scheduling problem. These authors consider three different objective functions: total
374 flow time, total completion time and makespan. Vahedi-Nouri et al. (2014, [93]) present a heuristic
375 method and a Simulated Annealing algorithm for a NPFS problem with learning effects, availability
376 constraints and release dates. The objective function optimize is total flow time. Benavides and Ritt
377 (2015, [14]) study the advantages of NPFS over PFS schedules. They use a two-phase heuristics and
378 consider the case of total completion time as objective function. In the first phase, an iterated local
379 search algorithm seeks a good permutation solution, and in the second phase, an effective insertion
380 neighborhood improves that solution by exploring close non-permutation solutions. Henneberg and
381 Neufeld (2016, [33]) study a NPFS with missing operations when the objective is total completion

382 time. They solve it with a modification of the NPS-set heuristic presented in [22], based on a two-
383 phase version of Simulated Annealing.

384 3.2. Due-date based objectives

385 Here we will focus on papers in which the objective functions represent a due-date concept.
386 These problems are known for being computationally hard, being even “binary NP-hard” in two-
387 machine cases (Błażewicz, et al 2005, [10]). Nevertheless, these problems have been extensively
388 studied in the PFS setting (Błażewicz , et al (2008, [12]); Pesch and Sterna (2009, [62]))

389 The objective functions that will be contemplated in this section are: maximum tardiness,
390 total tardiness and total weighted tardiness.

391 Swaminathan et al. (2007, [88]) study the impact of the enforcement permutation condition
392 on the general flow shop (non-permutation) problem. The goal analyzed is total weighted tardiness.
393 To obtain the solution they use three approaches: pure permutation, shift-based and pure dispatching.
394 The latter is the one able to yield non-permutation schedules. Their results show that PFS provides
395 an inefficient approach to this problem. Swaminathan et al. (2004, [87]) study the same problem in a
396 simplified version. Liao and Huang (2010, [44]) study the NPFS problem with total tardiness as a
397 goal, presenting and evaluating three different MIP formulations. Then, they present also two Tabu
398 Search algorithms. The comparison of NPFS to PFS indicates that NPFS is much more suitable for
399 these types of problems. Ziaee (2013, [101]) addresses the NPFS problem with sequence dependent
400 setup times with the minimization of total weighted tardiness as objective. This author proposes a
401 two-phase heuristic with the usual pattern. Namely, the first phase looks for a good permutation
402 solution, and second one, improves it through a non-permutation local search. Xiao et al. (2015, [94])
403 analyze flow-shop scheduling with order acceptance under weighted tardiness. The authors present
404 two different formulations of the problem. The first is a MIP formulation, which CPLEX can solve
405 for small instances. The second one, is a NIP (non-linear integer programming) formulation that can
406 be solved, in particular its medium and large size instances, by a two-phase genetic algorithm.

407 3.3. Experimental mono-objective studies

408 In this subsection, we present a group of papers comparing the quality of the solutions of the
409 PFS and NPFS problems in experimental analyses. These papers consider different given mono-
410 objective manufacturing settings, in order to assess the extra computational effort required by the
411 NPFS problems. The validity of the comparisons of these papers comes from the fact that the
412 problems are tested under the same parametrization and same instances while the solutions are
413 obtained running the same algorithms. In this way, these papers provide valuable experimental

414 insights to the non-permutation literature. The objectives analyzed in all the cases are the six more
415 common ones used in scheduling: three are completion-time based criteria (makespan, total
416 completion time and total weighted completion time), and the other three are due-date based criteria
417 (maximum tardiness, total tardiness and total weighted tardiness).

418 Liao et al. (2006, [43]) were the first to carry out this type of research. They tested a classic
419 flow-shop system under six objective functions. Their results indicate that, in general, NPFS
420 schedules improve very little over the PFS ones the value of completion-time based objectives.
421 However, for due-date based criteria the improvement is significant, especially for problems with
422 more than thirty jobs. They used as optimization tools a Genetic Algorithm and a Tabu Search
423 algorithm. Lin et al. (2009, [47]) presents a similar study, with the same objective functions but for a
424 flow line manufacturing cell with a sequence-dependent family of setups. Again, the conclusion for
425 completion-time based objectives is that non-permutation and permutation schedules have a similar
426 performance, being non-permutation a little better. But for due-date based objectives, non-
427 permutation schedules clearly outperform permutation ones. The authors solve the problems using a
428 Genetic Algorithm, Simulated Annealing and Tabu Search. The Simulated Annealing procedure
429 outperforms the other two meta-heuristics. Ying et al. (2010) [98] revisit [47], testing different setup
430 ranges, concluding that, for larger setup ranges NPFS overtakes PFS for most of the cases yielding
431 larger improvements. They find that NPFS performs better, in general, under the six objective
432 functions, but for due-date based ones, its performance is much better than that of PFS. In this case,
433 all the solutions are found running a Simulated Annealing algorithm.

434 3.4. Multi-objective versions

435 A promising area of study for non-permutation scheduling involves the optimization of
436 several objectives, mainly because the non-permutation case allows for a dearth of new solutions that
437 do not arise in the permutation setting. The papers that analyze multiple-objective instances of the
438 NPFS problems will be reviewed next.

439 Mehravaran and Logendran (2012, [51]) were the first to study multi-objective problems
440 under non-permutation schemes. They consider a flow-shop setting with sequence-dependent setup
441 times assuming machine availability constraints, job releasing and missing operations. They use a bi-
442 objective function. The goal is the minimization of the normalized sum of weighted completion time
443 and weighted tardiness. The authors present a MIP formulation and a Tabu Search algorithm.
444 Mehravaran and Logendran (2013, [52]) address the NPFS problem considering dual resources:
445 machines and labor. The goal is the minimization of the total weighted completion time and the total
446 weighted tardiness. As in [51] they use a weighted sum combining the two objectives. The

447 specification of the problem includes different skill levels, sequence-dependent setups, machine
448 availability constraints and job release dates. A two-layered procedure yields the solution. The outer
449 layer solves the traditional flow-shop problem (considering only job sequencing), and the inner layer,
450 finds an assignation of jobs to labor in agreement to the machine schedule. Three different search
451 algorithms are developed. These authors, the first ones to investigate flow-shop scheduling with two
452 resources problem, emphasize on the superiority of non-permutation schedules over permutation
453 ones. Rahmani et al. (2014, [68]) study a stochastic NPFS problem. Processing times and release date
454 are stochastic parameters that have a normal distribution. Three different objectives are minimized:
455 makespan, total flow time and tardiness. To deal with uncertainty they apply both a chance
456 constrained programming and a fuzzy goal programming approach. They also adapt a genetic
457 algorithm to handle large-size problem. Amirian and Sahraeian (2015, [6]) analyze a NPFS problem
458 minimizing simultaneously the makespan, the sum of flow time and maximum tardiness. The setting
459 includes release dates, past sequence-dependent set-up times, learning effects and machine
460 availability constraints. The authors use, as solution methods, Augmented ϵ -constraint and a heuristic
461 based on it.

462 3.5. Economic objective functions

463 In this section, we review works that evaluate objective functions from an economic point of
464 view, trying either to minimize operation costs or to maximize profits. In particular, we review papers
465 that study NPFS problems in which the cost is the objective function. In these five contributions, the
466 specification of which cost has to be minimized varies.

467 Grau et al. (1995, [30]) study a NPFS problem seeking to minimize the product changeover
468 cost of the production plan. This cost is incurred each time the production is set to produce a different
469 product. The authors develop a Branch and Bound procedure to solve the problem. Doganis et al
470 (2005, [23]) analyzes flow shop lubricant production processes. A MILP model is used to generate
471 schedules that are potentially NPFS, but not allowing Schedule changes at all stages since between
472 some of them buffering is of NIS type. The objective is the maximization of the income accrued by
473 the firm. Liberopoulos et al (2010, [45]) study problems of production plants of PET resins with
474 intermediate storage facilities specific to each product. The objective is the minimization of costs of
475 set up of intermediate buffers, in order to adapt products to alternative buffers, a costly activity,
476 without hampering the operational capacity of the system. Mohammadi et al. (2010, [55]) address
477 both the lot sizing and the scheduling problem in a NPFS system. They develop a MIP formulation
478 for the problem and present five MIP-based heuristics to minimize setup, storage and production
479 costs. Some of these heuristics are only capable of solving the PFS version of the problem. Vahedi-

480 Nouri et al. (2013, [92]) analyze a NPFS problem with learning effects and flexible maintenance
481 activities. The objective is the minimization of the sum of tardiness and maintenance costs. The
482 authors develop a hybrid of a Firefly algorithm and Simulated Annealing to solve a MIP formulation
483 of the problem. Ramezani and Saidi-Mehrabad (2013, [71]) investigate the lot sizing and
484 scheduling flow-shop problem, considering sequence-dependent setups, capacity constraints,
485 uncertain processing times and uncertain multiproduct and multi-period demand. A MIP model joint
486 with a big bucket time approach represents the problem. Two MIP-based heuristics with a rolling
487 horizon framework are applied. The authors also develop a hybrid meta-heuristic based on a
488 combination of Simulated Annealing, a Firefly algorithm and an ad-hoc heuristic for scheduling.
489 Babaei et al. (2014, [7]) also analyze the lot sizing and scheduling problem under slightly different
490 constraints, namely sequence-dependent setups, setup carryover and backlogging. They propose a
491 MIP formulation solved by the application of a genetic algorithm.

492 **Table 1.**

493 Summary of the reviewed literature

494 References: for the β field: *rc*: resource constrained, *skip*: skipping operations, *avail*: machine availability
495 conditions, *fmls*: family group products, *learn*: learning effect, *hr*: heterogeneous resources, *rp*: relocation, *dr*:
496 dual resources. A β entry in capital letters means a stochastic parameter. In the Comments column, B&B:
497 Branch and Bound, SA: Simulated Annealing, MPF: Mathematical Programming Formulation, SS: Scatter
498 Search, PR: Path Relinking, TS: Tabu Search, OM: Other Metaheuristics, GA: Genetic Algorithm, ACO: Ant
499 Colony Optimization, IG: Iterated Greedy, CLP: Constraint Logic Programming, CCP: Chance Constrained
500 Programming, FGP: Fuzzy Goal Programming.

Reference	Problem	Comments
Janiak (1988) [36]	$F rc C_{max}$	B&B procedure
Potts, et al. (1991) [64]	$F C_{max}$	bound between NPFS C_{max} and PFS C_{max} for special instances
Tandon, et al. (1991) [90]	$F C_{max}$	Enumerative for small instances and SA big instances
Strusevich, et al (1994) [86]	$F2 s_{ijk}, removal\ times C_{max}$	PFS is not optimal and the problem is NP- hard
	$F2 block C_{max}$	PFS is not optimal and the problem is NP- hard
Deal et al 1994 [21]	$F b_i C_{max}$	heuristic for balancing resources usage
Grau, et al. (1995) [30]	$F batch Costs$	B&B procedure
Grau, et al. (1996) [31]	$F batch, finite\ wait C_{max}$	tailored recursive procedure
Koulamas (1998) [40]	$F C_{max}$	HFC heuristic
Schwindt et al (2000) [84]	$F time\ lags C_{max}$	MPF
Rajendran, et al (2001) [69]	$F skip \Sigma C_j$	dispatching rules & heuristic
Jain, et al (2002) [35]	$F C_{max}$	Meta-heuristic, based on SS and PR, and TS
Liu, et al (2002) [50]	$F C_{max}$	OM

Pugazhendhi, et al. (2003) [65]	$F skip C_{max}$	heuristic
Brucker, et al. (2003) [16]	$F block C_{max}$	TS
Méndez et al (2003) [53]	$F b_i C_{max}$	MPF
Aggoune (2004) [1]	$F avail C_{max}$	GA and TS
Pugazhendhi, et al. (2004) [66]	$F skip \gamma$	$\gamma \in \{\Sigma w_j F_j, \Sigma F_j\}$ Heuristic: NPS set
Pugazhendhi, et al. (2004) [67]	$F skip, s_{ijk} \gamma$	$\gamma \in \{\Sigma w_j F_j, C_{max}\}$ Tailored heuristic and NPS-set
Swaminathan, et al. (2004) [87]	$F stochastic Costs$	GA and ATC heuristic
Doganis et al (2005) [23]	$F b_i Revenue$	MPF
Rebaine (2005) [76]	$F time delays C_{max}$	NP-hard, for 2 machines PFS not optimal
Liao, et al. (2006) [43]	$F \gamma$	$\gamma \in \{C_{max}, \Sigma C_j, \Sigma w_j C_j, T_{max}, \Sigma T_j, \Sigma w_j T_j\}$ TS and GA, compares all the six objective functions
Färber, et al (2006) [24]	$F block \Sigma w_j C_j$	GA
Haq, et al. (2007) [32]	$F C_{max}$	SS
Ying, et al (2007) [96]	$F C_{max}$	ACO
Färber, et al. (2007) [25]	$F block \Sigma w_j C_j$	GA and CLP
Swaminathan, et al. (2007) [88]	$F \Sigma w_j T_j$	ATC heuristics and GA
Ying (2008) [97]	$F C_{max}$	IG
Rayward-Smith, et al (2008) [72]	$F2 p_{ij}=p, time delays C_{max}$	heuristic - (uet: unit execution time)
Sadjadi, et al. (2008) [82]	$F \Sigma w_j T_j$	MPF
	$F time lags C_{max}$	
	$F s_{ijk} C_{max}$	
Sadjadi (2008) [83]	$F \gamma$	$\gamma \in \{\Sigma F_j, C_{max}\}$ ACO and local search
Lin, et al. (2009) [47]	$F fmls, s_{ijk} \gamma$	$\gamma \in \{C_{max}, \Sigma C_j, \Sigma w_j C_j, T_{max}, \Sigma T_j, \Sigma w_j T_j\}$ SA, TS and GA
Lin, et al (2009) [46]	$F C_{max}$	SA and TS
Nagarajan, et al (2009) [58]	$F C_{max}$	Comparison of PFS and NPFS makespan for the general case
Ying, et al. (2010) [98]	$F fmls, setup \gamma$	$\gamma \in \{C_{max}, \Sigma C_j, \Sigma w_j C_j, T_{max}, \Sigma T_j, \Sigma w_j T_j\}$ SA, setup depends on the family sequence
Liao, et al. (2010) [44]	$F \Sigma T_j$	TS
Li, et al. (2010) [41]	$F2 block \Sigma w_j C_j$	GA

Liberopoulos et al (2010) [45]	$F b_i Costs$	MPF
Mohammadi, et al. (2010) [55]	$F s_{ijk} Costs$	MPF based heuristic
Zheng, et al (2010) [100]	$F C_{max}$	Quantum Differential Evolutionary Algorithm (QDEA)
Farber, et al. (2010) [26]	$F C_{max}$	hybrid CLP and GA
Brucker, et al (2011) [17]	<i>inverse scheduling</i> - C_{max}	sufficient conditions for optimal sequence
Ramezani, et al. (2011) [70]	$F skip C_{max}$	GA and TS
Rudek (2011) [79]	$F2 learn C_{max}$	NEH-based heuristic
Mehravaran, et al (2012) [51]	$F \Sigma w_j C_j \& \Sigma w_j T_j$	TS with progressive perturbation
Cheng, et al. (2012) [18]	$F2 rp C_{max}$	complexity analysis, is NP-hard
Vahedi-Nouri, et al. (2013) [91]	$F learn, avail \Sigma F_j$	heuristic: VFR
Vahedi-Nouri, et al. (2013) [92]	$F learn, avail Costs$	hybrid firefly-SA
Ziaee (2013) [101]	$F s_{ijk} \Sigma w_j T_j$	local search heuristic
Isenberg, et al (2013) [34]	$F batch, fmls, r_j \gamma$	$\gamma \in \{\Sigma F_j, \Sigma C_j, C_{max}\}$ MPF
Mehravaran, et al (2013) [52]	$F skip, dr, s_{ijk}, avail, r_j \Sigma w_j C_j \& \Sigma w_j T_j$	OM
Rossi, et al (2013) [41]	$F C_{max}$	ACO
Rossi, et al (2013) [40]	$F bi = n-2 C_{max}$	ACO
Ramezani, et al (2013) [71]	$F s_{ijk}, P_{ij} Costs$	MPF-Heuristics and OM, uncertain demands
Shen, et al. (2014) [85]	$F batch, setup C_{max}$	TS
Gharbi, et al. (2014) [27]	$Fm C_{max}$	bounding procedures
Moukrim, et al. (2014) [56]	$F2 uet, time delays C_{max}$	B&B
Rossi, et al (2014) [77]	$F C_{max}$	ACO
Benavides, et al. (2014) [13]	$F hr C_{max}$	Heuristic: SS and PR
Nikjo, et al (2014) [59]	$Fm s_{ijk}, r_j C_{max}$	GA and TS
Vahedi-Nouri, et al. (2014) [93]	$F learn, avail, r_j \Sigma F_j$	Heuristic and SA
Babaei, et al. (2014) [7]	$F backlog Costs$	GA
Zhang, et al. (2014) [99]	$F setup, avail C_{max}$	ACO
Rahmani et al. (2014) [68]	$F R_j, P_{ij} C_{max} \& \Sigma F_j \& \Sigma T_j$	CCP and FGP
Xiao, et al. (2015) [94]	$F OA = order acceptance \Sigma w_j T_j$	TS-GA
Amirian, et al (2015) [6]	$F learn, s_{ijk} C_{max} \& \Sigma F_j \& T_{max}$	Augmented ϵ -constraint, heuristic

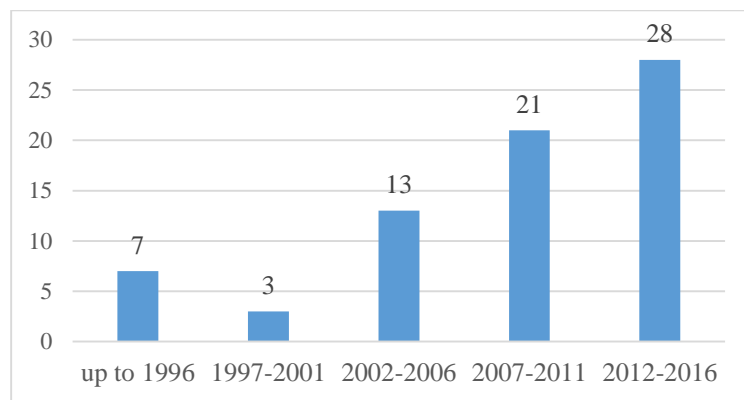
Benavides, et al (2015) [14]	$F \mid \mid \Sigma C_j$	IG
Benavides, et al (2016) [15]	$F \mid \mid C_{max}$	OM
Cui, et al. (2016) [20]	$F \mid avail \mid C_{max}$	OM
Henneberg, et al (2016) [33]	$F \mid skip \mid \Sigma F_j$	SA
Rossit, et al. (2016) [78]	$F \mid lot-streaming \mid C_{max}$	MPF

501

502 4. A quantitative analysis of the literature

503 This review has analyzed 72 papers, representing, as far as we know, the whole NPFS
504 literature (not including Hybrid Flow-Shop variants). Our analysis follows closely other reviews, as
505 for instance Yenisey and Yagmahan (2014, [95]) on multi-objective flow-shop formulations and Ruiz
506 and Vásquez-Rodríguez (2010, [81]) on hybrid flow-shop problems.

507 A remarkable aspect of this scheduling literature is that more than the 65% of the papers have
508 been published after 2007. This is can be seen in Figure 2, in which for clarity papers are grouped in
509 terms of their publication in five-year periods. Given the clear trend to an increasing number of
510 publications, while still low compared to those devoted to other well-developed scheduling issues,
511 we can infer that NPFS is a promising area for further developments.

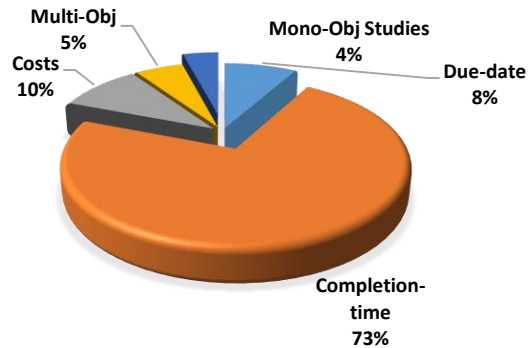


512

513 **Figure 2.** Number of papers published in five-year periods.

514 Figure 3 shows the different NPFS problems that have been analyzed in the literature,
515 indicating the proportion of papers devoted to each kind of objective function. As was already
516 mentioned, completion-time based are by far the most frequent objectives functions: 73% of the
517 papers focus on them. A special case of completion-time objective is makespan, covered by 56% of
518 the papers. Other kinds of completion-time objectives are analyzed in 17% of the publications. This
519 is not surprising, giving the primacy of makespan over other objective functions in the literature on

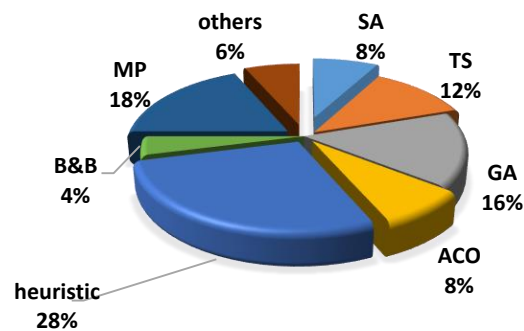
520 scheduling, as indicated in [81]. The other types of objectives functions are considered in the
 521 remaining 27% of the literature. From them, due-date based objectives functions represents only the
 522 8% of the publications, indicating that these important objective functions are under-represented,
 523 requiring further and deeper attention. This has been emphasized in particular in [43], [47] and [98].



524
 525

Figure 3. Distribution of objective functions considered in the literature.

526 The distribution of the different optimization techniques applied in the literature is presented
 527 in Figure 4. This shows that in general, exact approaches (mathematical programming and Branch
 528 and Bound) are not frequently applied, representing only 22% of the literature. In contrast, heuristics
 529 are used in 28% of the publications. Particular cases of meta-heuristic, Simulated Annealing, Tabu
 530 Search, Genetic Algorithms and Ant Colony Optimization algorithms are the most frequently applied
 531 methods of solution.



532

533 **Figure 4.** Distribution of optimization tools used. ACO: Ant Colony Optimization, GA: Genetic Algorithm,
 534 TS: Tabu Search, SA: Simulated Annealing, MP: Mathematical Programming, B&B: Branch and Bound.

535 To conclude, we can point out that there does not exist yet a consensus on the state-of-the art
 536 optimization methods for NPFS methods. We can state that exact methods seem not to be (currently)
 537 the most adequate for the solution of problems of intermediate and large size, while heuristic and
 538 meta-heuristic methods have shown to be able to yield solutions for them of good and very good

539 quality. The downside of this is that heuristic methods are not yet able to handle general cases. On
 540 the other hand, among meta-heuristic methods, those based on Tabu Search yield better results than
 541 others to which they have been compared. Those comparisons, it must be noted, are not exhaustive
 542 and thus Tabu Search cannot be deemed yet as the best possible approach to solving NPFS problems.
 543 The natural similarities between NPFS and PFS problems have led some authors ([16]) to develop
 544 sequential improvement procedures that start by solving, in a standard way, the PFS problem. The
 545 result of such procedures is, at the very least, a very good PFS solution but sometimes yielding a
 546 NPFS one. On the other hand, Rossi and Lanzetta (2014, [77]) applied meta-heuristics (ACO) to
 547 NPFS problems just from the start, instead of finding a previous PFS solution. This allows to search
 548 directly the space of NPFS solutions. The proviso is that this approach is more adequate in the cases
 549 in which the optimal NPFS and PFS solutions differ markedly. When those solutions are rather
 550 similar, starting from PFS solutions seems a better approach to reach the optimal NPFS ones. Both
 551 approaches profit from the flow shop structure, in which the sequence is the same for all jobs.

552 4.1. Bibliometric analysis

553 Also is of interest to provide some bibliometric information about the literature on NPFS. We
 554 follow the approach of other reviews, such as Aguezzoul (2014, [2]), Merigó et al (2016, [54]) and
 555 Gorman (2016 [28]), who showed that bibliometric information can be very useful for the evaluation
 556 of the research on a new topic. The relevant information includes the list of journals where papers on
 557 the topic have been published, the frequency of publication and their impact. On the latter, [28]
 558 centers its attention in the number of citations reported by Google Scholar at the time the article was
 559 retrieved. This means, in our case, August 2016.

560 **Table 2.**

561 List of journals that have published two or more articles on NPFS. Note: the percentage is over the total of
 562 papers reviewed.

Publication name	No. of Papers	Percentage
<i>International Journal of Production Research</i>	8	11%
<i>Inter. Jour. of Advanced Manufacturing Technology</i>	7	10%
<i>Computers & Operations Research</i>	6	8%
<i>Proceedings</i>	6	8%
<i>Computers & Chemical Engineering</i>	5	7%
<i>European Journal of Operational Research</i>	4	5%
<i>Computers & Industrial Engineering</i>	3	4%
<i>Journal of Scheduling</i>	3	4%

<i>OR-Spectrum</i>	2	3%
<i>Applied Mathematics and Computation</i>	2	3%
<i>Expert Systems with Applications</i>	2	3%
<i>Journal of Applied Sciences</i>	2	3%

563

564 Table 2 is the list of all the journals that have published two or more papers reviewed in this
565 work. We can see that the International Journal of Production Research has been the outlet for 11%
566 of all the papers in the field. It is closely followed by the International Journal of Advanced
567 Manufacturing Technology and Computers & Operations Research, that have published 7 and 6 of
568 the papers, respectively. With respect to conference proceedings, we only consider those indexed in
569 Scopus and Google Scholar and are written, at least its abstract, in English. The journals listed in
570 Table 2 have published 68% of the papers on NPFS reviewed here.

571 Journals other than those listed in Table 2 that have published at least one article on NPFS,
572 are Information Sciences, Journal of Manufacturing Systems, International Journal of Production
573 Economics and Applied Mathematical Modelling.

574 The impact of the work on NPFS is assessed in terms of the number of citations reported by
575 Google Scholar. Table 3 presents this information. We can see there the high impact of these articles,
576 totaling more than 1,400 citations. That means, in average, 20 citations per NPFS article while the
577 most cited one is Koulamas (1998 [40]) with 138 cites. On the other hand, we have to note that more
578 than half of the papers, 37 of them, have 10 or more cites.

579 **Table 3.**
580 Citations of NPFS papers drawn from Google Scholar, August 2016.

Bibliometric analysis	
<i>Numbers of total cites of NPFS papers</i>	1452
<i>Average number of cites per paper</i>	20
<i>Most cited paper (Koulamas 1998 [40])</i>	138
<i>Papers with ≥ 10 cites</i>	37 (50%)

581

582 4.2. Special cases

583 Since NPFS is far from being an extensively researched topic, we collect some important
584 results that may serve as guidelines for beginners or as a state-of-the-art reference for advanced
585 researchers or practitioners in the field. The first point to make is that NPFS schemes must yield the

586 same or better results than PFS ones for the same problem instance since the former includes all the
587 solutions of the latter and more. On the other hand, a highly relevant topic is the extra computational
588 effort required to solve NPFS problems in comparison to PFS problems. The oldest result in this
589 respect was presented by Conway et al. (1967, [19]) showing that, for the general flow-shop setting
590 (non-permutation for us) and makespan as objective function, the schedule on the first and the second
591 machine can be the same without hampering the optimal solution. The same is true for the last and
592 the second to last machines. Thus, for the case of $F_3 \mid C_{max}$, PFS is optimal. This result is clearly
593 proven in [27]. In consequence, the NPFS approach becomes beneficial for systems with more than
594 three machines. Newer results allow refining this analysis. In table 4, we highlight some of these
595 results. The first row presents the bound on the worst case if the problem is solved by a PFS scheme.
596 The next rows indicate special cases for which PFS cannot ensure optimality, even in the two-machine
597 case, because some of the conditions of [19] do not apply.

598 **Table 4.**
599 Special Non-permutation results, considering makespan as objective.

Problem	Comments	Source
$F \mid C_{max}$ vs $F \mid pmu \mid C_{max}$	PFS makespan worst case is: $2 \sqrt{\min\{m, n\}}$ times NPFS makespan.	[58]
$F_2 \mid removal\ times \mid C_{max}$	PFS approach does not ensure optimality. PFS makespan worst case is: $3/2$ times NPFS makespan.	[86]
$F_2 \mid block \mid C_{max}$	PFS approach does not ensure optimality.	[86]
$F_2 \mid time\ delays \mid C_{max}$	PFS does not ensure optimality. PFS makespan worst case is: 2 times NPFS makespan.	[73]
$F_2 \mid learning\ effect \mid C_{max}$	PFS does not ensure optimality.	[79]

600

601 Other relevant experimental results described recently are:

- 602 • For a wider range of processing times, the chances that NPFS schemes outperform
603 PFS schedules increase [90].
- 604 • In general, environments in which the objective functions are due-date based will
605 benefit more of the NPFS approach than environments in which they are based on
606 completion-time [43], [98] and [94].
- 607 • For a wider range of setup times it is more likely that the NPFS approach outperforms
608 the PFS approach [98] and [85]
- 609 • For simple flow-shop, the makespan is 2-3% better in the NPFS case [43] and [16].

5. Conclusions and directions for future research

In this paper, we have reviewed 72 articles on NPFS. We have classified these papers according to the variants of the problem considered in them, including the assumptions, constraints, objective functions and solution methods applied by the authors. We think this work may be helpful to other researchers in the field as well as a starting point for new research efforts.

The papers have been analyzed based on the type of objective function considered. Completion-time based criteria are the most frequent among the NPFS problems. Within this group, makespan is the most intensively studied (more than half of the papers have makespan as objective function). The other optimization criteria (due-date based and costs) and multi-objective approaches are covered in a quarter of all the publications. It is clear that these approaches are underrepresented in the literature. A conclusion from this review is that NPFS papers have, in average, 19 citations with more than half of them having been cited over 10 times.

Besides these conclusions, we present also a compendium of some theoretical and experimental results. On the theoretical aspect, we mentioned the problems for which the PFS approach does not ensure optimality, even in two-machine cases. That is, problems for which the NPFS approach becomes necessary to obtain high quality solutions. We also present a concise list of experimental results on the comparison of NPFS against PFS.

The NPFS problem is a recent and under-developed research topic (compared to traditional scheduling problems), and thus a promising area for further developments. The review allows us to suggest that the following are relevant inquiry issues. (1) NPFS problems with due-date based objective functions. (2) NPFS problems with three or more objectives. (3) real world case studies, comparing the costs of using NPFS and PFS approaches. (4) Scheduling under uncertainty is an interesting problem for which rescheduling could help to improve solutions. (5) The implementation of new meta-heuristics to address complex NPFS systems.

Acknowledgment

Thanks are due to the anonymous referees for their comments and criticisms that helped us to improve this paper.

640 References

- 641 [1] Aggoune, R. (2004). Minimizing the makespan for the flow shop scheduling problem with availability
642 constraints. *European Journal of Operational Research*, 153(3), 534-543.
- 643 [2] Aguezzoul, A. (2014). Third-party logistics selection problem: A literature review on criteria and
644 methods. *Omega*, 49, 69-78.
- 645 [3] Allahverdi, A., Gupta, J. N., & Aldowaisan, T. (1999). A review of scheduling research involving
646 setup considerations. *Omega*, 27(2), 219-239.
- 647 [4] Allahverdi, A., Ng, C. T., Cheng, T. E., & Kovalyov, M. Y. (2008). A survey of scheduling problems
648 with setup times or costs. *European Journal of Operational Research*, 187(3), 985-1032.
- 649 [5] Allahverdi, A. (2015). The third comprehensive survey on scheduling problems with setup
650 times/costs. *European Journal of Operational Research*, 246(2), 345-378.
- 651 [6] Amirian, H., & Sahraeian, R. (2015). Augmented ϵ -constraint method in multi-objective flowshop
652 problem with past sequence set-up times and a modified learning effect. *International Journal of*
653 *Production Research*, 53(19), 5962-5976.
- 654 [7] Babaei, M., Mohammadi, M., & Ghomi, S. F. (2014). A genetic algorithm for the simultaneous lot
655 sizing and scheduling problem in capacitated flow shop with complex setups and backlogging. *The*
656 *International Journal of Advanced Manufacturing Technology*, 70(1-4), 125-134.
- 657 [8] Błażewicz, J., Domschke, W., & Pesch, E. (1996). The job shop scheduling problem: Conventional
658 and new solution techniques. *European Journal of Operational Research*, 93(1), 1-33.
- 659 [9] Błażewicz, J., Pesch, E., Sterna, M., & Werner, F. (2005). A comparison of solution procedures for
660 two-machine flow shop scheduling with late work criterion. *Computers & Industrial*
661 *Engineering*, 49(4), 611-624.
- 662 [10] Błażewicz, J., Pesch, E., Sterna, M., & Werner, F. (2005). The two-machine flow-shop problem with
663 weighted late work criterion and common due date. *European Journal of Operational*
664 *Research*, 165(2), 408-415.
- 665 [11] Błażewicz, J., Ecker, K. H., Pesch, E., Schmidt, G., & Weglarz, J. (2007). *Handbook on scheduling:*
666 *from theory to applications*. Springer Science & Business Media.
- 667 [12] Błażewicz, J., Pesch, E., Sterna, M., & Werner, F. (2008). Metaheuristic approaches for the two-
668 machine flow-shop problem with weighted late work criterion and common due date. *Computers &*
669 *Operations Research*, 35(2), 574-599.
- 670 [13] Benavides, A. J., Ritt, M., & Miralles, C. (2014). Flow shop scheduling with heterogeneous
671 workers. *European Journal of Operational Research*, 237(2), 713-720.
- 672 [14] Benavides, A. J., & Ritt, M. (2015). Iterated Local Search Heuristics for Minimizing Total Completion
673 Time in Permutation and Non-permutation Flow Shops. In: *ICAPS* (pp. 34-41).

- 674 [15] Benavides, A. J., & Ritt, M. (2016). Two simple and effective heuristics for minimizing the makespan
675 in non-permutation flow shops. *Computers & Operations Research*, 66, 160-169.
- 676 [16] Brucker, P., Heitmann, S., & Hurink, J. (2003). Flow-shop problems with intermediate buffers. *OR*
677 *Spectrum*, 25(4), 549-574.
- 678 [17] Brucker, P., & Shakhlevich, N. V. (2011). Inverse scheduling: two-machine flow-shop
679 problem. *Journal of Scheduling*, 14(3), 239-256.
- 680 [18] Cheng, T. E., Lin, B. M., & Huang, H. L. (2012). Resource-constrained flowshop scheduling with
681 separate resource recycling operations. *Computers & Operations Research*, 39(6), 1206-1212.
- 682 [19] Conway, R. W., Maxwell, W. L., & Miller, L. W. (1967). *Theory of scheduling*. Courier Corporation
- 683 [20] Cui, W. W., Lu, Z., Zhou, B., Li, C., & Han, X. (2016). A hybrid genetic algorithm for non-permutation
684 flow shop scheduling problems with unavailability constraints. *International Journal of Computer*
685 *Integrated Manufacturing*, 1-18.
- 686 [21] Deal, D. E., Yang, T., & Hallquist, S. (1994). Job scheduling in petrochemical production: two-stage
687 processing with finite intermediate storage. *Computers & Chemical Engineering*, 18(4), 333-344.
- 688 [22] Demirkol, E., Mehta, S., & Uzsoy, R. (1998). Benchmarks for shop scheduling problems. *European*
689 *Journal of Operational Research*, 109(1), 137-141.
- 690 [23] Doganis, P., Sarimveis, H., Bafas, G., & Koufos, D. (2005). An MILP model for optimal scheduling
691 of the lubricant production plant. *Chemical Engineering Communications*, 192(8), 1067-1084.
- 692 [24] Färber, G., & Moreno, A. M. C. (2006). Performance study of a genetic algorithm for sequencing in
693 mixed model non-permutation flowshops using constrained buffers. In: *International Conference on*
694 *Computational Science and Its Applications* (pp. 638-648). Springer Berlin Heidelberg.
- 695 [25] Färber, G., Salhi, S., & Moreno, A. M. C. (2007). Semi-dynamic Demand in a Non-permutation
696 Flowshop with Constrained Resequencing Buffers. In: *International Conference on Large-Scale*
697 *Scientific Computing* (pp. 536-544). Springer Berlin Heidelberg.
- 698 [26] Farber, G., Coves Moreno, A. M., & Salhi, S. (2010). Performance evaluation of hybrid-CLP vs. GA:
699 non-permutation flowshop with constrained resequencing buffers. *International Journal of*
700 *Manufacturing Technology and Management*, 20(1-4), 242-258.
- 701 [27] Gharbi, A., Labidi, M., & Louly, M. A. (2014). The Nonpermutation Flowshop Scheduling Problem:
702 Adjustment and Bounding Procedures. *Journal of Applied Mathematics*, vol. 2014, Article ID 273567,
703 14 pages, 2014. doi:10.1155/2014/273567
- 704 [28] Gorman, M. F. (2016). A “Metasurvey” analysis in Operations Research and Management Science: A
705 survey of literature reviews. *Surveys in Operations Research and Management Science*, 21(1), 18-28.
- 706 [29] Graham, R. L., Lawler, E. L., Lenstra, J. K., & Kan, A. R. (1979). Optimization and approximation in
707 deterministic sequencing and scheduling: a survey. *Annals of Discrete Mathematics*, 5, 287-326.
- 708 [30] Grau, R., Espuña, A., & Puigjaner, L. (1995). Environmental considerations in batch production
709 scheduling. *Computers & Chemical Engineering*, 19, 651-656.

- 710 [31] Grau, R., Espuña, A., & Puigjaner, L. (1996). Completion times in multipurpose batch plants with set-
711 up, transfer and clean-up times. *Computers & Chemical Engineering*, 20, S1143-S1148.
- 712 [32] Haq, A. N., Saravanan, M., Vivekraj, A. R., & Prasad, T. (2007). A scatter search approach for general
713 flowshop scheduling problem. *The International Journal of Advanced Manufacturing*
714 *Technology*, 31(7-8), 731-736.
- 715 [33] Henneberg, M., & Neufeld, J. S. (2016). A constructive algorithm and a simulated annealing approach
716 for solving flowshop problems with missing operations. *International Journal of Production*
717 *Research*, 54(12), 3534-3550.
- 718 [34] Isenberg, M. A., & Scholz-Reiter, B. (2013). The Multiple Batch Processing Machine Problem with
719 Stage Specific Incompatible Job Families. In: *Dynamics in Logistics* (pp. 113-124). Springer Berlin
720 Heidelberg.
- 721 [35] Jain, A. S., & Meeran, S. (2002). A multi-level hybrid framework applied to the general flow-shop
722 scheduling problem. *Computers & Operations Research*, 29(13), 1873-1901.
- 723 [36] Janiak, A. (1988). General flow-shop scheduling with resource constraints. *The International Journal*
724 *of Production Research*, 26(6), 1089-1103.
- 725 [37] Kis, T. (2003). Job-shop scheduling with processing alternatives. *European Journal of Operational*
726 *Research*, 151(2), 307-332.
- 727 [38] Kis, T., & Pesch, E. (2005). A review of exact solution methods for the non-preemptive multiprocessor
728 flowshop problem. *European Journal of Operational Research*, 164(3), 592-608.
- 729 [39] Kis, T., & Kovács, A. (2012). On bilevel machine scheduling problems. *OR Spectrum*, 34(1), 43-68.
- 730 [40] Koulamas, C. (1998). A new constructive heuristic for the flowshop scheduling problem. *European*
731 *Journal of Operational Research*, 105(1), 66-71.
- 732 [41] Li, J., Zhang, L., ShangGuan, C., & Kise, H. (2010). A GA-based heuristic algorithm for non-
733 permutation two-machine robotic flow-shop scheduling problem of minimizing total weighted
734 completion time. In: *Industrial Engineering and Engineering Management (IEEM), 2010 IEEE*
735 *International Conference on* (pp. 1281-1285). IEEE.
- 736 [42] Li, J. Q., & Pan, Q. K. (2015). Solving the large-scale hybrid flow shop scheduling problem with
737 limited buffers by a hybrid artificial bee colony algorithm. *Information Sciences*, 316, 487-502.
- 738 [43] Liao, C. J., Liao, L. M., & Tseng, C. T. (2006). A performance evaluation of permutation vs. non-
739 permutation schedules in a flowshop. *International Journal of Production Research*, 44(20), 4297-
740 4309.
- 741 [44] Liao, L. M., & Huang, C. J. (2010). Tabu search for non-permutation flowshop scheduling problem
742 with minimizing total tardiness. *Applied Mathematics and Computation*, 217(2), 557-567.
- 743 [45] Liberopoulos, G., Kozanidis, G., & Hatzikonstantinou, O. (2010). Production scheduling of a multi-
744 grade PET resin plant. *Computers & Chemical Engineering*, 34(3), 387-400.

- 745 [46]Lin, S. W., & Ying, K. C. (2009). Applying a hybrid simulated annealing and tabu search approach to
746 non-permutation flowshop scheduling problems. *International Journal of Production Research*, 47(5),
747 1411-1424.
- 748 [47]Lin, S. W., Ying, K. C., & Lee, Z. J. (2009). Metaheuristics for scheduling a non-permutation flowline
749 manufacturing cell with sequence dependent family setup times. *Computers & Operations*
750 *Research*, 36(4), 1110-1121.
- 751 [48]Lin, Shih-Wei, and Kuo-Ching Ying. "Optimization of makespan for no-wait flowshop scheduling
752 problems using efficient matheuristics." *Omega* 64 (2016): 115-125.
- 753 [49]Linn, R., & Zhang, W. (1999). Hybrid flow shop scheduling: a survey. *Computers & Industrial*
754 *Engineering*, 37(1), 57-61.
- 755 [50]Liu, S., & Ong, H. L. (2002). A comparative study of algorithms for the flowshop scheduling
756 problem. *Asia-Pacific Journal of Operational Research*, 19(2), 205.
- 757 [51]Mehravaran, Y., & Logendran, R. (2012). Non-permutation flowshop scheduling in a supply chain
758 with sequence-dependent setup times. *International Journal of Production Economics*, 135(2), 953-
759 963.
- 760 [52]Mehravaran, Y., & Logendran, R. (2013). Non-permutation flowshop scheduling with dual
761 resources. *Expert Systems with Applications*, 40(13), 5061-5076.
- 762 [53]Méndez, C. A., & Cerdá, J. (2003). An MILP continuous-time framework for short-term scheduling
763 of multipurpose batch processes under different operation strategies. *Optimization and*
764 *Engineering*, 4(1), 7-22.
- 765 [54]Merigó, José M., and Jian-Bo Yang. "A Bibliometric Analysis of Operations Research and
766 Management Science." *Omega* (2016).
- 767 [55]Mohammadi, M., Fatemi Ghomi, S. M. T., Karimi, B., & Torabi, S. A. (2010). MIP-based heuristics
768 for lotsizing in capacitated pure flow shop with sequence-dependent setups. *International Journal of*
769 *Production Research*, 48(10), 2957-2973.
- 770 [56]Moukrim, A., Rebaine, D., & Serairi, M. (2014). A branch and bound algorithm for the two-machine
771 flowshop problem with unit-time operations and time delays. *RAIRO-Operations Research*, 48(2),
772 235-254.
- 773 [57]Nawaz, M., Enscore, E. E., & Ham, I. (1983). A heuristic algorithm for the m-machine, n-job flow-
774 shop sequencing problem. *Omega*, 11(1), 91-95.
- 775 [58]Nagarajan, V., & Sviridenko, M. (2009). Tight bounds for permutation flow shop
776 scheduling. *Mathematics of Operations Research*, 34(2), 417-427.
- 777 [59]Nikjo, B., & Zarook, Y. (2014). A Non-Permutation Flow Shop Manufacturing Cell Scheduling
778 Problem with Part's Sequence Dependent Family Setup Times. *International Journal of Applied*
779 *Metaheuristic Computing (IJAMC)*, 5(4), 70-86.

- 780 [60]Pan, Q. K., Tasgetiren, M. F., Suganthan, P. N., & Chua, T. J. (2011). A discrete artificial bee colony
781 algorithm for the lot-streaming flow shop scheduling problem. *Information Sciences*, 181(12), 2455-
782 2468.
- 783 [61] Papadimitriou, C. H., & Kanellakis, P. C. (1980). Flowshop scheduling with limited temporary
784 storage. *Journal of the ACM (JACM)*, 27(3), 533-549
- 785 [62]Pesch, E., & Sterna, M. (2009). Late work minimization in flow shops by a genetic
786 algorithm. *Computers & Industrial Engineering*, 57(4), 1202-1209.
- 787 [63]Pinedo, M. (2012). *Scheduling*. Springer.
- 788 [64]Potts, C. N., Shmoys, D. B., & Williamson, D. P. (1991). Permutation vs. non-permutation flow shop
789 schedules. *Operations Research Letters*, 10(5), 281-284.
- 790 [65]Pugazhendhi, S., Thiagarajan, S., Rajendran, C., & Anantharaman, N. (2003). Performance
791 enhancement by using non-permutation schedules in flowline-based manufacturing
792 systems. *Computers & Industrial Engineering*, 44(1), 133-157.
- 793 [66]Pugazhendhi, S., Thiagarajan, S., Rajendran, C., & Anantharaman, N. (2004). Generating non-
794 permutation schedules in flowline-based manufacturing systems with sequence-dependent setup times
795 of jobs: a heuristic approach. *The International Journal of Advanced Manufacturing
796 Technology*, 23(1-2), 64-78.
- 797 [67]Pugazhendhi, S., Thiagarajan, S., Rajendran, C., & Anantharaman, N. (2004) b. Relative performance
798 evaluation of permutation and non-permutation schedules in flowline-based manufacturing systems
799 with flowtime objective. *The International Journal of Advanced Manufacturing Technology*, 23(11-
800 12), 820-830.
- 801 [68]Rahmani, D., Ramezani, R., & Saidi-Mehrabad, M. (2014). Multi-objective flow shop scheduling
802 problem with stochastic parameters: fuzzy goal programming approach. *International Journal of
803 Operational Research*, 21(3), 322-340.
- 804 [69]Rajendran, C., & Ziegler, H. (2001). A performance analysis of dispatching rules and a heuristic in
805 static flowshops with missing operations of jobs. *European Journal of Operational Research*, 131(3),
806 622-634.
- 807 [70]Ramezani, R., Saidi-Mehrabad, M., & Rahmani, D. (2011). Flow Shop Scheduling Problem with
808 Missing Operations: Genetic Algorithm and Tabu Search. *International Journal of Applied
809 Operational Research*, 1(2), 21-30.
- 810 [71]Ramezani, R., & Saidi-Mehrabad, M. (2013). Hybrid simulated annealing and MIP-based heuristics
811 for stochastic lot-sizing and scheduling problem in capacitated multi-stage production system. *Applied
812 Mathematical Modelling*, 37(7), 5134-5147.
- 813 [72]Rayward-Smith, V. J., & Rebaïne, D. (2008). Analysis of heuristics for the UET two-machine flow
814 shop problem with time delays. *Computers & Operations Research*, 35(10), 3298-3310.
- 815 [73]Rebaïne, D. (2005). Flow shop vs. permutation shop with time delays. *Computers & Industrial
816 Engineering*, 48(2), 357-362.

- 817 [74] Ribas, I., Leisten, R., & Framiñan, J. M. (2010). Review: Review and classification of hybrid flow
818 shop scheduling problems from a production system and a solutions procedure perspective. *Computers*
819 *& Operations Research*, 37(8), 1439-1454.
- 820 [75] Rossi, A., & Lanzetta, M. (2013). Nonpermutation flow line scheduling by ant colony
821 optimization. *Artificial Intelligence for Engineering Design, Analysis and Manufacturing*, 27(04),
822 349-357.
- 823 [76] Rossi, A., & Lanzetta, M. (2013). Scheduling flow lines with buffers by ant colony digraph. *Expert*
824 *Systems with Applications*, 40(9), 3328-3340.
- 825 [77] Rossi, A., & Lanzetta, M. (2014). Native metaheuristics for non-permutation flowshop
826 scheduling. *Journal of Intelligent Manufacturing*, 25(6), 1221-1233.
- 827 [78] Rossit, D., Tohmé, F., Frutos, M., Bard, J., & Broz, D. (2016). A non-permutation flowshop scheduling
828 problem with lot streaming: A Mathematical model. *International Journal of Industrial Engineering*
829 *Computations*, 7(3), 507-516.
- 830 [79] Rudek, R. (2011). Computational complexity and solution algorithms for flowshop scheduling
831 problems with the learning effect. *Computers & Industrial Engineering*, 61(1), 20-31.
- 832 [80] Ruiz, R., Maroto, C., & Alcaraz, J. (2005). Solving the flowshop scheduling problem with sequence
833 dependent setup times using advanced metaheuristics. *European Journal of Operational*
834 *Research*, 165(1), 34-54.
- 835 [81] Ruiz, R., & Vázquez-Rodríguez, J. A. (2010). The hybrid flow shop scheduling problem. *European*
836 *Journal of Operational Research*, 205(1), 1-18.
- 837 [82] Sadjadi, S. J., Aryanezhad, M. B., & Ziaee, M. (2008). The general flowshop scheduling problem:
838 mathematical models. *Journal of Applied Sciences*, 8(17), 3032-3037.
- 839 [83] Sadjadi, S. J., Bouquard, J. L., & Ziaee, M. (2008). An ant colony algorithm for the flowshop
840 scheduling problem. *Journal of Applied Sciences*, 8(21), 3938-3944.
- 841 [84] Schwindt, C., & Trautmann, N. (2000). Batch scheduling in process industries: an application of
842 resource-constrained project scheduling. *OR Spectrum*, 22(4), 501-524.
- 843 [85] Shen, L., Gupta, J. N., & Buscher, U. (2014). Flow shop batching and scheduling with sequence-
844 dependent setup times. *Journal of Scheduling*, 17(4), 353-370.
- 845 [86] Strusevich, V. A., & Zwaneveld, C. M. (1994). On non-permutation solutions to some two machine
846 flow shop scheduling problems. *Zeitschrift für Operations Research*, 39(3), 305-319.
- 847 [87] Swaminathan, R., Fowler, J. W., Pfund, M. E., & Mason, S. J. (2004) Minimizing total weighted
848 tardiness in a dynamic flowshop with variable processing times. In: *IIE Annual Conference*.
849 *Proceedings* (p. 1). Institute of Industrial Engineers-Publisher.
- 850 [88] Swaminathan, R., Pfund, M. E., Fowler, J. W., Mason, S. J., & Keha, A. (2007). Impact of permutation
851 enforcement when minimizing total weighted tardiness in dynamic flowshops with uncertain
852 processing times. *Computers & Operations Research*, 34(10), 3055-3068.

- 853 [89] Taillard, E. (1993). Benchmarks for basic scheduling problems. *European Journal of Operational*
854 *Research*, 64(2), 278-285.
- 855 [90] Tandon, M., Cummings, P. T., & LeVan, M. D. (1991). Flowshop sequencing with non-permutation
856 schedules. *Computers & Chemical Engineering*, 15(8), 601-607.
- 857 [91] Vahedi-Nouri, B., Fattahi, P., & Ramezani, R. (2013). Minimizing total flow time for the non-
858 permutation flow shop scheduling problem with learning effects and availability constraints. *Journal*
859 *of Manufacturing Systems*, 32(1), 167-173.
- 860 [92] Vahedi Nouri, B., Fattahi, P., & Ramezani, R. (2013). Hybrid firefly-simulated annealing algorithm
861 for the flow shop problem with learning effects and flexible maintenance activities. *International*
862 *Journal of Production Research*, 51(12), 3501-3515.
- 863 [93] Vahedi-Nouri, B., Fattahi, P., Tavakkoli-Moghaddam, R., & Ramezani, R. (2014). A general flow
864 shop scheduling problem with consideration of position-based learning effect and multiple availability
865 constraints. *The International Journal of Advanced Manufacturing Technology*, 73(5-8), 601-611.
- 866 [94] Xiao, Y., Yuan, Y., Zhang, R. Q., & Konak, A. (2015). Non-permutation flow shop scheduling with
867 order acceptance and weighted tardiness. *Applied Mathematics and Computation*, 270, 312-333.
- 868 [95] Yenisey, M. M., & Yagmahan, B. (2014). Multi-objective permutation flow shop scheduling problem:
869 Literature review, classification and current trends. *Omega*, 45, 119-135.
- 870 [96] Ying, K. C., & Lin, S. W. (2007). Multi-heuristic desirability ant colony system heuristic for non-
871 permutation flowshop scheduling problems. *The International Journal of Advanced Manufacturing*
872 *Technology*, 33(7-8), 793-802.
- 873 [97] Ying, K. C. (2008). Solving non-permutation flowshop scheduling problems by an effective iterated
874 greedy heuristic. *The International Journal of Advanced Manufacturing Technology*, 38(3-4), 348-
875 354.
- 876 [98] Ying, K. C., Gupta, J. N., Lin, S. W., & Lee, Z. J. (2010). Permutation and non-permutation schedules
877 for the flowline manufacturing cell with sequence dependent family setups. *International Journal of*
878 *Production Research*, 48(8), 2169-2184.
- 879 [99] Zhang, S.-Y., Lu, Z.-Q., Cui, W.-W. (2014). Flow shop scheduling optimization algorithm with
880 periodical maintenance. *Jisuanji Jicheng Zhizao Xitong/Computer Integrated Manufacturing Systems,*
881 *CIMS*. 20(6), 1379-1387.
- 882 [100] Zheng, T., & Yamashiro, M. (2010, September). A novel quantum differential evolutionary
883 algorithm for non-permutation flow shop scheduling problems. In: *Electrical Engineering Computing*
884 *Science and Automatic Control (CCE), 2010 7th International Conference on* (pp. 357-362). IEEE.
- 885 [101] Ziaee, M. (2013). General flowshop scheduling problem with the sequence dependent setup
886 times: A heuristic approach. *Information Sciences*, 251, 126-135.