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A variable corona during the transition from type-C to type-B quasi-periodic oscillations in the black hole X-ray binary MAXI J1820+070

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ABSTRACT

We analyse a *Neutron Star Interior Composition Explorer* observation of the black hole X-ray binary MAXI J1820+070 during a transition from type-C to type-B quasi-periodic oscillations (QPOs). We find that below ~2 keV, for the type-B QPOs the rms amplitude is lower and the magnitude of the phase lags is larger than for the type-C QPOs. Above that energy, the rms and phase-lag spectra of the type-B and type-C QPOs are consistent with being the same. We perform a joint fit of the time-averaged spectra of the source, and the rms and phase-lag spectra of the QPOs with the time-dependent Comptonization model vkompth to study the geometry of the corona during the transition. We find that the data can be well fitted with a model consisting of a small and a large corona that are physically connected. The sizes of the small and large coronae increase gradually during the type-C QPO phase whereas they decrease abruptly at the transition to type-B QPO. At the same time, the inner radius of the disc moves inward at the QPO transition. Combined with simultaneous radio observations showing that discrete jet ejections happen around the time of the QPO transition, we propose that a corona that expands horizontally during the type-C QPO phase, from ~10⁴ km (~ 800 R_g) to 10⁵ km (~ 8000 R_g) overlying the accretion disc, transforms into a vertical jet-like corona extending over ~10⁴ km (~ 800 R_g) during the type-B QPO phase.

Key words: accretion, accretion discs – stars: black holes – stars: individual: MAXI J1820+070 – X-rays: binaries.

1 INTRODUCTION

Most black hole binaries (BHBs) are transient sources that, after months or even decades in a quiescent state, show an X-ray outburst that typically lasts weeks to months, driven by mass accretion from the secondary star on to the black hole primary (Tanaka & Shibazaki 1996). For a typical black hole transient (BHT), the emission in the X-ray band is mainly produced by two components in the accretion flow: At low energies, the spectrum is dominated by a geometrically thin, optically thick accretion disc (Shakura & Sunyaev 1973) that produces a blackbody-like thermal spectrum with a characteristic temperature around 1.0 keV (see McClintock & Remillard 2006, for a review). At high energy, the spectrum is dominated by emission from a plasma of highly energetic electrons, the so-called X-ray corona, in which the disc photons are inverse-Compton scattered producing a power-law-like component extending up to 100 keV (e.g. Sunyaev & Titarchuk 1980). A reflection component from fluorescence, photoabsorption, and Compton scattering due to the irradiation of the accretion disc by the hot corona (Basko, Sunyaev & Titarchuk 1974; George & Fabian 1991) is also observed in some sources (e.g. Xu et al. 2018; Chakraborty et al. 2021; Liu et al. 2022b). In the time-averaged spectrum, the main features of this component are a broad Fe K α line at 6.4–7 keV, a Fe K edge at 7–10 keV, and a broad Compton hump at 20–30 keV (see Gilfanov 2010, for a review).

A 'canonical' outburst of a BHT is divided into different X-ray spectral states (e.g. Méndez & van der Klis 1997) as the source follows a counterclockwise 'q' shape in the hardness intensity diagram (HID; e.g. Homan et al. 2001; Homan & Belloni 2005; Belloni & Motta 2016). At the beginning of the outburst, the source is in the low hard state (LHS), and the time-averaged spectrum is dominated by the non-thermal component with a power-law index $\Gamma \sim 1.5$. Both strong low-frequency band-limited noise components and low-frequency quasi-periodic oscillations (QPOs; van der Klis et al. 1985; van der Klis 2006) usually appear in this state (see below). In this scenario, in the LHS the accretion disc is truncated, with a truncation radius of tens to hundreds of R_g (McClintock et al. 2001; Done, Gierliński & Kubota 2007; Done & Diaz Trigo 2010).

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However, the detection of broad iron lines (e.g. Miller et al. 2006) and residual thermal disc emission (e.g. Rykoff et al. 2007) in the LHS suggest that the disc remains at or near the innermost stable circular orbit (ISCO; Esin, McClintock & Narayan 1997). The radio emission coming from a compact, persistent jet also exists in this state (e.g. Fender 2001). As the luminosity increases, the inner radius of the accretion disc moves inward (Gierliński, Done & Page 2008), the disc temperature increases, and the emission of the disc component becomes comparable to that of the non-thermal component (Cúneo et al. 2020), indicating that the source enters the intermediate state (IMS; see Homan & Belloni 2005; McClintock & Remillard 2006, and references therein). The IMS can be further divided into the hard intermediate (HIMS) and soft intermediate states (SIMS), with the spectrum of the source being softer in the SIMS than in the HIMS (Homan & Belloni 2005). The strong broad-band noise and QPOs in the LHS and HIMS are replaced by a relatively weaker broadband noise and QPO components in the SIMS (Homan & Belloni 2005). The compact jet is quenched and then a highly relativistic and discrete jet is launched in the IMS (Fender, Belloni & Gallo 2004). When the source enters the high-soft state (HSS), the thermal accretion-disc component dominates the time-averaged spectrum, and the power-law index of the non-thermal component increases to $\Gamma > 2.1$ (McClintock & Remillard 2006). A weak QPO together with weak broad-band noise sometimes appears in this state (Motta 2016). In the HSS, the jet turns off and the inner radius of the disc reaches the ISCO. As the flux of the source decreases, the source returns to the intermediate state and the low-hard state where the compact jet reappears (McClintock & Remillard 2006), and finally, the source goes back into quiescence.

1.1 Low-frequency quasi-periodic oscillations

The fast X-ray variability in BHTs has been widely studied as an important characteristic of the source during outbursts. OPOs are one of the most prominent features observed in these sources during the outburst (e.g. van der Klis et al. 1985; van der Klis 2006), which appear as one or more narrow peaks in the power density spectrum (PDS) of the source (see van der Klis 1989; Ingram & Motta 2019). When the centroid frequency is between mHz and \sim 30 Hz, the QPOs are classified as low-frequency QPOs (LFQPOs; Motta 2016). According to the shape and strength of the noise component in the PDS and the root mean square (rms) amplitude and phase lags of the QPOs, LFQPOs are classified as type-A, -B, or -C QPOs (Wijnands, Homan & van der Klis 1999; Remillard et al. 2002; Casella, Belloni & Stella 2005). Type-C QPOs are the most common and strongest QPOs in BHTs and are generally observed in the LHS and HIMS. The rms amplitude of type-C QPOs can reach up to 20 per cent, with a high-quality factor, $Q \ge 10$ ($Q = \nu$ /FWHM, where ν and FWHM are the centroid frequency and the full width at half-maximum of the QPO, respectively). Type-C QPOs usually show subharmonics, second, and sometimes third harmonics, and are accompanied by a strong broad-band noise component in the PDS.

The models proposed to explain the type-C QPOs are roughly divided into two categories. One class of models explains the type-C QPO as either some sort of instability in the accretion flow, e.g. an accretion-ejection instability in a magnetized disc (Tagger & Pellat 1999), oscillations in a transition layer in the accretion flow (Titarchuk & Fiorito 2004), or corona oscillations caused by magnetoacoustic waves (Cabanac et al. 2010). The other class of models explains the QPO as a geometric effect under general relativity. The most popular of this class of models is the Lense–Thirring (LT) model proposed by Stella & Vietri (1998). In particular, Ingram, Done &

Fragile (2009, see also You, Bursa & Życki 2018) developed the LT model considering a precessing accretion flow inside a truncated accretion disc to explain the evolution of the spectral parameters of the source as a function of the type-C QPO cycle (Ingram et al. 2016).

Type-B QPOs are weaker than type-C QPOs and appear in the SIMS (in fact, the appearance of type-B QPOs is one of the characteristics that defines the start of the SIMS). These QPOs have rms amplitudes of ~4 per cent, $Q \ge 6$, and are accompanied by a weak low-frequency noise component. One of the explanations for type-B QPOs is that they originate from the jet (e.g. Soleri, Belloni & Casella 2008; Stevens & Uttley 2016; de Ruiter et al. 2019; Liu et al. 2022a). Type-A QPOs are the weakest LFQPOs, they appear in the HSS and are rarely detected (Motta 2016).

Transitions between different types of QPOs have been reported in several BHTs. QPO transitions in GX 339-4 in four outbursts were systematically studied by Motta et al. (2011), who suggested that type-C and type-A OPOs have different origins than type-B OPOs. The transition from type-B to type-A QPOs in XTE J1550-564 is associated with an increase in the count rate and discrete ejections in the radio jet (Homan et al. 2001; Sriram, Rao & Choi 2016). However, the same type-B to type-A QPO transition in XTE J1817-330 is connected to a flux decrease (Sriram, Rao & Choi 2012). XTE J1859+262 shows a variety of changes in the parameters of the accretion disc during the type-B to type-A QPOs transition (Sriram, Rao & Choi 2013), whereas the transition from type-C to type-A and type-B QPOs in this source appears to be related to relativistic ejection episodes (Casella et al. 2004). Liu et al. (2022a) reported that the transition between type-B and type-C QPOs in MAXI J1348-630 is associated with an increase of the Comptonized flux, the hardening of the energy spectrum, and a significant change of the inner radius of the accretion disc. Soleri et al. (2008) reported the transition between type-C and type-B QPOs in GRS 1915+105 and proposed that the type-B QPOs are related to discrete jet ejections in the SIMS. Recently, Homan et al. (2020) reported the transition from type-C to type-B QPOs in MAXI J1820+070 and provided strong evidence that the appearance of type-B QPOs is related to discrete jet ejections.

Phase lags give extra information about the X-ray variability in BHTs. The phase lags of the variability are measured using the Fourier cross-spectrum computed from light curves in two different energy bands (Miyamoto & Kitamoto 1989; Cui et al. 1997; Nowak et al. 1999). There are a variety of mechanisms proposed to explain the phase lags. For example, hard lags, in which high-energy photons are delayed with respect to the low-energy ones, could originate from the Comptonization of soft disc photons in the corona (Payne 1980; Kazanas, Hua & Titarchuk 1997). Alternatively, accretion rate fluctuations in the accretion disc that propagate inward could also explain the observed hard phase lags (Lyubarskii 1997; Kotov, Churazov & Gilfanov 2001). Soft phase lags, on the other hand, could be produced when hard photons from the corona irradiate the accretion disc and are reprocessed and re-emitted at a later time than the corona photons that go directly to the observer (e.g. Uttley et al. 2014; Ingram & Motta 2019).

1.2 Geometry of the corona from the energy-dependent variability

The geometry of the accretion flow near the black hole in these systems remains a topic of debate, and several accretion disc–corona coupling models have been proposed (e.g. Reig, Kylafis & Giannios 2003; Ingram et al. 2009; Kylafis & Reig 2018; Marcel et al. 2018; Zdziarski et al. 2021; Kawamura et al. 2022; Mastichiadis, Petropoulou & Kylafis 2022).

Recently, Karpouzas et al. (2020) and Bellavita et al. (2022) developed a time-dependent Comptonization model that addresses this coupling. These models are based on the ideas originally proposed by Lee & Miller (1998), Lee, Misra & Taam (2001) and Kumar & Misra (2014). In this model, the OPO arises from the coupled oscillation between the corona and the disc that leads to the oscillation of the physical parameters that describe the spectrum of the system: the temperature of the corona, $kT_{\rm e}$, the temperature of the seed photons from the (disc) blackbody, kT_s , and the external heating rate that keeps the corona in thermal equilibrium, \dot{H}_{ext} . In addition, these models give the corona size, L, and the feedback fraction, $0 \leq$ $\eta < 1$, which is defined as the fraction of the flux of the disc due to feedback from the corona. The feedback fraction, η , is related to the fraction of the flux of corona photons that return to the disc, η_{int} (intrinsic feedback fraction; see Karpouzas et al. 2020). Based on the above parameters, we can obtain information on the geometry of the corona. This model is generically called vkompth,² and has been applied to the QPOs in a number of X-ray binaries to place constraints on the corona geometry of these systems. For example, the model was applied successfully to the kilohertz (kHz) OPOs in the neutron star system 4U 1636-53 (Karpouzas et al. 2020), the type-B QPO in the black hole system MAXI J1348-630 (García et al. 2021; Bellavita et al. 2022), GX 339-4 (Peirano et al. 2023), MAXI J1535-571 (Zhang et al. 2023), and the type-C QPOs in GRS 1915+105 (Karpouzas et al. 2021: García et al. 2022: Méndez et al. 2022), and MAXI J1535-571 (Zhang et al. 2022; Rawat et al. 2023). Here, we apply this time-dependent Comptonization model to the type-C and type-B QPOs in the black hole system MAXI J1820+070 in the observation presented in Homan et al. (2020).

1.3 MAXI J1820+070

MAXI J1820+070 is a BHT (Tucker et al. 2018) that exhibited a rich variety of spectral and timing properties during its 2018 outburst. MAXI J1820+070 was discovered with the All-Sky Automated Survey for SuperNovae (ASAS-SN; Shappee et al. 2014; Kochanek et al. 2017) as the optical transient ASASSN-18ey on 2018 March 6 (MJD 58183; Denisenko 2018; Tucker et al. 2018). Around 5 d later, this source was observed in the X-ray band with the Monitor of All-sky X-ray Image Gas Slit Camera (MAXI/GSC; Matsuoka et al. 2009) on 2018 March 11 (MJD 58188; Kawamuro et al. 2018). The position of the source is RA $(J2000) = 18^{h}20^{m}21^{s}94$ and Dec. $(J2000) = +07^{\circ}11'07''.19$ (Gandhi et al. 2019). MAXI J1820+070 is a dynamically confirmed BH with a mass of $8.48^{+0.79}_{-0.72}\,M_{\odot}$ and an inclination of $63^{\circ} \pm 0.3^{\circ}$ (Torres et al. 2020) at a distance of 2.96 ± 0.33 kpc (Atri et al. 2020). The source was observed at several wavelength bands, such as radio (e.g. Atri et al. 2020; Homan et al. 2020; Wood et al. 2021), near-infrared (e.g. Özbey Arabacı et al. 2022; Yoshitake et al. 2022), optical (e.g. Paice et al. 2021; Thomas et al. 2022), ultraviolet (e.g. Kajava et al. 2019; Özbey Arabacı et al. 2022), and X-ray (e.g. Buisson et al. 2019; Kara et al. 2019; Bright et al. 2020; Wang et al. 2020; Ma et al. 2021; You et al. 2021). After being in the hard state for about 110 d, MAXI J1820+070 transitioned to the intermediate state from MJD 58303.5 to MJD 58310.7 (Shidatsu et al. 2019). During this period, there was

²The VKOMPTH model is publicly available at https://github.com/candebellav ita/vkompth.

a switch from type-C to type-B QPOs, accompanied by a flare in the 7–12 keV band (Homan et al. 2020) and a radio flare associated with a superluminal ejection (Bright et al. 2020). The reports of Homan et al. (2020) and Wood et al. (2021) suggest that the ejection is most likely linked to the QPO transition.

In this paper, we use the time-dependent Comptonization model vkcmpth to explore the evolution of the coronal geometry of MAXI J1820+070 during the transition from type-C to type-B QPO. The paper is structured as follows: We describe the observations and data reduction in Section 2, where we also describe the model and parameters used to fit the time-averaged spectra of the source and the rms and phase-lag spectra of the QPOs. We present the results of the joint fitting of all these spectra for the intervals with type-C and type-B QPOs as a function of time and frequency in Section 3. In Section 4, we discuss the corona geometry during the QPO transition. Finally, we summarize our conclusions in Section 5.

2 OBSERVATION AND DATA ANALYSIS

The *Neutron Star Interior Composition Explorer (NICER;* Gendreau et al. 2016) is an X-ray telescope onboard the *International Space Station (ISS)*. The primary scientific instrument of *NICER* is the X-ray Timing Instrument (XTI), consisting of 56 X-ray concentrator optics (XRC), covering the 0.2–12 keV energy range with ~100 ns time resolution. *NICER* observed the outburst of MAXI J1820+070 from 2018 March 6 (MJD 58183) to 2018 November 21 (MJD 58443).

We process the observations with the *NICER* data analysis software (NICERDAS) version 2021-09-01_V008c, using the CALDB version xti20210707. We reprocess the data using *nicerl2* with the standard filtering criteria (see e.g. Wang et al. 2021) and estimate the background using *nibackgen3C50* and the 3C50 model (Remillard et al. 2022).

This work focuses on ObsID 1200120197, made on MJD 58305, since this observation covers the transition from type-C to type-B QPOs. To study the source properties during the QPO transition, we split this observation into a total of 15 segments that correspond, more or less, to *NICER* orbits. From now on we call these segments orbits. We discard the last two orbits because there is no significant QPO signal while the first 10 orbits show type-C QPOs and the remaining three orbits show type-B QPOs (see Homan et al. 2020 for the QPO identification). The transition time of type-C to type-B QPOs happens on ~MJD 58305.66 (see also Homan et al. 2020).

2.1 Light curve and hardness intensity diagram

To have a global view of the 2018 outburst of MAXI J1820+070, we process the ObsIDs 1200120101-1200120312, in total 134 observations (MJD 58190-58443). We compute the background-subtracted light curve of the source in the 0.5-10 keV energy band for each ObsID separately. We also produce the HID with the hardness ratio (HR) defined as the ratio of count rates in the 2.0-10.0 keV band to that in the 0.5-2.0 keV band.

2.2 Time-averaged spectra

We extract the source and background spectra using *nibackgen3C50*, and generate ARF and RMF files using *nicerarf* and *nicerrmf*, respectively. We group the time-averaged spectra such that there are a minimum of 25 counts per bin and we oversample the intrinsic resolution of the instrument by a factor of 3.

¹The intrinsic feedback fraction is defined as the ratio of the flux of the corona that illuminates the disc to the total corona flux.

We fit the time-averaged spectra with XSPEC v12.12.1 (Arnaud 1996), using the 0.5–10 keV band data adding a 1 per cent systematic error to the data below 3 keV to account for calibration uncertainties.³ First, we jointly fit the time-averaged spectra of all 13 orbits with the model TBfeo*(diskbb + nthComp) in XSPEC. TBfeo represents the neutral absorption from the interstellar medium in the direction of the source with the abundance and cross-section tables from Wilms, Allen & McCray (2000) and Verner et al. (1996), respectively. In the component TBfeo, the parameter $N_{\rm H}$ describes the hydrogen column density along the line of sight to the source. This model component also allows to fit the abundance of Fe and O in the absorber. We fixed these abundances to solar in our fits. We use the component diskbb (Mitsuda et al. 1984; Makishima et al. 1986) to model the optically thick and geometrically thin disc (Shakura & Sunyaev 1973). This component has two parameters: the inner disc temperature, kT_{in} , and a normalization. We use the component nthComp (Zdziarski, Johnson & Magdziarz 1996; Życki, Done & Smith 1999) to model the thermal Comptonization component, with the following parameters: the photon index, Γ , the corona temperature, $kT_{\rm e}$, the seed photon temperature, $kT_{\rm bb}$, and a normalization. In our fitting, we link kT_{in} in diskbb with kT_{bb} in nthComp since we assume that the seed photons originate from the disc.

The fit with this model shows significant residuals at 6-7 keV, likely due to the reflection component (see also. Wang et al. 2021). Therefore, we add the relativistic reflection component, $relxillCp^4$ (Dauser et al. 2014), to the model.⁵ We note that the seed photons in relxillCp correspond to the Comptonized nthComp spectrum of a disc-blackbody source with a fixed temperature of $kT_{\rm in} = 0.05 \,\rm keV$, which in the X-ray band is essentially identical to a power law with a high-energy cut-off. This spectrum is very different from the Comptonized spectrum of low-mass X-ray binaries (LMXBs), with typical disc-blackbody temperatures $kT_{\rm in} \sim 0.5-2$ keV. This choice introduces a bias in the spectral modelling, which manifests as a soft excess at energies $\leq 2 \text{ keV}$ that becomes more evident in low-energy NICER data when the absorption column is low, as in MAXI J1820+070 ($N_{\rm H}$ $\approx 0.04 \times 10^{22} \,\mathrm{cm}^{-2}$, see Section 3.2). As a first-order attempt to correct for this soft-excess introduced by relxillCp, we renormalize this component by the ratio between an nthComp model evaluated at $kT_{in} = kT_{diskbb}$ and the nthComp at 0.05 keV, using the so-called nthratio⁶ model. We note that nthratio adds no extra parameters because all its parameters are linked to the corresponding parameters of nthComp. Considering the calibration uncertainties of the data around 0.5 keV, we also add an extra Gaussian absorption component, gabs, to the model, which is now TBfeo*(diskbb+nthratio*relxillCp + nthComp) *gabs. We link kT_e and Γ in relxillCp with the corresponding parameters kT_e and Γ in nthComp. We also fix kT_e and the BH spin,

³https://heasarc.gsfc.nasa.gov/docs/nicer/analysis_threads/plot-ratio/ ⁴http://www.sternwarte.uni-erlangen.de/~dauser/research/relxill/

⁵In this paper, we use relxill version 1.4.3 because the latest version, v2.3, assumes a factor of five lower temperature of the seed photon source than this one; as we explain in this, this difference has an impact on the low-energy part of the spectrum. In Appendix A, we discuss the differences in the fits using the latest version of relxill.

⁶The NTHRATIO model applies an empirical correction to relxillCp to account for the fact that the relxillCp tables have been computed for a fixed seed photon temperature of 0.05 keV, whereas in galactic BHBs the temperatures are ~10 times higher than that. The model is publicly available at https://github.com/garciafederico/nthratio.

 a_* , at 40 keV and 0.998, respectively, consistent with the values given by Wang et al. (2021). We also link the inclination, *i*, and iron abundance, $A_{\rm Fe}$, in all 13 orbits during the joint fit. As before, we also link the hydrogen column density, $N_{\rm H}$, of the 13 orbits. To get only the reflected emission of relxillCp, we fix the reflection fraction to -1. We set the disc inner radius, $R_{\rm in}$, at the ISCO, link the emissivity indices of the relxillCp, $\alpha 1$, and $\alpha 2$, to be the same, and we let the ionization parameter, ξ , and the normalization of the relxillCp component fit freely.

2.3 Power spectra

We use GHATS⁷ to generate PDS in the full energy band (0.5-12 keV). We set the length of the segment and time resolution of each Fast Fourier Transformation (FFT) to, respectively, 16 s and 0.25 ms, such that the corresponding lowest and Nyquist frequency of each FFT is 0.06 and 2000 Hz, respectively. We average the PDS of all segments to obtain a PDS per orbit. We subtract the Poisson level using the averaged power in the frequency range of >100 Hz, and apply a logarithmic rebin in frequency such that the size of each bin is a factor exp(1/100) larger than that of the previous bin. We finally normalize the PDS to units of rms² per Hz (Belloni & Hasinger 1990) without considering the background count rate because it is negligible compared to the count rate of the source.

We fit the PDS with a combination of Lorentzians (Nowak 2000; Belloni, Psaltis & van der Klis 2002) in the frequency range 0.06– 30 Hz using XSPEC v12.12.1. For orbits with type-C QPOs, the model consists of three Lorentzians for the QPO, high- and low-frequency noise/subharmonic of the QPO, respectively, plus an extra Lorentzian for the second harmonic of the QPO. For orbits with type-B QPOs, we fit three Lorentzians for the QPO fundamental and high- and low-frequency noise components.

To obtain the rms spectra of the source, we compute FFTs in eight separate sub-bands: 0.5-0.75, 0.75-1.0, 1.0-1.5, 1.5-2.5, 2.5-4.0, 4.0-5.0, 5.0-6.5, and 6.5-12.0 keV using the same length of the FFT and Nyquist frequency as for the full-band PDS. We normalized the PDS in each band to rms² per Hz and fitted them with the same multi-Lorentzian model we used to fit the full-band PDS. We checked that the centroid frequency and FWHM of all the Lorentzian are consistent with being energy-independent, therefore we take the bestfitting value of these parameters from the full energy band and fix them for the fits to the PDS of the eight sub-bands, letting only the normalization free during the fit. Finally, we calculate the square root of the normalization of the best-fitting Lorentzianes to compute the fractional rms amplitude and obtain the energy-dependent rms spectra of the QPOs. We also compute the 1σ confidence error of the rms amplitude.

2.4 Cross-spectra

We compute the Fourier cross-spectra of each orbit to calculate the phase lags of the QPO in different energy bands. To do this we use the same time resolution and segment length as for the PDS. The energy bands selected are the same as for the rms spectra, and we use the full energy band (0.5–12 keV) as the reference band. We also compute cross-spectra and phase lags of the QPO in two broad energy bands, the reference and subject bands being 0.5–2.0 and

⁷GHATS is accessible at http://www.brera.inaf.it/utenti/belloni/GHATS_Pac kage/Home.html.

2.0–12.0 keV, respectively. For the fits of the cross-spectra in the subbands, we take the parameters of the best-fitting model of the PDS in the full energy band as the baseline, fixing the centroid frequency and FWHM of each Lorentzian, and letting only the normalization free when we fit jointly the real and imaginary parts of the cross-spectra. We added a constant to the model of the real part of the crossspectrum to account for the correlation introduced by the fact that the photons in the subject bands are also in the reference band. The phase lags of the QPO are therefore $\Delta \phi = \arctan(\frac{N_{\rm Im}}{N_{\rm Re}})$, where $N_{\rm Im}$ and $N_{\rm Re}$ are the normalizations of the QPO Lorentzian component in the imaginary and real part of the cross-spectrum, respectively (see Peirano & Méndez 2022; Alabarta et al. 2022, for more details). As with the rms amplitude, the uncertainties of the phase lag correspond to the 68 per cent confidence range.

2.5 Joint fitting of the time-averaged, rms, and phase-lag spectra

Finally, to infer the properties of the corona, we fit the time-averaged spectra of the source plus the rms spectra and phase-lag spectra of the QPOs simultaneously. We need to mention here that, ideally, we should jointly fit the 39 spectra (i.e. 13 time-averaged, 13 rms, and 13 phase-lag spectra) of the orbits with QPOs. However, since there are too many data sets, such joint fitting is very complex and time-consuming. We therefore choose to fit, for each orbit, jointly the time-averaged spectra of the source and the rms and lag spectra of the QPOs, fixing $N_{\rm H}$ and the source inclination and iron abundance in relxillCp to the values we obtained from the simultaneous fit to the 13 time-averaged spectra (see Section 2.2). Other parameters in the components diskbb, relxillCp, and nthComp are free to vary (see also Zhang et al. 2022), except that $kT_{\rm e}$ is fixed at 40 keV.

Before we explain the details of the joint fitting, we give a description of the time-dependent Comptonization model vkompth and its parameters. The steady-state version of the vkompth model is the same as the thermal Comptonized model nthComp, whereas the model has extra parameters that only affect the time-dependent version of the model. There are two versions of the vkompth model, for one or two coronae. For the model of one corona, called vkompthdk or vkompthbb depending on whether the seed photon source is, respectively, a disc or a blackbody, the model parameters are the electron temperature, $kT_{\rm e}$, the seed photons temperature, $kT_{\rm s}$, the photon index, Γ , the corona size, L, the feedback fraction, η , the amplitude of the variability of the external heating rate, $\delta \dot{H}_{ext}$, the size of the seed photon source, a_f , and the reference lag, *reflag*. The model for two different, but physically connected, coronae are called vkdualdk and vkdualbb (García et al. 2021; Bellavita et al. 2022). For the *dual* corona models, there are two sets of parameters $kT_{s,1}/kT_{s,2}, kT_{e,1}/kT_{e,2}, \Gamma_1/\Gamma_2, L_1/L_2, \eta_1/\eta_2$, and $\delta \dot{H}_{ext,1}/\delta \dot{H}_{ext,2}$ to describe the physical properties of the *small(1)* and *large(2)* coronae, respectively. The remaining parameters of the *dual* models are the size of the seed photon source and the reference lag, plus an additional parameter, ϕ , that describes the phase difference between the two coronae (see García et al. 2021, for more details).

First, we perform a joint fit using the model for one corona and seed photons from a disc, vkompthdk. Although the model generally reproduces the data, the fits give relatively large χ^2 , with the largest residuals coming from the rms and lag spectra. We therefore replace vkompthdk by vkdualdk with two Comptonized regions. The reduced chi-square decreases from 288.69 for 234 degrees of freedom (dof) for one corona to 230.89 for 230 dof for two coronae for a typical data set. We note that the χ^2 and dof are dominated by the time-averaged spectrum since this one has the largest number of energy channels. The improvement in the χ^2 when going from a model with one to a model with two coronae happens in the fits to the rms and lag spectra of the QPOs. For instance, in the example mentioned above the χ^2 of the fit to the rms and lag spectra of the QPO goes, respectively, from 33.18 to 20.87 and from 51.41 to 6.49 for eight channels, showing that a model with two coronae improves the fit significantly compared to that with only one corona.

We therefore fit together the time-averaged spectra of the source and the rms and lag spectra of the QPO of all orbits as follows: (i) We use the model described in Section 2.2 to fit the time-averaged spectra of the source, with the parameters setting being the same as in Section 2.2. (ii) We fit the rms spectra of the QPO with the model vkdualdk*dilution, where the component dilution is the ratio of the energy-dependent flux density of the Comptonized component to the flux density of the total continuum and is a factor that accounts for the decrease of the observed rms amplitude compared to the amplitude of the corona given by the model due to the emission of the non-variable components in the energy spectrum of the source (see Bellavita et al. 2022). The dilution component is necessary because we assume that the QPO originates from the corona, and the other components (such as diskbb and relxillCp) do not contribute, or at least not at the QPO frequency, to the variability. We link the parameters $kT_{s,1}$, $kT_{e,1} = kT_{e,2}$, and $\Gamma_1 = \Gamma_2$ in vkdualdk to the corresponding parameters kT_{in} , kT_e , and Γ in the diskbb and nthComp components that fit the time-averaged spectra, and we let the parameters $kT_{s,2}$, L_1 , L_2 , η_1 , η_2 , $\delta \dot{H}_{ext,1}$, $\delta \dot{H}_{ext,2}$, ϕ , and reflag free during the fit. We link all the parameters of the dilution component to the corresponding parameters of the model of the timeaveraged spectrum. We note that the vkompth model is not sensitive to the size of the seed photon emitting region, a_f , therefore we fix a_f to 250 km in our work (see García et al. 2022, for more details). (iii) For the phase-lag spectra of the QPO, the model is similar to the model for the rms spectra but without the dilution component, i.e. the fitting model is vkdualdk. The parameters of the vkdualdk model for the phase-lag spectra are all linked to the same parameters for the model of the rms spectra.

3 RESULTS

3.1 Light curve and HID

We present the 0.5-10 keV NICER light curve of MAXI J1820+070 during the 2018 outburst with one point per obsID in the left-hand panel of Fig. 1. At the beginning of the outburst, the count rate increases rapidly from \sim 760 cts s⁻¹ on MJD 58 196 to \sim 16 600 cts s⁻¹ on MJD 58205. The count rate then remains more or less constant except for a small excursion down and up between MJD 58264–58304 that reaches a count rate as low as \sim 4700 cts s⁻¹. From MJD 58304-58311, the source is in the intermediate state, and then stays in the soft state until MJD 58 380 (e.g. Shidatsu et al. 2019). After MJD 58381, the count rate drops rapidly from \sim 17 000 to \sim 5 cts s⁻¹ on MJD 58443, and after that, the source is almost undetectable. The observation on MJD 58 305 that we use in our work is marked in red. In that observation, the source is in the intermediate state, with the QPO transitioning from type-C to type-B (Homan et al. 2020). The inset in the left-hand panel of Fig. 1 shows the light curve of this observation with a time resolution of 10 s.

We also display the HID of the source in the right-hand panel of Fig. 1. The trace of the HID shows a typical 'q' shape seen in most BHTs (e.g. Fender et al. 2004; Belloni & Motta 2016). In the early



Figure 1. *NICER* light curve (left-hand panel) and HID (right-hand panel) of MAXI J1820+070 during the 2018 outburst. In both panels, the intensity is the background-subtracted count rate in the 0.5–10 keV band, while the HR in the right-hand panel is the ratio of the count rate in the 2–10 keV band to that in the 0.5–2 keV band. Each point corresponds to one *NICER* ObsID. The observation used in our work is marked in red. In the left-hand panel, the inset shows the background-subtracted light curve (0.5–10 keV) of the observation used in this paper, with a time resolution of 10 s.

stage of the outburst, the count rate of MAXI J1820+070 increases rapidly as the HR decreases from 0.3 to 0.2, and the source moves rapidly from the right branch of the HID to the upper branch. In the upper branch, the HR continues decreasing to 0.09 while the count rate remains more or less constant. The count rate then decreases rapidly, with an increase of the HR to 0.26, indicating that the source reaches the end of the outburst. The observation used in this work is marked in red in this panel.

3.2 Time-averaged spectra results

We fit the time-averaged spectra of the 13 orbits simultaneously. As described in Section 2.2, we link hydrogen column density, $N_{\rm H}$, inclination angle, *i*, and iron abundance, $A_{\rm Fe}$, to be the same for the 13 orbits. Our fitting results give a relatively low $N_{\rm H} = 4.17^{+0.25}_{-0.15} \times 10^{20} \,{\rm cm}^{-2}$, consistent with $N_{\rm H} \sim 5 \times 10^{20} \,{\rm cm}^{-2}$ given by Fabian et al. (2020). The inclination angle $i = 66.9^{\circ +0.2}_{-1.0}$ is consistent with previous reports of the orbital inclination ($66^{\circ} < i < 89^{\circ}$, Torres et al. 2020) and the jet angle ($i = 63 \pm 3^{\circ}$, Atri et al. 2020; $i = 64 \pm 5^{\circ}$, Wood et al. 2021). The chi-square of the joint fitting is 3036.7 for 2932 dof.

We display two representative 0.5-10.0 keV time-averaged spectra of an orbit with a type-C and another with a type-B QPO in Fig. 2. The evolution of the geometrical and spectral parameters will be described in Section 3.4.

3.3 Timing results

3.3.1 Rms and phase lags of the QPOs as a function of time

We present representative 0.5–12 keV PDS with the type-C and type-B QPOs in Fig. 3. There is a significant second harmonic in the case of the type-C but not for the type-B QPOs. The centroid frequency of the type-C QPOs increases gradually with time during the observation, from 4.4 to 7.7 Hz, while that of the type-B QPOs decreases gradually from 4.2 to 3.1 Hz (see Table 1). We need to mention that during the transition from type-C to type-B QPOs in orbit 09, due to the rapid decrease of the significance of the type-C QPO, the errors of the parameters are large in the data.

We show the evolution of the full-band rms amplitude of the QPOs of the 13 orbits in the 0.5-12.0 keV energy band in Fig. 4. The full-band rms amplitude of the type-C QPO gradually decreases from ~ 2 to ~ 1 per cent with time and then remains more or less constant, whereas the full-band rms amplitude of the type-B QPO is lower than that of the type-C QPO and decreases gradually from \sim 1 to \sim 0.5 per cent. As shown in the right-hand panel of Fig. 4, the full-band rms amplitude of type-C and type-B QPOs shows different correlations as a function of the centroid frequency of the OPOs. The average rms amplitude of type-B OPOs appears to be positively correlated with the QPO centroid frequency (although there are only three measurements of the type-B QPO), whereas there is an anticorrelation in the case of type-C QPOs. We note that the average rms amplitude of the last type-C OPO point is relatively small (~ 0.5 per cent), which is probably due to the weaker type-C QPO signal and the rapid change of the QPO frequency during the transition from type-C to type-B QPOs.

We present representative cross-spectra (2.0–12.0 keV with respect to 0.5–2.0 keV) of one type-C and one type-B QPOs in Fig. 5. The shape of the cross-spectra when the type-C and type-B QPOs are at the same centroid frequency is different. The real part of the crossspectrum at the QPO frequency is positive for both QPOs, but the real part of the type-C QPO is larger than that of the type-B QPO. On the other hand, the imaginary part of the cross-spectrum of the type-C QPO is small and positive, whereas for the type-B QPO it is large and negative. This indicates that in these examples, when comparing these two energy bands, the type-C QPO has a small positive phase lag whereas the type-B QPO has a relatively large negative phase lag (see Section 2.4 for details on the calculation of the phase lags).

We show the evolution of the average phase lags of the QPOs in the left-hand panel of Fig. 6. The average phase lags of both type-C and type-B QPOs gradually decrease with time, from ~0.2 to ~-0.3 rad and from ~-0.7 to ~-1.2 rad, respectively. We also show the dependence of the average phase lags on the centroid frequency of the QPO in the right-hand panel of Fig. 6. In the case of type-C QPOs, the average phase lags are anticorrelated with the QPO frequency, whereas for the type-B QPOs the average phase lags are either positively or uncorrelated with the centroid frequency. Again, for the last point of type-C QPO, the average phase lag has a small value with a large error bar due to the lower significance of the QPO.



Figure 2. Representative time-averaged spectra of MAXI J1820+070 in the 0.5-10 keV energy band with *NICER*. Left-hand panel: Time-averaged spectrum of orbit 01 with a type-C QPO. Right-hand panel: Time-averaged spectrum of orbit 10 with a type-B QPO. In both panels, the upper plot shows the data, the total model (black line), and the diskbb (dashed line), nthComp (dashed-dotted line), and relxillCp (dotted line) components, respectively, while the lower panels show the residuals of the best-fitting model.



Figure 3. Representative PDS of MAXI J1820+070 in the 0.5–12 keV energy band with *NICER*. Left-hand panel: PDS of orbit 01 with a type-C QPO. Right-hand panel: PDS of orbit 10 with a type-B QPO. In both panels, the upper plot shows the data, the total model (black line), and the individual Lorentzian components (dotted lines), while the lower panels show the residuals of the best-fitting model.

3.3.2 Rms and phase-lag spectra of the QPOs

To further explore the rms and phase-lag energy dependence of different types of QPOs, especially during the QPO transition period, we plot representative rms-energy spectra of the type-B and type-C QPOs in the left-hand panel of Fig. 7. Both for the type-C and type-B QPOs, the rms amplitude increases as the energy increases, similar to the results of several low- and high-frequency QPOs reported in other sources (e.g. Sobolewska & Życki 2006; Méndez et al. 2013, and references therein). The rms amplitude of the type-C QPOs increases monotonically with energy from 1 to 10 per cent. For the type-B QPOs, the rms amplitude remains more or less constant at ~0.5–0.7 per cent from 0.5 to ~1.5–2 keV, and then increases to a similar level, ~10 per cent, as for the type-C QPOs at the highest energy band.

We show the corresponding lag-energy spectra of the type-C and type-B QPOs in the right-hand panel of Fig. 7 using the full band as the reference band. For the type-C QPO, the phase lags decrease

from ~ -0.1 to ~ -0.4 rad as the energy increases from 0.5 to 2 keV, and the phase lags increase again to ~ -0.1 rad when the energy increases up to 12 keV. For the type-B QPO, the phase lags decrease from ~ 1.0 rad at the lowest energy band to ~ -0.4 rad as the energy increases from 0.5 to 2 keV, and then the phase lags increase again to ~ 0.1 rad as the energy increases further up to 12 keV. (Notice that, since the lags are relative quantities, not the actual value of the lags but only the shape of the lag spectrum is important.) As it is apparent from both panels of Fig. 7, the rms and lag spectra of the type-C and type-B QPO are consistent with being the same for energies above \sim 1.5–2 keV, but as the energy decreases below \sim 1.5–2 keV the rms spectrum decreases more rapidly and reaches a lower rms amplitude, whereas the lag spectrum increases more rapidly and reaches a larger phase lag value at the lowest energies for type-B than for the type-C QPOs. In fact, from this Figure, it appears that going from type-C to type-B QPOs, the only changes in the rms and lag spectra happen at energies below $\sim 1.5-2$ keV.

Orbit	Start time (MJD 58305)	Stop time (MJD 58305)	Rate ^{a} (cts s ⁻¹)	Frequency (Hz)	FWHM (Hz)	Full-band rms ^b (per cent)	Average phase lag ^c (rad)	QPO type
00	0.02704	0.04084	20800 ± 30	4.44 ± 0.07	$0.5^{+0.6}_{-0.2}$	$1.7^{+0.5}_{-0.2}$	0.17 ± 0.13	С
01	0.09140	0.09656	21040 ± 30	4.64 ± 0.05	$0.52^{+0.18}_{-0.13}$	$1.89_{-0.18}^{+0.23}$	0.07 ± 0.09	С
02	0.15593	0.16398	22060 ± 30	5.01 ± 0.05	$0.58\substack{+0.30\\-0.18}$	$1.56^{+0.19}_{-0.15}$	0.06 ± 0.11	С
03	0.22011	0.23366	22970 ± 30	5.50 ± 0.05	$0.54_{-0.12}^{+0.15}$	1.29 ± 0.11	0.12 ± 0.11	С
04	0.28464	0.31375	23500 ± 30	5.83 ± 0.05	$0.64_{-0.16}^{+0.19}$	1.08 ± 0.10	-0.09 ± 0.09	С
05	0.35088	0.37810	23940 ± 30	6.04 ± 0.06	1.0 ± 0.2	1.23 ± 0.11	-0.16 ± 0.10	С
06	0.41478	0.44108	24620 ± 30	6.56 ± 0.11	1.5 ± 0.6	$1.22_{-0.16}^{+0.20}$	-0.22 ± 0.13	С
07	0.47925	0.50079	24190 ± 30	6.34 ± 0.05	$0.49^{+0.18}_{-0.13}$	0.94 ± 0.10	-0.27 ± 0.15	С
08	0.54464	0.57048	25240 ± 30	7.2 ± 0.2	2.7 ± 0.9	1.22 ± 0.19	-0.34 ± 0.13	С
09	0.60972	0.63542	26800 ± 30	7.7 ± 0.3	$0.81^{+1.6}_{-0.6}$	$0.47\substack{+0.28\\-0.14}$	$0.8^{-1.2}_{+0.5}$	С
10	0.67056	0.69663	30220 ± 40	4.23 ± 0.04	0.61 ± 0.09	1.01 ± 0.06	-0.73 ± 0.10	В
11	0.73783	0.76422	31490 ± 40	3.98 ± 0.04	0.59 ± 0.11	0.77 ± 0.05	-0.78 ± 0.10	В
12	0.80227	0.81218	23650 ± 30	3.14 ± 0.17	$0.6^{+0.8}_{-0.2}$	$0.48^{+0.15}_{-0.12}$	-1.2 ± 0.6	В

 Table 1. Observation log and parameters of the QPOs of MAXI J1820+070. Uncertainties are given at the 90 per cent confidence level.

Note. ^aCount rate of the source in the 0.5–10.0 keV band.

^bThe rms amplitude of the QPO in the 0.5–12.0 keV band.

^cThe phase lag of the QPO between photons in the 2.0–12.0 keV band with respect to those in the 0.5–2.0 keV band.



Figure 4. Left-hand panel: Evolution of full-band (0.5–12 keV) rms amplitude of the QPO during the transition from type-C to type-B QPOs for MAXI J1820+070. The vertical dashed line represents the transition time from type-C to type-B QPO. Right-hand panel: Full-band rms amplitude of the QPO as a function of the centroid frequency of QPO. In both panels, orange and blue points represent orbits with type-C and type-B QPOs, respectively.

3.4 Joint fitting of the time-averaged spectrum of the source and the rms and phase-lag spectra of the QPOs

We show two examples of the best-fitting model and residuals of the data with type-C and type-B QPOs in Fig. 8. We give the bestfitting parameters and the corresponding contour plots for the fits of these two examples in Table 2 and Figs B1 and B2, respectively (for clarity reasons we only show the contour plots of selected parameters in these Figures, but Table 2 contains the values and errors of all the parameters). We compute the error of the parameters using MCMC, and we give the parameter value and corresponding errors for the 13 orbits in Table B1. For the MCMC simulation, we use the Goodman– Weare algorithm (Goodman & Weare 2010) with 160 walkers and a total of 160 000 samples using a Cauchy proposal distribution after we discard the first 320 000 steps of the MCMC to ensure convergence.

3.5 Evolution of the parameters

As shown in Fig. 9, for the orbits with type-C QPOs the disc temperature, $kT_{\rm in}$, increases gradually from ~0.5 to ~0.6 keV while the normalization of the diskbb component decreases gradually from 2.4 × 10⁴ to 1.5 × 10⁴. At the same time the photon index, Γ , increases from 2.4 to 2.7. Compared to the orbits of type-C QPOs, for the orbits with type-B QPOs the Comptonized component is steeper with a photon index $\Gamma \sim 2.8$, while the inner disc temperature is higher, $kT_{\rm in} \sim 0.7$ keV, with a smaller disc normalization ~1.3 × 10⁴. The value of the ionization parameter, log ξ , suddenly increases from 3.3 for observations with type-C QPOs to 3.7 in observations with type-B QPOs. Considering that $\xi = L/nR^2$, where *L* is the ionizing luminosity, *n* is the density of the disc and *R* is the distance to the ionizing source, a sudden change of this parameter implies a change in the intrinsic properties of the source during the QPO transition



Figure 5. Representative cross-spectra of the 2.0–12.0 keV band with respect to the 0.5–2.0 keV band of MAXI J1820+070. The black and red symbols and lines represent, respectively, the real and imaginary parts of the cross-spectrum. Left-hand panel: Cross-spectrum of orbit 01 with a type-C QPO. Right-hand panel: Cross-spectrum of orbit 10 with a type-B QPO. In both panels, we show the best-fitting model to the real and imaginary part of the cross-spectrum and the residuals of the best-fitting model.



Figure 6. Left-hand panel: Evolution of the QPO phase lags of the 2.0–12.0 keV band with respect to 0.5–2.0 keV band of MAXI J1820+070 during the transition from type-C to type-B QPOs. The vertical dashed line represents the transition time from type-C to type-B QPO. Right-hand panel: QPOs phase lags as a function of the centroid frequency of the QPO. Orange and blue points represent orbits with the type-C and type-B QPOs, respectively. The large error bars associated with orbit 09 (last orange point) are due to the lower significance of the type-C QPO in that segment, possibly because the transition has already started.



Figure 7. Representative rms spectra (left-hand panel) and phase-lag spectra (right-hand panel) of the type-C and type-B QPO of MAXI J1820+070. The orbits are the same as in Fig. 3.



Figure 8. First and third columns: From top to bottom, representative joint fitting of the time-averaged spectrum of the source and the rms and lag spectra of the type-C (first column) and type-B QPO (third column) of MAXI J1820+070. The second and fourth columns show the residuals of the best-fitting model. The orbits for the type-C and type-B QPOs are the same as in Fig. 3.

period. As it is apparent from the Figure, the changes in all the parameters are very significant.

We also plot in Fig. 9, the evolution of the sizes, L_1 (small corona) and L_2 (large corona), and intrinsic feedback fraction, $\eta_{\text{int}, 1}$ and $\eta_{\text{int}, 2}$, of the two coronae and the temperature of the seed photon source that illuminates each corona, $kT_{\text{s}, 1}$ (= kT_{in}) and $kT_{\text{s}, 2}$. In observations with type-C QPOs, the size of both coronae tends to increase, L_1 from ~20–60 to ~100 km and L_2 from ~10⁴ to ~10⁵ km. At the same time, the intrinsic feedback fraction of the large corona, $\eta_{\text{int}, 2} \sim 20$ –30 per cent, is always larger than that of the small corona, $\eta_{\text{int}, 1} \sim 5$ –15 per cent. Finally, the seed photon temperature of both coronae increases gradually, with $kT_{\text{s}, 2} \sim 0.3$ –0.5 keV always being lower than $kT_{\text{s}, 1} \sim 0.4$ –0.6 keV.

Compared to the observations with type-C QPOs, in the observations with type-B QPOs the size of both coronae drops abruptly and significantly, L_1 form ~100 to ~20 km and L_2 from ~10⁵ to ~10⁴ km. During the transition from type-C to type-B QPOs, the intrinsic feedback fraction of the small corona increases from 15 to 30 per cent, while that of the large corona decreases abruptly from 20–30 per cent to 0. During the transition the temperature of the seed photon source of the large corona is consistent with being constant, $kT_{s,2} \sim 0.3$ keV, whereas the temperature of the seed photon source

of the small corona, $kT_{s,1} = kT_{in}$, increases significantly from 0.65 to 0.70 keV. Here, we do not give the values of the external heating rate $\delta \dot{H}_{ext}$ as they are not very well constrained (see Tables 2 and B1). For completeness, in Fig. B3 we plot the parameters of the joint fits versus QPO frequency.

We note that while some parameters change abruptly at the time at which the type-C disappears and the type-B QPO appears (e.g. kT_{in} , log ξ , L_2 and $\eta_{int, 2}$), others evolve more or less continuously across the transition from the HIMS to the SIMS (e.g. N_{disc} and Γ). In fact, some of the parameters (e.g. log ξ and L_2) appear to be changing already in the HIMS, just before the transition. This suggests that the state transition, from the HIMS to the SIMS, is not a discontinuous process, but it starts before the QPO switches from type-C to type-B.

4 DISCUSSION

We analyse a *NICER* observation of MAXI J1820+070 during the transition from the HIMS to the SIMS. A type-C QPO with a frequency that increases from 4.4 up to 7.7 Hz in the HIMS disappears at the time of the transition to the SIMS and is replaced by a type-B QPO at 4.2 Hz that decreases to 3.1 Hz as the source evolves further. We present the first comparison of the rms and lag spectra

Table 2. Representative best-fitting spectral and corona parameters for observations with a type-C and a type-B QPOs in MAXI J1820+070. Uncertainties are given at the 90 per cent confidence level. All model parameters for all observations are given in Appendix B1.

Component	Parameter	Type-C QPO ¹	Type-B QPO ²
TBfeo	$N_{\rm H}(10^{20}{\rm cm}^{-2})$	[4.2] ^c	[4.2] ^c
diskbb	$kT_{\rm in}~({\rm keV})$	$0.478\substack{+0.007\\-0.013}$	$0.666\substack{+0.003\\-0.010}$
	$N_{\rm disk}(10^4)$	2.4 ± 0.3	$1.29\substack{+0.06 \\ -0.03}$
nthComp	Г	2.45 ± 0.03	2.80 ± 0.03
	$kT_{\rm e}~({\rm keV})$	[40] ^a	$[40]^{a}$
	NnthComp	10.2 ± 0.4	$11.7\substack{+0.8\\-0.2}$
relxillCp	α1	$2.23\substack{+0.20 \\ -0.14}$	$2.06_{-0.13}^{+0.32}$
	a_*	[0.998] ^a	[0.998] ^a
	<i>i</i> (°)	[67.3] ^a	[67.3] ^a
	$\log \xi \; (\log[\mathrm{erg}\mathrm{cm}\mathrm{s}^{-1}])$	$3.31\substack{+0.17\\-0.10}$	$3.68^{+0.09}_{-0.18}$
	A _{Fe} (solar)	[10] ^{<i>a</i>, <i>b</i>}	[10] ^{<i>a</i>, <i>b</i>}
	$N_{\rm refl}$	0.10 ± 0.03	0.19 ± 0.05
gabs	<i>lineE</i> (keV)	$0.552\substack{+0.008\\-0.021}$	$0.541\substack{+0.007\\-0.033}$
	$\sigma (10^{-2} \mathrm{keV})$	$7.8^{+2.0}_{-0.9}$	$9.9^{+0.7}_{-3.2}$
	Strength (10^{-2})	$4.9^{+1.4}_{-0.5}$	$6.9^{+2.4}_{-0.3}$
vkdualdk	$kT_{\rm s, 2}$ (keV)	$0.22\substack{+0.13 \\ -0.03}$	$0.313\substack{+0.132 \\ -0.007}$
	L_1 (km)	<74	<36
	$L_2 (10^4 \text{ km})$	$1.0^{+1.5}_{-0.5}$	1.5 ± 0.3
	η_1	$0.51\substack{+0.14 \\ -0.40}$	$0.96^{+0.03}_{-0.39}$
	η_2	$1.0^{c}_{-0.5}$	$0_d^{+0.16}$
	ϕ (rad)	$2.6^{+1.4}_{-0.4}$	$3.8^{+0.70}_{-0.14}$
	reflag	0.07 ± 0.07	$-0.31\substack{+0.02\\-0.09}$
	$\eta_{ m int,\ 1}$	0.11 ± 0.07	0.27 ± 0.07
	$\eta_{ m int,\ 2}$	0.22 ± 0.07	$0_d^{+0.01}$
	χ^2/v	246.02/230	233.46/230
	frequency (Hz)	4.64 ± 0.05	4.23 ± 0.04

Notes. ¹Orbit 01.

²Orbit 10.

^{*a*}The parameters $N_{\rm H}$, $kT_{\rm e}$, a_* , *i*, and $A_{\rm Fe}$ have been fixed during the fitting at, respectively, 4.2×10^{20} cm⁻², 40 keV (due to the energy range of the *NICER* data this parameter cannot be constrained), 0.998, 67.3°, and 10 times solar, as obtained from the joint fits of the energy spectra described in Section 3.2. ^{*b*}While in this version of rexillCp, the iron abundance pegs at the upper limit, if we use the latest version with variable disc density, the iron abundance decreases to approximately 5; the other parameters of the fit remain unchanged.

^cThe positive error of the parameter pegged at the upper limit. ^dThe negative error of the parameter pegged at the lower limit.

of the low-frequency QPO in a black hole X-ray binary during such state transition. The rms and lag spectra of the type-C QPO before, and the type-B QPO after, the transition are consistent with being the same above $\sim 1.5-2$ keV but, remarkably, differ significantly below that energy. From fits to the energy spectra of the source and the rms and lag spectra of the QPOs in each of the 13 orbits in this observation with the time-dependent Comptonization model vkompth (Karpouzas et al. 2020; Bellavita et al. 2022), we infer for the first time the physical and geometrical properties of the corona in a black hole candidate (BHC) during the transition from the type-C to type-B QPOs.

The data require two physically coupled coronae, a large one, with a size of 10^4-10^5 km, that dominates the rms and lag spectra of the QPO and a small one, with a size of $\sim 20-100$ km, that impacts on the time-averaged spectra of the source. We find that in the HIMS $\sim 5-15$ per cent of the flux of the small corona and $\sim 20-30$ per cent of the flux of the large corona return to the disc. In the HIMS, while the returning flux of the small corona increases to 20-30 per cent, that of the large corona notably drops to zero in the SIMS.

These results indicate that a larger part of the accretion disc is enshrouded by the small corona in the SIMS than in the HIMS even though the corona is smaller, suggesting that the inner disc radius extends closer to the BH in the SIMS than in the HIMS. The high fraction of returning flux of the large corona in the HIMS suggests that in this state this corona covers a big portion of the accretion disc. On the contrary, the fact that the large corona is as large in the SIMS as it was in the HIMS, but the returning flux is zero, indicates that in this state this corona does not cover the disc and therefore must extend vertically. This change in the geometry of the large corona coincides with the sudden increase of the radio emission of the source (Bright et al. 2020), providing evidence of a connection between the X-ray corona and the radio jet in MAXI J1820+070, similar to what was observed in GRS 1915+105 (Méndez et al. 2022) and MAXI J1535-571 (Zhang et al. 2022).

In the next subsections, we first discuss the rms and lag spectra of the type-C and type-B QPOs and the evolution of the corona properties. Subsequently, we examine our results in the context of models of the low-frequency QPO and discuss the corona geometry during the state transition.

4.1 The rms and lag spectra of the type-C and type-B QPOs

Both for the type-C and type-B QPOs, the rms amplitude increases with energy up to the highest energy, similar to what is observed in other BHs, e.g. GX 339–4 (Zhang et al. 2017), GRS 1915+105 (Zhang et al. 2020; Karpouzas et al. 2021), MAXI J1535+571 (Huang et al. 2018; Zhang et al. 2022, 2023), and MAXI J1348–630 (Belloni et al. 2020; Alabarta et al. 2022; Liu et al. 2022a). The large rms amplitude at energies above 10 keV (in some cases the rms amplitude of the QPO is ~12 per cent at 100–200 keV; Ma et al. 2021) implies that the variability must be produced by the corona, given that neither the disc nor the reflection component contributes significantly to the emission at those energies (e.g. Gilfanov 2010; Liu et al. 2022a).

We find that at energies above $\sim 2 \text{ keV}$, the rms spectrum of the two types of QPOs is similar, or the rms amplitude of the type-B QPO is somewhat higher than that of the type-C QPO. At energies below $\sim 1.5-2$ keV, however, the rms amplitude of the type-C QPO is larger than 1 per cent, whereas that of the type-B QPOs is as low as 0.5 per cent, and significantly lower than that of the type-C QPO (see the left-hand panel of Fig. 7). In the time-dependent Comptonization model, this is expected if one considers that Γ is smaller and the feedback fraction of the large corona, η_2 , is larger in the HIMS than in the SIMS (see Tables 2 and B1) because, if the rms amplitude and lags of the QPO are due to the variability of the Comptonized component, these trends lead to a lower variability at low energies (see figs 2 and 3 in Bellavita et al. 2022). At high energies, on the other hand, variable Comptonization predicts that the rms amplitude increases as Γ increases (see again Bellavita et al. 2022), consistent with the (slightly) higher rms amplitude of the type-B than of the type-C QPO above $\sim 2 \text{ keV}$.

As in other BHCs, the phase-lag spectra of both type-C and type-B QPOs in MAXI J1820+070 are 'U' shaped. For example, Alabarta



Figure 9. Evolution of the best-fitting geometrical and spectral parameters during the transition from type-C to type-B QPOs of MAXI J1820+070. The parameters are kT_{in} , the inner disc temperature, which is linked to the seed photon temperature of the small corona, $kT_{s, 1}$, N_{disc} , the normalization of diskbb, Γ , the photon index, log ξ , the disc ionization parameter, L_1/L_2 and $\eta_{int, 1}/\eta_{int, 2}$, respectively, the size and the intrinsic feedback fraction of the small/large corona, and $kT_{s, 2}$, the temperature of the seed photon source of the large corona. Uncertainties are at the 90 per cent confidence level for each parameter. Orange and blue points represent, respectively, orbits with the type-C and type-B QPOs. The vertical dashed line represents the transition time from type-C to type-B QPO.

et al. (2022) reported that the lags of the type-C QPO in MAXI J1348–630 decreased abruptly with energy in the range 0.5–1.0 keV and increased again as the energy increased further above that. A similar shape was reported for the phase-lag spectra of the type-C QPOs in MAXI J1535–571 (Zhang et al. 2022) and the type-B QPOs in MAXI J1348–630 (Belloni et al. 2020; García et al. 2021), and GX 339–4 (Peirano et al. 2023).

Comparing the lag spectra of the type-C and type-B QPOs in MAXI J1820+070, we find a significant difference in the phase lags at energies below $\sim 1.5-2$ keV, but almost no differences above that: The lag of the type-B QPO at the lowest energy band, 0.5 keV, with respect to the minimum lag at 2 keV is \sim 1.4 rad, whereas for the type-C QPO the lag is significantly lower, $\sim 0.2 \text{ rad}$ (see the righthand panel of Fig. 7). In the context of variable Comptonization, the lower the feedback fraction the larger the magnitude of the lags at lower energies (other parameters have a smaller impact on the lags, see figs 2 and 3 of Bellavita et al. 2022). The difference of the lag spectra of the type-C and type-B QPOs at energies below 2 keV are therefore consistent with the drop of the feedback fraction of the large corona in the fits, from $\eta_{\rm int,2} \sim 0.2$ –0.3 in the HIMS (type-C QPO) to $\eta_{int,2} = 0$ in the SIMS (type-B QPO). Moreover, De Marco et al. (2021) reported that during the state transition the thermal reverberation lags' amplitude suddenly increased as the frequency decreased; they proposed that these changes were associated with the appearance of relativistic jet ejections.

In addition, there is a marginally significant feature around 5–7 keV in the phase-lag spectra of some type-C QPOs but not in

the phase-lag spectra of the type-B QPOs (see the right-hand panel of Fig. 7), which may correspond to the Fe K α line. Zhang et al. (2017) reported a similar feature in the phase-lag spectra of the type-C QPO of GX 339–4, and speculated that it could be associated with the reflection component. We note that, given the quality of the current data, there are no significant residuals in the lags in the range 5–7 keV when we fit them with the time-resolved Comptonization model.

4.2 Coronae properties

From the values of Γ and kT_e , we can compute the optical depth of the two coronae (Zdziarski et al. 1996):

$$\tau = \sqrt{\frac{9}{4} + \frac{3m_{\rm e}c^2}{kT_{\rm e}\left(\Gamma - 1\right)\left(\Gamma + 2\right)}} - \frac{3}{2}.$$
(1)

Since we linked $\Gamma_1 = \Gamma_2$ and $kT_{e,1} = kT_{e,2}$ during the fits, both coronae will have the same optical depth. In the transition from type-C to type-B QPOs, Γ increases from 2.4 to 2.9, which corresponds to a decrease of τ from 1.4 to 1.0. Since kT_e is fixed at 40 keV in our fits because there is no cut-off in the spectrum within *NICER*'s passband, the values of τ are likely upper limits.

As the source transitions from HIMS to SIMS, the Compton parameter, $y = (4kT_e/m_ec^2)\max(\tau, \tau^2)$ (Zel'dovich & Shakura 1969; Shapiro, Lightman & Eardley 1976), decreases from ~0.6 to ~0.3. These values indicate that the Comptonization spectrum is in the



Figure 10. Top panel: From left to right, unabsorbed flux of the, diskbb, nthComp, and relxillCp components in MAXI J1820+070 in the 0.5-10 keV band. Bottom panel: The ratio of the flux of each component to the total flux.

unsaturated regime, which is consistent with the assumptions of the time-dependent Comptonization model.

The total flux of the source as well as the fluxes of the disc and Comptonization components increase during the HIMS to SIMS, whereas the flux of the reflection component remains constant in the HIMS and decreases slightly during the transition (see Fig. 10). Furthermore, the ionization parameter increases accompanied by a softening of the time-averaged spectrum (see also, Basak et al. 2017; Steiner et al. 2017). These changes may be associated with changes in the geometry of the corona.

Fig. 9 (see also B3) shows the evolution of all parameters as the source transitions from the HIMS to the SIMS. For the small corona both the size and the feedback fraction are more or less constant in the HIMS; in the SIMS the feedback fraction appears to increase, while we only find upper limits to the size of the corona. For the large corona, in the HIMS the size and intrinsic feedback fraction increase with time, whereas in the SIMS, while the size is consistent with being constant at similar values as those in the HIMS at the start of the observation, the intrinsic feedback fraction is zero.

Any description of the evolution of the corona in this observation of MAXI J1820+070 needs to explain the fact that, while the size of the large corona is more or less the same at the start of the HIMS and in the SIMS, the feedback fraction is very different in the two states.

It is easy to imagine that a large fraction of the corona photons will impinge on to the disc, as it happens in the HIMS where the feedback is \sim 20 per cent, if the disc is enshrouded by the corona. On the contrary, it is very difficult to explain how in the SIMS a more or less equally large corona as in the HIMS would extend over the disc surface and yet give zero feedback. Considering the relatively small intrinsic feedback of such a large corona, especially in the SIMS,

it is likely that the assumption of spherical symmetry of the corona in the vkompth model does not apply, and the best-fitting values should be taken as characteristic corona sizes rather than as the actual radius of a spherical corona. The size of the large corona and very low feedback suggest that in the SIMS this corona extends vertically.

Similar situations have also been reported in other sources. For instance, for the type-C QPO in GRS 1915+105, Karpouzas et al. (2021), Méndez et al. (2022), and García et al. (2022) found that the size of the corona decreased from $\sim 10^3$ to $\sim 10^2$ km with a large feedback fraction when the QPO frequency decreased from ~ 6 to \sim 2 Hz, while the corona size increased again to \sim 2 \times 10⁴ km, but this time with zero feedback, when the OPO frequency decreased further from \sim 2 to \sim 0.5 Hz. Méndez et al. (2022) interpreted these results as a change of the geometry of the corona, from a toruslike corona covering a large fraction of the accretion disc when the QPO frequency was larger than ~ 2 Hz, to a vertically extended, jetlike, corona when the QPO frequency was below ~ 2 Hz. Similar interpretations of the geometry of the corona based on the type-B QPO in MAXI J1348-630 and the type-C QPOs in MAXI J1535+571 were given by García et al. (2021) and Zhang et al. (2022), respectively.

4.3 Other models of the low frequency QPOs

4.3.1 Models of the type-C QPO

Ingram et al. (2009) proposed that the type-C QPOs originate from the LT precession of a hot inner flow, located inside the truncated accretion disc, that periodically illuminates the (steady) accretion disc during the QPO phase. Ingram et al. (2016) reported that Γ and the centroid energy of the iron line were modulated during the QPO cycle ($\gtrsim 3\sigma$ confidence) in the BHB H1743–322, while Nathan et al. (2022) reported that Γ and the reflection fraction were modulated during the QPO cycle ($\succeq 3\sigma$ confidence) in the BHB GRS 1915+105. We note that the modulation of Γ is also expected in the case of time-dependent Comptonization as a result of oscillations of the disc and corona temperatures even if, as in the case of the vkompth model (Karpouzas et al. 2020; Bellavita et al. 2022), no explicit oscillations of Γ are included. While LT precession can in principle account for the dependence of the rms amplitude (Motta et al. 2015) and the phase/time lags (van den Eijnden et al. 2017) of the QPO upon the source inclination, recent results appear to challenge the LT idea at least in its current form. Specifically, Nathan et al. (2022) applied this model to the type-C QPO in GRS 1915+105 observed with NuSTAR and XMM-Netwon, and found that the model yields an uncomfortably small inner disc radius, R_{in} $\sim 1.4 R_{g}$, and a problematically long thermalization time-scale, t_{th} \sim 70 ms. They argue that such a long thermalization time-scale could be an artefact of some simplifications of the model, e.g. a possible radial dependence of the thermalization time-scale or the ionization parameter. According to Nathan et al. (2022), other effects that could lead to these results are the possible shadowing of the illumination profile, or that the model ignores the light crossing delay in the disc illumination profile, which could affect the disc temperature profile. Recently, Salvesen (2022) modelled thermalization as a random walk of photons in an α -disc, and found that for most of the disc $t_{th} < 1$ ms, much smaller than the values reported by Nathan et al. (2022).

Mass accretion rate fluctuations excited in each ring of the accretion disc and propagating towards the BH have been proposed as an explanation of the lags of the broad-band noise component in the PDS of these systems (Lyubarskii 1997; Kotov et al. 2001; Arévalo & Uttley 2006). This mechanism also explains the rms-flux relation in BHBs (e.g. Uttley & McHardy 2001; Uttley, McHardy & Vaughan 2005). Ingram & van der Klis (2013) combined the propagating mass accretion rate fluctuations and the LT precession of the inner flow and applied this idea to reproduce the power and lag spectra of the BHB XTE J1550-564. A recent study of MAXI J1820+070 shows that propagation of mass accretion rate fluctuation can explain the broad-band noise and the hard lags observed in this source but not the soft lags (Kawamura et al. 2022). On the other hand, Rapisarda, Ingram & van der Klis (2017) showed that this model fails to reproduce the power and cross-spectra of the BHC XTE J1550-564, and concluded that these discrepancies are generic to the propagating fluctuations paradigm.

A model with two accretion flows, a standard accretion disc (SAD) in the outer parts and a jet-emitting disc (JED) in the inner parts (SAD–JED) was proposed by Ferreira (1997), and further developed by Marcel et al. (2018). In this model, the type-C QPOs are related to the transition radius between the SAD and the JED (Marcel et al. 2020). In the SAD–JED model, the variability is due to the propagation of mass accretion rate fluctuation and therefore has the same issues explaining the soft lags.

Recently, Mastichiadis et al. (2022) proposed that the type-C QPOs in the BHXRB could arise from the coupling of the Comptonizing corona and the accretion disc. They suggested that, under certain circumstances, this coupled system would oscillate at a characteristic frequency that depends upon the fraction of the corona photons that return to the disc, the mass accretion rate, the size of the corona, and the black hole mass. They found that for typical values of these parameters this characteristic frequency matches the range of frequencies of the type-C QPO in these systems. The essence of the proposal of Mastichiadis et al. (2022) is the same as that of vkompth, the time-dependent Comptonization model of Karpouzas et al. (2020); while Mastichiadis et al. (2022) consider the disccorona coupling to explain the frequency of the QPO, the vkompth model uses the same coupling to explain the rms and phase-lag spectra of the QPO. The QPO frequency predicted by Mastichiadis et al. (2022) is

$$f_{0} \simeq 5 \operatorname{Hz} \left(\frac{\eta_{\text{int}}}{0.2}\right)^{1/2} \left(\frac{\dot{m}}{10^{-3}}\right)^{1/2} \left(\frac{L}{30R_{\text{g}}}\right)^{-3/2} \times \left(\frac{\xi f}{3}\right)^{-1/2} \left(\frac{M}{10M_{\odot}}\right)^{-1},$$
(2)

where f_0 is the QPO frequency, \dot{m} is the accretion rate in Eddington units, $\eta_{\rm int}$ and *L* are, respectively, the intrinsic feedback fraction and the corona size (in units of $R_{\rm g} = GM/c^2$) in the vkompth model, ξ is a factor that can be either 1/2 or 3 for, respectively, a maximally and a non-rotating black hole, *f* is the fraction of the gravitational energy that is injected into the corona, and *M* is the black hole mass in solar masses. If we take $\eta_{\rm int} \sim 0.2$ and $L \sim 800 R_{\rm g}$ from our results, $M \sim 8 M_{\odot}$ (Torres et al. 2020), $\xi = 1/2$ for a maximally spinning black hole (e.g. Wang et al. 2021) and f = 0.1-0.2, the QPO frequency is $f_0 \simeq 2-8$ Hz for $\dot{m} \sim 0.1 - 0.5 \dot{M}_{\rm Edd}$ (e.g. Dunn et al. 2010, but notice that due to the uncertainties in $\eta_{\rm int}$ and *L* these frequencies have large errors).

4.3.2 Models of the type-B QPO

Stevens & Uttley (2016) analysed the type-B QPO in the BHB GX 339–4 using phase-resolved spectroscopy, and they found that Γ varies periodically during the QPO cycle. They interpreted this as the precession of the jet in this source. Subsequently, using Monte Carlo simulations Kylafis, Reig & Papadakis (2020) explained these variations of Γ as the precession of the jet in GX 339–4, further supporting this idea. Liu et al. (2022a) studied the type-B QPOs in MAXI J1348–630 and suggested that it also originates from the jet precession; they also attributed the disappearance of the type-B QPOs to instabilities of the disc–jet structure.

If the type-B QPO is indeed produced by the precession of the jet, it is reasonable to expect a correlation between the properties (e.g. rms and lag) of type-B QPOs and the inclination of the jet with respect to the line of sight. The lag spectra in the 1–10 keV band of MAXI J1348–630 (García et al. 2021), GX 339–4 (Peirano et al. 2023), and MAXI J1820+070 in this work show that, for the type-B QPOs the \sim 2–3 keV photons always lead the photons in other energy bands, and that the magnitude of lags is always larger below than above that energy. Given the similarities of the lag spectra of the type-B QPO in these three sources, the fact that the inclination of the jet in these sources is quite different (\sim 33° for MAXI J1348–630, Mall, Vadakkumthani & Misra 2023; \sim 35–45° for GX 339–4, Liu et al. 2023; \sim 63° for MAXI J1820+070, Torres et al. 2020) appears to question this scenario.

4.4 Evolution of the corona

Using the combined results of the fits to the time-averaged spectra of the source and the rms and lag spectra of the QPO plus the quasisimultaneous radio observation (Bright et al. 2020, see Fig. 11), we propose a possible scenario during the transition from the HIMS to the SIMS in Fig. 12.



Figure 11. The evolution of the size of the large corona and the radio flux of MAXI J1820+070 during the transition from type-C to type-B QPOs. The black, blue, and red points represent the size of the large corona, L_2 , the intrinsic feedback fraction of the large corona, $\eta_{int,2}$, and the AMI-LA radio flux, respectively. The black vertical line represents the QPOs transition time, and the red dashed and dash-dotted lines represent the best-fitting evolution of, respectively, the radio emission of the core that decreases steadily during the period with type-C QPOs and the radio flare during the period with type-B QPOs. The radio data and lines showing the evolution of the radio emission are from Bright et al. (2020).

4.4.1 State transition, radio flare, and jet ejections

We first checked and confirmed that the PDS of orbit 09 and orbit 10 with *NICER* change significantly, indicating that the QPO transition occurs in this period. We find that the PDS of the whole orbit 09 shows a strong broad-band noise component, whereas the PDS of the whole orbit 10 shows a weak broad-band noise component (see Fig. B4). This indicates that in orbit 09, MAXI J1820+070 is still in the HIMS, whereas in orbit 10, it is already in the SIMS. The transition time must have therefore occurred between these two orbits, i.e. MJD 58305.66 \pm 0.02.

Subsequently, we re-examined the results of the radio data during this state transition. Bright et al. (2020) reported that, in addition to a core quenching with gradually decreasing flux, the observations of MAXI J1820+070 with AMI-LA showed a radio flare that peaked ~ 0.3 d after the time of the transition of type-C to type-B OPOs (see Fig. 11), which they associated with the ejection of ballistic jets at around the time of the transition. Using the dynamic phase centre tracking technique to fit all the VLBI data, Wood et al. (2021) found that the launch date was MJD 58305.60 \pm 0.04 (see Bright, Fender & Motta 2018; Espinasse et al. 2020, who found a similar launch date modelling a subset of the same data). From this it appears that the ejection that caused the flare on ~MJD 59 306 may have been launched already during orbit 09, when the source was still in the HIMS with a type-C QPO, just before the transition to the SIMS with type-B QPO. It is worth noting that L_2 , the size of the large corona, was already increasing before that date, and reached its maximum value during orbit 09 (see Fig. 9).

4.4.2 Corona geometry in the HIMS

In the HIMS, the centroid frequency of the QPO increases from 4.4 to 7.7 Hz (see Section 4.2 and Figs 9 and 11 for the evolution of the parameters of the coronae). The temperature of the seed photons that illuminate the large corona shows an increasing trend while being always lower than the temperature of the seed photon source that illuminates the small corona. These results suggest that the small



Figure 12. Schematic picture of the corona evolution during the transition from type-C QPOs to type-B QPOs in MAXI J1820+070. In the type-C QPOs case, the small corona is located inside the inner disc radius and the seed photons come from the inner disc. The large corona extends horizontally covering the inner parts of the disc, and the seed photons for this corona come from the outer parts of the disc. The values of $\eta_{int, 1}$ and $\eta_{int, 2}$ indicate that both coronae illuminate the disc (top panel). As the outburst evolves, the size of both coronae increases while the inner disc radius moves inwards (middle panel). The radio emission increases rapidly at the transition from the type-C to the type-B QPOs (see Fig. 11 and Bright et al. 2020). In the type-B QPOs case the small corona is still located inside the inner disc radius, while the large corona extends vertically, consistent with the detection of the relativistic ejecta (bottom panel).

corona is located inside the inner edge of the accretion disc and is illuminated by the central parts of the disc, while the large corona covers a large fraction of the accretion disc and is illuminated by a cooler part of the disc (top and middle panels of Fig. 12).

The Imaging X-ray Polarimetry Explorer (IXPE; Weisskopf et al. 2022) observed that Cyg X–1 in the non-thermal component dominated state has a polarization degree ~4 per cent in the 2–8 keV energy band at a position angle of \sim -21° (Krawczynski et al. 2022), consistent with the position angle of the jet on the sky (Miller-Jones et al. 2021). Modelling of these results indicates that in Cyg X–1 in the non-thermal dominated state, Comptonization takes place in a sandwich corona located above and below the disc and extending laterally. The proposed geometry of MAXI J1820+070 in the HIMS that we deduce from our X-ray analysis is consistent with that of Cyg X–1 deduced from those X-ray polarimetric measurements.

Steady, optically thick, radio emission is observed in this source in the HIMS (Bright et al. 2020), and other sources both in the LHS and the HIMS (e.g. Corbel et al. 2003; Fender et al. 2004). That the existence of this emission does not correspond to a vertically extended corona (see our results here and Krawczynski et al. 2022), suggests that the radio emission is not from material ejected into a narrow jet, but comes from a mildly relativistic outflow that originates from a relatively large radius in the disc (e.g. Kylafis & Reig 2018; Marcel et al. 2018; Reig & Kylafis 2021). In the SIMS, the centroid frequency of the OPO decreases from 4.2 to 3.1 Hz. The parameters of two coronae during SIMS, and the comparison with the HIMS, are shown in Section 4.2 and Figs 9 and 11. The parameters of the coronae indicate that, as in the HIMS, in the SIMS the small corona is also located inside the inner edge of the disc, whereas the vanishing small intrinsic feedback fraction indicates that the geometry of the large corona changes significantly. From all this we interpret that the radius of the large corona is in fact a characteristic size and that the large corona is vertically extended (see also, Méndez et al. 2022; Zhang et al. 2023). As in the HIMS, in the SIMS the temperature of the seed photon source of the small corona is higher than that of the large corona. Moreover, the temperature of the seed photon source of the small corona increases further in the SIMS compared to the HIMS, whereas that of the large corona decreases from the HIMS to the SIMS. This indicates that in the SIMS the large corona is illuminated from the parts farther away from the BH than in the HIMS, consistent with the proposed geometry.

We compare our results to the radio observation during the QPO transition period. As shown in Fig. 11 and described in Section 4.4.1, the launch date of the discrete ejection that produced the radio flare, MJD 58305.60 \pm 0.04, is consistent with the QPO transition time, MJD 58305.66 \pm 0.02. Both Espinasse et al. (2020) and Wood et al. (2021) suggest that the radio flare is associated with the occurrence of type-B QPOs. Homan et al. (2020) also reported the relation between the type-B QPOs and the radio flare, that the appearance of type-B QPOs was accompanied by an X-ray flare in the 7-12 keV energy band, and that a strong radio flare appeared 2-2.5 h after the type-B QPOs was observed. They interpreted the delay of the radio flare with respect to the X-ray flare and the QPO transition as the time for the ejecta to catch up with the material of the previous slower ejecta, or the time for the ejecta to interact with the interstellar medium. Based on our and the above radio results, we suggest that the large corona is a jet-like corona extending vertically with no photons feeding back to the disc, and the small corona is located inside the inner disc radius (bottom panel of Fig. 12).

4.4.4 Comparison with other corona geometries in MAXI J1820+070

From an X-ray spectroscopic analysis of *NICER* data, Zdziarski et al. (2021) also proposed that, in the hard state, the corona of MAXI J1820+070 consists of two Comptonization regions. These authors find that a hotter corona, which is located farther away from the accretion disc, dominates the narrow reflection component and is responsible for the reverberation lags, whereas a cooler component located closer to the BH is responsible for the broader reflection component. Subsequent analysis of the energy spectra of the Lorentzian functions used to fit the PDS of the source also suggested the existence of two Comptonized regions with different temperatures and optical depths (Dziełak, De Marco & Zdziarski 2021).

Broad-band variability studies also indicate that the accretion flow structure changed during the state transition in MAXI J1820+070. Fits of the lag-energy spectra in a broad frequency range using the reverberation model reltrans (Ingram et al. 2019) showed that the corona expanded vertically and the height⁸ of the corona increased

during the state transition of MAXI J1820+070 (Wang et al. 2021), reaching corona heights comparable to the size of the large corona that we find here (see also Lucchini et al. 2023). Through timingspectral analysis, De Marco et al. (2021) also reported a dramatic change in the structure of the innermost accretion flow during the state transition, although they suggested that the transition of the source was accompanied by a decrease of the disc inner radius rather than an increase of the corona height.

5 CONCLUSIONS

We analyse *NICER* data of 13 orbits during the state transition of MAXI J1820+070 from the HIMS to the SIMS. We use the timedependent Comptonization model, vkompth, to fit jointly the timeaveraged spectra of the source and the rms and lag spectra of the QPOs to study the spectral-timing evolution of this source. Our main findings are:

(1) We detect a type-C QPO with a centroid frequency increasing from 4.4 to 7.7 Hz in the HIMS that evolves to a type-B QPO with a centroid frequency that decreases from 4.2 to 3.1 Hz in the SIMS.

(2) The rms and lag spectra of both the type-C and type-B QPOs are consistent with being the same above $\sim 1.5-2$ keV. At energies below $\sim 1.5-2$ keV the type-C QPOs show a larger rms amplitude and a lower magnitude of the phase lag than the type-B QPOs.

(3) The data can be fitted with a time-dependent Comptonization model of two physically coupled coronae: In the HIMS the system consists of a small corona of $\sim 20-100$ km with an intrinsic feedback fraction of $\sim 5-15$ per cent, and a large corona of $\sim 10^4-10^5$ km with an intrinsic feedback fraction of $\sim 20-30$ per cent. In the SIMS, the size of the small corona decreases to ~ 20 km with an intrinsic feedback fraction of $\sim 20-30$ per cent, while the size of the large corona is $\sim 10^4$ km with an intrinsic feedback fraction of 0. At the same time, the inner radius of the disc inferred from the *diskbb* component decreases during the transition.

(4) From the fitting results from *NICER* and the radio data previously published, we propose a possible evolution of the corona geometry during the state transition. In the HIMS, the system consists of a large and horizontally extended corona covering the inner parts of the accretion disc, and a small corona located inside the inner edge of the disc. In the SIMS, the small corona is still located inside the inner edge of the disc, whereas the large corona is vertically extended and is associated with the material that produced the radio flare.

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⁸Because the reltrans model assumes that the corona is a point source, the model gives the height of this point source above the accretion disc instead of the size of the corona.

DATA AVAILABILITY

The data used in this article are available in the HEASARC data base (https://heasarc.gsfc.nasa.gov). The VKOMPTH model is publicly available in a Github repository (https://github.com/candebellavita/vkompth). The corner plots were created using TKXSPECCORNER (https://github.com/garciafederico/pyXspecCorner).

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APPENDIX A: FIT WITH RELXILLCP V2.3

During our spectral fitting using relxillCp v1.4.3, we find that the iron abundance is always $A_{\rm Fe} > 9.91$. Similar values of the iron abundance have been reported in the past from fits with relxill to the spectra of Cyg X–1 (Tomsick et al. 2018) and GX 339–4 (Jiang et al. 2019), and were attributed to limitations of the model that at the time was computed for a low disc density $N = 10^{15}$ cm⁻³. Since version 2.3 of relxill includes tables with *N* ranging from 10¹⁵ to 10^{20} cm⁻³, we fit the data using the new version and find a best-fitting disc density $N \sim 10^{17}$ cm⁻³ and $A_{\rm Fe} \simeq 5$. Other parameters of the fit are consistent with the ones we find using version 1.4.3 within errors. Since in this paper we are not interested in the iron abundance, we give the fits with version 1.4.3 because the temperature of the seed photon source is fixed at $kT_{\rm bb} = 0.05$ keV, whereas in version 2.3 it is fixed at $kT_{\rm bb} = 0.01$ keV.

APPENDIX B: TABLE WITH ALL FITTING PARAMETERS AND EXTRA PLOTS



Figure B1. Representative corner plot of the parameters of MAXI J1820+070 for an observation with the type-C QPO (orbit 01). The contours indicate the 1σ , 2σ , and 3σ levels for two parameters, while the vertical lines indicate the 1σ confidence range for one parameter.



Figure B2. Same as Fig. B1 but for an observation with the type-B QPO (orbit 10).



Figure B3. Best-fitting parameters as a function of QPO frequency during the transition from type-C to type-B QPOs of MAXI J1820+070. The parameters and colours are the same as in Fig. 9.



Figure B4. Power density spectra in the 0.5–12 keV energy band of MAXI J1820+070 with *NICER*. The orange data correspond to orbit 09 in the HIMS, while the blue data correspond to orbit 10 in the SIMS.

Table B1. Best-fitting parameters of the 13 orbits during the transition from type-C (orbit 00-obit 09) to type-B (orbit 10-orbit 12) QPO of MAXI J1820+070. Uncertainties are at 90 per cent confidence levels.

Component	Parameter	orbit 00	orbit 01	orbit 02	orbit 03	orbit 04	orbit 05	orbit 06	orbit 07	orbit 08	orbit 09	orbit 10	orbit 11	orbit 12
TBfeo	$N_{ m H}(10^{20}{ m cm^{-2}})$	$[4.2]^{a}$	$[4.2]^{a}$	$[4.2]^{a}$	$[4.2]^{a}$	[4.2] ^a	$[4.2]^{a}$	$[4.2]^{a}$	$[4.2]^{a}$	[4.2] ^a	$[4.2]^{a}$	$[4.2]^{a}$	[4.2] ^a	$[4.2]^{a}$
diskbb	$kT_{\rm in}$ (keV)	$0.475_{-0.012}^{+0.004}$	$0.478\substack{+0.007\\-0.013}$	0.501 ± 0.010	$0.526\substack{+0.003\\-0.006}$	0.542 ± 0.005	$0.542\substack{+0.004\\-0.009}$	$0.563\substack{+0.005\\-0.009}$	$0.561\substack{+0.006\\-0.009}$	$0.579\substack{+0.005\\-0.012}$	0.596 ± 0.008	$0.666^{+0.003}_{-0.010}$	$0.685^{+0.005}_{-0.011}$	$0.702\substack{+0.001\\-0.019}$
	$N_{ m disk}{}^{b}(10^4)$	$2.40\substack{+0.27\\-0.08}$	$2.4_{-0.2}^{+0.3}$	2.2 ± 0.2	1.99 ± 0.11	$1.85\substack{+0.12\\-0.08}$	$1.93_{-0.07}^{+0.15}$	$1.72_{-0.08}^{+0.12}$	$1.68\substack{+0.12\\-0.08}$	$1.60\substack{+0.09\\-0.06}$	1.47 ± 0.07	$1.29\substack{+0.06\\-0.03}$	1.24 ± 0.04	$1.31\substack{+0.08\\-0.02}$
	$F_{ m disk}^{*} (10^{-9} { m ergs} { m cm}^{-2} { m s}^{-1})$	18.9 ± 1.4	19.2 ± 1.3	22.1 ± 1.1	24.7 ± 0.8	26.1 ± 0.6	27.3 ± 0.8	28.7 ± 0.6	27.6 ± 0.5	$30.2^{\pm 1.0}_{-1.6}$	$31.4^{+2.2}_{-1.2}$	$43.4^{+1.4}_{-0.9}$	$48.2^{\pm1.4}_{-3.2}$	55 ± 3
nthComp	Ц	2.43 ± 0.04	2.45 ± 0.03	2.47 ± 0.03	2.51 ± 0.02	2.543 ± 0.016	2.54 ± 0.02	$2.590\substack{+0.020\\-0.010}$	$2.589^{+0.021}_{-0.012}$	2.64 ± 0.03	2.78 ± 0.03	2.80 ± 0.03	$2.87\substack{+0.06\\-0.03}$	$2.812\substack{+0.097\\-0.018}$
	$kT_{\rm e}$ (keV)	$[40]^{a}$												
	$N_{ m nthComp}$	9.8 ± 0.3	10.2 ± 0.4	10.2 ± 0.3	$10.19\substack{+0.25\\-0.12}$	10.2 ± 0.3	10.5 ± 0.3	10.5 ± 0.3	10.3 ± 0.3	$10.6^{+0.6}_{-0.3}$	11.7 ± 0.5	$11.7^{\pm 0.8}_{-0.3}$	$11.9^{\pm 1.1}_{-0.4}$	$9.88^{+1.72}_{-0.09}$
		45.6 ± 1.1	47.2 ± 1.0	48.2 ± 1.0	48.9 ± 0.9	49.3 ± 0.7	$50.5^{\pm1.1}_{-0.7}$	50.9 ± 0.9	49.8 ± 1.1	$51.4^{+1.6}_{-1.1}$	55.0 ± 1.6	$60.8^{+1.0}_{-3.4}$	61 ± 3	5.5 ± 0.4
relxillCp	$F_{\text{inthComp}^*}(10^{-y} \text{ ergs cm}^{-z} \text{ s}^{-1})$ $\alpha 1$	$2.09\substack{+0.18\\-0.13}$	$2.23^{+0.20}_{-0.14}$	2.13 ± 0.15	2.13 ± 0.10	2.12 ± 0.08	$2.09\substack{+0.09\\-0.12}$	2.13 ± 0.11	2.28 ± 0.13	2.19 ± 0.11	2.18 ± 0.12	$2.06\substack{+0.10\\-0.16}$	2.12 ± 0.13	$2.17\substack{+0.08\\-0.31}$
	a_*	$[0.998]^{a}$	$[0.998]^{a}$	ⁿ [866.0]	$[0.998]^{a}$	ⁿ [866.0]	^{<i>p</i>} [866.0]							
	<i>i</i> (°)	$[67.3]^{a}$												
	$\log \xi (\log[erg cm s^{-1}])$	$3.34_{-0.13}^{+0.20}$	$3.31_{-0.10}^{+0.17}$	$3.30_{-0.12}^{+0.09}$	3.29 ± 0.04	$3.30^{+0.05}_{-0.07}$	3.30 ± 0.06	$3.30^{+0.08}_{-0.05}$	$3.30_{-0.04}^{+0.07}$	$3.32^{+0.12}_{-0.03}$	$3.65^{+0.09}_{-0.22}$	$3.68^{+0.09}_{-0.18}$	$3.71_{-0.11}^{+0.17}$	$3.69_{-0.10}^{+0.22}$
	$A_{\rm Fe}$ (solor)	$[10]^{a}$												
	$N_{ m refl}$	$0.105\substack{+0.013\\-0.021}$	0.10 ± 0.03	0.10 ± 0.04	0.12 ± 0.02	0.14 ± 0.02	0.12 ± 0.03	0.16 ± 0.03	0.17 ± 0.03	0.19 ± 0.04	0.21 ± 0.05	0.19 ± 0.05	0.22 ± 0.05	$0.25\substack{+0.03\\-0.09}$
	$F_{ m refl}^{ m *}$ (10 ⁻⁹ ergs cm ⁻² s ⁻¹)	$7.5^{+1.9}_{-1.6}$	6.6 ± 1.6	6.3 ± 1.3	6.3 ± 1.0	6.4 ± 0.8	5.6 ± 1.0	6.2 ± 0.9	$6.7^{+0.9}_{-0.5}$	6.4 ± 1.0	7.6 ± 1.2	5.4 ± 0.9	$5.8^{+1.0}_{-0.6}$	$6.0^{\pm 1.6}_{-1.3}$
gabs	lineE (keV)	0.556 ± 0.010	$0.552\substack{+0.008\\-0.021}$	$0.555^{+0.007}_{-0.016}$	$0.554\substack{+0.008\\-0.027}$	$0.553\substack{+0.008\\-0.015}$	$0.551\substack{+0.007\\-0.021}$	$0.549\substack{+0.010\\-0.023}$	$0.550\substack{+0.008\\-0.026}$	$0.548\substack{+0.009\\-0.026}$	$0.543\substack{+0.011\\-0.031}$	$0.541\substack{+0.007\\-0.033}$	0.52 ± 0.02	$0.531\substack{+0.011\\-0.028}$
	σ (10 ⁻² keV)	$7.0^{+1.2}_{-0.8}$	$7.8^{+2.1}_{-0.9}$	$7.4_{-0.8}^{+1.7}$	$7.5^{+2.2}_{-1.0}$	$7.7^{+1.6}_{-0.9}$	$8.0^{+1.9}_{-0.7}$	$8.4^{+2.0}_{-1.0}$	$8.1^{+2.2}_{-0.8}$	$8.7^{+2.2}_{-0.9}$	$9.2^{+2.7}_{-1.0}$	$9.9^{+2.9}_{-0.6}$	$12.1^{\pm 1.6}_{-1.5}$	$11.0^{+2.7}_{-0.8}$
	Strength (10^{-2})	$4.2\substack{+0.8\\-0.4}$	$4.9^{\pm 1.4}_{-0.5}$	$4.7^{+1.0}_{-0.4}$	$4.7^{+1.4}_{-0.5}$	$4.8_{-0.5}^{+0.9}$	$5.2^{+1.2}_{-0.3}$	$5.3^{+1.4}_{-0.5}$	$5.1^{\pm 1.5}_{-0.4}$	$5.5^{+1.5}_{-0.5}$	$6.1^{+2.0}_{-0.6}$	$6.9^{\pm 2.4}_{-0.3}$	$8.8^{+1.4}_{-1.2}$	$7.9^{+2.2}_{-0.6}$
vkdualdk	$kT_{\rm s, 2}$ (keV)	$0.34\substack{+0.09\\-0.04}$	$0.22\substack{+0.13\\-0.03}$	$0.279\substack{+0.112\\-0.018}$	0.34 ± 0.06	$0.35\substack{+0.07\\-0.04}$	0.39 ± 0.04	$0.43\substack{+0.08\\-0.05}$	0.48 ± 0.06	0.45 ± 0.05	$0.42\substack{+0.11\\-0.05}$	$0.313\substack{+0.132\\-0.007}$	$0.305\substack{+0.036\\-0.009}$	$0.35\substack{+0.53\\-0.02}$
	L1 (km)	50^{+80}_{-30}	<74	27^{+56}_{-10}	33^{+33}_{-20}	40^{+30}_{-20}	110^{+90}_{-40}	70^{+60}_{-30}	150^{+180}_{-70}	100^{+90}_{-40}	<34	<38	<19	<95
	$L_2 (10^4 { m km})$	1.2 ± 0.4	$1.00\substack{+0.15\\-0.54}$	$1.09\substack{+0.12\\-0.54}$	1.1 ± 0.3	1.2 ± 0.4	$2.7^{+2.0}_{-0.7}$	1.4 ± 0.6	$2.8^{+2.9}_{-0.7}$	$3.8^{+2.3}_{-0.9}$	13 ± 5	1.5 ± 0.3	1.2 ± 0.3	$1.7^{\pm 3.7}_{-0.9}$
	η_1	$0.23\substack{+0.09\\-0.16}$	$0.51\substack{+0.14\\-0.40}$	$0.43\substack{+0.05\\-0.21}$	0.38 ± 0.09	$0.44\substack{+0.09\\-0.14}$	0.43 ± 0.09	0.35 ± 0.14	0.33 ± 0.10	0.42 ± 0.10	0.5 ± 0.2	$0.96\substack{+0.03\\-0.39}$	$1.00^b_{-0.08}$	$0.82\substack{+0.13\\-0.69}$
	η_2	$1.0^{b}_{-0.4}$	$1.0^b_{-0.5}$	$0.995^{+0.013}_{-0.565}$	$1.0^{b}_{-0.3}$	$1.0^{b}_{-0.3}$	$1.0^{b}_{-0.2}$	$1.0^{b}_{-0.3}$	$1.0^b_{-0.6}$	$1.0^{b}_{-0.6}$	1.0^b_c	$0.00_c^{+0.16}$	$0.00_c^{+0.11}$	$0.0_c^{+0.9}$
	ϕ (rad)	2.7 ± 0.4	$2.6^{+1.4}_{-0.4}$	$2.55^{+0.61}_{-0.09}$	$2.44_{-0.14}^{+0.34}$	2.3 ± 0.3	1.6 ± 0.5	2.3 ± 0.4	$1.8^{+0.2}_{-0.7}$	1.3 ± 0.5	$-0.06\substack{+0.19\\-0.06}$	$2.48^{+0.70}_{-0.14}$	2.6 ± 0.3	$2.6^{\pm 3.0}_{-1.1}$
	reflag	$0.14\substack{+0.06\\-0.12}$	$0.07^{+0.06}_{c}$	$0.05_c^{+0.08}$	$0.05_c^{+0.07}$	-0.11 ± 0.07	-0.15 ± 0.06	-0.18 ± 0.08	$-0.26\substack{+0.14\\-0.11}$	-0.32 ± 0.10	0.3 ± 0.3	$-0.31\substack{+0.02\\-0.09}$	-0.33 ± 0.05	-0.5 ± 0.3
	$\eta_{ m int, 1}$	0.05 ± 0.03	0.11 ± 0.07	0.09 ± 0.04	0.08 ± 0.02	0.10 ± 0.03	0.10 ± 0.02	0.09 ± 0.04	0.08 ± 0.03	0.11 ± 0.03	0.15 ± 0.07	0.27 ± 0.07	0.29 ± 0.01	$0.2_{c}^{\pm 0.2}$
	$\eta_{ m int,2}$	0.21 ± 0.06	0.22 ± 0.07	0.22 ± 0.08	0.22 ± 0.04	0.23 ± 0.04	0.23 ± 0.04	0.24 ± 0.04	0.23 ± 0.09	0.25 ± 0.08	0.277 ± 0.001	$0.00_c^{+0.03}$	$0.00_c^{+0.02}$	$0.00_c^{+0.2}$
	χ^2/v	242.7/230	246.0/230	195.2/230	231.0/230	265.6/230	273.7/230	240.3/230	249.1/230	201.9/230	265.1/230	230.5/230	276.8/230	225.9/230
	frequency (Hz)	4.44 ± 0.07	4.64 ± 0.05	5.01 ± 0.05	5.50 ± 0.05	5.83 ± 0.05	6.04 ± 0.06	6.56 ± 0.11	6.34 ± 0.05	7.2 ± 0.2	7.7 ± 0.3	4.23 ± 0.04	3.98 ± 0.04	3.1 ± 0.2
Note. Colu	nns and fitting limits are defined	as in Table 2. Pa	rameter values fr	ozen during the f	itting are given i	n square brackets								